# What do we want? And when do we want it? Alternative objectives and their implications for experimental design.

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#### Introduction – big picture motivation

- Decision making based on data requires normative assumptions:
   We have to specify what objective we want to maximize!
- This is reflected in the normative frameworks of different fields:
  - Decision theory (in statistics):
     Loss function, action space, identifying assumptions.
  - Social welfare analysis (in economics):
     Measures of individual welfare, aggregation across individuals.
  - Construction of autonomous agents (in artificial intelligence):
     Signals from perceptors, actions through actuators, rewards.
- Different objectives lead to different recommendations.
- This is in particular true for experimental design, understood as a decision problem.

#### Experimental design as a decision problem

#### Experimental design decision:

• How to assign treatments, given the available information and objective.

Key ingredients defining a decision problem:

#### 1. Objective function:

What is the ultimate goal? What will the experimental data be used for?

#### 2. Action space:

What information can experimental treatment assignments depend on?

- 3. Ways to evaluate a decision function:
  - a Risk function (expected loss conditional on parameters),
  - b Bayes risk (averaging risk function over prior distribution of parameters),
  - c Minimax risk (worst case risk function over some set of parameters).

#### Four possible types of objective functions for experiments

- 1. Squared error for estimates.
  - For instance for the average treatment effect.
  - Possibly weighted squared error of multiple estimates.
- 2. **In-sample average** outcomes.
  - Possibly transformed (inequality aversion),
  - costs taken into account, discounted.
- Policy choice to maximize average observed outcomes.
  - Choose a policy after the experiment.
  - Evaluate the experiment based on the implied policy choice.
- 4. Policy choice to maximize utilitarian welfare.
  - Similar, but welfare is not directly observed.
  - Instead, maximize a weighted average (across people) of equivalent variation.

#### This talk:

Review of several of my papers, considering each of these in turn.

#### Space of possible experimental designs

What information can treatment assignment condition on?

- 1. Covariates?
  - ⇒ Stratified and targeted treatment assignment.
- 2. Earlier outcomes for other units, in sequential or batched settings?
  - ⇒ Adaptive treatment assignment.

#### This talk:

- First conditioning on covariates, then settings without conditioning (for exposition only).
- First non-adaptive, then adaptive experiments.

#### Two approaches to optimization

- 1. Fully optimal designs.
  - Conceptually straightforward (dynamic stochastic optimization), but numerically challenging.
  - Preferred in the economic theory literature,
     which has focused on tractable (but not necessarily practically relevant) settings.
  - Do not require randomization.
- 2. Approximately optimal or rate optimal designs.
  - · Heuristic algorithms.
  - Prove (rate)-optimality ex post.
  - Preferred in the machine learning literature.
     This is the approach that has revived the bandit literature and made it practically relevant.
  - Might involve randomization.

#### This talk:

- Approximately optimal algorithms.
- Bayesian algorithms, but we characterize the *risk function*, i.e., behavior conditional on the true parameter.

#### This talk: Several papers considering different objectives

#### Minimizing squared error:

Kasy, M. (2016). Why experimenters might not always want to randomize, and what they could do instead. *Political Analysis*, 24(3):324–338.

#### Maximizing in-sample outcomes:

Caria, S., Gordon, G., Kasy, M., Osman, S., Quinn, S., and Teytelboym, A. (2020). Job search assistance for refugees in Jordan: An adaptive field experiment. *Work in progress*.

#### Optimizing policy choice – average outcomes:

Kasy, M. and Sautmann, A. (2020). Adaptive treatment assignment in experiments for policy choice. *Working Paper*. (R&R at Econometrica)

#### Optimizing policy choice – utilitarian welfare:

Kasy, M. (2020). Adaptive experiments for optimal taxation. *Work in progress*. building on

Kasy, M. (2019). Optimal taxation and insurance using machine learning – sufficient statistics and beyond. *Journal of Public Economics*.

