

# Intro to Hypothesis Testing

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# Learning goals

- Understand basic ideas of hypothesis testing
- Familiarity with basic jargon
- Interpretation of  $p$ -values

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- Null hypothesis  
 $H_0$ : At least 50% of the U.S. registered voters views the president favorable.
- Alternative hypothesis  
 $H_1$ : Less than 50% of the U.S. registered voters views the president favorable.

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What is the probability of getting 48% or less in the poll if 50% of the U.S. population views the president favorable.

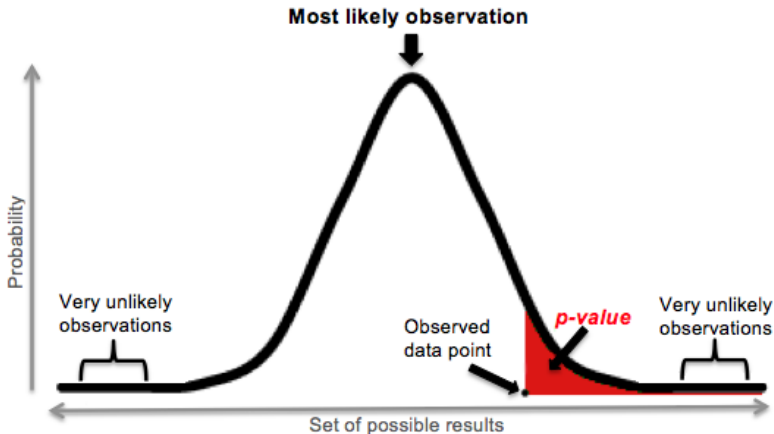
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$p$ -value

$$p = 0.13$$

# How to do hypothesis testing?



**A *p-value* (shaded red area) is the probability of an observed (or more extreme) result arising by chance**

## How to do hypothesis testing?

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NBC/WSJ poll held from February 14 to 16 among 800 registered voters, 48% favorable
- Probability of observing  $Y$  or more different from  $H_1$  under  $H_0$   
What is the probability of getting 48% or less in the poll if 50% of the U.S. population views the president favorable.  
 $p$ -value  
 $p = 0.13$
- Reject  $H_0$  if  $p < \alpha$  where  $\alpha$  is the significance level.

# Learning goals

- Understand basic ideas of hypothesis testing
- Familiarity with basic jargon  
 $H_0$ ,  $H_1$ ,  $p$ -value, significance level
- Basic interpretation of  $p$ -values