

#### Microeconomics III: Problem Set 7<sup>a</sup>

Thor Donsby Noe (thor.noe@econ.ku.dk) & Christopher Borberg (christopher.borberg@econ.ku.dk) November 6 2019

Department of Economics, University of Copenhagen

<sup>&</sup>lt;sup>a</sup>Slides created for exercise class 3 and 4, with reservation for possible errors.

#### **Outline**

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PS7, Ex. 1 (A): Imperfect recall (imperfect information)
PS7, Ex. 2 (A): Three conditions for a subgame (imperfect information)
PS7, Ex. 3 (A):
PS7, Ex. 4:
PS7, Ex. 5:
PS7, Ex. 6:
PS7, Ex. 7:
PS7, Ex. 8:
PS7, Ex. 9:
PS7, Ex. 10:
Code examples
```

1

# PS7, Ex. 1 (A): Imperfect recall (imperfect information)

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In this course we normally consider games in which there is 'perfect recall': players can always remember what they themselves have done in the past.

We have seen an example in class of a game with 'imperfect recall' where the player forgets his own actions. But what would a game where he forgets the opponent's actions look like? Construct a game with two players. The timing is as follows: Player 1 moves first, then Player 2, and then Player 2 again. Everytime they move, the players choose one of two actions:  $\{L, R\}$ .

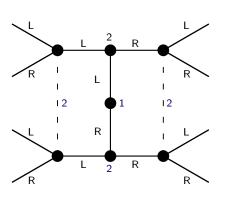
Draw the game tree and construct the information sets such that (a) Player 2 observes Player 1's action the first time he moves, but (b) when Player 2 moves the second time, he has forgotten what Player 1 chose. However, he recalls his own action.

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4

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Under imperfect information, a subgame Exammust satisfy three properties:

Example of violation of condition 1:

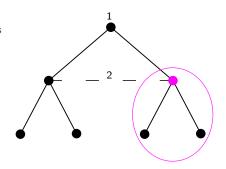
1. It begins at a decision node *n* that is a singleton information set.

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1. It begins at a decision node *n* that is a singleton information set.

Example of violation of condition 1:



The purple decision node to the right is not a singleton information set.

## PS7, Ex. 3 (A):

PS7, Ex. 3 (A):

PS7, Ex. 3.a (A):

#### PS7, Ex. 4:

PS7, Ex. 4:

#### PS7, Ex. 4.a:

# PS7, Ex. 5:

#### PS7, Ex. 5:

#### PS7, Ex. 5.a:

#### PS7, Ex. 6:

#### PS7, Ex. 6:

#### PS7, Ex. 6.a:

#### PS7, Ex. 7:

#### PS7, Ex. 7:

#### PS7, Ex. 7.a:

#### PS7, Ex. 8:

#### PS7, Ex. 8:

PS7, Ex. 8.a:

## PS7, Ex. 9:

#### PS7, Ex. 9:

#### PS7, Ex. 9.a:

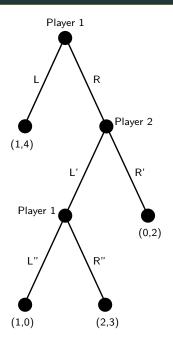
#### PS7, Ex. 10:

#### PS7, Ex. 10:

#### PS7, Ex. 10.a:

# Code examples

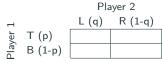
#### **Code examples**



Matrix, no player names:

	L (q)	R (1-q)
T (p)		
B (1-p)		

Matrix, no colors:



Matrix, with colors:

