

Notes: The Distributional Consequences of Trade and Policy Responses.

What are the distributional impacts of trade? And what can policy do to alleviate the negative consequences of trade? These are the questions that interest me and the goal of this course is to provide a limited introduction to the recent literature studying these issues. By limited, I'm going to provide you my world view of these issues in the literature by organizing it around my own work in: Lyon and Waugh (2019), Lyon and Waugh (2018), and Waugh (2019).

While this is a limited view (I only have 3 meetings), I do want to emphasize that there are issues here which are way broader than trade. In fact, some of the most important policy issues that we are facing today regard distributional issues associated with technical change (i.e., robots) and immigration. And what I'm going to talk about relate very closely. Specifically, the empirical techniques used to measure distributional impacts and the modeling approaches to infer the aggregate, welfare, and policy prescriptions are directly applicable to these issues mentioned above. So what I'm saying is if you are looking for a PhD thesis topic/job market paper, these are not bad places to start.

1. What is the issue?

A. High-Level

At a high-level, here is how I think of the issues at hand: In the US, there has been a dramatic rise in inequality over the last 40 years. My take is that for a while the discussion about these issues focused essentially on technological change and the role that it plays. Moreover, inequality/distributional issues were viewed as second-order to issues such as economic growth or cross-county income inequality (Lucas makes this point well). From the a trade perspective, inequality issues were always recognized and a core issue in the literature (H-O model predicts this), but it was hard to find trade driven inequality in the data on top of the problems associated with the H-O model.

I think a couple of things changed within the past 10 years that generated a lot of interest. One is the Great Recession in the US and the observations (particularly of Mian and Sufi (2014)) regarding the role that distributional issues played in it. That is some guys had housing wealth that collapsed and these were the guys that bore the brunt of the shock. Second, from the trade perspective, was the work of Autor, Dorn, and Hanson (2013), who found large distributional effects from China's rise in early 2000's. This is, perhaps, the first time one really saw trade matter with respect to inequality. Overall, one way to put this is the following: **at the center of the two most important (aggregate) macroeconomic events of the 2000s—rise of China and Great Recession—are distributional issues.**

Also important to reflect on is this: The two key papers here both essentially use the same research design of a local-labor-markets approach. That is they thought about a labor market as being associated with a narrowly defined geography. And then studied how differential exposure of that geography correlates with exposure to China or a credit shock. In this sense, the distributional issues seem strongly related

to the spatial distribution of activity.¹ This fact shapes my thinking a lot about these issues as you will see below.

A third issue is technological change. I think the profession has made a lot of progress in working with heterogeneous agents (firms, workers, consumers). 10 years ago, there was a lot. Now there is even more. So the point is that we have even better models/computational approaches for dealing with these issues.

Finally, and this is just casual observations, but distributional issues seem first-order to understanding the political change in the US, UK, elsewhere. Hence, economists are revisiting these issues. Forget about trade, just think about the huge explosion of papers talking about competition, market power, labor share, etc. are all motivated by distributional concerns.

B. Low-Level

As mentioned above, it is empirical observations (the diff-in-diff evidence) that drive the boat here. At a low-level, the research question(s) are really about this: **While the diff-in-diff evidence are what they are, the key issue is interpretation.** Interpretation is very nuanced for a lot of reasons, I'm going to focus on two:²

- **Level and general equilibrium effects.** While the diff-in-diff evidence is super compelling, it has a huge weakness in that it can never tell you about what is going on with the level (and GE effects). The trade case is really clear. A perfectly plausible interpretation of the Autor et al. (2013) evidence is that all labor markets gained, just some gained more than others. Why? The simplest story is through GE where the price of goods is falling making all households better off, even though some labor markets perform relatively worse than others.
- **So what? The normative implications.** Again the diff-in-diff is super compelling, but what should a policy maker do? The diff-in-diff evidence tells us nothing! You can't look at Autor et al. (2013) and say, well we should not trade with China. And by placing a tariff on Chinese goods will save jobs. Yet the irony is that diff-in-diff evidence is so compelling/interesting it cries out for some kind of investigation into what good policy might look like.

A solution to these issues is layer in an economic model to help us better understand the "real world evidence" in a controlled environment where we know what is going on. Economic models have weaknesses, i.e. they rely upon strong assumptions about preferences, technology, market behavior. But being explicit about the environment is also a strength, it allows us confront these assumptions and determine if they are important to the model's interpretation of the evidence and then further refine.

¹I could go on forever about this. At first glance you might think this is natural, but in some sense it's odd. You could still have large distributional effects, but it is within a geography and the local-labor-markets approach would not detect them. Another way to see this is to measure income inequality across county's say in the US. It virtually tracks the change in inequality using individual-level data.

²As an example of stuff I will omit, I'm not even going to touch or engage the explosion of papers revisiting Bartik and Shift-Share approaches.

Second, within an economic model, one can evaluate outcomes associated with different policy. And even think about the best policies (in a formal sense). This is my goal.

A final point that I alluded to above is this: the local-labor-markets approach is predicated on the idea that labor is not moving (at least in the short run). Thus, these research designs are avoiding what is perhaps the **BIG** question: **Why is not labor moving to exploit spatial arbitrage opportunities?**

2. Data, Model, Data

A. Data

Per the discussion above, the “want operator” is to think about an empirical relationship that takes the form:

$$\Delta \log Y_{it} = \beta \Delta \log Z_{it} + \gamma_t + \epsilon_{it}. \quad (1)$$

where Y_{it} is some outcome in i at t and Z_{it} is some “shock”. There is a time fixed effect to control for aggregate changes. And everything is done in differences. This is a classic difference in difference specification. The i variable is often geography, something like a county or a commute zone (measure of a local labor market). The shock might be actual trade flows (we can talk about how they do this), tariffs as in my new paper Waugh (2019), a measure of trade uncertainty in Pierce and Schott (2016), etc. Note also this is essentially the same specification that Mian, Rao, and Sufi (2013) use in their stuff. It also looks a lot like the stuff that Townsend (1994) was doing on risk sharing in village India.

