

```
In [3]: ffddata <- read.delim("ffdata.txt", header = FALSE, sep = "")
```

```
In [4]: secdata <- read.delim("secdata.txt", header = FALSE, sep = "")
```

```
In [5]: retdata <- read.delim("retdate.txt", header = FALSE)
```

```
In [6]: ticker <- read.delim("ticker.txt", header = FALSE)
```

```
In [359]: stock_returns <- matrix(secdata[,2], nrow = 1511, ncol = 1877)
```

```
In [8]: market_cap <- matrix(secdata[,3], nrow = 1511, ncol = 1877)
```

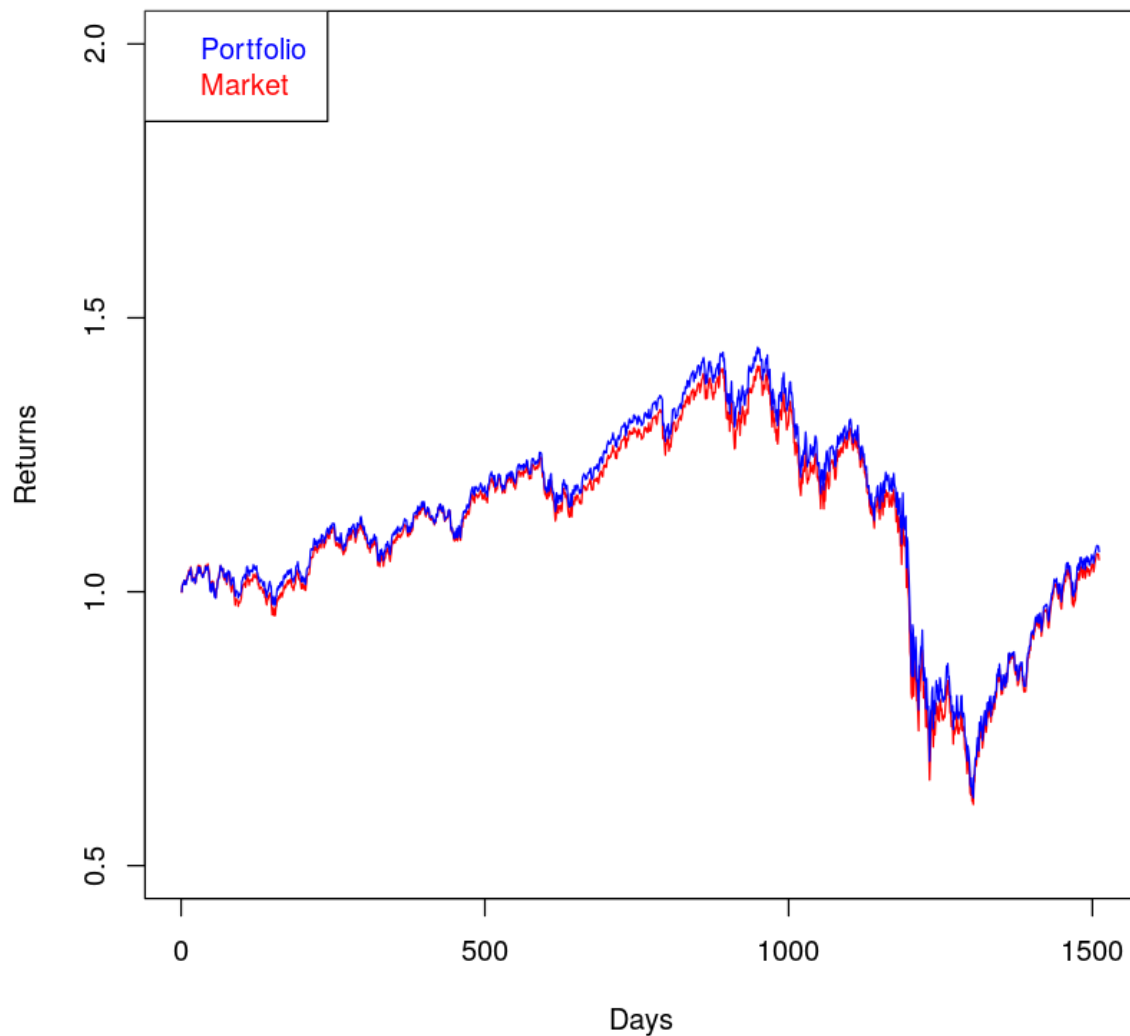
Question 1 Part a)

```
In [37]: net_returns <- c(rep(1,1511))
for (i in 2:1511) {
  net_returns[i] <- sum(market_cap[i,])/sum(market_cap[i-1,])
}
cum_net_returns <- c(rep(0,1511))
for (i in 1:1511) {
  cum_net_returns[i] <- prod(net_returns[1:i])
}
```

```
In [38]: ff_returns <- ffddata[,1] + 1
cum_ff_returns <- c(rep(0,1511))
for (i in 1:1511) {
  cum_ff_returns[i] <- prod(ff_returns[1:i])
}
```

```
In [39]: plot(cum_ff_returns, type = "l", ylim = c(0.5,2), col = "red", main = "Cumulative Return of the 1877 Stocks vs. Cumulative Market Return", xlab = "Days", ylab = "Returns")
legend("topleft", text.col = c("blue", "red"), c("Portfolio", "Market"))
lines(cum_net_returns, col = "blue")
```

Cumulative Return of the 1877 Stocks vs. Cumulative Market Return



We observe that the cumulative returns of the 1877 stocks and the cumulative returns of the market are overlapping, which suggests that the 1877 stocks we chose are a good tracker for market returns.

Question 1 Part b)

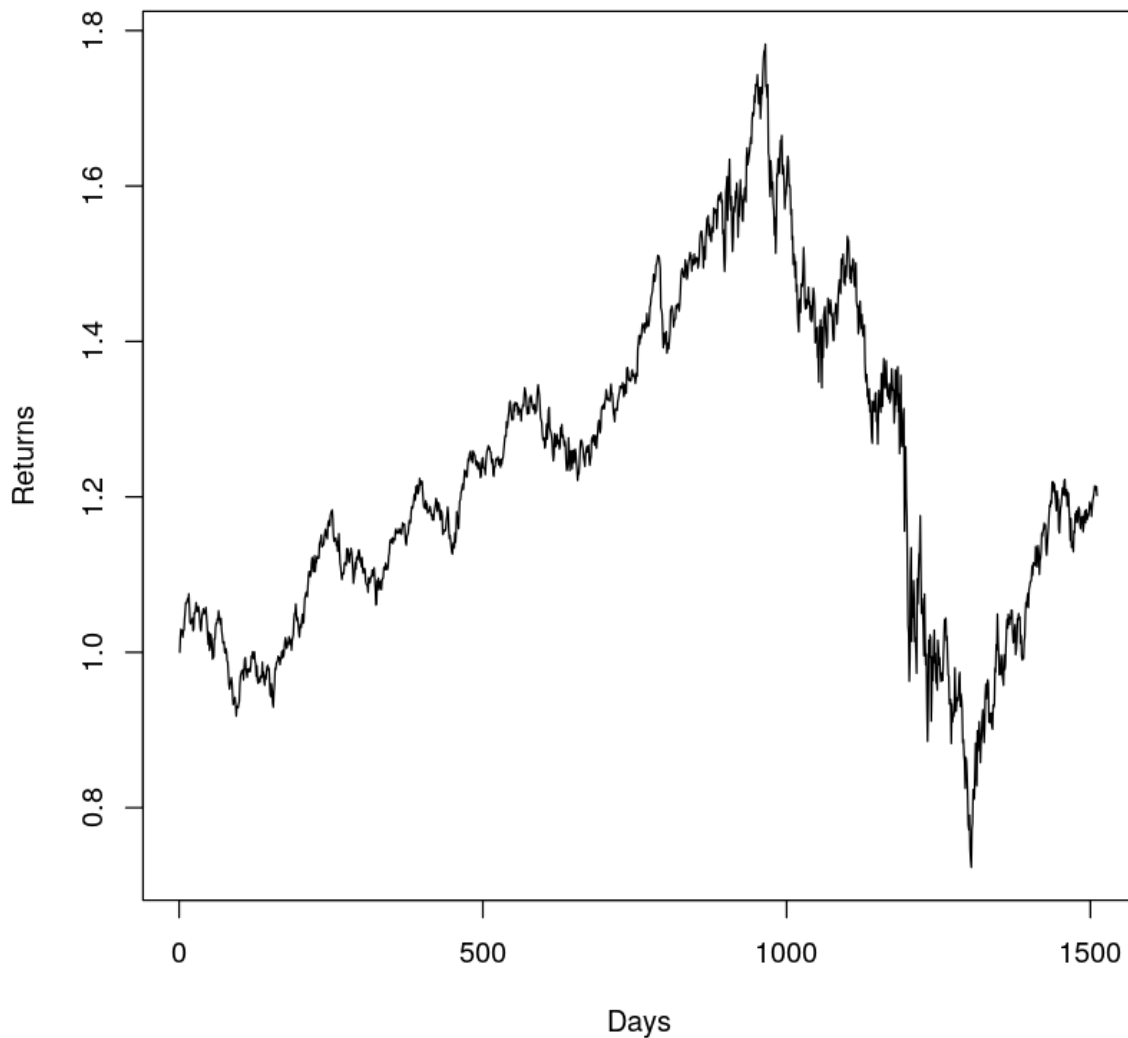
We will pick 50 stocks by randomly selecting 50 stocks from the first 800 stocks (alphabetically). We will first find and plot the cumulative returns of these randomly selected stocks. We will also find the RMSE

```
In [109]: set.seed(100)
rnd_stocks <- c(sample(1:800,50,replace=F))
rnd_stocks_return <- stock_returns[,rnd_stocks]
rnd_stocks_market_cap <- market_cap[,rnd_stocks]
```

```
In [110]: rnd_stock_net_returns <- c(rep(1,1511))
for (i in 2:1511) {
  rnd_stock_net_returns[i] <- sum(rnd_stocks_market_cap[i,])/sum(rnd_s
tocs_market_cap[i-1,])
}
cum_rnd_stock_net_returns <- c(rep(0,1511))
for (i in 1:1511) {
  cum_rnd_stock_net_returns[i] <- prod(rnd_stock_net_returns[1:i])
}
```

```
In [111]: plot(cum_rnd_stock_net_returns, type = "l",main = "Cumulative Return of
a Randomly Generated 50-stock portfolio", xlab = "Days", ylab = "Return
s" )
```