#### Literature

- Statistical decision theory: Berger (1985), Robert (2007).
- Non-parametric Bayesian methods: Ghosh and Ramamoorthi (2003), Williams and Rasmussen (2006), Ghosal and Van der Vaart (2017).
- Stratification and re-randomization: Morgan and Rubin (2012), Athey and Imbens (2017).
- Adaptive designs in clinical trials: Berry (2006), FDA et al. (2018).
- Bandit problems:
   Weber et al. (1992),
   Bubeck and Cesa-Bianchi (2012),
   Russo et al. (2018).

- Best arm identification:
   Glynn and Juneja (2004),
   Bubeck et al. (2011),
   Russo (2016).
- Bayesian optimization: Powell and Ryzhov (2012), Frazier (2018).
- Reinforcement learning: Ghavamzadeh et al. (2015), Sutton and Barto (2018).
- Optimal taxation:
   Mirrlees (1971),
   Saez (2001),
   Chetty (2009),
   Saez and Stantcheva (2016).

#### Minimizing squared error

Maximizing in-sample outcomes

Optimizing policy choice: Average outcomes

Optimizing policy choice: Utilitarian welfare

Conclusion and summary

#### No randomization in general decision problems

#### Theorem (Optimality of deterministic decisions)

Consider a general decision problem.

Let  $R^*(\cdot)$  equal either Bayes risk or worst case risk. Then:

- 1. The optimal risk  $R^*(\delta^*)$ , when considering only deterministic procedures is no larger than the optimal risk when allowing for randomized procedures.
- 2. If the optimal deterministic procedure is unique, then it has strictly lower risk than any non-trivial randomized procedure.

#### Sketch of proof (Kasy, 2016):

- The risk function of a randomized procedure is a weighted average of the risk functions of deterministic procedures.
- The same is true for Bayes risk and minimax risk.
- The lowest risk is (weakly) smaller than the weighted average.

## Minimizing squared error: Setup

- 1. **Sampling:** Random sample of n units. Baseline survey  $\Rightarrow$  vector of covariates  $X_i$ .
- 2. **Treatment assignment:** Binary treatment assigned by  $D_i = d_i(\mathbf{X}, U)$ .  $\mathbf{X}$  matrix of covariates; U randomization device .
- 3. Realization of outcomes:  $Y_i = D_i Y_i^1 + (1 D_i) Y_i^0$
- 4. **Estimation:** Estimator  $\widehat{\beta}$  of the (conditional) average treatment effect,  $\beta = \frac{1}{n} \sum_{i} E[Y_{i}^{1} Y_{i}^{0}|X_{i}, \theta]$

#### Prior:

- Let  $f(x,d) = E[Y_i^d | X_i = x]$ .
- Let C((x,d),(x',d')) be the prior covariance of f(x,d) and f(x',d').

#### Expected squared error

- Notation:
  - $C: n \times n$  covariance matrix of the  $f(X_i, D_i)$ .
  - $\bar{C}$ : n vector of covariances of  $f(X_i, D_i)$  with the CATE  $\beta$ .
  - $\widehat{\beta}$ : The posterior best linear predictor of  $\beta$ .
- Kasy (2016):

The Bayes **risk** (expected squared error) of a treatment assignment equals

$$Var(\beta|\mathbf{X}) - \overline{C}' \cdot (C + \sigma^2 I)^{-1} \cdot \overline{C},$$

where the prior variance  $Var(\beta|\mathbf{X})$  does not depend on the assignment, but  $\overline{C}$  and C do.

#### Optimal design

- The **optimal design** minimizes the Bayes risk (expected squared error).
- Simple approximate optimization algorithm: Re-randomization.
- For continuous covariates, the optimum is generically unique, and a non-random assignment is optimal.
- Expected squared error is a measure of balance across treatment arms.
- Variations:
  - Different estimators (difference in means, or linear controls for covariates).
  - Different priors (symmetric across treatments, or assuming functional form).
- Two Caveats:
  - Randomization inference requires randomization outside of decision theory.
  - If minimizing worst case risk given procedure, but not given randomization, mixed strategies can be optimal (Banerjee et al., 2017).

