Inner Product Spaces, Orthogonality, Projection: Solutions

4 September 2018

Exercises

- 1. Let *X* and *Y* be normed linear spaces. Let $\{x_1, ..., x_n\}$ be a basis for *X* and $\{y_1, ..., y_m\}$ a basis for *Y*. Prove that if $x_i \perp y_j$ for all $i \in \{1, ..., n\}$, $j \in \{1, ..., m\}$, then *X* and *Y* are orthogonal spaces.
- 2. Prove: If a vector α is in the null space of a set of vectors $\{x_1,...,x_n\}$, then it is orthogonal to the space spanned by $\{y_1,...,y_m\}$ where

$$y_i = \{x_{1i}, ..., x_{ni}\}$$

3. Donald Trump tweeted 100 times in April, 150 times in May, and 110 times in June. Let b = (100, 150, 110) represent the number of tweets in each month. Project b onto the space spanned by a = (1, 1, 1). Interpret your result.

¹ Disclaimer: these data are of suspect quality.