Problems and Solutions in Applied Statistics

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Chapter 1

Introduction

This is the introduction to my book.

Chapter 2

Getting used to R and R Studio

```
library(tidyverse)
## -- Attaching packages -----
## v ggplot2 3.0.0
                                 0.2.5
                       v purrr
## v tibble 1.4.2
                       v dplyr
                                 0.7.6
## v tidyr
            0.8.1
                       v stringr 1.3.1
## v readr
             1.1.1
                       v forcats 0.3.0
## -- Conflicts -----
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
```

The very basics in R

Do this question in R. It is just like the one on Assignment 0.

(a) Read the data 1, 2, 3, 4, 5, 7 into a variable in R. Verify that your variable contains the correct values. (Hint: c().)

Solution

Call the variable whatever you like. I used w.

```
w=c(1,2,3,4,5,7)
w
```

```
## [1] 1 2 3 4 5 7
```

Top two lines in a Script window, echoed in the Console; bottom line in the Console.

(b) Find the mean and the standard deviation of your variable.

Solution

Ask for them, one by one:

```
mean(w)
```

```
## [1] 3.666667
```

and

sd(w)

[1] 2.160247

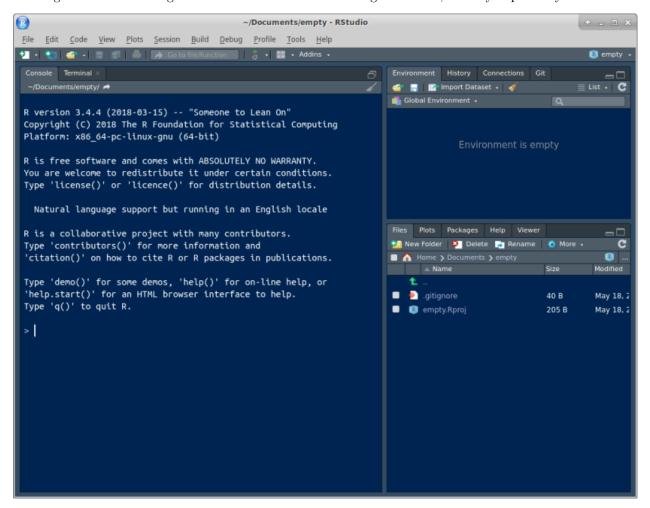
Getting used to R Studio

This question is to get you started using R.

(a) Start R Studio Cloud, in some project. (If you started up a new project in the previous question and are still logged in, use that; if not, create a new project.)

Solution

You ought to see something like this. I have a dark blue background here, which you probably do not.

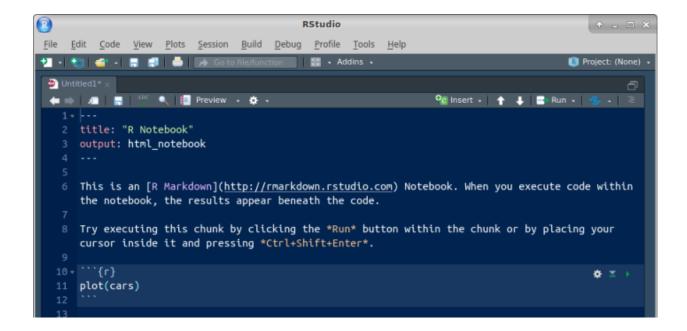


It won't look exactly like that (for example, the background will probably be white) but there should be one thing on the left half, and at the top right it'll say "Environment is empty". Extra: if you want to tweak things, select Tools (at the top of the screen) and from it Global Options, then click Appearance. You can make the text bigger or smaller via Editor Font Size, and choose a different colour scheme by picking one of the Editor Themes (which previews on the right). My favourite is Tomorrow Night Blue. Click Apply or OK when you have found something you like. (I spend a lot of time in R Studio, and I like having a dark background to be easier on my eyes.)

(b) We're going to do some stuff in R here, just to get used to it. First, make an R Notebook by selecting File, New File and R Notebook.