Cumulative Return of a Randomly Generated 50-stock portfolio



We will now find the RMSE of this stock portfolio compared to the market return based on 1-day simple return of the market.

```
In [112]: (sum((rnd_stock_net_returns - ff_returns)^2)/1511)^(1/2)
0.00629367147361637
```

We can certainly reduce the RMSE by choosing a different portfolio of 50 stocks. To show this, let's now select another 50 stocks by randomly sampling from the last 800 stocks (alphabetically). This gives us the following RMSE

```
In [106]: set.seed(100)
rnd_stocks_2 <- c(sample(1077:1877,50,replace=F))
rnd_stocks_return_2 <- stock_returns[,rnd_stocks_2]
rnd_stocks_market_cap_2 <- market_cap[,rnd_stocks_2]
```

```
In [107]: rnd_stock_net_returns_2 <- c(rep(1,1511))
for (i in 2:1511) {
  rnd_stock_net_returns_2[i] <- sum(rnd_stocks_market_cap_2[i,])/sum(rnd_stocks_market_cap_2[i-1,])
}
```

```
In [108]: (sum((rnd_stock_net_returns_2 - ff_returns)^2)/1511)^(1/2)
0.00591688424400269
```

We see here that the RMSE has decreased slightly from 0.00629 to 0.00592. Hence, choosing a different portfolio of 50 stocks can reduce RMSE.

Question 1 part c)

25 10-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [105]: set.seed(100)
rnd_stock_10 <- matrix(rep(0,250), nrow =25, ncol = 10) #generates the i
ndices for 25 10-stock portfolios
for (i in 1:25) {
  rnd_stock_10[i,] <- c(sample(1:1877,10,replace=F))
}
RMSE_10 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_10[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_10[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_10) #Finds the average of the RMSEs
```

0.0125078924822289

25 20-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [104]: set.seed(100)
rnd_stock_20 <- matrix(rep(0,250), nrow =25, ncol = 20) #generates the i
ndices for 25 20-stock portfolios
for (i in 1:25) {
  rnd_stock_20[i,] <- c(sample(1:1877,20,replace=F))
}
RMSE_20 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_20[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_20[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_20) #Finds the average of the RMSEs
```

0.00988778984007995

25 30-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [103]: set.seed(100)
rnd_stock_30 <- matrix(rep(0,250), nrow =25, ncol = 30) #generates the i
ndices for 25 30-stock portfolios
for (i in 1:25) {
  rnd_stock_30[i,] <- c(sample(1:1877,30,replace=F))
}
RMSE_30 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_30[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_30[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_30) #Finds the average of the RMSEs
```

0.00837869963367009

25 40-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [102]: set.seed(100)
rnd_stock_40 <- matrix(rep(0,250), nrow =25, ncol = 40) #generates the i
ndices for 25 40-stock portfolios
for (i in 1:25) {
  rnd_stock_40[i,] <- c(sample(1:1877,40,replace=F))
}
RMSE_40 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_40[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_40[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_40) #Finds the average of the RMSEs
```

0.00755033712457847

25 50-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [101]: set.seed(100)
rnd_stock_50 <- matrix(rep(0,250), nrow =25, ncol = 50) #generates the i
ndices for 25 50-stock portfolios
for (i in 1:25) {
  rnd_stock_50[i,] <- c(sample(1:1877,50,replace=F))
}
RMSE_50 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_50[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_50[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_50) #Finds the average of the RMSEs
```

0.00724531884293953

25 60-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [100]: set.seed(100)
rnd_stock_60 <- matrix(rep(0,250), nrow =25, ncol = 60) #generates the i
ndices for 25 60-stock portfolios
for (i in 1:25) {
  rnd_stock_60[i,] <- c(sample(1:1877,60,replace=F))
}
RMSE_60 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_60[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_60[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_60) #Finds the average of the RMSEs
```

0.00602947940929144

25 70-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [99]: set.seed(100)
rnd_stock_70 <- matrix(rep(0,250), nrow =25, ncol = 70) #generates the i
ndices for 25 70-stock portfolios
for (i in 1:25) {
  rnd_stock_70[i,] <- c(sample(1:1877,70,replace=F))
}
RMSE_70 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_70[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_70[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_70) #Finds the average of the RMSEs
```

0.0060808373798493

25 80-stock portfolios of randomly chosen stocks and corresponding mean RMSE:

```
In [98]: set.seed(100)
rnd_stock_80 <- matrix(rep(0,250), nrow =25, ncol = 80) #generates the i
ndices for 25 80-stock portfolios
for (i in 1:25) {
  rnd_stock_80[i,] <- c(sample(1:1877,80,replace=F))
}
RMSE_80 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_80[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_80[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^(1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_80) #Finds the average of the RMSEs
```

0.00596200750032389

25 90-stock portfolios of randomly chosen stocks and corresponding mean RMSE:


```
In [132]: set.seed(100)
rnd_stock_90 <- matrix(rep(0,250), nrow =25, ncol = 90) #generates the i
ndices for 25 90-stock portfolios
for (i in 1:25) {
  rnd_stock_90[i,] <- c(sample(1:1877,90,replace=F))
}
RMSE_90 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_90[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_90[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511
)^ (1/2)} #calculates RMSE and stores it in a vector that compiles all 25
RMSEs
mean(RMSE_90) #Finds the average of the RMSEs
```

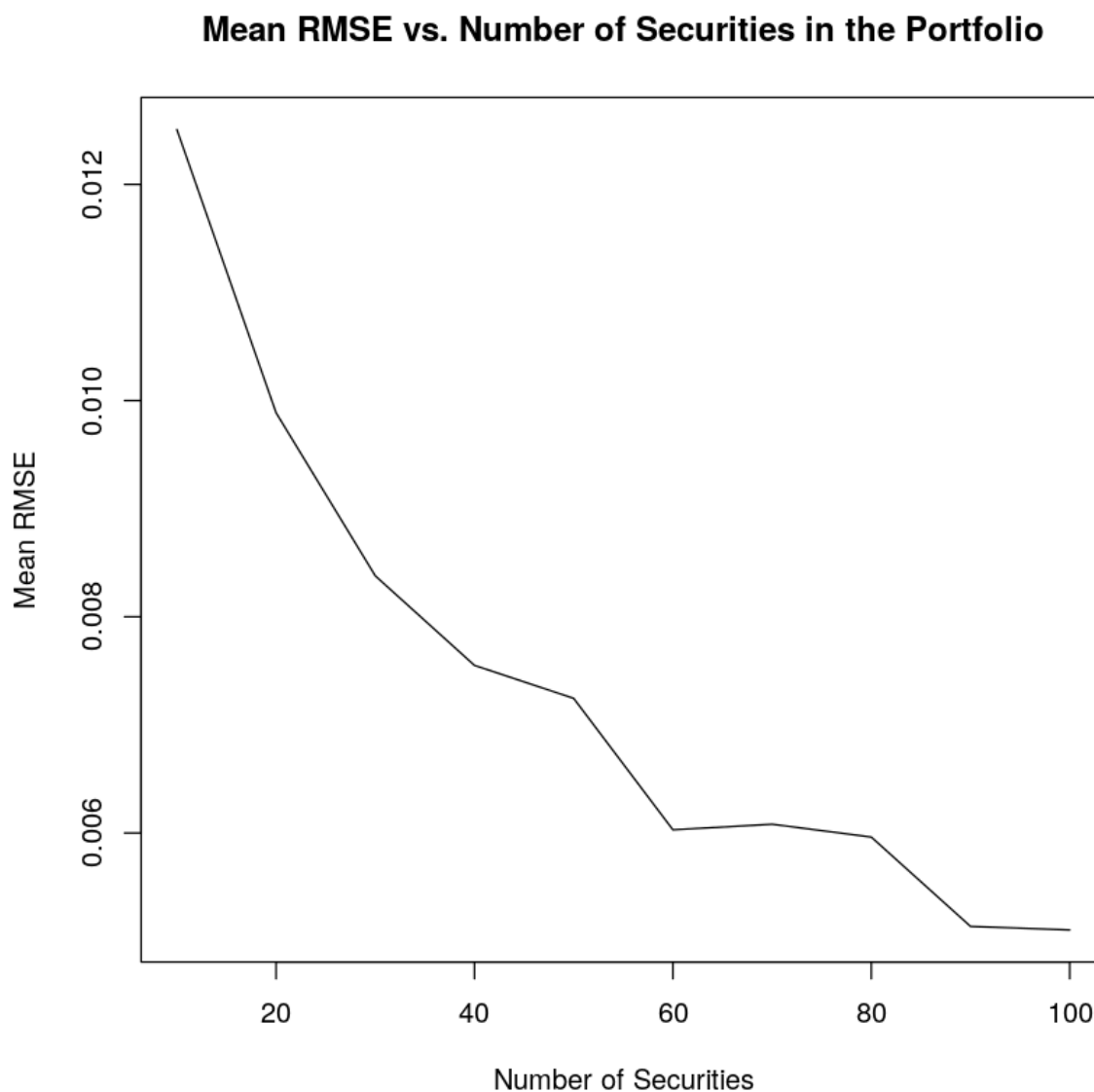
0.00513585463999323

25 100-stock portfolios of randomly chosen stocks:

```
In [114]: set.seed(100)
rnd_stock_100 <- matrix(rep(0,250), nrow =25, ncol = 100) #generates the
indices for 25 100-stock portfolios
for (i in 1:25) {
  rnd_stock_100[i,] <- c(sample(1:1877,100,replace=F))
}
RMSE_100 <- c(rep(0,25))
for (i in 1:25){
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_100[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  RMSE_100[i] <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/151
1)^ (1/2)} #calculates RMSE and stores it in a vector that compiles all 2
5 RMSEs
mean(RMSE_100) #Finds the average of the RMSEs
```

0.00510300091498504

```
In [115]: RMSEs <- c(mean(RMSE_10), mean(RMSE_20), mean(RMSE_30), mean(RMSE_40), mean(RMSE_50), mean(RMSE_60), mean(RMSE_70), mean(RMSE_80), mean(RMSE_90), mean(RMSE_100))
number_securities <- c(10,20,30,40,50,60,70,80,90,100)
plot(number_securities, RMSEs, type = "l", main = "Mean RMSE vs. Number of Securities in the Portfolio", xlab = "Number of Securities", ylab = "Mean RMSE")
```

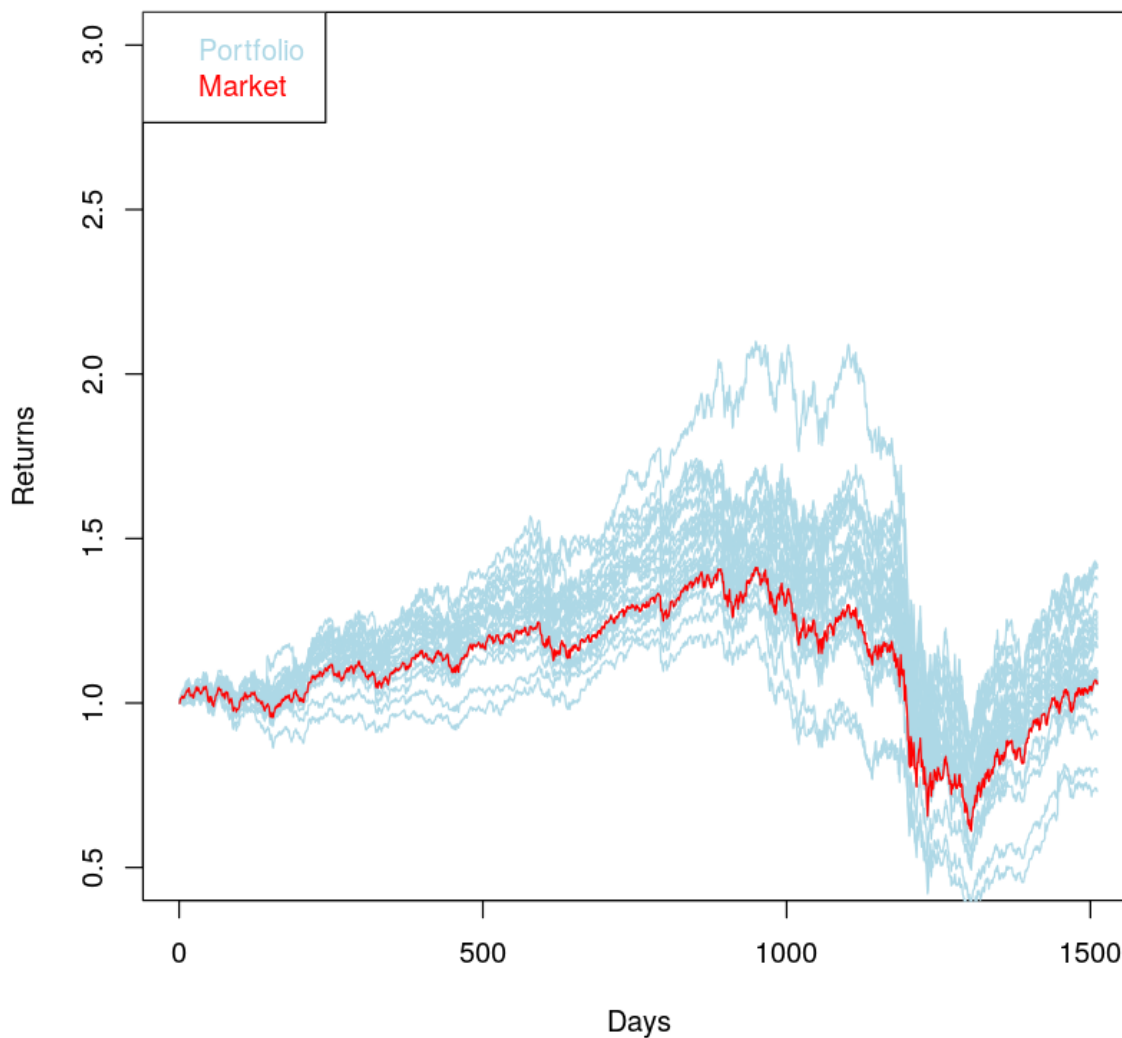


We observe in this graph that mean RMSE steadily decreases as the number of securities increase. This is within expectation as more securities means larger sample size, thus lower variance. We will now select $n=100$ and plot the cumulative returns of all 25 portfolios, and to the market, as follow.

```
In [121]: returns_of_25_portfolio <- matrix(rep(0,377750), nrow =25, ncol = 1511)
for (i in 1:25){
  rnd_stocks_return_dummy <- stock_returns[,rnd_stock_100[i,]]
  rnd_stocks_market_cap_dummy <- market_cap[,rnd_stock_100[i,]]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
  cum_rnd_stock_net_returns_dummy <- c(rep(0,1511))
  for (k in 1:1511) {
    cum_rnd_stock_net_returns_dummy[k] <- prod(rnd_stock_net_returns
_dummy[1:k])
  }
  returns_of_25_portfolio[i,] <- cum_rnd_stock_net_returns_dummy
}
```

```
In [122]: plot(cum_ff_returns, type = "l", ylim = c(0.5,3), col = "red", main = "Cumulative Returns of 25 100-stock portfolios vs. Cumulative Market Return", xlab = "Days", ylab = "Returns")
for (i in 1:25) {
  lines(returns_of_25_portfolio[i,], col = "light blue")
}
lines(cum_ff_returns, col = "red")
legend("topleft", text.col = c("light blue", "red"), c("Portfolio", "Market"))
```

Cumulative Returns of 25 100-stock portfolios vs. Cumulative Market Return



Question 1 Part d)

One heuristic that we can use is comparing each individual stock's returns with the market return and include the n stocks with the lowest RMSE in our n -stock portfolio.