Minimizing squared error

Maximizing in-sample outcomes

Optimizing policy choice: Average outcomes

Optimizing policy choice: Utilitarian welfare

Conclusion and summary

#### Maximizing in-sample outcomes

- Minimizing squared error is appropriate when you want to get precise estimates of policy effects.
- But in many settings we want to also **help participants** as much as possible.
- As argued by Kant (1791):
  - Act in such a way that you treat humanity, whether in your own person or in the person of any other, never merely as a means to an end, but always at the same time as an end.
- If we care about both participant welfare and estimator precision, we might try to trade both off.
- This is done by the  $\gamma$ -Thompson algorithm that I will introduce shortly. (Please let me know if you have a better name for the algorithm!)

## Adaptive targeted assignment: Setup

- Waves t = 1, ..., T, sample sizes  $N_t$ .
- Treatment  $D \in \{1, ..., k\}$ , outcomes  $Y \in \{0, 1\}$ , covariate  $X \in \{1, ..., n_x\}$ .
- Potential outcomes  $Y^d$ .
- Repeated cross-sections:  $(Y_{it}^0, \dots, Y_{it}^k, X_{it})$  are i.i.d. across both i and t.
- Average potential outcomes:

$$\theta^{dx} = E[Y_{it}^d | X_{it} = x].$$

• **Regret**: Difference in average outcomes from decision *d* versus the optimal decision,

$$\Delta^{dx} = \max_{d'} \theta^{d'x} - \theta^{dx}.$$

Average in-sample regret:

$$\frac{1}{M}\sum_{i,t}\Delta^{D_{it}X_{it}}.$$

## Thompson sampling and $\gamma$ -Thompson sampling

- Thompson sampling
  - Old proposal by Thompson (1933).
  - Popular in online experimentation.
- Assign each treatment with probability equal to the posterior probability that it is optimal, given X = x and given the information available at time t.

$$p_t^{dx} = P_t \left( d = \underset{d'}{\operatorname{argmax}} \ \theta^{d'x} \right).$$

•  $\gamma$ -**Thompson sampling**: Assign each treatment with probability equal to

$$(1-\gamma)\cdot p_t^{dx} + \gamma/k$$
.

Compromise between full randomization and Thompson sampling.

My development economics co-authors want to both publish estimates and help!

## Limiting behavior

#### Theorem (Caria et al. 2020)

Given  $\theta$ , as  $t \to \infty$ :

- 1. The **cumulative share**  $q_t^{dx}$  allocated to treatment d in stratum x converges in probability to  $\bar{q}^{dx} = (1 \gamma) + \gamma/k$  for  $d = d^{*x}$ , and to  $\bar{q}^{dx} = \gamma/k$  for all other d.
- 2. Average in-sample regret converges in probability to

$$\gamma \cdot \left(\frac{1}{k} \sum_{x,d} \Delta^{dx} \cdot \rho^{x}\right).$$

3. The normalized average outcome for treatment d in stratum x,  $\sqrt{M_t} \left( \bar{Y}_t^{dx} - \theta_0^{dx} \right)$ , converges in distribution to

$$N\left(0, \frac{\theta_0^{dx}(1-\theta_0^{dx})}{\bar{q}^{dx}\cdot p^x}\right).$$

#### Interpretation

- In-sample regret is (approximately) proportional to the share  $\gamma$  of observations fully randomized.
- The variance of average potential outcome estimators is proportional
  - to  $\frac{1}{\gamma/k}$  for sub-optimal d,
  - to  $\frac{1}{(1-\gamma)+\gamma/k}$  for conditionally optimal d.
- The variance of treatment effect estimators, comparing the conditional optimum to alternatives, is therefore decreasing in γ.
- An **optimal** choice of  $\gamma$  could **trade off** regret and estimator variance.

In the application coming next, we chose  $\gamma=.2$ , somewhat arbitrarily.

#### Application: Job search assistance for refugees in Jordan

- Jordan 2019, International Rescue Committee.
  - Participants: Syrian refugees and Jordanians.
  - Main locations: Amman and Irbid.
  - Sample size: 3770.
- Context: Jordan compact.

Gave refugees the right to work in low-skilled formal jobs.