Solution

The first time, you'll be invited to "install some packages" to make the Notebook thing work. Let it do that by clicking Yes. After that, you'll have this:

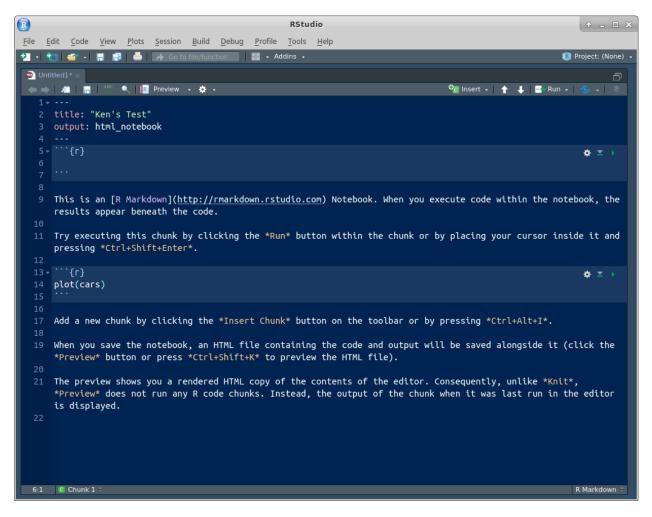


Find the Insert and Run buttons along the top of the R Notebook window. We'll be using them shortly. (The template notebook may or may not be maximized; it doesn't matter either way. You might see all four panes or as few as one. If you want to control that, select View at the top, then Panes, then either Show All Panes or Zoom Source, as you prefer. In the menus, you'll also see keyboard shortcuts for these, which you might find worth learning.)

(c) Change the title to something of your choosing. Then go down to line 5, click on the Insert button and select R. You should see a "code chunk" appear at line 5, which we are going to use in a moment.

Solution

Something like this:



(d) Type the line of code shown below into the chunk in the R Notebook:

mtcars

Solution

What this will do: get hold of a built-in data set with information about some different models of car, and display it.

```
Untitled1* x

In the preview of the
```

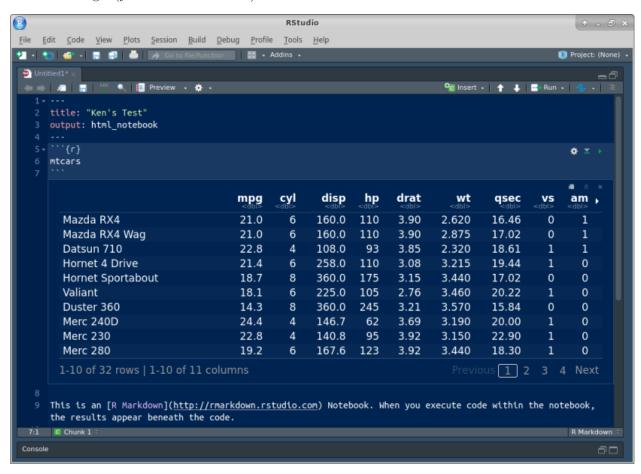
In approximately five seconds, you'll be demonstrating that for yourself.

(e) Run this command. To do that, look at the top right of your code chunk block (shaded in a slightly different colour). You should see a gear symbol, a down arrow and a green "play button". Click the play button. This will run the code, and show the output below the code chunk.

Solution

mtcars

Here's what I get (yours will be the same).