```
In [137]: RMSE_individual_stocks <- c(rep(0,1877))
for (i in 1:1877) {
  rnd_stocks_market_cap_dummy <- market_cap[,i]
  rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- rnd_stocks_market_cap_dummy[j]
    /rnd_stocks_market_cap_dummy[j-1]
  }
  RMSE_individual_stocks[i] <- (sum((rnd_stock_net_returns_dummy- ff_r
  eturns)^2)/1511)^(1/2)
}
```

```
In [140]: sorted_RMSE <- sort(RMSE_individual_stocks, index.return=TRUE, decreasin
g=FALSE) #sorts RMSE from smallest to largest
```

10-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [145]: set.seed(100)
top_stock_10 <- head(sorted_RMSE$ix,10) #generates the indices for top 1
0-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_10]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top10 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1
/2) #calculates RMSE
RMSE_top10
```

0.00648820572220311

20-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [146]: set.seed(100)
top_stock_20 <- head(sorted_RMSE$ix,20) #generates the indices for top 2
0-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_20]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dumm
y[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top20 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1
/2) #calculates RMSE
RMSE_top20
```

0.00616154394654657

30-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [147]: set.seed(100)
top_stock_30 <- head(sorted_RMSE$ix,30) #generates the indices for top 30-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_30]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top30 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top30
```

0.00607242031279169

40-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [148]: set.seed(100)
top_stock_40 <- head(sorted_RMSE$ix,40) #generates the indices for top 40-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_40]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top40 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top40
```

0.00599365353022826

50-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [149]: set.seed(100)
top_stock_50 <- head(sorted_RMSE$ix,50) #generates the indices for top 50-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_50]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top50 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top50

0.00555104258853075
```

60-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [150]: set.seed(100)
top_stock_60 <- head(sorted_RMSE$ix,60) #generates the indices for top 60-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_60]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top60 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top60

0.00552924208433045
```

70-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [151]: set.seed(100)
top_stock_70 <- head(sorted_RMSE$ix,70) #generates the indices for top 70-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_70]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top70 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top70

0.00554712520067994
```

80-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [152]: set.seed(100)
top_stock_80 <- head(sorted_RMSE$ix,80) #generates the indices for top 80-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_80]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top80 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top80
```

0.00543141458304822

90-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio

```
In [153]: set.seed(100)
top_stock_90 <- head(sorted_RMSE$ix,90) #generates the indices for top 90-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_90]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top90 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top90
```

0.00544453970022969

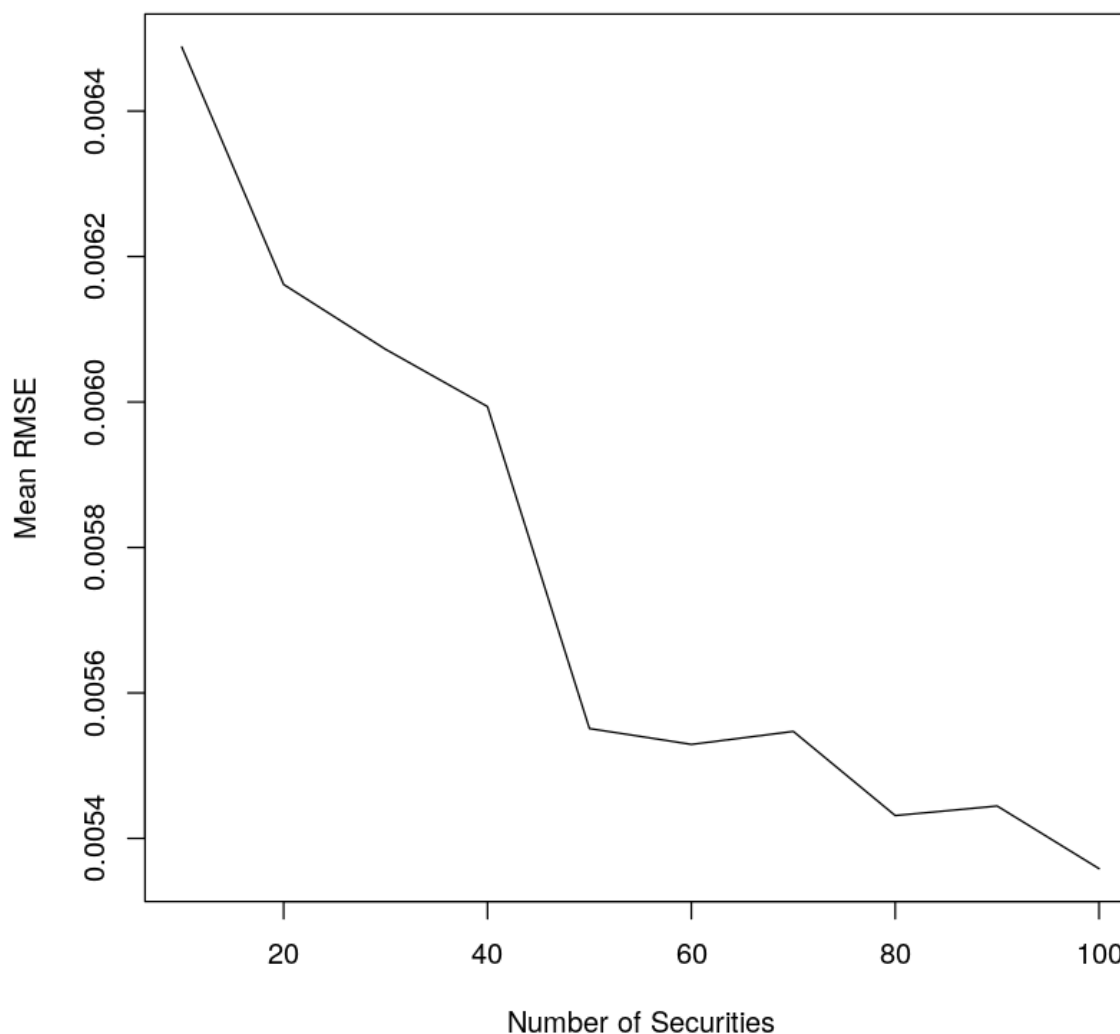
100-stock portfolios of stocks that have the lowest individual RMSEs with the market and the corresponding RMSE of the portfolio


```
In [154]: set.seed(100)
top_stock_100 <- head(sorted_RMSE$ix,100) #generates the indices for top 100-stock portfolios
rnd_stocks_market_cap_dummy <- market_cap[,top_stock_100]
rnd_stock_net_returns_dummy <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_dummy[j] <- sum(rnd_stocks_market_cap_dummy[j,])/sum(rnd_stocks_market_cap_dummy[j-1,])
  }
RMSE_top100 <- (sum((rnd_stock_net_returns_dummy- ff_returns)^2)/1511)^(1/2) #calculates RMSE
RMSE_top100
```

0.0053583577677806

```
In [155]: RMSEs <- c(RMSE_top10, RMSE_top20, RMSE_top30, RMSE_top40, RMSE_top50, RMSE_top60, RMSE_top70, RMSE_top80, RMSE_top90, RMSE_top100)
number_securities <- c(10,20,30,40,50,60,70,80,90,100)
plot(number_securities, RMSEs, type = "l", main = "RMSE of portfolios with top n individually lowest-RMSE securities", xlab = "Number of Securities", ylab = "Mean RMSE")
```

RMSE of portfolios with top n individually lowest-RMSE securities



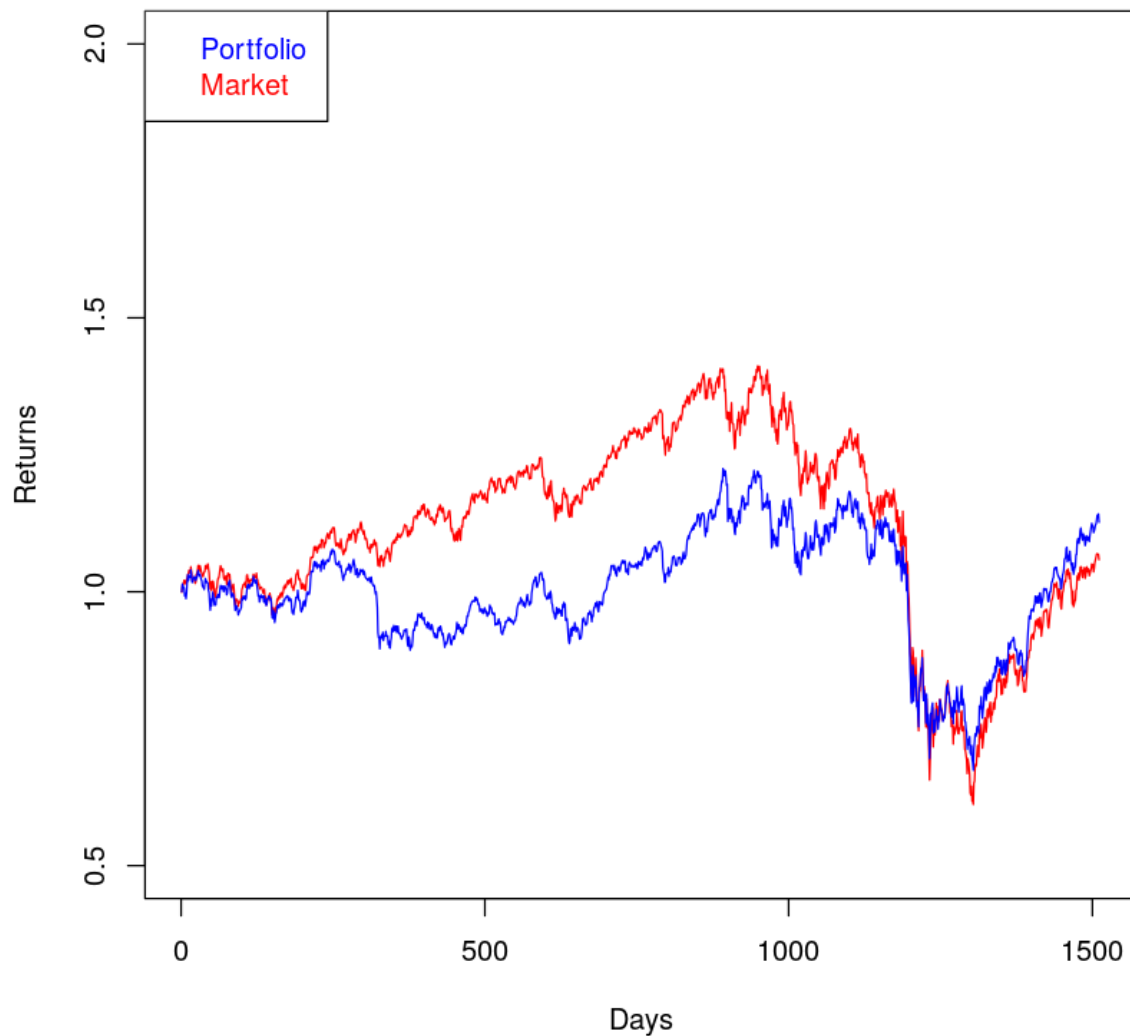
We observe that by constructing portfolios with n securities that have the n -lowest individual RMSE, we were able to drastically improve our RMSE for portfolios with lower numbers of securities. We were able to achieve an RMSE of 0.0065 with only 10 securities using this new method security selection. When we were using random security selection, the mean RMSE of 10 securities was 0.0125. Hence, this new method has cut the RMSE of portfolios with 10 securities by half. For larger numbers of securities, we see that the RMSE of this new method is pretty much the same as the RMSE of the old method where we randomly select securities. The value of this heuristic lies in the fact that we can minimize the number of securities that we put into our portfolio (to 10) without sacrificing as much RMSE as before.

Since $n=10$ yielded the most interesting results, we will plot the cumulative returns of $n=10$.