Now here are some specific issues that we want to think about:

- The error term. What is this? What are the issues? Why might there be problems? Autor et al. (2013) make a huge deal of this. I found it very hard to think through the issues until I did the stuff below. Often the discussion of the error term often gets overall focused on econometric issues. Fine. **But from an economic standpoint, it’s in the error term that some of the most interesting economic questions lie.**
- What is β ? You can appeal to some mumbo-jumbo about causal effect, but is this a parameter? A mixture of things (endogenous and exogenous)? If so how does it map into primitives? This steps need to be made when going from the empirical results to normative statements.
- The aggregate effects. If you are new to this, it might not seem obvious, but all the action is embedded in the time effect. We will see this below.

Again, what is the want: I want to understand what 1 is all about. To do so, all I’m going to do is to make a slight, but obviously important departure from the Canonical Ricardian model of trad—add the immobility of labor—and then work through the implications.

B. A Brief Primer on Ricardian Models and Eaton and Kortum (2002)

Here is my quickest introduction.

Production. Within a country, there is a continuum of intermediate goods indexed by $\omega \in [0, 1]$. As in the Ricardian model of Dornbusch, Fischer, and Samuelson (1977) and Eaton and Kortum (2002), intermediate goods are not nationally differentiated. Thus, intermediate ω produced in one country is a perfect substitute for the same intermediate ω produced by another country. Competitive firms produce intermediate goods with linear production technologies,

$$q(\omega) = z(\omega)\ell, \quad (2)$$

where z is the productivity level of firms and ℓ is the number of efficiency units of labor. Intermediate goods are aggregated by a competitive final-goods producer who has a standard CES production function:

$$Q = \left[\int_0^1 q(\omega)^\rho d\omega \right]^{\frac{1}{\rho}}, \quad (3)$$

where $q(\omega)$ is the quantity of individual intermediate goods ω demanded by the final-goods firm, and ρ controls the elasticity of substitution across variety, which is $\theta = \frac{1}{1-\rho}$. Transporting intermediate goods across countries is costly. Specifically, consumers and firms face iceberg trade costs when importing and exporting their products. The demand curve in (3) gives rise to the following demand curve for an individual variety:

$$q(\omega) = \left(\frac{p(\omega)}{P_h} \right)^{-\theta} Q. \quad (4)$$

where Q is the aggregate demand for the final good; P_h is the price associated with the final good which will be carried around.

Households. The basic way to think about this is that there is a representative consumer that eats Q and supplies labor inelastically (which we will normalize to one) to **any labor market within the country**. This is the free-labor mobility assumption that is standard/implicit in Ricardian models of trade.

Countries. To keep things simple, just imagine that there is the home country and a large ROW (which would be a collection of other countries). The way we will do this is the ROW, we will say that there are some prevailing world prices for each commodity ω which I will denote as $p_w(\omega)$.

Sketch of an equilibrium and how trade works. Ok, so let's just make a couple of observations.

- The first observation is that within a country, the key equilibrium price is the wage rate w . This wage is the same independent of the labor market / goods-producing sector / etc. This derives from the (within-country) free mobility of labor assumption. It's nice, but bad if you want to think about distributional issues.

- Why is it the key price? Because with free labor mobility (and CRS production function) know that price of any good is independent of who works there, if it's sold, etc. Given competitive firms and that they face the wage rate w , we know that their marginal cost (and hence price at which they are willing to sell the good domestically) must be

$$p(\omega) = \frac{w}{z(\omega)}. \quad (5)$$

This is why I love the Ricardian model. Think about this, who can sell at a low price. Well if your wage is low, so this helps China or Bangladesh. Or if your technology is really good, so if $z(\omega)$ is large, this helps the US and Germany. Then the most interesting part is how technology interacts with the wage to determine who trade what, etc.³

- Who buys what from whom? Second reason why I love the Ricardian model is that really is just an application of the min operator. So buy the good from the country with the lowest price:

$$\min \left\{ \frac{w}{z(\omega)}, \tau p_w(\omega) \right\} \quad (6)$$

where the thing on the left is the domestic price, and then the thing on the right is on the world price (inclusive of the trade cost).

- What I'm going to do is a bit strange, but it will help set up the next model. First, understand this: If the good is purchased from home, then we know there are workers there, they earn w . And how many workers are there? Well enough so that domestic demand (and possible foreign demand, i.e. exports) equals foreign supply, this would be inferred from the demand curve in (4).

Now let's think of some off equilibrium action. Consider a good ω where the world is the low cost producer, so the prevailing domestic price is $\tau p_w(\omega)$. If a domestic firm were to produce, it would have to be selling at that price. Ok. If it were to hire workers, the wage it could pay would equal $\tau p_w(\omega)z(\omega)$ or the value of the marginal product of labor. But we know from above that $\tau p_w(\omega)z(\omega) < w$. And because of free mobility of workers, no workers would accept that wage $\tau p_w(\omega)z(\omega)$.

So the domestic firm producing variety ω does not operate. No workers are actually ever "exposed to import competition." Again this is all about the free mobility of labor assumption.

- The distributional assumption to facilitate aggregation. A core insight of Eaton and Kortum (2002) is to treat the $z(\omega)$ as a random variable and then exploit the distributional assumptions to aggregate. The second insight is to pick a distribution that can handle the min (or max operator) easily, and that is the Frechet distribution. I won't get into the details about how to derive this. But to see how this works, think about how you would go about using simulation to compute trade flows.

³This is what distinguishes Eaton and Kortum (2002) from saying it is just an application of discrete choice theory.

- Step 1: Assume a distribution for z and p_w . Note I'm dropping the ω subscript as we can treat each good symmetrically given the demand curve associated with 3.
- Draw a bunch of pairs of z and p_w .
- Given a wage, for each pair of z and p_w figure out who is low cost supplier and compute demand, etc.
- Make sure labor demand equals labor supply. Note in this is the same as ensuring that trade is balanced (it's a static model). If not update the wage.

What have we learned. Not much. We built intuition for a more complicated setting in which labor is not mobile. As mentioned above, this is a key issue just to even get off the ground and start to think about distributional issues and trade.

C. Immobile Labor + Eaton and Kortum (2002) = Static Lyon and Waugh (2019)

So here is what I'm going to do. I'm going to think about a repeated static world of the model above, but where labor can not move. These I think are the minimal departures from the model above to think about the diff-in-diff approach and evidence.