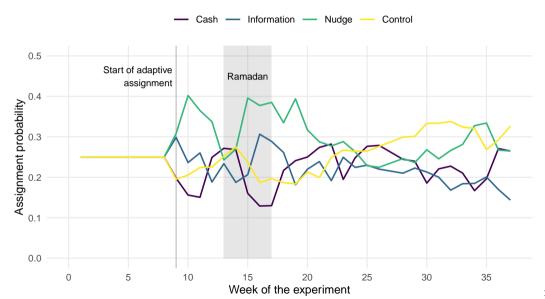
- 4 Treatments:
  - 1. Cash: 65 JOD (91.5 USD).
  - 2. Information: On (i) how to interview for a formal job, and (ii) labor law and worker rights.
  - 3. Nudge: A job-search planning session and SMS reminders.
  - 4. Control group.
- Conditioning variables for treatment assignment: 16 strata, based on
  - 1. nationality (Jordanian or Syrian),
  - 2. gender,
  - 3. education (completed high school or more), and
  - 4. work experience (having experience in wage employment).

## Irbid and Amman

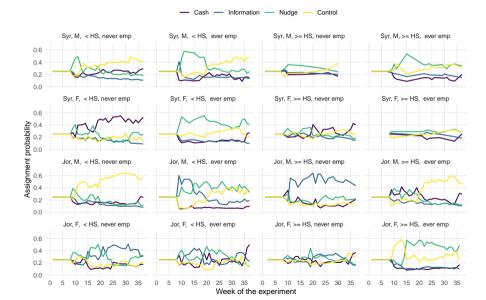




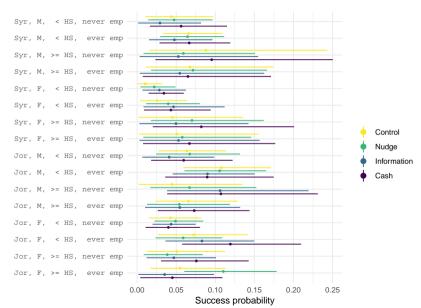
## Assignment probabilities over time



#### Assignment probabilities over time, by stratum



## Effect heterogeneity: Posterior means and 95% credible sets



Minimizing squared error

Maximizing in-sample outcomes

Optimizing policy choice: Average outcomes

Optimizing policy choice: Utilitarian welfare

Conclusion and summary

## Optimizing policy choice: Average outcomes

- Setup: As before, but without covariates (just for presentation).
- Suppose you will **choose a policy** after the experiment, based on posterior beliefs,

$$d_T^* \in \operatorname*{argmax}_d \hat{\theta}_T^d, \qquad \qquad \hat{\theta}_T^d = E_T[\theta^d].$$

- Evaluate experimental designs based on expected welfare (ex ante, given  $\theta$ ).
- Equivalently, expected policy regret

$$\mathsf{R}(\mathsf{T}) = \sum_{d} \Delta^d \cdot P\left(d_T^* = d\right), \qquad \qquad \Delta^d = \max_{d'} \theta^{d'} - \theta^d.$$

- Justification:
  - Continuing experimentation is costly and requires oversight.
  - Political constraints might prevent indefinite experimentation.
  - Experimental samples are often small relative to the policy-population.

## The rate-optimal allocation

- For good designs, R(T) converges to 0 at a fast rate.
- We can characterize the oracle-optimal shares  $\bar{q}^d$  allocated to each treatment d, given  $\theta$ , as follows:
- 1. The **rate** of convergence to 0 of **policy regret**  $R(T) = \sum_{d} \Delta^{d} \cdot P(d_{T}^{*} = d)$  is equal to the slowest rate of convergence of  $P(d_{T}^{*} = d)$  across the sub-optimal d.
- 2. The **rate** of convergence of the **probability**  $P(d_T^* = d)$  is increasing in the share  $\bar{q}^d$  assigned to d, and is also increasing in the effect size  $\Delta^d$ . It is equal to the rate of convergence of the posterior probability  $p_t^d$ .
- 3. The **optimal sample shares**  $\bar{q}^d$  equalize the rate of convergence of  $P(d_T^* = d)$  across sub-optimal d.