This is a rectangular array of rows and columns, with individuals in rows and variables in columns, known as a "data frame". When you display a data frame in an R Notebook, you see 10 rows and as many columns as will fit on the screen. At the bottom, it says how many rows and columns there are altogether (here 32 rows and 11 columns), and which ones are being displayed. You can see more rows by clicking on Next, and if there are more columns, you'll see a little arrow next to the rightmost column (as here next to am) that you can click on to see more columns. Try it and see. Or if you want to go to a particular collection of rows, click one of the numbers between Previous and Next: 1 is rows 1–10, 2 is rows 11–20, and so on. The column on the left without a header (containing the names of the cars) is called "row names". These have a funny kind of status, kind of a column and kind of not a column; usually, if we need to use the names, we have to put them in a column first. In future solutions, rather than showing you a screenshot, expect me to show you something like this:

```
## # A tibble: 32 x 11
                                                 qsec
                                                                      gear
##
         mpg
                cyl
                     disp
                               hp
                                   drat
                                             wt
                                                           vs
                                                                  am
##
       <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                              <dbl>
                                                                     <dbl>
                                                                            <dbl>
                                    3.9
    1
                  6
                      160
                              110
                                           2.62
                                                 16.5
                                                            0
                                                                   1
                                                                          4
                                                                                 4
    2
        21
                  6
                      160
                              110
                                   3.9
                                           2.88
                                                 17.0
                                                            0
                                                                          4
                                                                                 4
##
                                                                   1
```

```
3
        22.8
                      108
                                    3.85
                                           2.32
                                                   18.6
##
                                                              1
                                                                     1
    4
                      258
                                           3.22
                                                                            3
##
        21.4
                   6
                               110
                                    3.08
                                                   19.4
                                                              1
                                                                     0
                                                                                   1
##
    5
        18.7
                   8
                      360
                               175
                                    3.15
                                            3.44
                                                   17.0
                                                             0
                                                                            3
                                                                                   2
    6
        18.1
                      225
                               105
                                    2.76
                                                   20.2
                                                                     0
                                                                            3
##
                   6
                                           3.46
                                                              1
                                                                                   1
                                                   15.8
##
    7
        14.3
                   8
                      360
                               245
                                    3.21
                                            3.57
                                                             0
                                                                     0
                                                                            3
                                                                                   4
                   4
                                                                     0
                                                                            4
                                                                                   2
##
    8
        24.4
                      147.
                                62
                                    3.69
                                            3.19
                                                   20
                                                              1
    9
        22.8
                   4
                                                                                   2
##
                      141.
                                95
                                    3.92
                                           3.15
                                                   22.9
                                                             1
                                                                     0
                                                                            4
                      168.
## 10
        19.2
                   6
                               123
                                    3.92
                                           3.44
                                                   18.3
                                                              1
                                                                     0
                                                                            4
                                                                                   4
## # ... with 22 more rows
```

The top bit is the code, the bottom bit with the ## the output. In this kind of display, you only see the first ten rows (by default).

If you don't see the "play button", make sure that what you have really is a code chunk. (I often accidentally delete one of the special characters above or below the code chunk). If you can't figure it out, delete this code chunk and make a new one. Sometimes R Studio gets confused.

On the code chunk, the other symbols are the settings for this chunk (you have the choice to display or not display the code or the output or to not actually run the code). The second one, the down arrow, runs all the chunks prior to this one (but not this one).

The output has its own little buttons. The first one pops the output out into its own window; the second one shows or hides the output, and the third one deletes the output (so that you have to run the chunk again to get it back). Experiment. You can't do much damage here.

(f) Something a little more interesting: summary obtains a summary of whatever you feed it (the five-number summary plus the mean for numerical variables). Obtain this for our data frame. To do this, create a new code chunk below the previous one, type summary(mtcars) into the code chunk, and run it.

Solution

This is what you should see:

```
...{r}
summary(mtcars
                        cyl
                                         disp
                                                            hp
                                                                            drat
                                                                                              wt
         :10.40
                   Min.
                          :4.000
                                    Min.
                                            : 71.1
                                                     Min.
                                                               52.0
                                                                      Min.
                                                                              :2.760
                                                                                        Min.
                                                                                                :1.513
 Min.
  1st Qu.:15.43
                   1st Qu.:4.000
                                    1st Qu.:120.8
                                                     1st Qu.:
                                                               96.5
                                                                       1st Qu.:3.080
                                                                                        1st Qu.:2.581
 Median :19.20
                                    Median :196.3
                   Median :6.000
                                                     Median :123.0
                                                                      Median :3.695
                                                                                        Median :3.325
         :20.09
                   Mean
                          :6.188
                                    Mean
                                            :230.7
                                                     Mean
                                                             :146.7
                                                                      Mean
                                                                              :3.597
                                                                                        Mean
                                                                                                :3.217
 Mean
  3rd Qu.:22.80
                   3rd Qu.:8.000
                                    3rd Qu.:326.0
                                                     3rd Qu.:180.0
                                                                       3rd Qu.:3.920
                                                                                        3rd Qu.:3.610
                          :8.000
                                            :472.0
                                                                                                :5.424
         :33.90
                   Max.
                                    Max.
                                                     Max.
                                                             :335.0
                                                                      Max.
                                                                              :4.930
                                                                                        Max.
                         vs
                                                                              carb
       qsec
                                            am
                                                             gear
         :14.50
                          :0.0000
                                             :0.0000
                                                               :3.000
                   Min.
                                     Min.
                                                       Min.
                                                                         Min.
                                                                                :1.000
  1st Qu.:16.89
                   1st Qu.:0.0000
                                     1st Qu.:0.0000
                                                       1st Ou.:3.000
                                                                         1st Ou.:2.000
 Median :17.71
                   Median :0.0000
                                     Median :0.0000
                                                       Median :4.000
                                                                         Median :2.000
         :17.85
                          :0.4375
                                             :0.4062
                                                               :3.688
                                                                                :2.812
                   3rd Qu.:1.0000
                                                                         3rd Ou.:4.000
 3rd Qu.:18.90
                                     3rd Qu.:1.0000
                                                       3rd Ou.:4.000
         :22.90
                          :1.0000
                                             :1.0000
                                                               :5.000
                                                                                :8.000
                   Max.
                                     Max.
                                                       Max.
                                                                         Max.
```