First, I'm going to say that good-level productivity and world-prices take discrete states and follow a first order Markov chain, with $\mathcal{P}(z'|z)$ being the probability that z transits to z' . Similarly for world prices p_w .

Important! I'm going to assume that the evolution of z and world prices p_w are orthogonal to each other. Why is this important, wait for it. Now define \mathbf{s} as the domestic productivity and world price combination associated with that island, $\mathbf{s} = \{z, p_w\}$. We denote $\pi(\mathbf{s})$ as the stationary distribution of productivity states and world prices induced by the Markov Chain.

Important step! Denote $\mu(\mathbf{s})$ as the measure of households working on an island with state \mathbf{s} . The key issue is they can only work on islands of state \mathbf{s} . **They can not move.** Where does $\mu(\mathbf{s})$ come from? I'll layer a model of migration on this to determine it in equilibrium. But for now, just think of it as given. Second, note what this is doing in that what it is doing is tying the product space and the geography together. This is what I call "company towns" where a location is completely specialized in a product.

Wages. Competition implies that the wage at which a firm hires labor is:

$$w(\mathbf{s}) = p(\mathbf{s})z \quad (7)$$

or the value of the marginal product of labor. Only at the wage in (7) are intermediate-goods producers willing to produce. Notice how this is different than (5). Now the wage is indexed by the island specific state \mathbf{s} ! Why labor can not move across locations and try and exploit a wage differential. Instead the household is "captive" at wage rate $w(\mathbf{s})$.

International trade and market clearing. Like in the Eaton and Kortum (2002) world the final-goods producer purchases intermediate goods from the low-cost supplier (it's still a Ricardian model). But

now this decision gives rise to three cases with three different market-clearing conditions: if the good is non-traded; if the good is imported; and if the good is exported and hence different forms of price determination. What's the issue here? Unlike the simple Ricardian model, there is not one wage for which all prices goods prices can be inferred from. Now prices must actually be determined by labor demand and labor supply subject to the option to buy and sell abroad. Below, we describe demand and production in each of these cases.

- **Non-traded.** If the good is non-traded, then the domestic price for the home country must satisfy the following inequality: $\frac{p_w}{\tau_{ex}} < p(\mathbf{s}) < \tau_{im}p_w$. That is, from the home country's perspective, it is optimal to source the good domestically and not optimal for the home country to export the product.

In this case, the market-clearing condition is:

$$\left(\frac{p(\mathbf{s})}{P_h} \right)^{-\theta} Q = z(\mu(\mathbf{s})/\pi(\mathbf{s})) \quad (8)$$

or that domestic demand equals production. The left-hand part is demand and the right-hand side is supply. That is the the productivity of domestic suppliers multiplied by the supply of labor units in that market.

- **Imported.** If the good is imported, then the domestic price for the home country must be $p(\mathbf{s}) = \tau_{im}p_w$. Why? If the price were lower, then it would not be imported. If the domestic price were higher, then the good will be imported with no domestic production and, thus, the prevailing domestic price will equal the imported price. With frictional labor markets, there may be some domestic production so the quantity of imports is

$$\underbrace{\left(\left(\frac{\tau_{im}p_w}{P_h} \right)^{-\theta} Q \right) - z(\mu(\mathbf{s})/\pi(\mathbf{s}))}_{\text{imports}} > 0. \quad (9)$$

That is home demand (net of home production) is met by imports of the commodity. Rearranging gives

$$\left(\left(\frac{\tau_{im}p_w}{P_h} \right)^{-\theta} Q \right) = z(\mu(\mathbf{s})/\pi(\mathbf{s})) + \text{imports}(\mathbf{s}) \quad (10)$$

or domestic demand equals domestic production plus imports.

- **Exported.** If the good is exported, then the prevailing price must be $p(\mathbf{s})\tau_{ex} = p_w$. Why? If the home price were larger, then the good would not be purchased on the world market. And the price can not be lower, as arbitrage implies that the price of the exported good sold in the world market must equal the prevailing price in that market. Finally, note that only the trade cost, not the tariff,

matters here. At this price, the quantity of exports is

$$\underbrace{\left(\frac{p_w/\tau_{ex}}{P_h}\right)^{-\theta} Q - z(\mu(\mathbf{s})/\pi(\mathbf{s}))}_{- \text{ exports}} < 0 \quad (11)$$

or domestic demand net of production which should be negative, implying that the country is an exporter. Rearranging gives

$$\left(\frac{p_w/\tau_{ex}}{P_h}\right)^{-\theta} Q = z(\mu(\mathbf{s})/\pi(\mathbf{s})) - \text{ exports}(\mathbf{s}) \quad (12)$$

or domestic demand equals domestic production minus exports.

A sketch of an equilibrium Hopefully that you see that this is far more intricate than the simple Ricardian model for the reason that an equilibrium is a collection of prices $\{p(\mathbf{s})\}$ for each location that satisfy the demand and supply conditions discussed above. Then for everything to add up a simple condition would be for balanced trade to hold (like in the simple Ricardian model above). To see this last point we can work through the idea that production must equal expenditure. The the value of aggregate production of the final good must equal the value of intermediate goods production

$$Q = \int_{\mathbf{s}} p(\mathbf{s}) z \mu(\mathbf{s}) \quad (13)$$

which we can then connect with the expenditure side of GDP through the market clearing conditions for intermediate goods and final goods. Specifically, by connecting the production side with the demand side for non-traded goods in (8), imports in (10) and exports in (12) and the equating final demand with consumption we have

$$Q = C + \int_{\mathbf{s}} p(\mathbf{s}) \text{ exports}(\mathbf{s}) - \int_{\mathbf{s}} p(\mathbf{s}) \text{ imports}(\mathbf{s}). \quad (14)$$

Or GDP equals consumption (market) plus exports minus imports. Then with balanced trade (again, it's a static model), we get that output will equal what people are eating.

D. Trade

To illustrate the pattern of trade across islands, first define the following statistic:

$$\omega(\mathbf{s}) := \frac{p(\mathbf{s}) z \mu(\mathbf{s})}{p(\mathbf{s}) z \mu(\mathbf{s}) + p(\mathbf{s}) \text{ imports}(\mathbf{s}) - p(\mathbf{s}) \text{ exports}(\mathbf{s})}. \quad (15)$$

What does equation (15) represent? The denominator is the value of domestic consumption: everything domestically produced plus imports minus exports. The numerator is production. The interpretation of (15) is how much of domestic consumption at the island/variety level the home country is producing.