This is infeasible, since it requires knowledge of  $\theta$ !

#### Exploration sampling

- How do we construct a feasible algorithm that behaves in the same way?
- Agrawal and Goyal (2012) proved that Thompson-sampling is rate-optimal for the multi-armed bandit problem. It is not for our policy choice problem!
- We propose the following modification.
- Exploration sampling:

Assign shares  $q_t^d$  of each wave to treatment d, where

$$egin{aligned} q_t^d &= S_t \cdot p_t^d \cdot (1 - p_t^d), \ p_t^d &= P_t \left( d = \operatorname*{argmax}_{d'} \, heta^{d'} 
ight), \end{aligned} \qquad S_t = rac{1}{\sum_d p_t^d \cdot (1 - p_t^d)}. \end{aligned}$$

- This modification
  - 1. yields rate-optimality (theorem coming up), and
  - 2. improves performance in our simulations.

## Exploration sampling is rate optimal

#### Theorem (Kasy and Sautmann 2020)

Consider exploration sampling in a setting with fixed wave size  $N_t = N \ge 1$ . Assume that  $\theta^{d^{(1)}} < 1$  and that the optimal policy  $d^{(1)}$  is unique.

- As  $T \to \infty$ , the following holds: 1. The share of observations  $\bar{q}_T^{d^{(1)}}$  assigned to the best treatment
  - converges in probability to 1/2.

    2. The share of observations  $\bar{q}_{T}^{d}$  assigned to treatment d
    - converges in probability to a non-random share  $\bar{q}^d$  for all  $d \neq d^{(1)}$ .  $\bar{q}^d$  is such that  $-\frac{1}{NT}\log p_t^d \to^p \Gamma^*$  for some  $\Gamma^* > 0$  that is constant across  $d \neq d^{(1)}$ .
  - 3. Expected policy regret converges to 0 at the same rate  $\Gamma^*$ , that is,  $-\frac{1}{NT}\log \mathsf{R}(\mathsf{T}) \to^p \Gamma^*$ .

    No other assignment shares  $\bar{q}^d$  exist for which  $\bar{q}^{d^{(1)}} = 1/2$  and  $\mathsf{R}(\mathsf{T})$  goes to 0 at a faster rate than  $\Gamma^*$ .

## Sketch of proof

Our proof draws on several Lemmas of Glynn and Juneja (2004) and Russo (2016).

#### **Proof steps:**

- 1. Each treatment is assigned infinitely often.  $\Rightarrow p_T^d$  goes to 1 for the optimal treatment and to 0 for all other treatments.
- 2. Claim 1 then follows from the definition of exploration sampling.
- 3. Claim 2: Suppose  $p_t^d$  goes to 0 at a faster rate for some d. Then exploration sampling stops assigning this d. This allows the other treatments to "catch up."
- 4. Claim 3: Balancing the rate of convergence implies efficiency. This follows from the rate-optimal allocation discussed before.

## Application: Agricultural extension service for farmers in Odisha, India

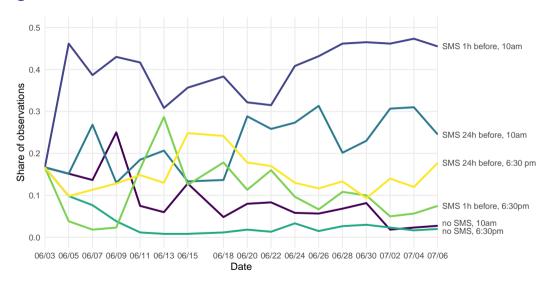
- Odisha (India), 2019.
   NGO Precision Agriculture for Development, and Government of Odisha.
- Context: Enrolling rice farmers into customized advice service by mobile phone.
  - [...] to build, scale, and improve mobile phone-based agricultural extension with the goal of increasing productivity and income of 100 million smallholder farmers and their families around the world.
- Sample: 10,000 calls, divided into waves of 600.
- 6 treatments:
  - The call is pre-announced via SMS 24h before, 1h before, or not at all.
  - For each of these, the call time is either 10am or 6:30pm.
- Outcome: Did the respondent answer the enrollment questions?

