Consider the following 2 \times 2 game where payoffs are monetary:

	L	R
Т	3, 3	0, 4
В	4, 0	1, 1

Before this game is played, Player 1 can choose whether, after the game is played, players should keep their own payoffs or split the aggregate payoff evenly between them. Player 2 observes this choice.

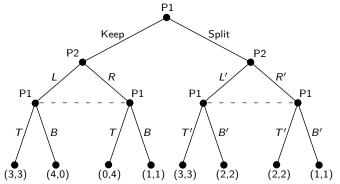
- (a) Write down the game tree of this two-stage game: be careful to represent the simultaneous-move game in the second stage using information sets.
- (b) Find the subgame perfect Nash Equilibria (SPNE).
- (c) Now suppose that Player 2 cannot observe Player 1's choice in the first stage. Draw the game tree (again using information sets) and find the subgame perfect Nash Equilibria (SPNE).

(a) Write down the game tree of this two-stage game: be careful to represent the simultaneous-move game in the second stage using information sets.

1st stage: Player 1 chooses Keep or Split. Player 2 observes the choice.

 2^{nd} stage: Player 2 chooses L or R (L' or R'). The action is private information.

 3^{rd} stage: Player 1 chooses T or B (T' or B') without knowing what Player 2 did.



The order of stage 2 and 3 is arbitrary, but the 2nd stage must be private information.

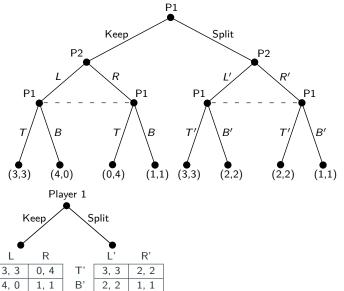
(b) Find the subgame perfect Nash Equilibria (SPNE).

>

(b) Find the subgame perfect Nash Equilibria (SPNE).

Т

В

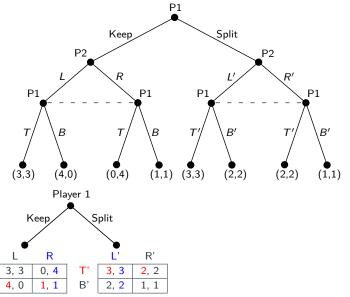


3

(b) Find the subgame perfect Nash Equilibria (SPNE).

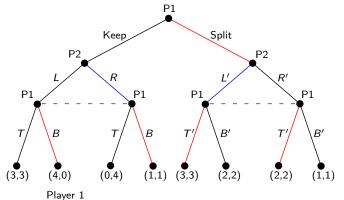
Т

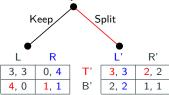
В



4

(b) Find the subgame perfect Nash Equilibria (SPNE).





Т

В

Write up the full strategy profiles for the subgame perfect Nash Equilibria (SPNE).

(b) Find the subgame perfect Nash Equilibria (SPNE).

R

0, 4

1, 1

T

B'

3, 3

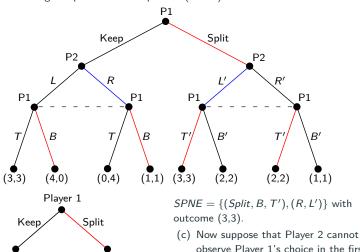
2, 2

Т

В

3, 3

4, 0



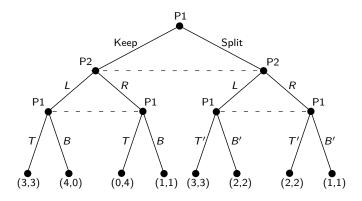
R'

2, 2

1, 1

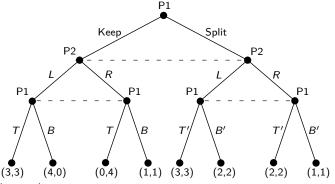
observe Player 1's choice in the first stage. *Draw the game tree (again using information sets)* and find the subgame perfect Nash Equilibria (SPNE).

(c) Now suppose that Player 2 cannot observe Player 1's choice in the first stage. Draw the game tree (again using information sets) and find the subgame perfect Nash Equilibria (SPNE).

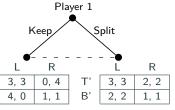


7

(c) Find the subgame perfect Nash Equilibria (SPNE).



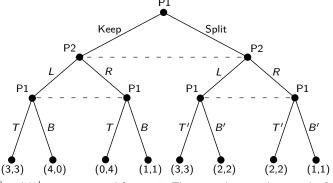
With 2^{nd} and 3^{rd} stage in normal form (Player 1 knows her own action in 1^{st} stage):



В

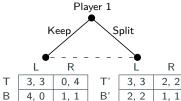
How many subgames are there?

(c) Find the subgame perfect Nash Equilibria (SPNE).



With 2^{nd} and 3^{rd} stage in normal form:

There is only one subgame; the full game itself.



Write up the game in normal form and solve it.

