

# Physic-Informed Neural Networks for Medical Data

Anh Thu VU, Thi Minh Nguyet LE

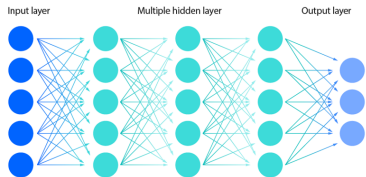
27/03/2025

- 1 Physics-Informed Neural Networks (PINNs)
- 2 Motivations
- 3 Methods
- 4 Limitations
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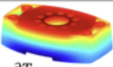
# Physics-Informed Neural Networks

Deep neural network



$$\mathcal{L}_{\text{supervised}} = \frac{1}{N} \sum_{i=1}^N (\hat{y}_i - y_{\text{true}})^2$$

Physics Knowledge


$$\rho c \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T)$$

$$\mathcal{L}_{\text{unsupervised}}$$

PINN

# Outline

- 1 Physics-Informed Neural Networks (PINNs)
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- Limited labeled data in biomedical settings

- Non-invasive diagnostic tools



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**Mammography:** exposing patients to ionizing radiation

Physics-informed neural network for fast prediction of temperature distributions in cancerous breasts as a potential efficient portable AI-based diagnostic tool

Olzhas Mukhmetov<sup>a</sup>, Yong Zhao<sup>a</sup>, Aigerim Mashekova<sup>a</sup>, Vasiliios Zarikas<sup>b,c</sup>,  
Eddie Yin Kwee Ng<sup>d,\*</sup>, Nurduman Aidossov<sup>a</sup>

PINN + thermograms from IR cameras  
+ 3D breast models from 3D scanner

- Non-invasive diagnostic tools



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PINN + thermograms from IR cameras  
+ 3D breast models from 3D scanner

“The comparison validates the PINN model as an accurate and fast method for thermal modeling and breast cancer diagnostic tool as the PINN simulation is found to be around 12 times faster than its Finite Element Analysis counterpart.”



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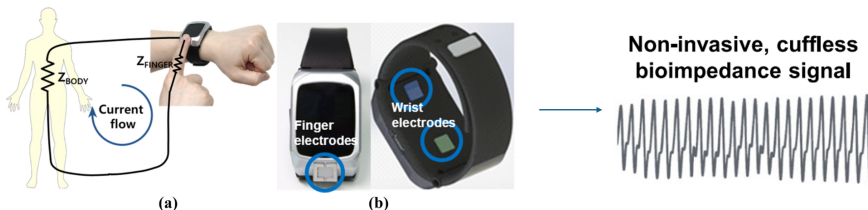
# Cuffless blood pressure estimation

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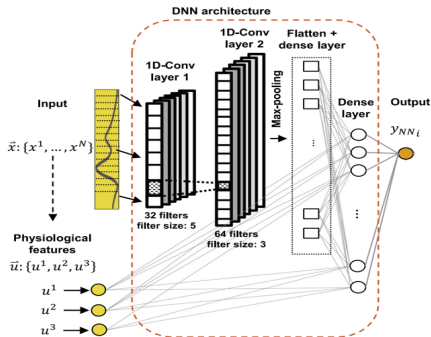
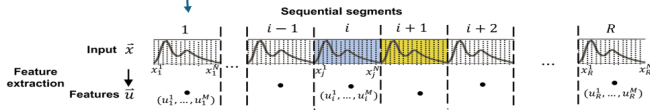
## Physics-informed neural networks for modeling physiological time series for cuffless blood pressure estimation

Kaan Sel<sup>1</sup>, Amirmohammad Mohammadi<sup>2</sup>, Roderic I. Pettigrew<sup>3</sup> and Roozbeh Jafari<sup>1,2,3</sup>✉