## Odisha





#### Assignment shares over time



## Outcomes and posterior parameters

Treatment			Outcomes			Posterior		
Call time	SMS alert	$m_T^d$	$r_T^d$	$r_T^d/m_T^d$	mean	SD	$ ho_T^d$	
10am	_	903	145	0.161	0.161	0.012	0.009	
10am	1h ahead	3931	757	0.193	0.193	0.006	0.754	
10am	24h ahead	2234	400	0.179	0.179	0.008	0.073	
6:30pm	-	366	53	0.145	0.147	0.018	0.011	
6:30pm	1h ahead	1081	182	0.168	0.169	0.011	0.027	
6:30 pm	24h ahead	1485	267	0.180	0.180	0.010	0.126	

 $m_T^d$ : Number of observations,  $r_T^d$ : Number of successes,  $p_T^d = P_T \left( d = \operatorname{argmax}_{d'} \theta^{d'} \right)$ .

Minimizing squared error

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Conclusion and summary

## Maximizing utilitarian welfare

- For both in-sample regret and policy regret:
   Objectives are defined in terms of observable outcomes.
- Contrast this to welfare economics / optimal tax theory:
   Objectives are defined in terms of revealed preference.
- Quantification: Equivalent variation.
   What money transfer would make people indifferent to a given policy change?
- Operationalization through the envelope theorem:
   In assessing welfare effects, we can hold behavior constant.
- Example: Optimal insurance.
  - Individual health care expenditures Y.
  - Share covered by insurance T.
  - Behavioral response  $Y = g(T, \epsilon)$ .
  - Per capita expenditures  $m(T) = E[g(T, \epsilon)]$ .

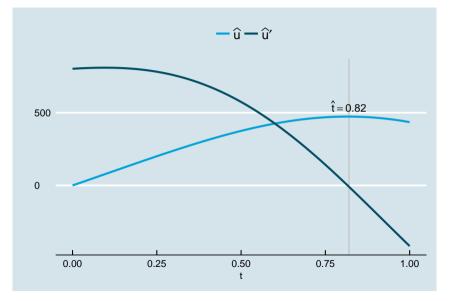
#### Deriving social welfare

- Effect of marginal change of t:
  - 1. On insurance expenditures:  $\partial_t(t \cdot m(t))$ .
  - 2. On patient welfare: m(t) (behavioral response is ignorable by envelope theorem).
  - 3. On social welfare:  $\lambda m(t) \partial_t (t \cdot m(t))$  (welfare weight  $\lambda > 1$ ).
- Integration yields social welfare:

$$u(t) = \lambda \int_0^t m(x) dx - t \cdot m(t).$$

- If we knew  $m(\cdot)$ , we could calculate this, and choose the policy  $t^* = \operatorname{argmax}_t u(t)$ .
- If we had experimental data, we could calculate the posterior expectation û of u, by plugging in the posterior expectation m̂ of m, and maximize posterior expected welfare, î = argmax t û(t)

## Example: RAND health insurance experiment, $\lambda=1.5$



## Bayesian updating (Kasy, 2019)

- Exogenously assigned T.  $Var(Y|T) = \sigma^2$ .
- Gaussian process prior for  $m(\cdot)$ ,

$$m(\cdot) \sim GP(0, C(\cdot, \cdot)).$$

• Prior covariance of u(t) and Y is D(t, T), where

$$D(t,t') = Cov(u(t), m(t')))$$

$$= \lambda \cdot \int_0^t C(x,t')dx - t \cdot C(t,t').$$

$$D(t) = (D(t,T_1), \dots, D(t,T_n)).$$

- Prior covariance matrix of outcomes **Y** is  $\mathbf{C} + \sigma^2 \mathbf{I}$ .
- Posterior expectation of u(t):

$$\widehat{u}(t) = \mathbf{D}(t) \cdot \left[ \mathbf{C} + \sigma^2 \mathbf{I} \right]^{-1} \cdot \mathbf{Y}.$$

#### Experimental design problem

- Expected welfare after the experiment:  $\max_t E[u(t)|data]$ .
- Ex-ante expected welfare:  $E[\max_t E[u(t)|\text{data}]]$ .
- Experimental design problem:

$$\underset{\text{design}}{\operatorname{argmax}} \ E[\max_t E[u(t)|\text{data}]].$$

Maximize the expectation of a maximum of an expectation!