This is similar to the micro-level “home share” summary statistic emphasized in Arkolakis, Costinot, and Rodríguez-Clare (2012). As we discuss below, this statistic (i) provides a clean interpretation of a labor market’s exposure to trade and (ii) is tightly connected with local labor market wages.

Figure 1 plots the home share (raised to the power of inverse θ) by world price and home productivity. There are three regions to take note of: where goods are imported, exported, and non-traded. First, in the regions where the home share lies below one, demand is greater than supply, and, hence, goods are being imported. This region naturally corresponds to the situation with low world prices or low home productivity—i.e. the economy has a comparative disadvantage in producing these commodities.

Second, in the regions where the home share lies above one, supply is greater than demand, and, hence, goods are being exported. This region corresponds to high world prices or high home productivity. In other words, this is where the country has a comparative advantage and is an exporter of the commodities.

Third, there is the “table top” region in the middle, where the home share equals one. Hence, this is the region where the goods are non-traded. Exactly like the inner, non-traded region in the Ricardian model of Dornbusch et al. (1977), the reason is trade costs. In this region, world prices and domestic productivity are not high enough for a producer to be an exporter of these commodities given trade costs. Furthermore, world prices and domestic productivity are not low enough to merit importing these commodities either. Thus, these goods are non-traded.

E. Trade and Wages

One can connect the pattern of trade across islands/labor markets in Figure (1) with the structure of wages in the economy. As we show in the Appendix, real wages in a market with state variable \mathbf{s} equal

$$w(\mathbf{s}) = \omega(\mathbf{s})^{\frac{1}{\theta}} \hat{\mu}(\mathbf{s})^{\frac{-1}{\theta}} z^{\frac{\theta-1}{\theta}} Q^{\frac{1}{\theta}}. \quad (16)$$

Here $\omega(\mathbf{s})$ is the home share defined in (15); $\hat{\mu}(\mathbf{s}) = \frac{\mu(\mathbf{s})}{\pi(\mathbf{s})}$ is the number of labor units; z is domestic productivity; C is aggregate consumption. Below we walk through the algebraic steps to deriving the relationship discussed above. Note the general insight about this: CES models provide a very tight relationship between expenditure shares and prices, this is what I’m exploiting here.

1. Begin with the following (generalized) labor demand and supply conditions in units of the final good:

$$p(\mathbf{s})\pi(\mathbf{s}) \left(\frac{p(\mathbf{s})}{P_h} \right)^{-\theta} Q = p(\mathbf{s})z\mu(\mathbf{s}) + p(\mathbf{s})\text{imports}(\mathbf{s}) - p(\mathbf{s})\text{exports}(\mathbf{s}), \quad (17)$$

where by generalized we mean that the last two terms are only active if the good is imported or exported.