```
In [157]: top_stock_10 <- head(sorted_RMSE$ix,10) #generates the indices for top 10-stock portfolios
rnd_stocks_market_cap_top10 <- market_cap[,top_stock_10]
rnd_stock_net_returns_top10 <- c(rep(1,1511))
  for (j in 2:1511) {
    rnd_stock_net_returns_top10[j] <- sum(rnd_stocks_market_cap_top10[j,])/sum(rnd_stocks_market_cap_top10[j-1,])
  }
cum_rnd_stock_net_returns_top10 <- c(rep(0,1511))
  for (k in 1:1511) {
    cum_rnd_stock_net_returns_top10[k] <- prod(rnd_stock_net_returns_top10[1:k])
  }
```

```
In [158]: plot(cum_ff_returns, type = "l", ylim = c(0.5,2), col = "red", main = "Cumulative Returns of top 10 securities with lowest individual RMSE vs. Cumulative Market Return", xlab = "Days", ylab = "Returns")
lines(cum_rnd_stock_net_returns_top10, col = "blue")
legend("topleft", text.col = c("blue", "red"), c("Portfolio", "Market"))
```

a Returns of top 10 securities with lowest individual RMSE vs. Cumulative



Question 4 Part a) i) For 504 windows

```
In [441]: set.seed(100)
rnd_stocks_ff <- c(1:10)
```

```
In [467]: beta_storage <- matrix(rep(0,30210), nrow = 30, ncol = 1007) #For storing betas. Every three rows represents the rolling betas for a given security
for (j in 0:99) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1007))
  beta_SMB <- c(rep(0,1007))
  beta_HML <- c(rep(0,1007))
  for (i in 1:1007) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+503)] ~ rm_minus_rf[i:(i+503)] + SMB[i:(i+503)] + HML[i:(i+503)]) #OLS to find bets at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <- ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader beta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML
}
```

Question 4 Part a) ii) For 504 windows

```
In [470]: cov_matrix_storage <- list() #this part is for building fama-french covariance matrices
for (i in 1:1007) {
  A <- matrix(beta_storage[,i], nrow=100, ncol = 3, byrow = TRUE)
  cov_matrix_storage[[i]] <- cov(A)
}
```

```
In [472]: idio_var_storage <- matrix(rep(0,100700), nrow = 100, ncol = 1007) #For storing idiosyncratic variances
for (j in 0:99) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  var_residuals <- c(rep(0,1007))
  for (i in 1:1007) {
    ols <- lm(ri_minus_rf[i:(i+503)] ~ rm_minus_rf[i:(i+503)] + SMB[i:(i+503)] + HML[i:(i+503)]) #perform OLS to obtain residuals
    var_residuals[i] <- var(ols$residuals) #find variance of residuals
  }
  idio_var_storage[j+1,] <- var_residuals
}
```

Question 4 Part a) iii) For 504 windows

```
In [473]: variance_storage <- c(rep(0,1007)) #obtain the variances for all rolling windows
for (i in 1:1007) {
  beta <- matrix(beta_storage[,i], nrow=100, ncol = 3, byrow = TRUE)
  w <- matrix(market_cap[(i+503),rnd_stocks_ff] / sum(market_cap[(i+503),rnd_stocks_ff]))
  delta <- diag(idio_var_storage[,i])
  variance_storage [i] <- t(w) %*% delta %*% w + t(w) %*% beta %*% cov_matrix_storage[[i]] %*% t(beta) %*% w
}
```

Question 4 Part a) iv) For 504 windows

```
In [463]: one_day_ahead_storage <- c(rep(0,1007))#obtain one-day-ahead returns
for (i in 1:1007) {
  w <- market_cap[(i+504),rnd_stocks_ff ] / sum(market_cap[(i+504),rnd_stocks_ff])
  stock_returns_ahead <- stock_returns[(i+504),rnd_stocks_ff ]
  weighted_returns <- 0
  for (j in 1:100) {
    weighted_returns <- weighted_returns + w[j]* stock_returns_ahead[j]
  }
  one_day_ahead_storage[i] <- weighted_returns
}
```

Question 4 Part a) v) For 504 windows

```
In [594]: standardized_outcome <- c(rep(0,1007))
for (i in 1:1007) {
  standardized_outcome[i] <- one_day_ahead_storage[i]/ (variance_storage[i])^(1/2)
}
```

```
In [595]: var(standardized_outcome)^(1/2)
```

2.16216814281339

Question 4 Part a) i) For 252 windows

```
In [476]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1259) #For storing beta s. Every three rows represents the rolling betas for a given security
for (j in 0:99) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1259))
  beta_SMB <- c(rep(0,1259))
  beta_HML <- c(rep(0,1259))
  for (i in 1:1259) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+251)] ~ rm_minus_rf[i:(i+251)] + SMB[
i:(i+251)] + HML[i:(i+251)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <-ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader b
eta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML
}
```

Question 4 Part a) ii) For 252 windows

```
In [477]: cov_matrix_storage <- list() #this part is for building fama-french cova
riance matrices
for (i in 1:1259) {
  A <- matrix(beta_storage[,i], nrow=10, ncol = 3, byrow = TRUE)
  cov_matrix_storage[[i]] <- cov(A)
}
```

```
In [479]: idio_var_storage <- matrix(rep(0), nrow = 10, ncol = 1259) #For storing
idiosyncratic variances
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  var_residuals <- c(rep(0,1259))
  for (i in 1:1259) {
    ols <- lm(ri_minus_rf[i:(i+251)] ~ rm_minus_rf[i:(i+251)] + SMB[
i:(i+251)] + HML[i:(i+251)]) #perform OLS to obtain residuals
    var_residuals[i] <- var(ols$residuals) #find variance of residua
ls
  }
  idio_var_storage[j+1,] <- var_residuals
}
```

Question 4 Part a) iii) For 252 windows

```
In [481]: variance_storage <- c(rep(0,1259)) #obtain the variances for all rolling windows
for (i in 1:1259) {
  beta <- matrix(beta_storage[,i], nrow=10, ncol = 3, byrow = TRUE)
  w <- matrix(market_cap[(i+251),rnd_stocks_ff] / sum(market_cap[(i+251),rnd_stocks_ff]))
  delta <- diag(idio_var_storage[,i])
  variance_storage [i] <- t(w) %*% delta %*% w + t(w) %*% beta %*% cov_matrix_storage[[i]] %*% t(beta) %*% w * 0
}
```

Question 4 Part a) iv) For 252 windows

```
In [482]: one_day_ahead_storage <- c(rep(0,1259)) #obtain one-day-ahead returns
for (i in 1:1259) {
  w <- market_cap[(i+252),rnd_stocks_ff ] / sum(market_cap[(i+252),rnd_stocks_ff])
  stock_returns_ahead <- stock_returns[(i+252),rnd_stocks_ff ]
  weighted_returns <- 0
  for (j in 1:10) {
    weighted_returns <- weighted_returns + w[j]* stock_returns_ahead[j]
  }
  one_day_ahead_storage[i] <- weighted_returns
}
```

Question 4 Part a) v) For 252 windows

```
In [484]: standardized_outcome <- c(rep(0,1259))
for (i in 1:1259) {
  standardized_outcome[i] <- one_day_ahead_storage[i]/ (variance_storage[i])^(1/2)
}
```

```
In [597]: var(standardized_outcome)^(1/2)
```

1.80970289091147

Question 4 Part a) i) For 126 windows


