## Lecture 3: Descriptive Statistics

**STAT 324** 

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# **Objectives**

- 1. "Previously on STAT 324..."
- 2. Descriptive Statistics
  - Types of data/variables
  - Numerical summaries
  - Graphical summaries

# Previously on STAT 324...

- The general setup
- Three parts of this class:
  - 1. Descriptive Statistics
  - 2. Probability
  - 3. Inferential Statistics

- What: the art of describing data with few important measures ('summary statistics')
- Why:
  - know your population!!
  - explore your data
- How: try to get an idea of the distributions of variables included
  - what's a distribution?!
  - what's a variable?!

- Discrete data
  - categorical
    - no natural ordering
    - examples: sex, race, blood type, political orientation, etc.
  - ordinal
    - naturally ordered
    - educational level, age groups, disease severity scales, counts, etc.
  - summarized by
    - frequency counts
    - relative frequencies
- Continuous data
  - numerical
    - examples: age, height, weight, BMI, proportions, etc.
  - infinite (uncountable, actually...) number of potential values
  - summarized by
    - location measures
    - spread/variation measures
    - shape

Data example: STAR WARS

First, some R setup:

```
library(tidyverse)
library(DT); library(kableExtra)

# Change theme for plots
theme_set(theme_bw())

# Change color scheme for plots
scale_color_continuous <- scale_color_viridis_c
scale_color_discrete <- scale_color_viridis_d

scale_fill_continuous <- scale_fill_viridis_c
scale_fill_discrete <- scale_fill_viridis_d</pre>
```

Data example: STAR WARS

Let's load some data, and take a look:

	name 🛊	height +	mass +	hair_color 🛊	skin_color \	eye_color +
1	Luke Skywalker	172	77	blond	fair	blue
2	C-3PO	167	75		gold	yellow
3	R2-D2	96	32		white, blue	red
4	Darth Vader	202	136	none	white	yellow

### Data example: STAR WARS

How many films have the characters been in?

Ordinal variable. Summarized using frequency counts, and relative frequencies.

#### Numerical summary:

n_films	frequency	relative
1	46	0.5287356
2	18	0.2068966
3	13	0.1494253
4	2	0.0229885
5	5	0.0574713
6	2	0.0229885
7	1	0.0114943

### Data example: STAR WARS

How many films have the characters been in?

Ordinal variable. Summarized using frequency counts, and relative frequencies.

Graphical summary:

### Data example: STAR WARS

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Ordinal variable. Summarized using frequency counts, and relative frequencies.

Graphical summary:

### Data example: STAR WARS

When would we use relative frequencies rather than frequencies? When comparing groups.

gender	n_films	frequencies	relative
female	1	9	0.4736842
female	2	6	0.3157895
female	3	3	0.1578947
female	5	1	0.0526316
hermaphrodite	3	1	1.0000000
male	1	34	0.5483871
male	2	12	0.1935484
male	3	9	0.1451613
male	4	2	0.0322581
male	5	4	0.0645161
male	6	1	0.0161290
none	1	2	1.0000000
NA	1	1	0.3333333
NA	6	1	0.3333333
NA	7	1	0.3333333

### Data example: STAR WARS

When would we use relative frequencies rather than frequencies? When comparing groups.

### Data example: STAR WARS

When would we use relative frequencies rather than frequencies? When comparing groups.

For continuous data, measures of location and spread

Measures of location:

- mean/average:  $ar{x}=rac{1}{n}(x_1+x_2+\ldots+x_n)=rac{1}{n}\sum_{i=1}^n x_i$
- median: the observation in the middle of the data.
- minimum and maximum: the smallest and largest observations, respectively

Simple example data: 1, 5, 2, -3, 7, -12, 0.

Mean: 0

Median: 1

Minimum and maximum: -12 and 7

### Measures of spread:

- variance:  $s^2 = rac{1}{n-1} \sum_{i=1}^n (x_i ar{x})^2$
- standard deviation:  $s=\sqrt{s^2}$
- range:  $\max \min$
- percentiles (sometimes referred to as quantiles):

The p'th percentile of a set of measurements is the one that has p% of the data below it.

- Inter Quartile Range (IQR): 75th percentile 25th percentile
  - 25th percentile = first quartile = median of 1st half including median
  - median = second quartile
  - 75th percentile = third quartile = median of 2nd half including median

Simple example data: 1, 5, 2, -3, 7, -12, 0.