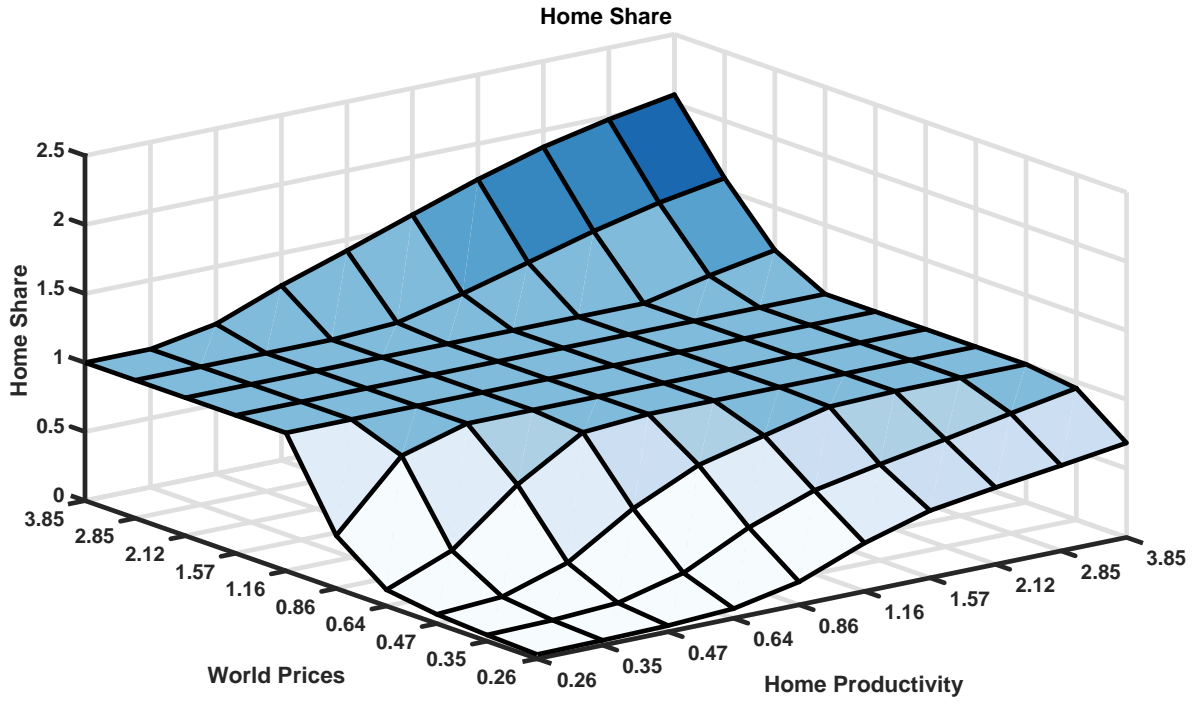


Figure 1: Trade: Home Share, $\omega(\mathbf{s})^{\frac{1}{\theta}}$

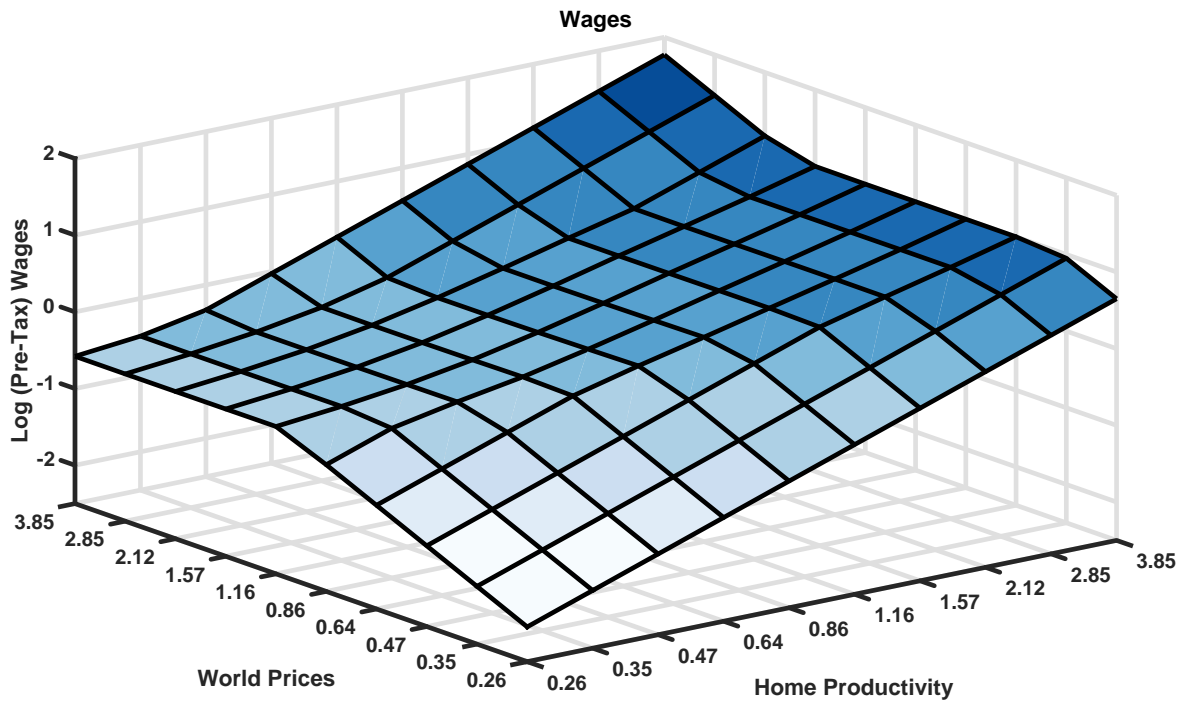


Figure 2: Wages

2. Divide both sides by $p(\mathbf{s})z\mu(\mathbf{s})$ so that we have

$$\frac{p(\mathbf{s})\pi(\mathbf{s})}{p(\mathbf{s})z\mu(\mathbf{s})} \left(\frac{p(\mathbf{s})}{P_h} \right)^{-\theta} Q = \omega(\mathbf{s})^{-1} \quad (18)$$

And now the left hand side is in terms of the home share for the good that the local labor market produces. The key issue is that not all of world prices cancel out and we need to some how connect this with wages. Thus, the next step

3. Then we combine this with how wages are set. Wages equal the value of the marginal product of labor...

$$w(\mathbf{s}) = \frac{p(\mathbf{s})z}{P_h}, \quad (19)$$

so wages reflect prices. Then if you carefully examine (7) and (18), you notice that the relationship between wages and prices and how you can substitute one for each other in the demand curve giving.

$$\frac{\pi(\mathbf{s})}{z\mu(\mathbf{s})} \left(\frac{w(\mathbf{s})}{z} \right)^{-\theta} Q = \omega(\mathbf{s})^{-1} \quad (20)$$

4. Now it is simply about rearranging terms and then substituting in the market clearing condition of Q with consumption C which gives rise to the following:

$$w(\mathbf{s}) = \omega(\mathbf{s})^{\frac{1}{\theta}} \hat{\mu}(\mathbf{s})^{\frac{-1}{\theta}} z^{\frac{\theta-1}{\theta}} Q^{\frac{1}{\theta}}. \quad (21)$$

Equation (16) connects the trade exposure measure in (15) with island-level wages. A smaller home share implies that wages are lower with elasticity $\frac{1}{\theta}$. This means that if imports (relative to domestic production) are larger, then wages in that labor market are lower. Similarly, a larger home share means that wages are higher. While this looks like the “micro-level” analog of the aggregate result of Arkolakis et al. (2012) it is different in one important respect: the micro-level wage response to micro-level trade exposure to trade takes the exact opposite sign.

Figure 2 illustrates these observations by plotting the logarithm of pre-tax wages by world price and home productivity so it exactly matches up with Figure 1. As equation (16) makes clear, there is a tight correspondence between wages and the home share in Figure 1. As in Figure 1, there are three regions to take note of.

The first region is where import competition is prevalent (low world prices or low home productivity) wages are low. A way to understand this result is as follows: wages reflect the value of the marginal product of labor. In import competing islands, trade results in lower prices and, hence, lower wages. The second region is where exporting is prevalent. Exporting regions are able to capture high world prices, and, thus, wages are high in these islands. Finally, the center region is where commodities are

non-traded. Here, the gradient of wages very much mimics the increase in domestic productivity. In contrast, where goods are imported or exported, the wage gradient mimics the change in world prices.

What have we achieved? Remember the problem with the standard Ricardian model was that labor mobility killed any way to think about distributional issues. There was one wage. So while Figure 1 would look the same in the mobile vs. immobile labor model; Figure 2 would look radically different. In the standard Ricardian model, there would be flat surface which is independent of productivity or wages. In contrast, the immobile labor model delivers a relationship between how much labor is exposed to trade and the wage that labor earns.

F. Back to Data: The ADH Equation

The preceding results relate closely to the empirical specification and evidence of Autor et al. (2013). To do illustrate the connection, start with (16) and take log differences across time yielding

$$\Delta \log w(\mathbf{s}) = \underbrace{\frac{1}{\theta} \Delta \log (\omega(\mathbf{s})/\hat{\mu}(\mathbf{s}))}_{\beta} + \underbrace{\frac{1}{\theta} \Delta \log Q}_{\gamma_t} + \underbrace{\Delta \log \left(z^{\frac{\theta-1}{\theta}} \right)}_{\epsilon_{s,t}}, \quad (22)$$

which says that the change in wages across locations is summarized by (i) trade exposure via the change in per-worker home share, (ii) the change in aggregate consumption and (iii) the change in location-specific productivity. Equation (22) is the empirical specification in equation (1).

