Topic analysis

```
In [1]:
         import json
         from sklearn.feature extraction.text import TfidfVectorizer
         import os
         import re
         def get fnames():
             """Read all text files in a folder.
             fnames = []
             for root,_,files in os.walk("./abstracts/awards_2002"):
                 for fname in files:
                     if fname[-4:] == ".txt":
                         fnames.append(os.path.join(root, fname))
             return fnames
         print("Number of abstracts in folder awards_2002: {}".format(len(get_fnames())
        Number of abstracts in folder awards_2002: 9923
In [2]:
         name_list = get_fnames()
         def read file(fname):
             with open(fname, 'r', encoding="ISO-8859-1") as f:
                 # skip all lines until abstract
                 for line in f:
                     if "Abstract :" in line:
                         break
                 # get abstract as a single string
                 abstract = ' '.join([line[:-1].strip() for line in f])
                 abstract = re.sub(' +', ' ', abstract) # remove double spaces
                 return abstract
In [3]:
         documents = []
         for i in name list:
             documents.append(read_file(i))
In [4]:
         print(documents[6])
```

This proposal focuses on problems in q-series and partitions. There are five s eparate parts of this work. The first part considers research tied to applicat ions of the construction of representations of Lie algebras. Next the investig ator looks at new q-series methods related to special problems in number theor y. The third part discusses applications of the Omega software package (http:/ /www.uni-linz.ac.at/research/ combinat/risc/software/Omega/) which is being de veloped by the investigator in collaboration with colleagues at Linz. The focu s in this latter section is on mutli-dimensional partitions. The fourth sectio n is devoted to the study of Bailey chains and a consideration ofhow recent di scoveries of the investigator may lead to new applications of this concept. Th e proposal concludes with consideration of three major unsolved problems in th e theory of partitions: (1) the Friedman-Joichi- Stanton conjecture, (2) the B orwein conjecture and (3) the Okada conjecture. Each of these three conjecture s has been around for some time. The theme of this proposal put succinctly mig ht be: Building bridges from partitions and q-series (two intrinsically deep a nd charming but sometimes rather introverted topics) to several branches of ma thematics and science. The first two sections are devoted to relating this wor k to representation theory and number theory, two branches of mathematics; in each instance, it is clear that this interaction will not only enrich the obje ct fields, but also will provide new insights for partitions and q-series. The work on the Omega package has great potential. Here the investigator and his c ollaborators have found numerous instances where research discoveries have gon e from being unthinkable to easily reached. The possible applications to multi -dimensional partitions should lead to insights in combinatorics and, hopefull y, the combinatorial aspects of physics. The work on Bailey chains in the past has had profound impact on statistical mechanics in physics. The more this met hod is advanced, the more we may expect these mutually beneficial applications to continue. The final section on three unsolved problems appears, at first, t o be a purely internal study. However, as has often happend in the past, whene ver new methods are discovered to solve really hard problems, there is almost always a spillover into vital applications.