```
In [489]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1385) #For storing beta s. Every three rows represents the rolling betas for a given security
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1385))
  beta_SMB <- c(rep(0,1385))
  beta_HML <- c(rep(0,1385))
  for (i in 1:1385) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+125)] ~ rm_minus_rf[i:(i+125)] + SMB[i:(i+125)] + HML[i:(i+125)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <- ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader beta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML
}
```

Question 4 Part a) ii) For 126 windows

```
In [495]: cov_matrix_storage <- list() #this part is for building fama-french covariance matrices
for (i in 1:1385) {
  A <- matrix(beta_storage[,i], nrow=10, ncol = 3, byrow = TRUE)
  cov_matrix_storage[[i]] <- cov(A)
}
```

```
In [496]: idio_var_storage <- matrix(rep(0), nrow = 10, ncol = 1385) #For storing idiosyncratic variances
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  var_residuals <- c(rep(0,1385))
  for (i in 1:1385) {
    ols <- lm(ri_minus_rf[i:(i+125)] ~ rm_minus_rf[i:(i+125)] + SMB[i:(i+125)] + HML[i:(i+125)]) #perform OLS to obtain residuals
    var_residuals[i] <- var(ols$residuals) #find variance of residuals
  }
  idio_var_storage[j+1,] <- var_residuals
}
```

Question 4 Part a) iii) For 126 windows

```
In [499]: variance_storage <- c(rep(0,1385)) #obtain the variances for all rolling
          windows
          for (i in 1:1385) {
            beta <- matrix(beta_storage[,i], nrow=10, ncol = 3, byrow = TRUE)
            w <- matrix(market_cap[(i+125),rnd_stocks_ff] / sum(market_cap[(i+125),rnd_stocks_ff]))
            delta <- diag(idio_var_storage[,i])
            variance_storage [i] <- t(w) %*% delta %*% w + t(w) %*% beta %*% cov_matrix_storage[[i]] %*% t(beta) %*% w * 0
          }
```

Question 4 Part a) iv) For 126 windows

```
In [504]: one_day_ahead_storage <- c(rep(0,1385)) #obtain one-day-ahead returns
          for (i in 1:1385) {
            w <- market_cap[(i+126),rnd_stocks_ff] / sum(market_cap[(i+126),rnd_stocks_ff])
            stock_returns_ahead <- stock_returns[(i+126),rnd_stocks_ff]
            weighted_returns <- 0
            for (j in 1:10) {
              weighted_returns <- weighted_returns + w[j]* stock_returns_ahead[j]
            }
            one_day_ahead_storage[i] <- weighted_returns
          }
```

Question 4 Part a) v) For 126 windows

```
In [518]: standardized_outcome <- c(rep(0,1385))
          for (i in 1:1385) {
            standardized_outcome[i] <- one_day_ahead_storage[i] / (variance_storage[i])^(1/2)
          }
```

```
In [598]: var(standardized_outcome)^(1/2)
```

1.57396040336633

Question 4 Part a) i) For 63 windows

```
In [508]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1448) #For storing beta s. Every three rows represents the rolling betas for a given security
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1448))
  beta_SMB <- c(rep(0,1448))
  beta_HML <- c(rep(0,1448))
  for (i in 1:1448) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+62)] ~ rm_minus_rf[i:(i+62)] + SMB[i:(i+62)] + HML[i:(i+62)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <- ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader beta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML
}
```

Question 4 Part a) ii) For 63 windows

```
In [513]: cov_matrix_storage <- list() #this part is for building fama-french covariance matrices
for (i in 1:1448) {
  A <- matrix(beta_storage[,i], nrow=10, ncol = 3, byrow = TRUE)
  cov_matrix_storage[[i]] <- cov(A)
}
```

```
In [514]: idio_var_storage <- matrix(rep(0), nrow = 10, ncol = 1448) #For storing idiosyncratic variances
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,rnd_stocks_ff][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  var_residuals <- c(rep(0,1448))
  for (i in 1:1448) {
    ols <- lm(ri_minus_rf[i:(i+62)] ~ rm_minus_rf[i:(i+62)] + SMB[i:(i+62)] + HML[i:(i+62)]) #perform OLS to obtain residuals
    var_residuals[i] <- var(ols$residuals) #find variance of residuals
  }
  idio_var_storage[j+1,] <- var_residuals
}
```

Question 4 Part a) iii) For 63 windows

```
In [515]: variance_storage <- c(rep(0,1448)) #obtain the variances for all rolling
          windows
          for (i in 1:1448) {
            beta <- matrix(beta_storage[,i], nrow=10, ncol = 3, byrow = TRUE)
            w <- matrix(market_cap[(i+62),rnd_stocks_ff] / sum(market_cap[(i+62),rnd_stocks_ff]))
            delta <- diag(idio_var_storage[,i])
            variance_storage [i] <- t(w) %*% delta %*% w + t(w) %*% beta %*% cov_matrix_storage[[i]] %*% t(beta) %*% w * 0
          }
```

Question 4 Part a) iv) For 63 windows

```
In [516]: one_day_ahead_storage <- c(rep(0,1448)) #obtain one-day-ahead returns
          for (i in 1:1448) {
            w <- market_cap[(i+62),rnd_stocks_ff] / sum(market_cap[(i+62),rnd_stocks_ff])
            stock_returns_ahead <- stock_returns[(i+62),rnd_stocks_ff]
            weighted_returns <- 0
            for (j in 1:10) {
              weighted_returns <- weighted_returns + w[j]* stock_returns_ahead[j]
            }
            one_day_ahead_storage[i] <- weighted_returns
          }
```

Question 4 Part a) v) For 63 windows

```
In [521]: standardized_outcome <- c(rep(0,1448))
          for (i in 1:1448) {
            standardized_outcome[i] <- one_day_ahead_storage[i]/ (variance_storage[i])^(1/2)
          }
```

```
In [528]: var(standardized_outcome) ^ 1/(2)
```

1.45611471984054

Question 5 part 1

```
In [559]: random_stocks <- matrix(0, nrow = 50, ncol = 10)
          for (i in 1:50) {
            random_stocks[i,] <- c(sample(1:1877,10,replace=F))
          }
```

```
In [560]: weighted_market_cap_1005 <- market_cap[1005,random_stocks[1,]]/sum(market_cap[1005,random_stocks[1,]])
```

```
In [562]: weighted_market_cap_503 <- market_cap[503,random_stocks[1,]]/sum(market_
cap[503,random_stocks[1,]])
```

```
In [561]: weighted_market_cap_1510 <- market_cap[1510,random_stocks[1,]]/sum(marke
t_cap[1510,random_stocks[1,]])
```

```
In [569]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1448) #For storing beta
s. Every three rows represents the rolling betas for a given security
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,random_stocks][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1448))
  beta_SMB <- c(rep(0,1448))
  beta_HML <- c(rep(0,1448))
  for (i in 1:1448) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+62)] ~ rm_minus_rf[i:(i+62)] + SMB[i:
(i+62)] + HML[i:(i+62)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <-ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader b
eta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML}

beta_storage_503 <- beta_storage[,439:503]
```

```
In [565]: for (i in 1:64){
  beta <- weighted_market_cap_503 %%% matrix(beta_storage_503[,1], nro
w = 10, ncol =3, byrow = TRUE)
}
```

A matrix: 1 × 3 of type dbl