Now recall the issues we wanted to think about:

- **The error term. What is this? What are the issues?** The error term reflects the unobserved, local productivity shock. This is nice because we have a clear understanding of the problem. There is something confounding the story when we see a labor market with low/declining wages. Is it because the technology is bad? Or is it trade? The model here creates this nice tension! Note this is the classic issue, e.g. steel plants in the US are constantly saying their issues are related to trade, but they also have outdated technology. Which is it?

Now if absolute advantage was uncorrelated with comparative advantage, then from an econometric stand point (I think things are ok). The problem is that if comparative advantage aligns with absolute advantage (i.e. most productive places are also likely to have a comparative advantage (and this is the natural case and what comes out of Eaton and Kortum (2002)), the error term is correlated with a localities trade exposure. Thus an instrumental variable strategy is necessary to identify the causal effect of trade exposure on wages. **Deep/non-trivial insight: through Ricardian comparative advantage, the local productivity shock will be correlated with a localities import exposure!**

The structure of the model suggests several instrumental variable strategies. One valid instrument would be to use the world price (if observed) directly. The world price is orthogonal to domestic productivity (the exclusion restriction), yet correlated with the home trade share. The exclusion

restriction follows from our assumption that the stochastic process in for world prices is assumed to be orthogonal to z .⁴ An alternative strategy would be to use another country's imports as an instrument. Another country's imports would be orthogonal to the home country's productivity, but correlated with world prices. This, in fact, is quite similar to the instrument proposed in Autor et al. (2013).

- **What is β ?** It tells us something about the labor demand curve. Which in this model, labor demand is derived from the CES production function. Hence it tells us something about how substitute products are across space. This is progress because now we can use external evidence to validate this.

Can you work this out? What if there was a simple labor supply curve in each location? Would that show up in this. What about an employment equation?

- **The aggregate effects.** These are all embedded in the time effect. And the way I wrote this done, the only aggregate variable is consumption (if, for example, I was carrying around a TFP term, this would show up here as well. Note, need to do this). Here is why the diff-in-diff stuff is so problematic. Any change in aggregate trade exposure will also change in aggregate consumption, i.e. the C term. That is all workers benefit from the "aggregate gains to trade", but the island-level incidence will vary with its trade exposure and may mitigate or completely offset the aggregate benefits from trade. In the static version of this model, this is the key general equilibrium effect. If labor supply were variable, then this would also move aggregate consumption as well.

If you stare at this long enough, you really start to understand why it is so hard to jump from the coefficient β , i.e. more trade leads to lower wages, without factoring in what is going on with the aggregate effect.

A couple of final points? Ok, why not just read off the time effect and... hold on. The example of TFP is relevant here in that the time effect will embed GE forces and exogenous changes like technological change so you can't separate them out. One thought to solve this issue is to use the model which would impose some "cross-equation" restriction so that the GE component of the diff-in-diff time effect can be reverse engineered. For example, micro-found labor supply and I'm sure that there would be a time effect showing up as well. Maybe we should work on this.

⁴Moreover, the model makes clear that one should be concerned, in general equilibrium, that a change in domestic productivity would feed into world prices and, thus, invalidate this strategy.

3. The ADH Data

Open up notebook on github:

- Aggregate Facts
- Trade on income and wages
- Employment effects
- Social assistance

A. Open Issues

- What is up with manufacturing vs. non-manufacturing?
- 1990s is a Red Herring, 2000s is where the action is.
- Migration issue

4. Static Model of Migration/Labor Supply

So I want to connect these results with the literature (specifically Artuç, Chaudhuri, and McLaren (2010), Caliendo, Dvorkin, and Parro (2015), Galle, Rodriguez-Clare, and Yi (2015)) on migration and labor supply and more generally the “quantitative spatial models” many people have worked on recently. I’m going to present a static framework along the lines of Caliendo et al. (2015) (which is a dynamic framework), but then at the end circle back and discuss where the dynamics are important and how they matter. Full disclosure, I have conflicting opinions on these models being (i) these are great models for developing understanding and intuition about the world but (ii) have some questionable implications that I will comeback to at then end.

The basic setup is a Roy model. That is workers are heterogenous as in that they are endowed with a vector of preferences specific to each island \mathbf{s} . In the derivations below, I’m going to think about two types of islands \mathbf{s}_h and \mathbf{s}_l , but this is not important. I will provide the general formulas a bit latter (as practice you might want to derive them your self). A workers utility associated with working in an island is (say, of type h) is

$$\varepsilon(\mathbf{s}_h)w(\mathbf{s}_h) \quad (23)$$

where ε_h is the workers preference for being in location h and $w(\mathbf{s}_h)$ is the wage discussed above. A couple of notes about this formulation. The multiplicative shock may seem strange, but it is essentially the same formulation as Caliendo et al. (2015). There, they have log preferences and additive preference shocks with a distributional assumption on the additive shocks which are equivalent to a log transformation of the shocks outline above. A worker then chooses the location that delivers maximal utility.

$$\max\{ \varepsilon(\mathbf{s}_h)w(\mathbf{s}_h) , \varepsilon(\mathbf{s}_l)w(\mathbf{s}_l) \} \quad (24)$$

Note that already you can get a sense of some of the issues with this formulation. When you see somebody in a location, even if wages are bad, or the labor market looks bad, this model says the reason the guy is there is because he has a strong preference for this location. In other words, it’s where he wants to be.

Timing. Again, this will be a repeated static model. Each period all states are revealed including the shocks ε associated with each island type \mathbf{s} . Then the workers chose where to work given complete information. The next period/day/year things start anew.