or the other way:

summary(mtcars)

```
##
         mpg
                           cyl
                                            disp
                                                               hp
                                                                : 52.0
##
    Min.
            :10.40
                             :4.000
                                               : 71.1
                                                        Min.
                     Min.
                                       Min.
    1st Qu.:15.43
                     1st Qu.:4.000
                                       1st Qu.:120.8
                                                        1st Qu.: 96.5
                     Median :6.000
    Median :19.20
                                       Median :196.3
                                                        Median :123.0
##
```

```
##
            :20.09
                              :6.188
                                               :230.7
                                                                 :146.7
    Mean
                      Mean
                                       Mean
                                                         Mean
##
    3rd Qu.:22.80
                      3rd Qu.:8.000
                                       3rd Qu.:326.0
                                                         3rd Qu.:180.0
                                               :472.0
##
    Max.
            :33.90
                      Max.
                             :8.000
                                       Max.
                                                         Max.
                                                                 :335.0
##
                            wt
         drat
                                             qsec
                                                                vs
##
    Min.
            :2.760
                      Min.
                              :1.513
                                       Min.
                                               :14.50
                                                         Min.
                                                                 :0.0000
                                       1st Qu.:16.89
##
    1st Qu.:3.080
                      1st Qu.:2.581
                                                         1st Qu.:0.0000
                      Median :3.325
##
    Median :3.695
                                       Median :17.71
                                                         Median: 0.0000
##
    Mean
            :3.597
                      Mean
                              :3.217
                                       Mean
                                               :17.85
                                                         Mean
                                                                 :0.4375
##
    3rd Qu.:3.920
                      3rd Qu.:3.610
                                       3rd Qu.:18.90
                                                         3rd Qu.:1.0000
##
    Max.
            :4.930
                      Max.
                              :5.424
                                       Max.
                                               :22.90
                                                         Max.
                                                                 :1.0000
##
                            gear
                                              carb
           am
                               :3.000
                                                :1.000
##
    Min.
            :0.0000
                       Min.
                                        Min.
##
    1st Qu.:0.0000
                       1st Qu.:3.000
                                        1st Qu.:2.000
                       Median :4.000
##
    Median :0.0000
                                        Median :2.000
##
    Mean
            :0.4062
                       Mean
                               :3.688
                                        Mean
                                                :2.812
##
    3rd Qu.:1.0000
                       3rd Qu.:4.000
                                        3rd Qu.:4.000
    Max.
            :1.0000
                               :5.000
                                                :8.000
                       Max.
                                        Max.
```

For the gas mileage column mpg, the mean is bigger than the median, and the largest value is unusually large compared with the others, suggesting a distribution that is skewed to the right.

There are 11 numeric (quantitative) variables, so we get the five-number summary plus mean for each one. Categorical variables, if we had any here, would be displayed a different way.