Features extraction by tf-idf with different parameters

```
In [5]: len(documents)
Out[5]: 9923
In [6]: # Set parameters and initialize
    tfidf_vectorizer = TfidfVectorizer()
    # Tip: the vectorizer also supports extracting n-gram features (common short
    # Calcualate term-document matrix with tf-idf scores
    tfidf_matrix = tfidf_vectorizer.fit_transform(documents)
    # Check matrix shape
    tfidf_matrix.toarray().shape # N_docs x N_terms
Out[6]: (9923, 53816)
```

```
In [7]:
          # Set parameters and initialize
          tfidf_vectorizer1 = TfidfVectorizer(stop_words = 'english', lowercase= True,
          # Tip: the vectorizer also supports extracting n-gram features (common short
          # Calcualate term-document matrix with tf-idf scores
          tfidf matrix1 = tfidf vectorizer1.fit transform(documents)
          # Check matrix shape
          tfidf matrix1.toarray().shape # N docs x N terms
Out[7]: (9923, 27001)
In [8]:
         # Set parameters and initialize
          tfidf vectorizer2 = TfidfVectorizer(stop words = 'english', lowercase= True,
          # Tip: the vectorizer also supports extracting n-gram features (common short
          # Calcualate term-document matrix with tf-idf scores
          tfidf matrix2 = tfidf vectorizer2.fit transform(documents)
          # Check matrix shape
          tfidf_matrix2.toarray().shape # N docs x N terms
Out[8]: (9923, 190731)
 In [9]:
          # Set parameters and initialize
          tfidf_vectorizer3 = TfidfVectorizer(stop_words = 'english', lowercase= True,
          # Tip: the vectorizer also supports extracting n-gram features (common short
          # Calcualate term-document matrix with tf-idf scores
          tfidf matrix3 = tfidf vectorizer3.fit transform(documents)
          # Check matrix shape
          tfidf matrix3.toarray().shape # N docs x N terms
Out[9]: (9923, 117124)
In [10]:
          # Set parameters and initialize
          tfidf vectorizer4 = TfidfVectorizer(stop words = 'english', lowercase= True,
          # Tip: the vectorizer also supports extracting n-gram features (common short
          # Calcualate term-document matrix with tf-idf scores
          tfidf matrix4 = tfidf vectorizer4.fit transform(documents)
          # Check matrix shape
          tfidf matrix4.toarray().shape # N docs x N terms
```

2506

systems

```
Out[10]: (9923, 334856)
In [11]:
          # Set parameters and initialize
          tfidf_vectorizer5 = TfidfVectorizer(stop_words = 'english', lowercase= True,
          # Tip: the vectorizer also supports extracting n-gram features (common short
          # Calcualate term-document matrix with tf-idf scores
          tfidf_matrix5 = tfidf_vectorizer5.fit transform(documents)
          # Check matrix shape
          tfidf matrix5.toarray().shape # N docs x N terms
Out[11]: (9923, 54049)
In [12]:
          ## Inspect document frequencies (counts) of terms
          from collections import Counter
          terms in docs = tfidf vectorizer1.inverse transform(tfidf matrix1)
          token_counter = Counter()
          for terms in terms_in_docs:
              token_counter.update(terms)
          for term, count in token_counter.most_common(20):
              print("%d\t%s" % (count, term))
         6642
                 research
         5401
                project
         3958
                 new
         3314 study
         3184
                 provide
         3037
               used
         2967
                 development
         2944
                 students
         2909
                 data
         2898
                 use
         2889
                 university
         2868
                 understanding
         2787
                 using
         2774
                 work
         2727
                 based
         2627
                high
         2606
                 program
         2596
                 develop
         2534
                 important
```

```
In [13]:
         ## Inspect key words per document
         features1 = tfidf_vectorizer1.get_feature_names()
         for doc i in range(5):
             print("\nDocument %d, key words by TF-IDF" % doc i)
             for term, score in sorted(list(zip(features1,tfidf matrix1.toarray())[doc
                 print("%.2f\t%s" % (score, term))
         Document 0, key words by TF-IDF
         0.30
                chow
         0.20
               hodge
         0.20
              algebraic
         0.15
                geometry
              subgroup
         0.15
         Document 1, key words by TF-IDF
         0.24
               friendships
         0.23 cultivating
         0.22 ethnically
         0.21
              control
         0.20
               exchanging
         Document 2, key words by TF-IDF
         0.31
               updating
         0.20
              reference
              secondly
         0.19
         0.18
                method
         0.16
                inman
         Document 3, key words by TF-IDF
         0.24
               conference
         0.21 computations
         0.20
              learn
         0.19
               theory
         0.19
                group
         Document 4, key words by TF-IDF
         0.22
               uncontrollable
         0.21 commonality
         0.19 uncertainties
```