# Cuffless blood pressure estimation

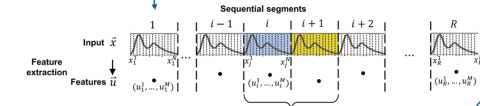
Non-invasive, cuffless  
bioimpedance signal



$$\text{Neural network: } y_{NN} = f_{NN}(\vec{x}, \vec{u}; \theta)$$

# Cuffless blood pressure estimation

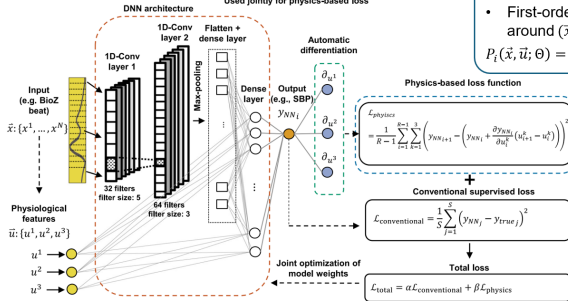
Non-invasive, cuffless  
bioimpedance signal



Used jointly for physics-based loss

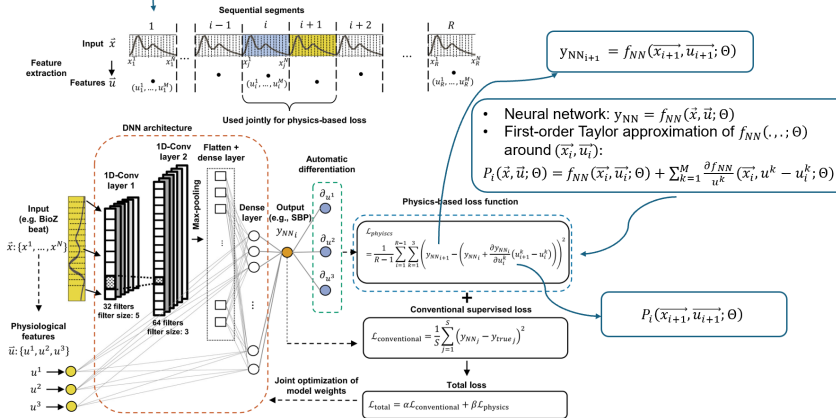
- Neural network:  $y_{NN} = f_{NN}(\vec{x}, \vec{u}; \Theta)$
- First-order Taylor approximation of  $f_{NN}(\cdot, \cdot; \Theta)$  around  $(\vec{x}_i, \vec{u}_i)$ :

$$P_i(\vec{x}, \vec{u}; \Theta) = f_{NN}(\vec{x}_i, \vec{u}_i; \Theta) + \sum_{k=1}^M \frac{\partial f_{NN}}{\partial u_i^k}(\vec{x}_i, u_i^k - u_i^k; \Theta)$$



# Cuffless blood pressure estimation

Non-invasive, cuffless  
bioimpedance signal





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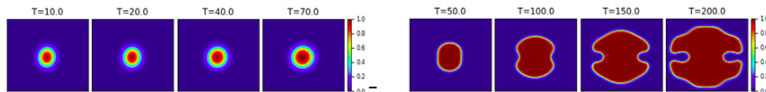
## Engineering Applications of Artificial Intelligence

journal homepage: [www.elsevier.com/locate/engappai](https://www.elsevier.com/locate/engappai)



### TGM-Nets: A deep learning framework for enhanced forecasting of tumor growth by integrating imaging and modeling

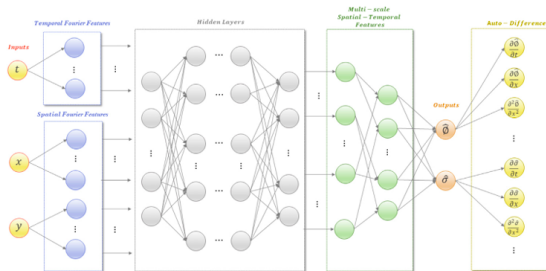
Qijing Chen <sup>a</sup>, Qi Ye <sup>b,c</sup>, Weiqi Zhang <sup>d,e</sup>, He Li <sup>e</sup>, Xiaoning Zheng <sup>a,\*</sup>