```
1.197618 0.3981891 -0.7618308
```

```
In [566]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1448) #For storing betas
s. Every three rows represents the rolling betas for a given security
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,random_stocks][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1448))
  beta_SMB <- c(rep(0,1448))
  beta_HML <- c(rep(0,1448))
  for (i in 1:1448) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+62)] ~ rm_minus_rf[i:(i+62)] + SMB[i:
(i+62)] + HML[i:(i+62)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <-ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader b
eta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML}
```

A data.frame: 1 × 4

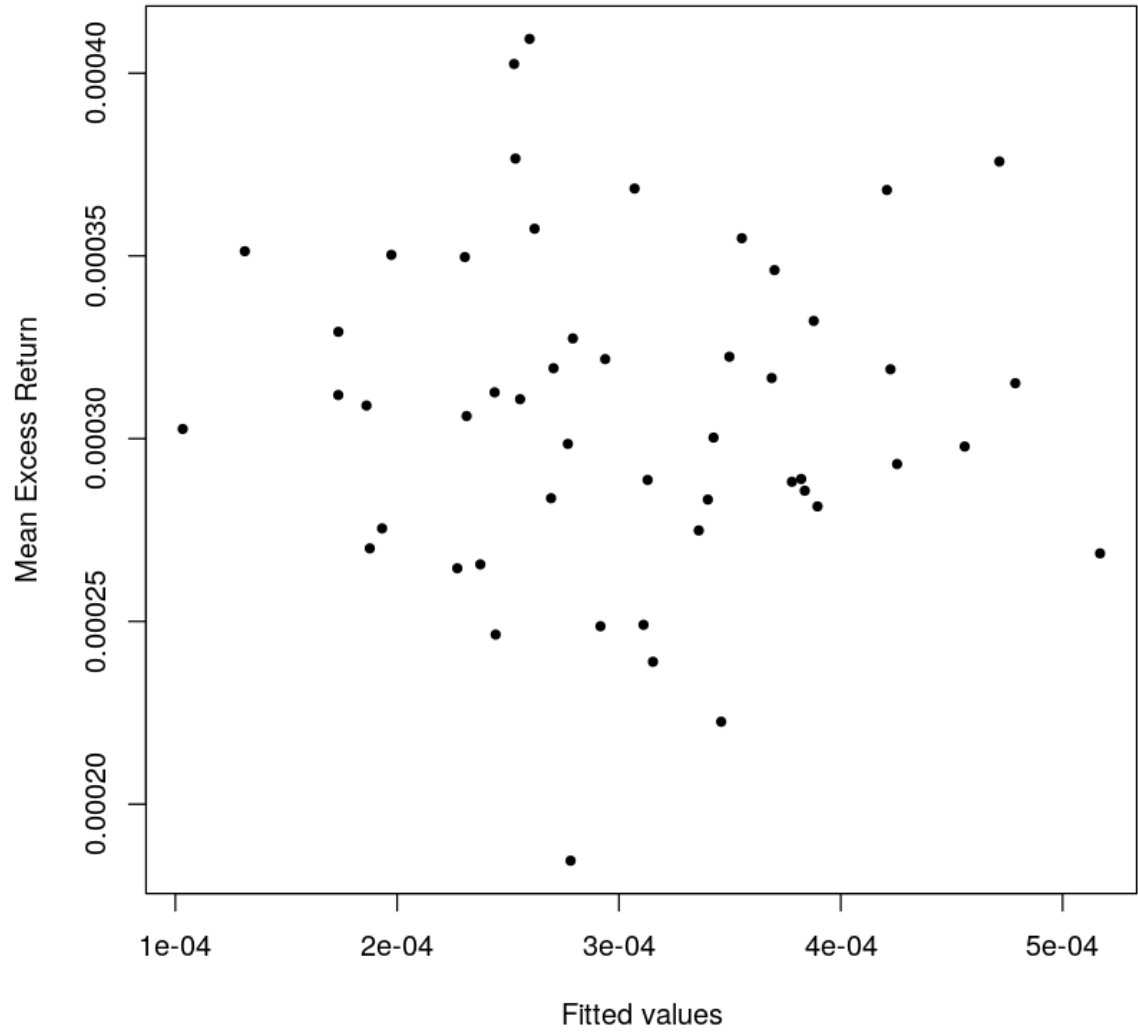
	V1	V2	V3	V4
	<dbl>	<dbl>	<dbl>	<dbl>
503	-0.0025	0	0.0023	0.00015