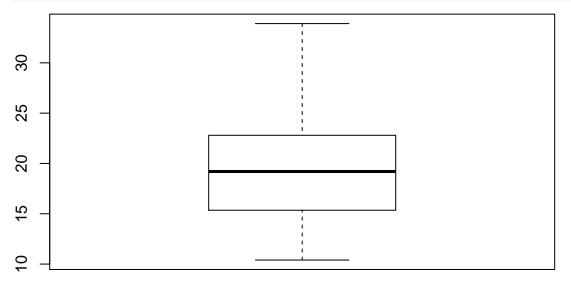
(In case you are wondering, the way without screenshots is obtained by my writing a notebook with code chunks and running them, so this output genuinely is obtained by running the code you see.)

(g) Let's make a boxplot of the gas mileage data. This is a "poor man's boxplot"; we'll see a nicer-looking way later. To do it this way, make another new code chunk, enter the code boxplot(mtcars\$mpg) into it, and run the chunk.

Solution

This is what you should see:

boxplot(mtcars\$mpg)



The long upper whisker supports our guess from before that the distribution is right-skewed.

(h) Some aesthetics to finish with: delete the template notebook (all the stuff you didn't type below your code chunks and output). Then add some narrative text above and below your code chunks. Above the

code chunk is where you say what you are going to do (and maybe why you are doing it), and below is where you say what you conclude from the output you just obtained.

Solution

My complete R Notebook is at http://www.utsc.utoronto.ca/~butler/c32/a0-notebook-1.Rmd. Take a look at it. I added one extra thing: my variable names have "backticks" around them. You'll see the effect of this in a moment. Backtick is on the key to the left of 1 and below Esc on your keyboard, along with a "squiggle" symbol that we'll be using later in the course.

(i) Save your notebook (the usual way with File and Save). This saves it on the R Studio Cloud servers (and not on your computer). This means that when you come back to R Studio Cloud later, even from another device, this notebook will still be available to you. Now click Preview. This produces a pretty HTML version of your notebook.

Solution

Note that the HTML document only contains output from the chunks you've run in the notebook, so it's up to you to run them there first.

My HTML document is at http://www.utsc.utoronto.ca/~butler/c32/a0-notebook-1.nb.html. Here's where you see the effect of the backticks: all the variable names are in typewriter font so that you can see they are variable names and not something else. If you want to try this notebook out yourself, you have a couple of options: (i) make a new R Notebook on R Studio Cloud and copy-paste the contents of my file (it's just text), or (ii) download my R Notebook onto your computer, and then upload it to R Studio Cloud. Look in the Files pane bottom right, and next to New Folder you should see Upload. Upload the file from wherever it got saved to when you downloaded it. Extra: if you're feeling ambitious, click the arrow to the right of Preview and select Knit to Word. The button changes to Knit with a ball of wool beside it. Now, when you "knit" the notebook, you get a Word document directly — look for it in the Files pane. If you want to, you can hand this kind of thing in (on later assignments), but you'll have to do a little work first: first, find it in your Files list, then click the checkbox to the left of it, then click More (with the gear, on the same line as New Folder and Upload), then select Export (and click Download). This will put a copy in your downloads folder on your computer, and you can open it from there. If you're feeling extra-ambitious, you can try Knit to PDF. This produces something that looks as if it was written in LaTeX, but actually wasn't. To make this work, if you have a library(tidyverse) line somewhere, as you probably will, find the code chunk it's in, and make it look like this:

" "

library(tidyverse)

"

Then it will work. Extra extra: if you like the keyboard better than the mouse, R Studio has a lot of keyboard shortcuts. Two that are useful now: control-alt-i inserts a code chunk where the cursor is, and control-shift-enter runs the code chunk that the cursor is in, if it is in one. (Mac users, "command" instead of "control" in both cases.) I use these two a lot.

(j) Optional extra: practice handing in your previewed R notebook, as if it were an assignment that was worth something. (It is good to get the practice in a low-stakes situation, so that you'll know what to do next week.)