The tumor growth dynamics are described by the following phase-field equations:

$$\begin{aligned}\frac{\partial \phi}{\partial t} &= \lambda \nabla^2 \phi - 2\phi(1 - \phi)f(\phi, \sigma) \\ \frac{\partial \sigma}{\partial t} &= \eta \nabla^2 \sigma + S_h(1 - \phi) + S_c\phi - (\gamma_h(1 - \phi) + \gamma_c\phi)\sigma \\ f(\phi, \sigma) &= M(1 - 2\phi - 3m(\sigma)) \\ m(\sigma) &= m_{ref} \left( \frac{\rho + A}{2} + \frac{\rho - A}{\pi} \arctan \left( \frac{\sigma - \sigma_l}{\sigma_r} \right) \right)\end{aligned}\tag{1}$$

# Tumor growth forecasting



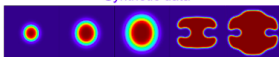
Loss Function

Mechanistic models

$$R_{\bar{\phi}} = \frac{\partial \bar{\phi}}{\partial t} - (\lambda \nabla^2 \bar{\phi} - 2\bar{\phi}(1 - \bar{\phi})f(\bar{\phi}, \bar{\phi}))$$

$$R_{\phi} = \frac{\partial \phi}{\partial t} - (\eta \nabla^2 \phi + S_h(1 - \bar{\phi}) + (S_c - s)\bar{\phi} - (\gamma_h(1 - \bar{\phi}) + \gamma_c \bar{\phi})\phi)$$

Synthetic data



Experimental data



Loss

$$Loss_{pde1} = \frac{1}{|X_{pde1}|} \sum_{x \in X_{pde1}} R_{\bar{\phi}}(x, \bar{\phi}, \dots, \bar{\phi}_{yy}, \bar{\phi}; \lambda)^2$$

$$Loss_{pde2} = \frac{1}{|X_{pde2}|} \sum_{x \in X_{pde2}} R_{\phi}(x, \bar{\phi}, \dots, \bar{\phi}_{yy}, \bar{\phi}; \lambda)^2$$

$$Loss_{data1} = \frac{1}{|X_{data1}|} \sum_{x \in X_{data1}} (\bar{\phi}(x) - \phi(x))^2$$

$$Loss_{data2} = \frac{1}{|X_{data2}|} \sum_{x \in X_{data2}} (\phi(x) - \phi(x))^2$$

$$Loss_{pde} = Loss_{pde1} + Loss_{pde2}$$

$$Loss_{data} = Loss_{data1} + Loss_{data2}$$

$$Loss = w_{pde} Loss_{pde} + w_{data} Loss_{data}$$



- $k_s, k_t$ : variance controlling hyperparameters.
- Weight matrices:  $B^s \sim \mathcal{N}(0, k_s^2)$  and  $B^t \sim \mathcal{N}(0, k_t^2)$ .
- The spatial and temporal Fourier features are then computed as:

$$\gamma^s(x) = \begin{pmatrix} \cos(2\pi B^s x) \\ \sin(2\pi B^s x) \end{pmatrix}, \quad \gamma^t(t) = \begin{pmatrix} \cos(2\pi B^t t) \\ \sin(2\pi B^t t) \end{pmatrix}$$

- Myocardial perfusion MRI quantification
- COVID-19 transmission dynamics analysis

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- PINNs are subject-specific due to personalized biological characteristics.
- PINNs still require certain assumptions in the model.
- In some applications, training PINNs requires dedicated hyperparameter tuning.

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- Q. Chen et. al, *TGM-Nets: A deep learning framework for enhanced forecasting of tumor growth by integrating imaging and modeling*, **Eng. Appl. Artif. Intell.** **126**, 2023.
- R.L.M. van Herten et. al, *Physics-informed neural networks for myocardial perfusion MRI quantification*, **Med. Image Anal** **8**, 2022.
- X. Ning, et. al, *Physics-Informed Neural Networks Integrating Compartmental Model for Analyzing COVID-19 Transmission Dynamics*, **Viruses** **15**, 2023.