preferences

alternative

0.19

```
In [14]:
          ## Inspect top terms per document
          features2 = tfidf_vectorizer2.get_feature_names()
          for doc i in range(5):
              print("\nDocument %d, key words by TF-IDF" % doc_i)
              for term, score in sorted(list(zip(features2,tfidf matrix2.toarray())[doc
                  print("%.2f\t%s" % (score, term))
         Document 0, key words by TF-IDF
         0.21
                 algebraic geometry
         0.17
                 geometry algebraic
         0.11
                 abelian varieties
         0.11
                 algebraic finite
         0.11
                 chow groups
         Document 1, key words by TF-IDF
              control engineering
         0.29
         0.19
                 2002 american
         0.19
                 academic positions
         0.19
                 special sessions
         0.19
                 support american
         Document 2, key words by TF-IDF
         0.20 basis method
         0.20
                 model updating
         0.17
               based simulation
         0.16
                 proposed effort
         0.14
                 model based
         Document 3, key words by TF-IDF
         0.19
              group theory
         0.16
                 open problems
         0.13
                 28 2003
         0.13
               area learn
         0.13
               conference goal
         Document 4, key words by TF-IDF
         0.23 design alternative
         0.20
              design selection
         0.19
              engineering design
         0.18
                 product line
         0.12
                 alternative set
In [15]:
          features3 = tfidf vectorizer3.get feature names()
          for doc i in range(5):
              print("\nDocument %d, key words by TF-IDF" % doc i)
              for term, score in sorted(list(zip(features3,tfidf matrix3.toarray())[doc
                  print("%.2f\t%s" % (score, term))
```

```
Document 0, key words by TF-IDF
               example algebraic geometry
         0.27
         0.27
                 focuses different aspects
         0.27
                phenomena mathematical problems
         0.27
                 problems various fields
         0.27
                 quantum mechanics theory
         Document 1, key words by TF-IDF
         0.47
               nsf career program
                 preparing students professional
         0.47
         0.45
                 american control conference
         0.43
                 diverse group students
         0.41
                 support travel expenses
         Document 2, key words by TF-IDF
         0.44
               model based simulation
         0.28
                 aim research develop
         0.28 daniel inman virginia
         0.28
                 proposed effort improve
         0.28
              research develop improved
         Document 3, key words by TF-IDF
               24 28 2003
         0.25
              goal provide forum
         0.25
         0.25
              including solid state
         0.25
                 march 24 28
         0.25
                 recent research developments
         Document 4, key words by TF-IDF
         0.41 develop integrated framework
         0.38
                research advance state
         0.38 research develop integrated
                 research provide opportunities
         0.36
         0.35
                 provide opportunities students
In [16]:
          features4 = tfidf vectorizer4.get feature names()
          for doc i in range(5):
             print("\nDocument %d, key words by TF-IDF" % doc i)
              for term, score in sorted(list(zip(features4,tfidf matrix4.toarray()[doc
                  print("%.2f\t%s" % (score, term))
```

```
Document 0, key words by TF-IDF
         0.21
               chow
         0.14
                 hodge
         0.14
              algebraic
         0.14
                 algebraic geometry
                 geometry algebraic
         0.11
         Document 1, key words by TF-IDF
         0.22
               control engineering
         0.15
                 2002 american
         0.15 academic positions
         0.15
                 nsf career program
         0.15
                 preparing students professional
         Document 2, key words by TF-IDF
         0.18
                updating
         0.15
               basis method
         0.15 model updating
                 model based simulation
         0.14
         0.13
                based simulation
         Document 3, key words by TF-IDF
         0.15
               group theory
         0.13
              open problems
         0.12 conference
         0.10
                 computations
         0.10
                learn
         Document 4, key words by TF-IDF
              design alternative
         0.17
         0.15
                 design selection
         0.14 engineering design
         0.14
                 uncontrollable
         0.14
                 product line
In [17]:
          features5 = tfidf vectorizer5.get feature names()
          for doc i in range(5):
             print("\nDocument %d, key words by TF-IDF" % doc i)
              for term, score in sorted(list(zip(features5,tfidf matrix5.toarray()[doc
                 print("%.2f\t%s" % (score, term))
```

