math 1MP assignment 2

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Due Wednesday 8 February at midnight (the end of the day), in the Dropbox on Avenue to Learn.

- Your assignment *must* be submitted as a module (text file) called yourmacid_hw2.py, e.g. mine would be bolker_hw2.py.
- All of your functions *must* have docstrings.
- 1. Write an implementation of *Eratosthenes' sieve*, an efficient way to find all the primes in a specified range. It must be defined as def eratos(n):, where n will be an integer
 - initialization:
 - create a list of boolean values of length n+1 (we want to check primes up to a value of n inclusive; we won't do anything with positions 0 and 1, but it's easier to index this way), which are all initially True
 - initialize a counter to 2
 - initialize an empty list for the results
 - start a while loop that runs as long as the the counter defined above is less than or equal to n
 - add the current value of the counter to the results list
 - set the values of the boolean list to False for all multiples of the current counter value <= n; you can do this with a while or a for loop. For example if i=3 and n=10 you should set elements 6 and 9 of the list to False</p>
 - search forward for the next possibly-prime value:
 - * first increment the counter by 1
 - * while the counter is less than or equal to n and the corresponding element of the boolean list is False, increment the counter by 1.
 - return the results list

Tests (should all be True):

```
print(eratos(1) == [])
print(eratos(2) == [2])
print(eratos(5) == [2,3,5])
print(len(eratos(1000)) == 168)
print(len(eratos(100000)) == 9592)
```

- 2. Write a function iterate with the following arguments:
- f: a function
- start: a numeric starting value
- tol: a numerical tolerance (default value 1e-6)
- itmax: a maximum number of iterations (default value 1000)

Starting from the initial value, your function should keep repeating calls to the function (e.g. y=f(y) as in the repeat_fun function in the class notes) until the absolute value of f(y)-y is less than tol or the number of iterations is equal to itmax. For example, if start=1.01, f is math.sqrt, and tol=1e-4, the sequence would look like this:

```
i y f(y)-y
0 1.01 1.004987562112089 -0.005012437887911059
1 1.004987562112089 1.0024906793143211 -0.00249688279776783
2 1.0024906793143211 1.0012445651859097 -0.0012461141284114685
3 1.0012445651859097 1.0006220890955335 -0.0006224760903761339
4 1.0006220890955335 1.0003109961884522 -0.00031109290708131176
```

```
5 1.0003109961884522 1.0001554860062771 -0.00015551018217507817 6 1.0001554860062771 1.0000777399813863 -7.77460248908568e-05
```

On step 6, the absolute value of the difference is less than the tolerance (1e-4), so the function returns [6, 1.0000777399813863].

Tests (should all be True):

```
def approx_equal(x,y,tol=1e-8):
    """helper function: test whether all elements of
       x and y are equal within tolerance
    if len(x) != len(y):
       return(False)
    for i in range(len(x)):
       if (abs(x[i]-y[i])>tol):
           return(False)
    return(True)
def disc_logist(x):
    """discrete logistic function"""
    return(1.5*x*(1-x))
print(approx_equal(iterate(disc_logist, 0.5), [15, 0.33333433255312184]))
print(approx_equal(iterate(disc_logist,0.5,tol=1e-8),[22, 0.33333334113969143]))
def half(x):
    """just what it says"""
    return(x/2)
print(approx equal(iterate(half,1000),[29, 9.313225746154785e-07]))
import math
print(approx_equal(iterate(math.sqrt,1.01,tol=1e-4),[6, 1.0000777399813863]))
print(approx_equal(iterate(math.cos,0),[34, 0.7390855263619245]))
print(approx_equal(iterate(math.cos,0,tol=1e-8),[46, 0.7390851366465718]))
print(approx_equal(iterate(math.cos,0,itmax=5),[5, 0.7013687736227565]))
```

3. Write a function read_evens that takes a single argument, the name of a file in the current directory. The file will contain a single integer on each line. Your function should return the number of even integers (remember that when you read a line it is a string (str) that you can convert to an integer with int()).

Tests: put the file even_nums.txt in the same directory as your Python file (in your project directory, if you're using PyCharm). Then read evens("even nums.txt") should return 3.