

Priors: pros & cons

Having a *prior* distribution:



brings **flexibility**



allows to incorporate **external knowledge**



adds intrinsic **subjectivity**

⇒ choice (or elicitation) of a *prior* distribution is sensitive !

Prior properties

- 1 *posterior* support must be included in the support of the *prior*:
if $\pi(\theta) = 0$, then $p(\theta|\mathbf{y}) = 0$
- 2 independence of the different parameters *a priori*

Prior Elicitation

Strategies to communicate with non-statistical experts

⇒ transform their **knowledge** into *prior* **distribution**

- **histogram method**: experts give weights to ranges of values
⚠ might give a zero *prior* for plausible parameter values
- choose a **parametric family** of distributions $p(\theta|\eta)$ in **agreement with what the experts think** (e.g. for quantiles or moments)
(solves the support problem but the parametric family has a big impact)
- elicit *priors* from the **literature**
- ...

The quest for non-informative *priors*

Sometimes, one has **no prior knowledge whatsoever**
Which *prior* distribution to use ?



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2 major difficulties:

- 1 **Improper distributions**
- 2 **Non-invariant distributions**

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Other solutions ?

Jeffreys' *priors*

A **weakly informative prior** invariant through re-parameterization

- unidimensional Jeffreys' *prior*:

$$\pi(\theta) \propto \sqrt{I(\theta)} \quad \text{where } I \text{ is Fisher's information matrix}$$

- multidimensional Jeffreys' *prior*:

$$\pi(\theta) \propto \sqrt{|I(\theta)|}$$

In practice, parameter are considered independent *a priori*