KMeans()

Out[18]:

```
Document 0, key words by TF-IDF
         0.27
                chow
         0.18
                 hodge
         0.18
                 algebraic
         0.18
                 algebraic geometry
         0.14
                 geometry algebraic
         Document 1, key words by TF-IDF
         0.27
               control engineering
         0.17
                 diverse group students
              particular students
         0.17
         0.17
                 students seeking
         0.16
                 cultivating
         Document 2, key words by TF-IDF
         0.22
                updating
         0.18
                 model based simulation
         0.16
              based simulation
         0.14
                 reference
         0.14
                 proposed effort
         Document 3, key words by TF-IDF
         0.20
               group theory
              open problems
         0.17
         0.16
              conference
         0.14
                 computations
         0.13
                 learn
         Document 4, key words by TF-IDF
         0.21
              design alternative
         0.18
                 engineering design
         0.17 product line
         0.16
                 commonality
         0.15
                 uncertainties
In [18]:
          from sklearn.cluster import KMeans
          km1 = KMeans()
         km1.fit(tfidf matrix1)
```

```
In [19]:
          import heapq, numpy as np
          # Custom function to print top keywords for each cluster
          def print clusters(matrix, clusters, n keywords=10):
              for cluster in range(min(clusters), max(clusters)+1):
                  cluster docs = [i for i, c in enumerate(clusters) if c == cluster]
                  print("Cluster: %d (%d docs)" % (cluster, len(cluster docs)))
                  # Keep scores for top n terms
                  new_matrix = np.zeros((len(cluster_docs), matrix.shape[1]))
                  for cluster i, doc vec in enumerate(matrix[cluster docs].toarray()):
                      for idx, score in heapq.nlargest(n keywords, enumerate(doc vec),
                          new matrix[cluster i][idx] = score
                  # Aggregate scores for kept top terms
                  keywords = heapq.nlargest(n_keywords, zip(new_matrix.sum(axis=0), fea
                  print(', '.join([w for s,w in keywords]))
                  print()
```

```
In [20]: print_clusters(tfidf_matrix1, km1.labels_)
```

```
Cluster: 0 (2424 docs)
         wireless, software, networks, power, sensor, grid, language, network, distribu
         ted, decision
         Cluster: 1 (1699 docs)
         polymer, magnetic, spin, quantum, nmr, reactions, laser, nano, molecules, film
         Cluster: 2 (225 docs)
         available, zygotic, zygomycota, zygomycetes, zygmund, zworski, zurich, zuni, z
         ro2, zr
         Cluster: 3 (1802 docs)
         workshop, conference, teachers, reu, stem, mathematics, engineering, meeting,
         learning, curriculum
         Cluster: 4 (1865 docs)
         ice, ocean, mantle, climate, solar, arctic, galaxies, seismic, stars, wind
         Cluster: 5 (84 docs)
         fellowship, mathematical, sciences, postdoctoral, informatics, training, micro
         bial, minority, fellowships, biology
         Cluster: 6 (578 docs)
         equations, manifolds, spaces, algebraic, theory, geometry, algebras, quantum,
         hyperbolic, topology
         Cluster: 7 (1246 docs)
         genes, species, protein, plant, proteins, gene, plants, genome, evolutionary,
         genetic
In [21]:
          from sklearn.cluster import KMeans
          # Do clustering
          km1 = KMeans()
          km1.fit(tfidf matrix2)
```