Solution

There are two steps: download the HTML file onto your computer, and then handing it in on Quercus. To download: find the HTML file that you want to download in the Files pane bottom right. There should be two files starting with the same thing, eg. test1.Rmd, which is the notebook you wrote, and test1.nb.html, which is the previewed version of it, and is the one you want to download. (The test1 part is the name you chose when you saved it.) Click the checkbox to the left of the HTML file. Now click on More above the bottom-right pane. This pops up a menu from which you choose Export. This will pop up another window called Export Files, where you put the name that the file will have on your computer. (I usually leave the

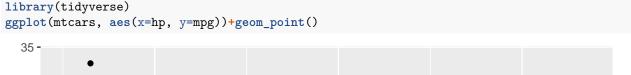
\$

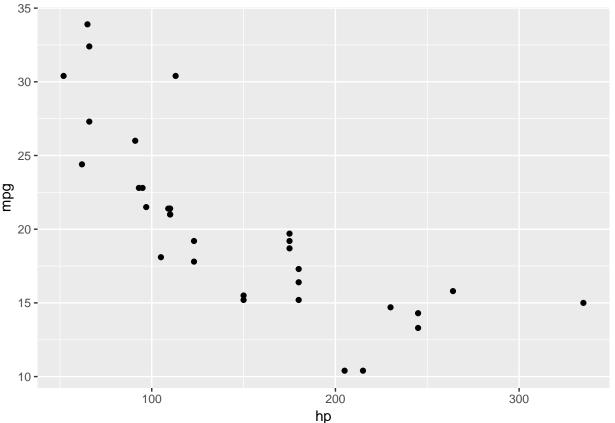
name the same.) Click Download. The file will go to your Downloads folder, or wherever things you download off the web go. Now, to hand it in. Open up Quercus at q.utoronto.ca, log in and navigate to this course. Click Assignments. Click (the title of) Assignment 0. There is a big blue Submit Assignment button top right. Click it. You'll get a File Upload at the bottom of the screen. Click Choose File and find the HTML file that you downloaded. Click Open (or equivalent on your system). The name of the file should appear next to Choose File. Click Submit Assignment. You'll see Submitted at the top right. If you want to try this again, you can Re-submit Assignment as many times as you like. (For the real thing, you can use this if you realize you made a mistake in something you submitted. The graders' instructions, for the real thing, are to grade the last file submitted, so in that case you need to make sure that the last thing submitted includes everything that you want graded. Here, though, it doesn't matter.)

(k) Optional extra. Something more ambitious: make a scatterplot of gas mileage mpg, on the y axis, against horsepower, hp, on the x-axis.

Solution

That goes like this. I'll explain the steps below.





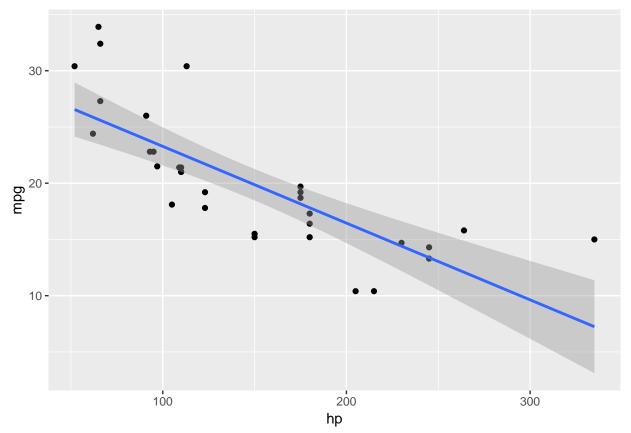
%\$ %\$

This shows a somewhat downward trend, which is what you'd expect, since a larger hp value means a more powerful engine, which will probably consume more gas and get *fewer* miles per gallon. As for the code: to make a ggplot plot, as we will shortly see in class, you first need a ggplot statement that says what to plot. The first thing in a ggplot is a data frame (mtcars here), and then the aes says that the plot will have hp on the x-axis and mpg on the y-axis, taken from the data frame that you specified. That's all of the what-to-plot. The last thing is how to plot it; geom_point() says to plot the data values as points.

You might like to add a regression line to the plot. That is a matter of adding this to the end of the plotting

command:





The line definitely goes downhill. Decide for yourself how well you think a line fits these data.

Data file operations

In this question, we read a file from the web and do some descriptive statistics and a graph. This is very like what you will be doing on future assignments, so it's good to practice it now.

