R Lab 3: Matrix Algebra with R

Ikuma Ogura

August 22, 2019

Today

- Vector and matrix algebra with R
- Accessing to vector/matrix elements with R
- (Time permitting) apply() function

Creating Vectors and Matrices

- As covered yesterday, in R we create vectors using c() command.
- We can create matrices with matrix() command

Usage

matrix(data, nrow, ncol, byrow)

where

- data: vector of matrix elements
- ▶ nrow, ncol: number of rows/columns
- ▶ byrow: if TRUE, the matrix is filled by rows; if FALSE, it is filled with columns

Creating Vectors and Matrices: Example

```
# Creating matrices
A \leftarrow matrix(data = c(1, 4, 3, 5), nrow = 2, byrow = TRUE)
B \leftarrow matrix(data = c(1, 4, 3, 5), nrow = 2, byrow = FALSE)
C \leftarrow matrix(data = c(9, 7, 6, 2, 1, 3), nrow = 2,
            byrow = TRUE)
D \leftarrow matrix(data = c(2, 4, 5, 7, 1, 2), nrow = 3,
            byrow = TRUE)
# Print
Α
## [,1] [,2]
## [1,] 1 4
## [2,] 3 5
В
## [,1] [,2]
## [1,] 1 3
## [2,] 4 5
```

Creating Vectors and Matrices: Example (cont.)

```
C

## [,1] [,2] [,3]

## [1,] 9 7 6

## [2,] 2 1 3

D

## [,1] [,2]

## [1,] 2 4

## [2,] 5 7

## [3,] 1 2
```

Vector Operations

```
# Creating vectors
a \leftarrow c(1, 4, 5, 3, 7)
b \leftarrow c(3, 2, 4, 7, 1)
c < -c(8, -2, -4)
# Vector operations
a + b # vector addition
## [1] 4 6 9 10 8
3 * a # scalar product
## [1] 3 12 15 9 21
a + 3 # !?
## [1] 4 7 8 6 10
```

Vector operations (cont.)

```
a %*% b # dot/inner product

## [,1]

## [1,] 59

a * b # different from above!

## [1] 3 8 20 21 7
```

Matrix operations

```
A - B # matrix addition/subtraction
## [,1] [,2]
## [1,] 0 1
## [2,] -1 0
3 * C # scalar product
## [,1] [,2] [,3]
## [1,] 27 21 18
## [2,] 6 3 9
A + 2
## [,1] [,2]
## [1,] 3 6
## [2,] 5 7
```

Matrix operations (cont.)

```
A %*% B # matrix product

## [,1] [,2]

## [1,] 17 23

## [2,] 23 34

A * B # different from above!

## [,1] [,2]

## [1,] 1 12

## [2,] 12 25
```

Matrix operations (cont.)

```
t(C) %*% B # t() to transpose matrices
## [,1] [,2]
## [1,] 17 37
## [2,] 11 26
## [3,] 18 33
C %*% c # vectors are treated as the k by 1 matrices
## [,1]
## [1,] 34
## [2,] 2
t(c) %*% D
## [,1] [,2]
## [1,] 2 10
```

Determinant & Inverse

```
det(A)
## [1] -7
solve(B)
## [,1] [,2]
```

```
## [1,] -0.7142857 0.4285714
## [2,] 0.5714286 -0.1428571
```

Solving System of Equations

- We can also use solve() command
- Example: Let's solve the following system of equations with R.

$$x + 3y = 7$$
$$2x + 5y = 10$$

```
coefs <- matrix(c(1, 3, 2, 5), nrow = 2, byrow = TRUE)
rhs <- c(7, 10)
solve(coefs, rhs)</pre>
```

```
## [1] -5 4
```

Vector/Matrix Operations: Summary

Command	Meaning
+	Summation
-	Subtraction
*	Element-wise product (Adamar product)
% * %	Matrix/Vector product
length()	(For vectors) Vector length
dim()	(For matrices) Matrix dimension
t()	Transpose
det()	Determinant
solve()	Inverse
diag(A)	(A is a square matrix) Extract diagonal elements
diag(k)	(k is a scalar) Create a $k \times k$ identity matrix
eigen()	Compute eigenvalues and eigenvectors

Accessing to Vector/Matrix Elements

- For vectors: vectorname[i] extracts the *i*th element of the vector
 - We can put in a vector within [] to extract multiple elements
 - ▶ If we specify negative numbers within [], R deletes corresponding elements
- For matrices: matrixname[i, j] extracts the element in ith row and jth column
 - ▶ matrixname[i,] extracts all the elements in *i*th row as a vector
 - ▶ matrixname[, j] extracts all the elements in jth column as a vector

Accessing to Vector/Matrix Elements: Example

```
b[3]
## [1] 4
a[c(2, 4)]
## [1] 4 3
b[c(-1, -5)]
## [1] 2 4 7
C[2, 1]
## [1] 2
D[-2,]
## [,1] [,2]
## [1,] 2
## [2,] 1
```

Accessing to Vector/Matrix Elements: Example (cont.)

```
B[1, 1] <- 9
B

## [,1] [,2]
## [1,] 9 3
## [2,] 4 5

C[, 2] <- c(8, 3)
C

## [,1] [,2] [,3]
## [1,] 9 8 6
```

[2,] 2 3 3

Exercises!

For the following matrix

$$\mathbf{A} = \begin{pmatrix} 7 & -3 & 0 \\ -2 & 6 & 1 \\ 0 & -5 & 6 \end{pmatrix},$$

- find the determinant
- calculate the inverse
- lacktriangledown replace the third row to (-4,2,-1) and recompute the determinant
- delete the first row and third column and find its inverse matrix

apply()

 We use apply() function when we apply a command/function to each row/column

Usage

```
apply(X, MARGIN, FUN...)
```

where

- X: a matrix we apply a function
- MARGIN: set 1 when we want to apply a function to each row; set 2 when we apply the function to each column
- ► FUN: function to apply

apply(): Example

```
apply(A, 1, sum)
## [1] 5 8
apply(C, 2, prod)
## [1] 18 24 18
```

Tomorrow

- Introduction to
 - ▶ loading data into R
 - data preprocessing with R
 - summarizing data with R