Out[21]: KMeans()

```
In [22]:
          import heapq, numpy as np
          # Custom function to print top keywords for each cluster
          def print clusters(matrix, clusters, n keywords=10):
              for cluster in range(min(clusters), max(clusters)+1):
                  cluster docs = [i for i, c in enumerate(clusters) if c == cluster]
                  print("Cluster: %d (%d docs)" % (cluster, len(cluster docs)))
                  # Keep scores for top n terms
                  new_matrix = np.zeros((len(cluster_docs), matrix.shape[1]))
                  for cluster i, doc vec in enumerate(matrix[cluster docs].toarray()):
                      for idx, score in heapq.nlargest(n keywords, enumerate(doc vec),
                          new matrix[cluster i][idx] = score
                  # Aggregate scores for kept top terms
                  keywords = heapq.nlargest(n_keywords, zip(new_matrix.sum(axis=0), fea
                  print(', '.join([w for s,w in keywords]))
                  print()
```

```
In [23]: print_clusters(tfidf_matrix2, km1.labels_)
```

Cluster: 0 (377 docs)

physical chemistry, transition metal, surface chemistry, number areas, areas i ncluding, ray diffractometer, time resolved, focus research, analytical surface, reactive intermediates

Cluster: 1 (57 docs)

sciences fellowship, mathematical sciences, biological informatics, goal fello wship, sciences fellowships, research training, entitled modeling, entitled in fluence, entitled role, fellowship fy2002

Cluster: 2 (758 docs)

mathematics science, middle school, computer science, community college, engin eering technology, science mathematics, program intended, graduate education, school districts, math science

Cluster: 3 (386 docs)

earth science, researchers represent, disciplinary databases, data sets, proof concept, knowledge discovery, digital library, analysis networked, amounts div erse, agencies geological

Cluster: 4 (6352 docs)

postdoctoral fellowship, number theory, real time, algebraic geometry, dynamic al systems, representation theory, microbial biology, solar wind, dark matter, star formation

Cluster: 5 (765 docs)

reu site, research experience, spin polarized, self assembly, shipboard scient ific, scientific support, support equipment, equipment including, magnetic properties, condensed matter

Cluster: 6 (746 docs)

sea ice, ice sheet, ice core, organic matter, carbon cycle, 000 years, carbon dioxide, climate change, southern ocean, ice cores

Cluster: 7 (482 docs)

research fellowship, ii project, phase ii, fuel cell, drug delivery, fuel cell s, silicon carbide, high temperature, rich media, cutting tool

```
In [24]: km1 = KMeans()
km1.fit(tfidf_matrix3)
```

Out[24]: KMeans()

```
In [25]:
          import heapq, numpy as np
          # Custom function to print top keywords for each cluster
          def print clusters(matrix, clusters, n keywords=10):
              for cluster in range(min(clusters), max(clusters)+1):
                  cluster docs = [i for i, c in enumerate(clusters) if c == cluster]
                  print("Cluster: %d (%d docs)" % (cluster, len(cluster docs)))
                  # Keep scores for top n terms
                  new_matrix = np.zeros((len(cluster_docs), matrix.shape[1]))
                  for cluster i, doc vec in enumerate(matrix[cluster docs].toarray()):
                      for idx, score in heapq.nlargest(n keywords, enumerate(doc vec),
                          new matrix[cluster i][idx] = score
                  # Aggregate scores for kept top terms
                  keywords = heapq.nlargest(n_keywords, zip(new_matrix.sum(axis=0), fea
                  print(', '.join([w for s,w in keywords]))
                  print()
```

```
In [26]: print_clusters(tfidf_matrix3, km1.labels_)
```

Cluster: 0 (100 docs)

support month research, award support month, fellowship program enables, inter national research fellowship, month research fellowship, archaeal bacterial viral, additional training microbial, bacterial viral species, avail unique research, assist new scientists

Cluster: 1 (142 docs)

engineering initiative nsf, funded experimental physical, initiative nsf 01, 1 57 category ner, 01 157 category, project funded experimental, physical chemis try program, students postdoctoral research, project addresses fundamental, re ceived response nanoscale