If we allow for adaptivity:
 Additional layers of expectation and maximization for each wave.
 Numerically infeasible.

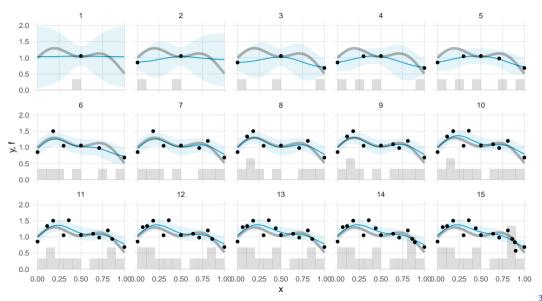
#### The knowledge gradient method

- Knowledge gradient method:
   An approximation successfully applied in the Bayesian optimization literature.
- Pretend that the experiment ends after the next wave. Solve

$$\underset{\text{assignment now}}{\operatorname{argmax}} E[\max_{t} E[u(t)| \text{data after this wave}]].$$

- This ignores the option-value of adapting in the future!
   But it provides an excellent approximation in practice.
- Work in progress:
  - Generalization to higher-dimensional policy spaces.
  - Adaptation to structural models of labor supply.
  - Modification of the method to account for wave structure.
  - Search for implementation partner.
     Basic income experiments?

#### Simulated example



#### Conclusion

- Any decision problem requires specification of an objective.
- The choice of objective matters for experimental design.
- Some possible choices:
  - 1. Squared error of effect estimates.
  - 2. In-sample regret.
  - 3. Policy-regret.
  - 4. Utilitarian welfare for policy choice.
- I discussed simple algorithms targeting each of these objectives.

## Algorithms for these objectives

1. Expected squared error: Minimize

$$Var(\beta|\mathbf{X}) - \overline{C}' \cdot (C + \sigma^2 I)^{-1} \cdot \overline{C}.$$

2. **In-sample regret** and squared error:  $\gamma$ -Thompson, with assignment probabilities

$$(1-\gamma) \cdot p_t^{dx} + \gamma/k, \qquad \qquad p_t^d = P_t \left( d = \operatorname*{argmax}_{d'} \, heta^{d'} 
ight).$$

3. Policy regret: Exploration sampling, with assignment probabilities

$$q_t^d = S_t \cdot p_t^d \cdot (1 - p_t^d), \qquad \qquad S_t = \frac{1}{\sum_d p_t^d \cdot (1 - p_t^d)}.$$

4. Utilitarian welfare: Knowledge gradient method for social welfare,

 $\underset{\text{assignment now}}{\mathsf{argmax}} \, E[\max_t E[u(t)| \text{data after this wave}]].$ 

## Summary of theoretical findings

- Randomization is sub-optimal in general decision problems:
   Randomization never decreases achievable Bayes / minimax risk,
   and is strictly sub-optimal if the optimal deterministic procedure is unique.
- 2. Measure of balance (MSE):

The expected MSE of an assignment is a measure of balance, and can be minimized for optimal assignments for estimation.

- 3.  $\gamma$ -Thompson sampling (In-sample regret and MSE): In-sample regret is asymptotically proportional to  $\gamma$ . The variance of treatment effect estimates is decreasing in  $\gamma$ .
- 4. Exploration sampling (Policy regret):

The oracle optimal allocation equalizes power across suboptimal treatments. Exploration sampling achieves this in large samples, and is thus (constrained) rate-efficient.

#### Web apps implementing the proposed procedures

- Minimizing expected squared error: https://maxkasy.github.io/home/treatmentassignment/
- Maximizing in-sample outcomes: https://maxkasy.github.io/home/hierarchicalthompson/
- Informing policy choice:
   https://maxkasy.shinyapps.io/exploration\_sampling\_dashboard/

## Thank you!