Variance: 38.6666667. Standard deviation: 6.2182527. Range: 19. 1st and 3rd quartiles (i.e. 25th and 75th percentiles): -1.5, 3.5. IQR: 5

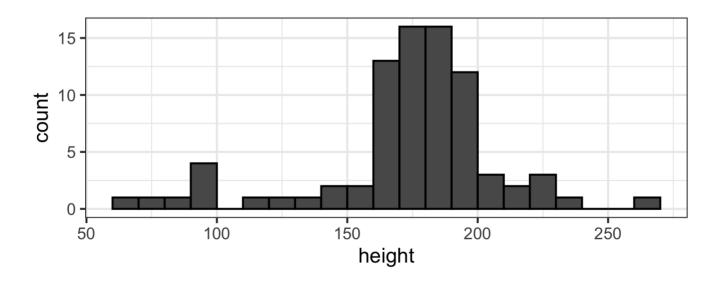
```
starwars %>%
  filter(!is.na(height), gender %in% c('male', 'female')) %>%
 group_by(gender) %>%
  summarize(n = n(),
            mean = mean(height),
            var = var(height),
            sd = sd(height),
            median = median(height),
            Q1 = quantile(height, p = 0.25),
            02 = quantile(height, p = 0.50),
            Q3 = quantile(height, p = 0.75),
            IOR = IOR(height),
            min = min(height),
            max = max(height),
            range = max - min) %>%
  kable(format = "markdown", digits = 2)
```

gender	n	mean	var	sd	median	Q1	Q2	Q3	IQR	min	max	range
female	17	165.47	530.39	23.03	166	163	166	178	15	96	213	117
male	59	179.24	1252.56	35.39	183	174	183	193	19	66	264	198

gender	n	10th percentile	57th percentile	82nd percentile
female	17	150	167.12	178.00
male	59	134	188.00	197.12

### Data example: STAR WARS

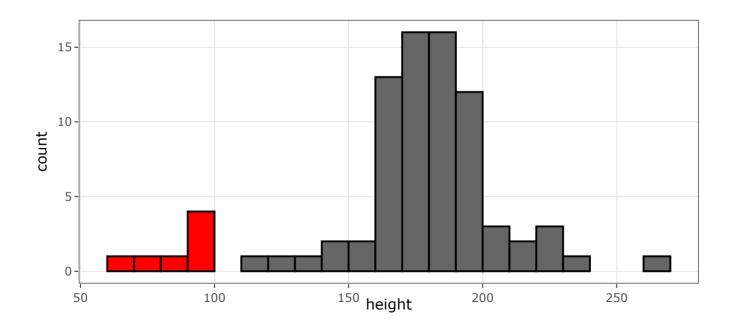
Visually, continous data can be summarized using a *histogram*.

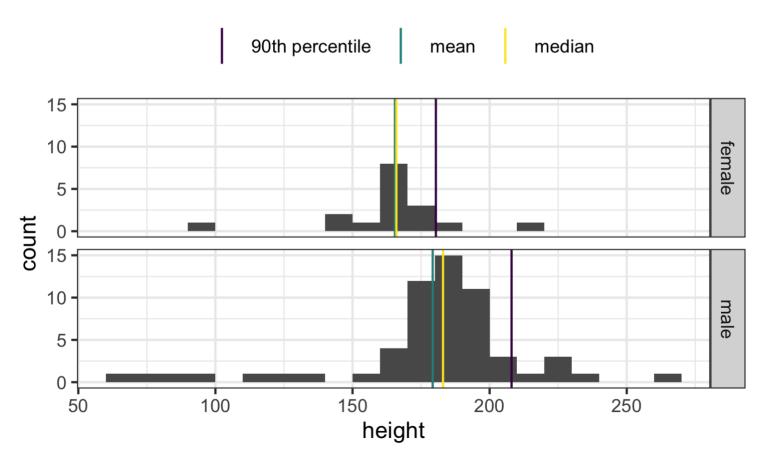


### Data example: STAR WARS

Proportion of an area is the proportion of data in the corresponding interval: proportion of characters with height less than  $100 = \frac{7 \cdot 10}{81 \cdot 10} \approx 0.086$ .

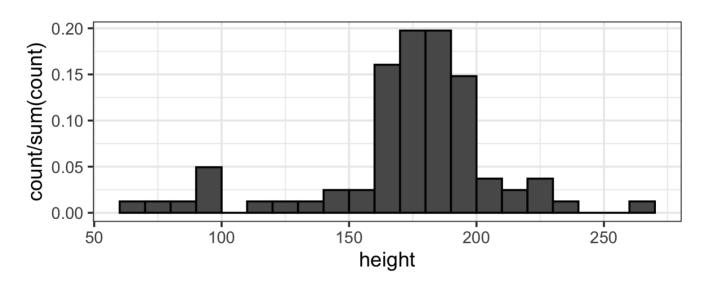
This will be **very** important to us later.