Now the want operator here is to connect the individual workers choice in (24) with the measure of workers $\mu(\mathbf{s})$ that determine labor supply and production within each location. To do so we will use the Eaton and Kortum (2002) insight to chose an well behave distribution on preferences with respect to the max operator above. So across the population of workers, preferences for each island state \mathbf{s} are

distributed according to independent Frechet distributions:

$$G(\varepsilon(\mathbf{s})) = \exp(-T(\mathbf{s})\varepsilon(\mathbf{s})^{-\gamma}). \quad (25)$$

The $T(\mathbf{s})$ parameter controls the average preference of a worker in island type \mathbf{s} and then γ controls the dispersion. This is parameterized as in Eaton and Kortum (2002) so a larger θ means there is less dispersion in preferences. I'm not going to do much with the $T(\mathbf{s})$, but one way to think about it is that in reduced form it could represent the idea that some islands with different states are more desirable than others. The common γ here is important though because without it the nice math below will not work out.

A. Deriving the Employment Shares

So we want to derive the employment shares—given an equilibrium wage. Note—for a second I will stop carrying around the \mathbf{s} . So to compute the share of workers choosing to be in \mathbf{s}_h , it boils down to computing the following probability:

$$\text{Prob}(w_h \varepsilon_h > w_l \varepsilon_l) = \text{Prob}(\tilde{w} \varepsilon_h > \varepsilon_l) = \int_0^\infty \left[\int_0^{\tilde{w} \varepsilon_h} g(\varepsilon_h, \varepsilon_l) d\varepsilon_l \right] d\varepsilon_h \quad (26)$$

where \tilde{w} is the relative wage. Equation 26 says the following: First, fix a ε_h and compute the probability that $\tilde{w} \varepsilon_h$ is larger (this is the inside bracket). Second, integrate over all possible ε_h s (this is the outside bracket). This then computes the probability that a worker selects into a type h island. Furthermore, notice that the inside bracket is just the marginal distribution $G'_{\varepsilon_h}(\varepsilon_h, \tilde{w} \varepsilon_h)$ evaluated at $\tilde{w} \varepsilon_h$.

Plugging in the Frechet distribution into Equation (26) and evaluating the integral we get

$$\mu(\mathbf{s}_h) = \text{Prob}(w_h \varepsilon_h > w_l \varepsilon_l) = \int_0^\infty \left[\int_0^{\tilde{w} \varepsilon_h} g(\varepsilon_h, \varepsilon_l) d\varepsilon_l \right] d\varepsilon_h = \frac{T_h w_h^\gamma}{T_l w_l^\gamma + T_h \tilde{w}^\gamma} \quad (27)$$

which is the standard share formula. So if workers receive a relatively higher wage in island h , then this means that the share of workers on island type h will be larger. Second, returning to T s, this says if island type h is a more “attractive” place to be in a utility sense, then more people will live and work there. Finally, note as well how a location is a relative statement. It's never about in absolute terms one place is better than the other, but how one place is relative to the “average” location (the object in the denominator) that matters.

Now to match it up with the model discussed above recall that there were a discrete number of states \mathbf{s} (the cross of z by p_w) which we will denote as N . Second, let's not worry about differences in T s across island states, so we can simply assume that the T s take the same value, one for example. Using the same algebra as above, the general formula is

$$\mu(\mathbf{s}) = \frac{w(\mathbf{s})^\gamma}{\sum_{\mathbf{s} \in \mathcal{S}} w(\mathbf{s})^\gamma} \quad (28)$$

Again, islands with higher wages will have more people working on them. This is what a lot of researchers in trade/spatial literature call the “labor supply curve.” It says that as wages in an island type increase, the supply of labor increases with elasticity γ . A couple of points about this labor supply curve:

- This setup does nicely pick up the idea that labor will act like it is fixed within a location, but how much labor is fixed there will depend upon the wage in that location. Labor will be in every location, like we started with. Do you know why?
- The elasticity γ plays the following role. As γ becomes larger, a given change in wages will translate into a larger change in the share of workers working there. Why? As γ becomes larger, the preference shocks become less dispersed. So workers are now more “sensitive” to wage considerations when choosing a location. In contrast, as γ becomes small, preferences matter more and thus a larger wage response is needed to get people to move.
- Also, reflect on this. In the standard Ricardian model with free mobility of labor, this is like γ becoming arbitrarily large. In other words, the labor supply curve becomes flat with its intercept at the one, common, equilibrium wage.
- Note that this way different than your traditional “macro” labor supply discussion. There the issues are either about intensive margin (hours worked) or extensive margin (work or not).⁵ Here the margin is really about location or migration. This is a relevant margin that I think the traditional macro labor supply literature has not thought about much. And is an important issue given the decline in migration in the US. But the repeat static nature of things does strain the interpretation here of this being a model of migration.

From here we can then setup the system of equations that an equilibrium must satisfy. Specifically, the following (generalized) labor demand and supply conditions in units of the final good:

$$\pi(\mathbf{s}) \left(\frac{p(\mathbf{s})}{P_h} \right)^{-\theta} Q = z \left(\frac{w(\mathbf{s})^\gamma}{\sum_{s \in \mathcal{S}} w(\mathbf{s})^\gamma} \right) + \text{imports}(\mathbf{s}) - \text{exports}(\mathbf{s}), \quad (29)$$

where the left-hand side is the total quantity demanded and then the right-hand supply is the quantity supplied. Where the quantity supplied would again depending upon the situation reflect the fact that domestic production may not equal domestic demand and, hence, there are imports or exports.

⁵Adding an extensive margin is easy, just add an island, w_o for being out of the labor force and treating w_o as a transfer or home production (would have to be mindful of market clearing)

B. Social Welfare

Now here is where things start to get (i) disappointing and (ii) still helpful for developing intuition. I'm going to define the following within country (utilitarian) social welfare function:

$$U = \sum_{s \in S} \left\{ \int \varepsilon(\mathbf{s}) w(\mathbf{s}) d\varepsilon \right\} \pi(\mathbf{s}) \quad (30)$$

where starting from the most inner part: utility for a worker on island \mathbf{s} , then integrated over all workers in choosing to work in island \mathbf{s} (I need better notation here), then integrated over all islands (this is the sum with the probability weights). So the key issue is to compute the inner bracket, that is utility conditional on choosing that sector.