Cluster: 2 (16 docs)

astrophysics postdoctoral fellowship, astronomy astrophysics postdoctoral, awa rded nsf astronomy, carry program research, fellowship carry program, research education experimental, particle physics based, experimental elementary particle, education experimental elementary, requests support group

Cluster: 3 (92 docs)

carnegie mellon university, collaborative research project, basis equality rec iprocity, international collaborative research, supports collaborative research, award supports collaborative, bringing leading experts, project multidiscip linary international, multidisciplinary international collaborative, principal investigator dr

Cluster: 4 (9124 docs)

mathematical sciences fellowship, national science foundation, partial differe ntial equations, science foundation support, small grant exploratory, grant ex ploratory research, proposal number cts, foundation support dr, dissertation r esearch project, world wide web

Cluster: 5 (32 docs)

doctoral dissertation research, award award provide, enable promising student, establish strong independent, economic cultural environmental, dissertation re search improvement, global innovation networks, serve baseline comparison, tre e ring chronologies, depth interviews key

Cluster: 6 (386 docs)

business innovation research, innovation research sbir, small business innovat ion, sbir phase project, research sbir phase, innovation research phase, research phase project, phase ii project, phase project develop, phase project proposes

Cluster: 7 (31 docs)

biological informatics occupational, informatics fy2002 fellowship, biological informatics fy2002, biological informatics research, biology informational computational, career biological informatics, computational mathematical statistical, contributing future vitality, attain goal fellowship, academia industry attain

In [29]:

```
In [27]:
          km1 = KMeans()
          km1.fit(tfidf_matrix4)
         KMeans()
Out[27]:
In [28]:
          import heapq, numpy as np
          # Custom function to print top keywords for each cluster
          def print_clusters(matrix, clusters, n_keywords=10):
              for cluster in range(min(clusters), max(clusters)+1):
                  cluster_docs = [i for i, c in enumerate(clusters) if c == cluster]
                  print("Cluster: %d (%d docs)" % (cluster, len(cluster_docs)))
                  # Keep scores for top n terms
                  new matrix = np.zeros((len(cluster docs), matrix.shape[1]))
                  for cluster_i, doc_vec in enumerate(matrix[cluster_docs].toarray()):
                      for idx, score in heapq.nlargest(n keywords, enumerate(doc vec),
                          new_matrix[cluster_i][idx] = score
                  # Aggregate scores for kept top terms
                  keywords = heapq.nlargest(n_keywords, zip(new_matrix.sum(axis=0), fea
                  print(', '.join([w for s,w in keywords]))
                  print()
```

print_clusters(tfidf_matrix4, km1.labels)

Cluster: 0 (446 docs)
fuel, phase ii project, sensor, drug, phase ii, ii project, coatings, fuel cel
l, silicon, drug delivery

Cluster: 1 (1721 docs)

sensor, wireless, grid, routing, software, agents, mobile, power, code, memory

Cluster: 2 (578 docs)

manifolds, equations, algebraic, algebras, hyperbolic, spaces, number theory, representation theory, conjecture, string

Cluster: 3 (225 docs)

available, zygotic, zygomycota aftol project, zygomycota aftol, zygomycota, zy gomycetes ascomycetes basidiomycetes, zygomycetes ascomycetes, zygomycetes, zygmund operators spaces, zygmund operators

Cluster: 4 (126 docs)

fellowship, sciences fellowship, mathematical sciences fellowship, mathematical sciences, mathematical, sciences, postdoctoral fellowship, biological informatics, postdoctoral, informatics

Cluster: 5 (1966 docs)

conference, workshop, stem, symposium, teachers, reu, reu site, meeting, girls , scholarship

Cluster: 6 (3540 docs)

ice, contract, galaxies, arctic, mantle, stars, forest, solar, soil, co2

Cluster: 7 (1321 docs)

nmr, spin, polymer, magnetic, french, films, reactions, cnrs, nanoparticles, n anotubes

```
In [30]:
    from sklearn.cluster import KMeans
    km1 = KMeans()
```

km1.fit(tfidf_matrix5)

