

# PS11: Signaling games in general

## Players:

- 2 players: Sender (S) and receiver (R). E.g. firm and consumer, or employer and employee (Spence).

## Timing:

- Nature chooses the sender's type from  $T = \{t_1, \dots\}$ .
- S: The sender realizes her type and sends a signal from  $M = \{m_1, \dots\}$ , typically either  $L$  (left) or  $R$  (right).
- R: The receiver observes  $m$  (but not the type  $t$ !) and forms his beliefs:

$$p = \mu(t_1|L) \text{ and } q = \mu(t_1|R)$$

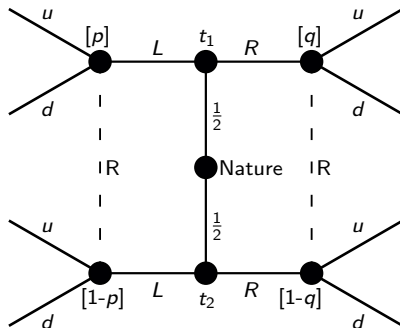
Consequently, for  $S$  having two possible types:

$$1 - p = \mu(t_2|L) \text{ and } 1 - q = \mu(t_2|R)$$

- R: The receiver chooses an action from  $A = \{a_1, \dots\}$ , e.g. *up* or *down*.
- Payoffs are realized.

## Four possible equilibria for two types:

- Pooling on  $L$  or pooling on  $R$ .
- Separating:  $t_1$  plays  $L$  and  $t_2$  plays  $R$  or the other way around.



**Cookbook: For each possible equilibrium go over signaling requirements 3 and 2:**

SR3: R: Find the beliefs  $p, q$  given  $S$ 's eq. strategy. (Only consider beliefs that are consistent with  $S$ 's eq. strategy.)

SR2R: R: Given beliefs, find  $a(m_j|\mu(t_1|m_j))$ .

SR2S: S: Does  $t_1$  or  $t_2$  want to deviate?

PBE: No deviation  $\rightarrow$  PBE. Pooling on  $L$ : Find off-eq.  $a(R|q) \rightarrow$  possibly two different PBE for different  $q$ .

## PS11, Ex. 3.b: Notation (separating PBE)

(b) Consider a possible separating PBE where  $t_1$  sends message  $R$ ,  $t_2$  sends message  $L$ , and where the receiver chooses  $u$  if and only if he receives message  $L$ . Can you write down payoffs for this game such that nobody has an incentive to deviate?

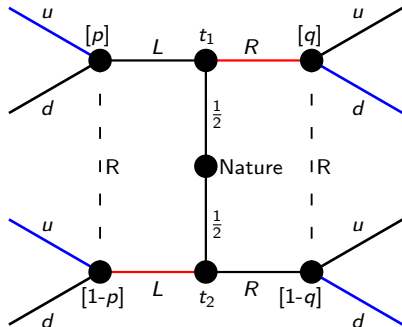
SR3: R: Find the beliefs of R given S's equilibrium strategy. (In equilibrium, we only consider beliefs of R that are consistent with S's eq. strategy.)

SR2R: R: Find R's optimal strategy given beliefs about S's strategy.

SR2S: S: Check whether S wants to deviate.

PBE: Write up the conditions such that SR2R and SR2S hold (no incentive to deviate) for the following PBE:

$$\{(\underbrace{R}_{m(t_1)}, \underbrace{L}_{m(t_2)}), (\underbrace{u}_{a(L)}, \underbrace{d}_{a(R)}), \underbrace{p=0}_{\mu(t_1|L)}, \underbrace{q=1}_{\mu(t_1|R)}\}$$



SR3: In the separating PBE, R has beliefs:  
 $\mu(t_1|L) = p^* = 0$

$$\mu(t_1|R) = q^* = 1$$

$$\begin{aligned} \text{SR2R: } \mathbb{E}[u_R(L, u|p=0)] &\geq \mathbb{E}[u_R(L, d|p=0)] \\ \mathbb{E}[u_R(R, d|q=1)] &\geq \mathbb{E}[u_R(R, u|q=1)] \end{aligned}$$

$$\begin{aligned} \text{SR2S: } u_S(R, d|t_1) &\geq u_S(L, d|t_1) \\ u_S(L, u|t_2) &\geq u_S(R, u|t_2) \end{aligned}$$