To compute expected utility conditional on choosing an island, we need to derive the preference distribution—conditional on those that select into the island. (Again to simplify notation, I'm going to revert back to the two state case and work through it, then show the general formula). This probability density is...

$$\text{Prob}(\varepsilon_h < \varepsilon | w_h \varepsilon_h > w_l \varepsilon_l) = \frac{\text{Prob}(\varepsilon_h < \varepsilon, w_h \varepsilon_h > w_l \varepsilon_l)}{\text{Prob}(w_h \varepsilon_h > w_l \varepsilon_l)} \quad (31)$$

where the right hand side is the probability that a workers productivity is less than some value, conditional on being in that island and the left hand side is the definition of this conditional density. To work through this, lets first compute the probability in the numerator

$$\text{Prob}(\varepsilon_h < \varepsilon, \tilde{w} \varepsilon_h > \varepsilon_l) = \int_0^\varepsilon \left[\int_0^{\tilde{w} \varepsilon_h} g(\varepsilon_h, \varepsilon_l) d\varepsilon_l \right] d\varepsilon_h. \quad (32)$$

This is the probability that a worker productivity for the h island has productivity below ε and chooses to work with an h type island. How to you compute this probability, first fix an $\tilde{w} \varepsilon_h$ and compute the probability that the ε_l is less than that value. This is what the integral in the bracket computes. Then sum up over the possible ε_h s up to the value ε . Like before, this observation also implies that the probability in the brackets is simply the marginal distribution $G'_{\varepsilon_h}(\varepsilon_h, \tilde{w} \varepsilon_h)$ evaluated at $\tilde{w} \varepsilon_h$. The probability in the denominator is closely related...

$$\text{Prob}(\tilde{w} \varepsilon_h > \varepsilon_l) = \int_0^\infty \left[\int_0^{\tilde{w} \varepsilon_h} g(\varepsilon_h, \varepsilon_l) d\varepsilon_l \right] d\varepsilon_h \quad (33)$$

Which just integrates over all possible ε_h s to compute the probability that a worker selects into a type h firm. Furthermore, this stuff in the brackets is also just the marginal distribution $G'_{\varepsilon_h}(\varepsilon_h, \tilde{w} \varepsilon_h)$ evaluated at $w \varepsilon_h$. Together, this implies that

$$\text{Prob}(\varepsilon_h < \varepsilon | w_h \varepsilon_h > w_l \varepsilon_l) = \int_0^\varepsilon G'_{\varepsilon_h}(\varepsilon_h, \tilde{w} \varepsilon_h) d\varepsilon_h \Bigg/ \int_0^\infty G'_{\varepsilon_h}(\varepsilon_h, \tilde{w} \varepsilon_h) d\varepsilon_h \quad (34)$$

Now how do we compute these integrals? So the marginal distribution $G'_{\varepsilon_h}(\varepsilon_h, \tilde{w}\varepsilon_h)$ is $g_{\varepsilon_h}(\varepsilon_h)G_{\varepsilon_l}(\tilde{w}\varepsilon_h)$ which follows from the independence of the draws. Then we just evaluate these integrals.

The denominator of this probability is the same as the share formula so

$$\int_0^\infty G'_{\varepsilon_h}(\varepsilon_h, \tilde{w}\varepsilon_h) d\varepsilon_h = \frac{T_h \tilde{w}^\gamma}{T_l + T_h \tilde{w}^\gamma} \quad (35)$$

Then the numerator of this probability is

$$\int_0^\varepsilon G'_{\varepsilon_h}(\varepsilon_h, \tilde{w}\varepsilon_h) d\varepsilon_h = \mu_h \exp \left[- (T_l \tilde{w}^{-\gamma} + T_h) \varepsilon^{-\gamma} \right] \quad (36)$$

which then implies that the ratio of the two is equal to

$$\text{Prob}(\varepsilon_h < \varepsilon | w_h \varepsilon_h > w_l \varepsilon_l) = \exp \left[- (T_l \tilde{w}^{-\gamma} + T_h) \varepsilon^{-\gamma} \right] \quad (37)$$

which says that the conditional probability is itself distributed Frechet with centering parameter $(T_l \tilde{w}^{-\gamma} + T_h)$.

To make things a bit more simple, notice that $(T_l \tilde{w}^{-\gamma} + T_h) = T_h \mu_h^{-1}$ in (27). This follow by multiplying and dividing the high share formula by $\tilde{w}^{-\gamma}$. Then to compute the conditional expectation we just simply compute the expected value associated with the distribution

$$\text{Prob}(\varepsilon_h < \varepsilon | w_h \varepsilon_h > w_l \varepsilon_l) = \exp \left[-T_h \mu_h^{-1} \varepsilon^{-\gamma} \right] \quad (38)$$

which implies—after abstracting from constant terms—the expected preference value a worker receives is

$$E(\varepsilon_h | \varepsilon_h w_h > \varepsilon_l w_l) = T_h^{\frac{1}{\gamma}} \mu_h^{\frac{-1}{\gamma}} \quad (39)$$

which has the flavor of the Arkolakis et al. (2012) formula. The key thing to notice is that as the share of workers becomes small, then average preference value increases. This is classic selection at work in the sense that only those who value a location the most will remain there. The general relationship takes the same form

$$E \left(\varepsilon(\mathbf{s}) | \varepsilon(\mathbf{s}) w(\mathbf{s}) > \max_{s \in S} \{ \varepsilon(\mathbf{s}) w(\mathbf{s}) \} \right) = T(\mathbf{s})^{\frac{1}{\gamma}} \mu(\mathbf{s})^{\frac{-1}{\gamma}} \quad (40)$$

Now for simplicity, let's drop the T 's and then ask what is utility within a group? It is the wage times the average preference for that location

$$w(\mathbf{s}) \mu(\mathbf{s})^{\frac{-1}{\gamma}} = w(\mathbf{s}) \left(\frac{w(\mathbf{s})^\gamma}{\sum_{s \in S} w(\mathbf{s})^\gamma} \right)^{\frac{-1}{\gamma}} = \left(\sum_{s \in S} w(\mathbf{s})^\gamma \right)^{\frac{1}{\gamma}} = \Phi. \quad (41)$$

Notice what just happened. **Utility is independent of the island a worker is on. It does not**

depend on s. It says, in terms of distributional effects, even though labor earnings are moving around with trade exposure (22), there is no effect on utility in the sense that one place gains more or less. It's all the same.

5. Welfare and Normative Issues

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