Out[30]: KMeans()

```
In [31]:
          import heapq, numpy as np
          # Custom function to print top keywords for each cluster
          def print clusters(matrix, clusters, n keywords=10):
              for cluster in range(min(clusters), max(clusters)+1):
                  cluster docs = [i for i, c in enumerate(clusters) if c == cluster]
                  print("Cluster: %d (%d docs)" % (cluster, len(cluster docs)))
                  # Keep scores for top n terms
                  new_matrix = np.zeros((len(cluster_docs), matrix.shape[1]))
                  for cluster i, doc vec in enumerate(matrix[cluster docs].toarray()):
                      for idx, score in heapq.nlargest(n keywords, enumerate(doc vec),
                          new matrix[cluster i][idx] = score
                  # Aggregate scores for kept top terms
                  keywords = heapq.nlargest(n_keywords, zip(new_matrix.sum(axis=0), fea
                  print(', '.join([w for s,w in keywords]))
                  print()
```

```
In [32]: print_clusters(tfidf_matrix5, km1.labels_)
```

```
Cluster: 0 (1232 docs)
stem, reu, teachers, reu site, scholarship, mathematics, girls, teacher, csems
, fellows
Cluster: 1 (3028 docs)
ice, mantle, solar, arctic, galaxies, ocean, forest, stars, wind, species
Cluster: 2 (444 docs)
phase ii, fuel, phase ii project, ii project, sensor, coatings, membrane, drug
, optical, fuel cell
Cluster: 3 (2299 docs)
manifolds, equations, quantum, grid, spaces, wireless, algebraic, code, softwa
re, power
Cluster: 4 (225 docs)
available, zurich, zr, zooplankton species, zooplankton, zoology, zoological,
zoning, zones long lived, zones long
Cluster: 5 (1802 docs)
protein, spin, nmr, proteins, complexes, polymer, molecules, magnetic, reactio
ns, arabidopsis
Cluster: 6 (126 docs)
fellowship, sciences fellowship, mathematical sciences fellowship, mathematica
1 sciences, mathematical, sciences, postdoctoral fellowship, abroad, biologica
l informatics, postdoctoral
Cluster: 7 (767 docs)
workshop, conference, symposium, meeting, french, cnrs, gordon, congress, sess
ions, speakers
```

change k for ngram =(1,3)

```
In [34]:
          import heapq, numpy as np
          # Custom function to print top keywords for each cluster
          def print clusters(matrix, clusters, n keywords=10):
              for cluster in range(min(clusters), max(clusters)+1):
                  cluster docs = [i for i, c in enumerate(clusters) if c == cluster]
                  print("Cluster: %d (%d docs)" % (cluster, len(cluster docs)))
                  # Keep scores for top n terms
                  new matrix = np.zeros((len(cluster docs), matrix.shape[1]))
                  for cluster i, doc vec in enumerate(matrix[cluster docs].toarray()):
                      for idx, score in heapq.nlargest(n keywords, enumerate(doc vec),
                          new matrix[cluster i][idx] = score
                  # Aggregate scores for kept top terms
                  keywords = heapq.nlargest(n_keywords, zip(new_matrix.sum(axis=0), fea
                  print(', '.join([w for s,w in keywords]))
                  print()
In [35]:
          print clusters(tfidf matrix5, model.labels )
         Cluster: 0 (225 docs)
         available, zurich, zr, zooplankton species, zooplankton, zoology, zoological,
         zoning, zones long lived, zones long
         Cluster: 1 (7098 docs)
         ice, mantle, quantum, magnetic, protein, solar, manifolds, arctic, sensor, fau
         Cluster: 2 (2600 docs)
         workshop, conference, fellowship, sciences fellowship, mathematical sciences f
         ellowship, mathematical sciences, stem, reu, teachers, mathematical
 In [ ]:
```