#### Data example: STAR WARS

Histograms can also be used to depict *relative frequencies*. To do so, you simply divide the counts by the total number of observations.



### Data example: STAR WARS

Another useful figure for numerical data: the boxplot (also known as box-and-whisker plot, or box-and-whisker diagram).

The key to decipher a box plot:

#### Outlier if

$$\mathrm{obs} < \mathrm{Q1} - 1.5 \cdot \mathrm{IQR}$$

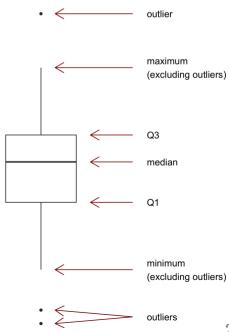
or

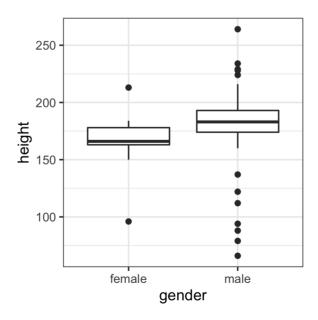
$$\mathrm{obs} > \mathrm{Q3} + 1.5 \cdot \mathrm{IQR}$$

25% of the data are above the box

50% of the data are in the the box

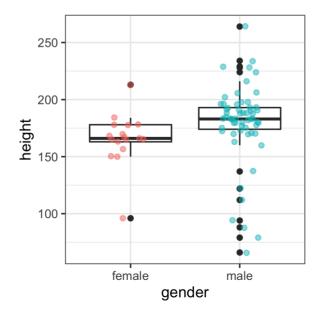
25% of the data are below the box





### Data example: STAR WARS

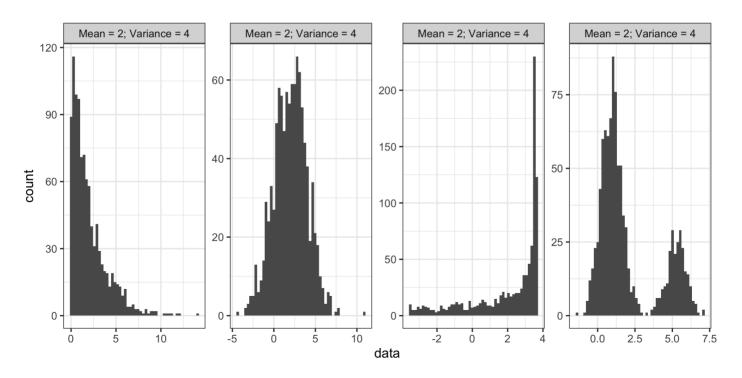
My personal favorite when data set not too large: boxplot + points!



### **Continuous Data: shape**

So far, only talked about *location* and *spread* of data.

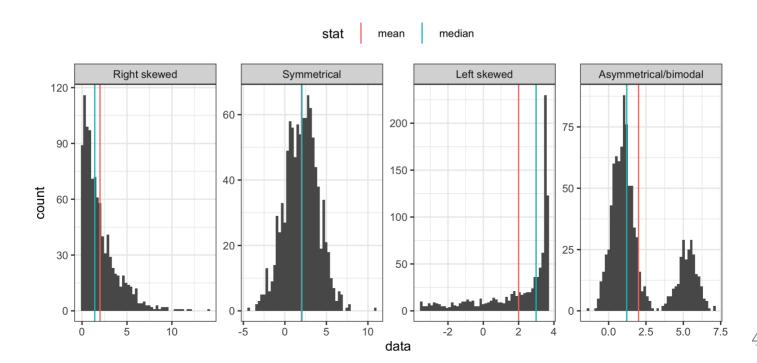
However, this does not provide the full picture:



#### **Continuous Data: shape**

The *shape* of the data is generally described as either *symmetrical* or *non-symmetrical*, and if non-symmetrical as either *right skewed* or *left-skewed*.

When symmetrical, mean = median. Right skewed, mean > median. Left skewed, mean < median.



#### **Continuous Data: shape**

Boxplots don't give us the entire shape, but they let us determine if the data is symmetrical:

#### For symmetrical data

- median is in the middle of the data.
- median = mean.

Right skewed data => median closer to bottom of box.

Left skewed data => median closer to top of box.