Take a look at the data file at https://www.utsc.utoronto.ca/~butler/c32/jumping.txt. These are measurements on 30 rats that were randomly made to do different amounts of jumping by group (we'll see the details later in the course). The control group did no jumping, and the other groups did "low jumping" and "high jumping". The first column says which jumping group each rat was in, and the second is the rat's bone density (the experimenters' supposition was that more jumping should go with higher bone density).

(a) What are the two columns of data separated by? (The fancy word is "delimited").

Solution

Exactly one space. This is true all the way down, as you can check.

(b) Make a new R Notebook. Leave the first four lines, but get rid of the rest of the template document. Start with a code chunk containing library(tidyverse). Run it.

Solution

You will get either the same message as before or nothing. (I got nothing because I had already loaded the tidyverse in this session.)

(c) Put the URL of the data file in a variable called my_url. Then use read_delim to read in the file. (See solutions for how.) read_delim reads data files where the data values are always separated by the same single character, here a space. Save the data frame in a variable rats.

Solution

Like this:

```
library(tidyverse)
my_url="https://www.utsc.utoronto.ca/~butler/c32/jumping.txt"
rats=read_delim(my_url," ")

## Parsed with column specification:
## cols(
## group = col_character(),
## density = col_integer()
## )
```

The second thing in read_delim is the thing that separates the data values. Often when you use read_delim it'll be a space.

(d) Take a look at your data frame, by making a new code chunk and putting the data frame's name in it (as we did with mtcars).

Solution

```
rats
```

```
## # A tibble: 30 x 2
      group
##
              density
##
      <chr>
                <int>
##
    1 Control
                  611
##
  2 Control
                  621
  3 Control
                  614
##
  4 Control
                  593
##
##
    5 Control
                  593
##
  6 Control
                  653
                  600
  7 Control
## 8 Control
                  554
## 9 Control
                  603
## 10 Control
                  569
## # ... with 20 more rows
```

There are 30 rows and two columns, as there should be.

(e) Find the mean bone density for rats that did each amount of jumping.

Solution

This is something you'll see a lot: group_by followed by summarize. Reminder: to get that funny thing with the percent signs (called the "pipe symbol"), type control-shift-M (or equivalent on a Mac):

```
rats %>% group_by(group) %>%
summarize(m=mean(density))
```

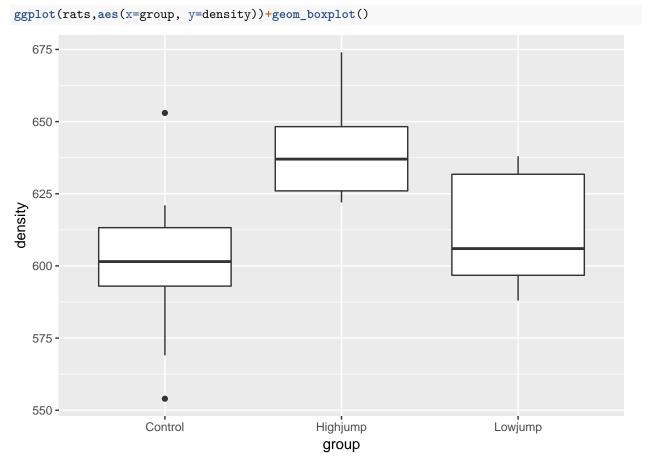
```
## # A tibble: 3 x 2
## group m
## <chr> <dbl>
## 1 Control 601.
## 2 Highjump 639.
## 3 Lowjump 612.
```

The mean bone density is clearly highest for the high jumping group, and not much different between the low-jumping and control groups.

(f) Make a boxplot of bone density for each jumping group.

Solution

On a boxplot, the groups go across and the values go up and down, so the right syntax is this:



Given the amount of variability, the control and low-jump groups are very similar (with the control group having a couple of outliers), but the high-jump group seems to have a consistently higher bone density than the others.

This is more or less in line with what the experimenters were guessing, but it seems that it has to be high jumping to make a difference.

You might recognize that this is the kind of data where we would use analysis of variance, which we will do later on in the course: we are comparing several (here three) groups.