```

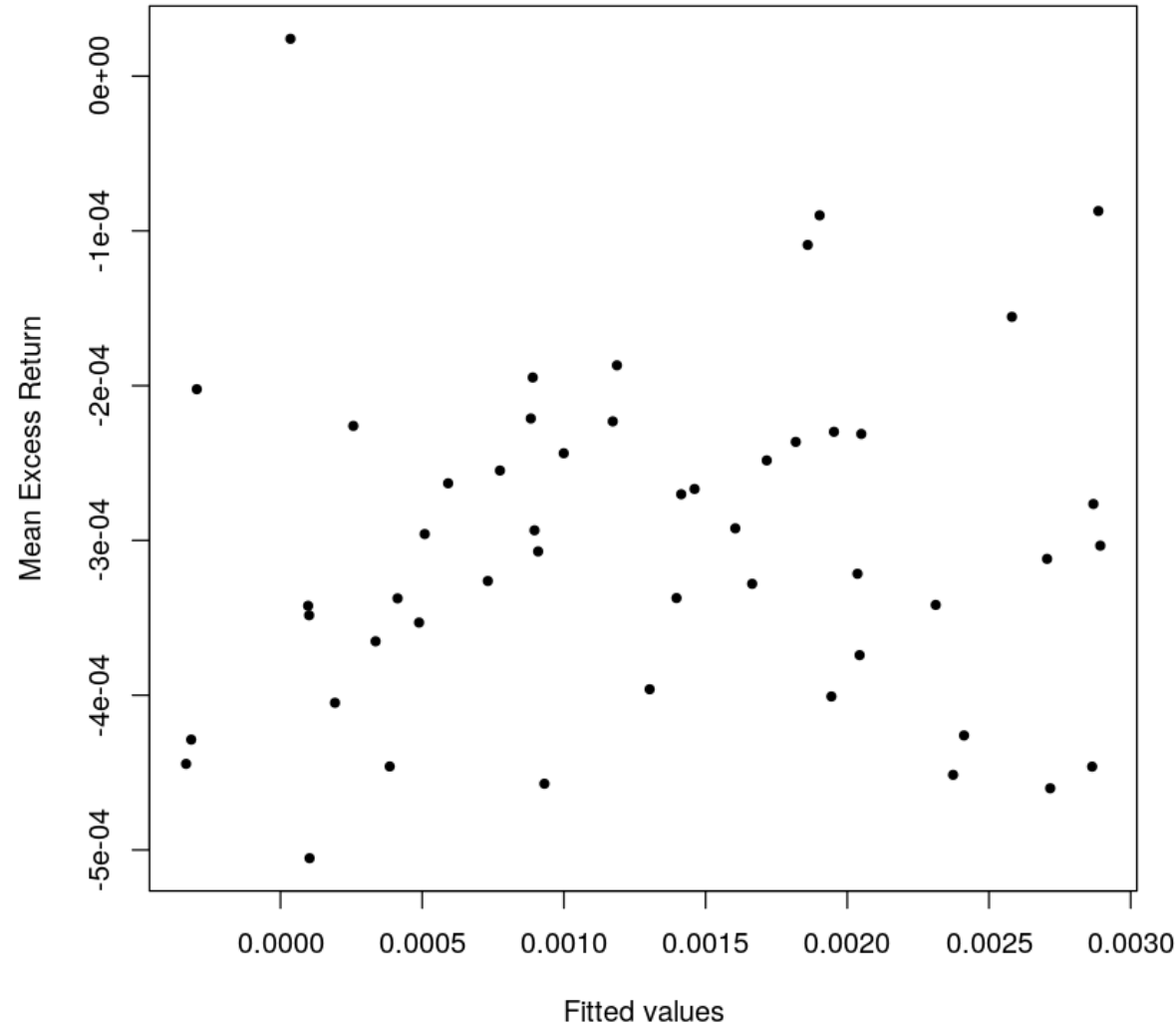
In [604]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1448) #For storing betas. Every three rows represents the rolling betas for a given security
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,random_stocks][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1448))
  beta_SMB <- c(rep(0,1448))
  beta_HML <- c(rep(0,1448))
  for (i in 1:1448) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+62)] ~ rm_minus_rf[i:(i+62)] + SMB[i:(i+62)] + HML[i:(i+62)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <-ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader beta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML}

```

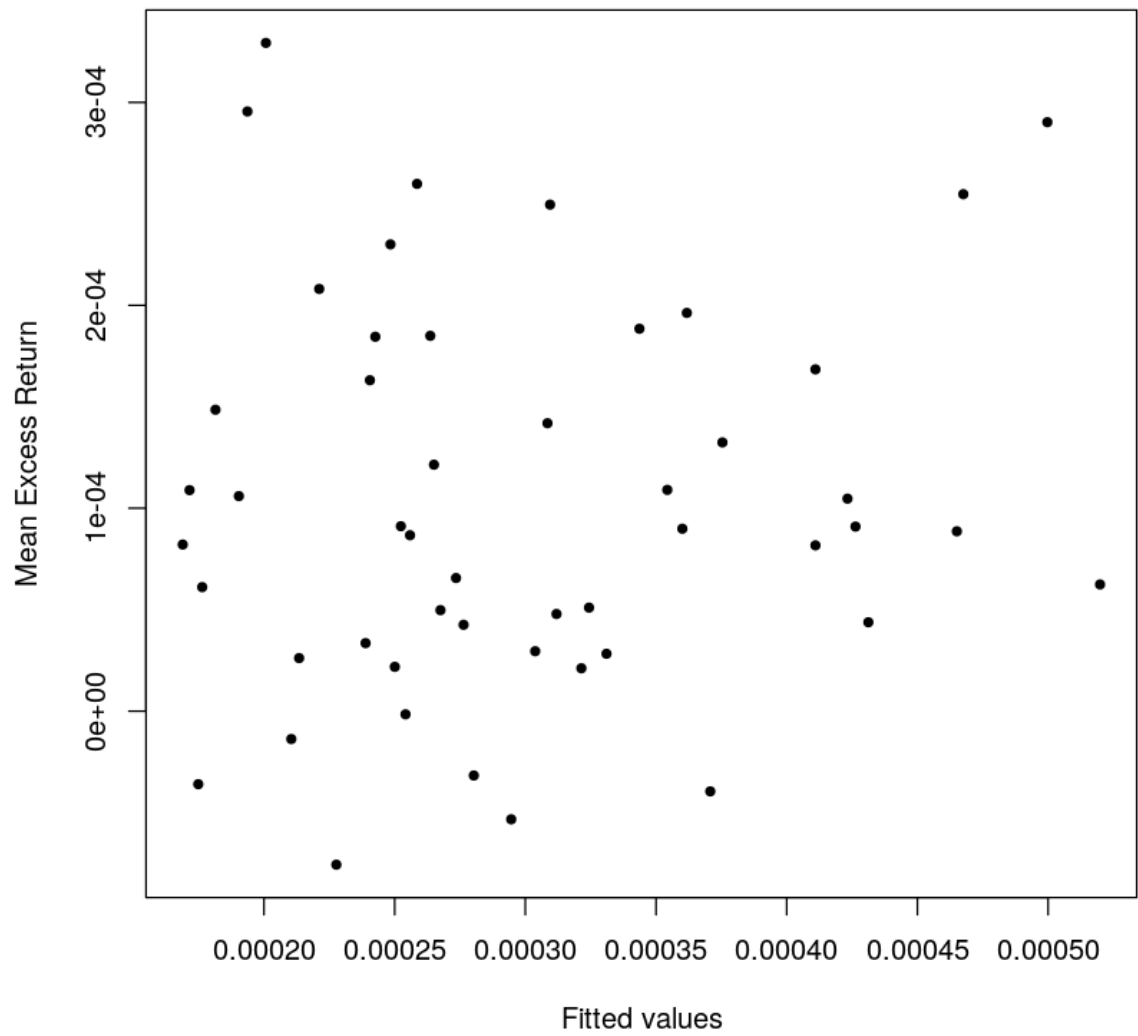
Fama French 12/30/2005 Fitted Values vs. Mean Excess Return



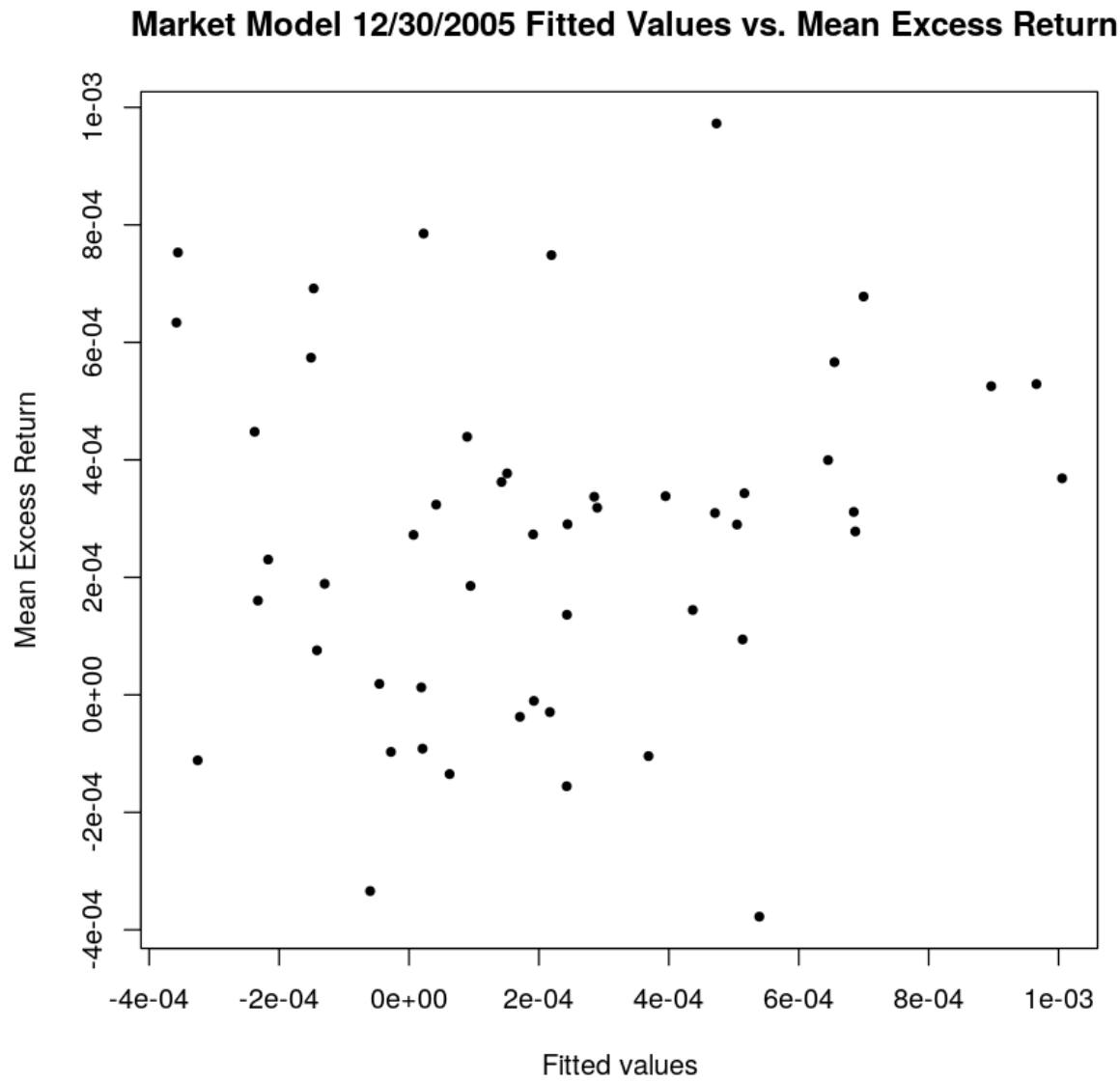
Fama French 12/31/2007 Fitted Values vs. Mean Excess Return



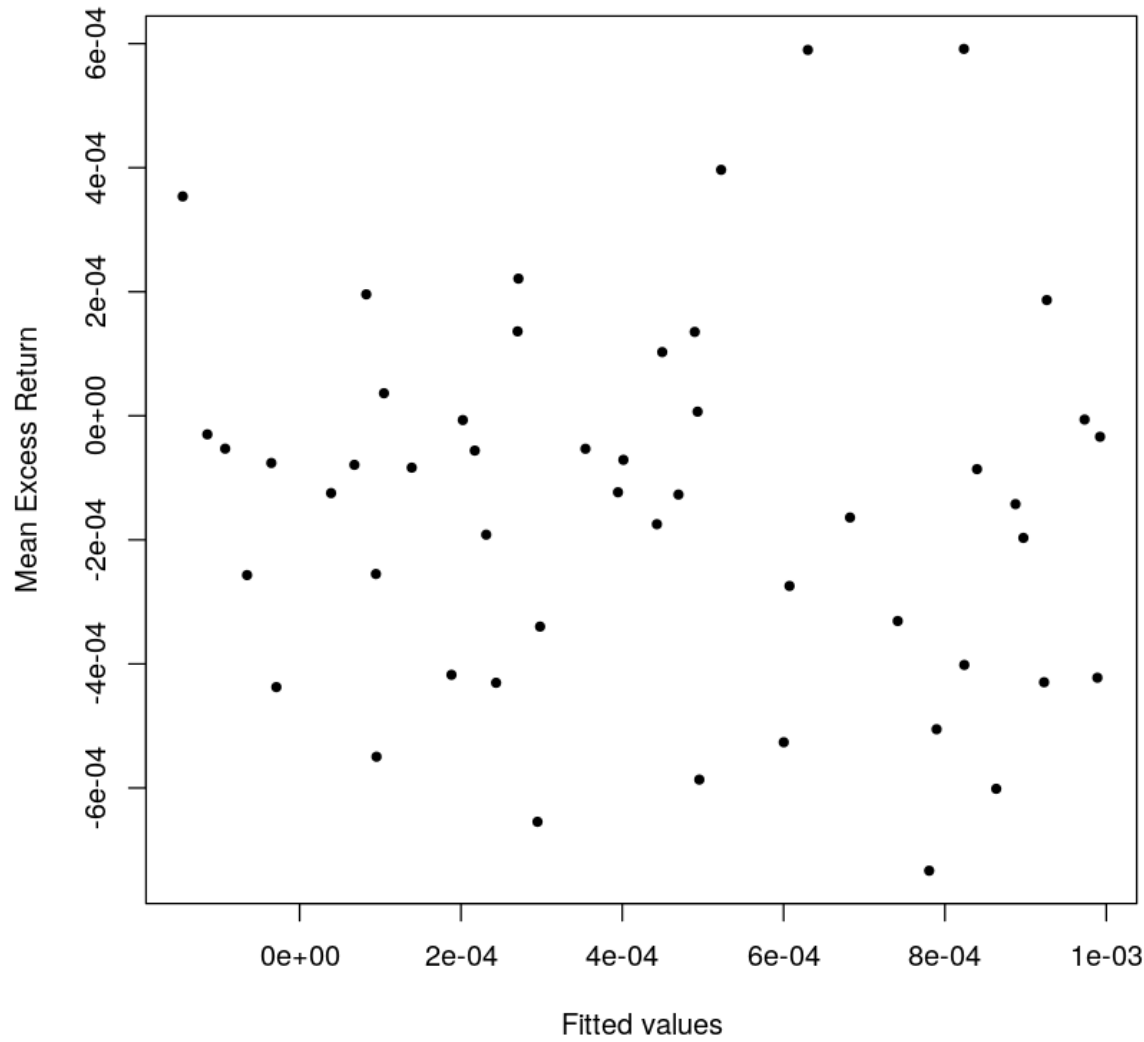
Fama Fench 12/31/2009 Fitted Values vs. Mean Excess Return



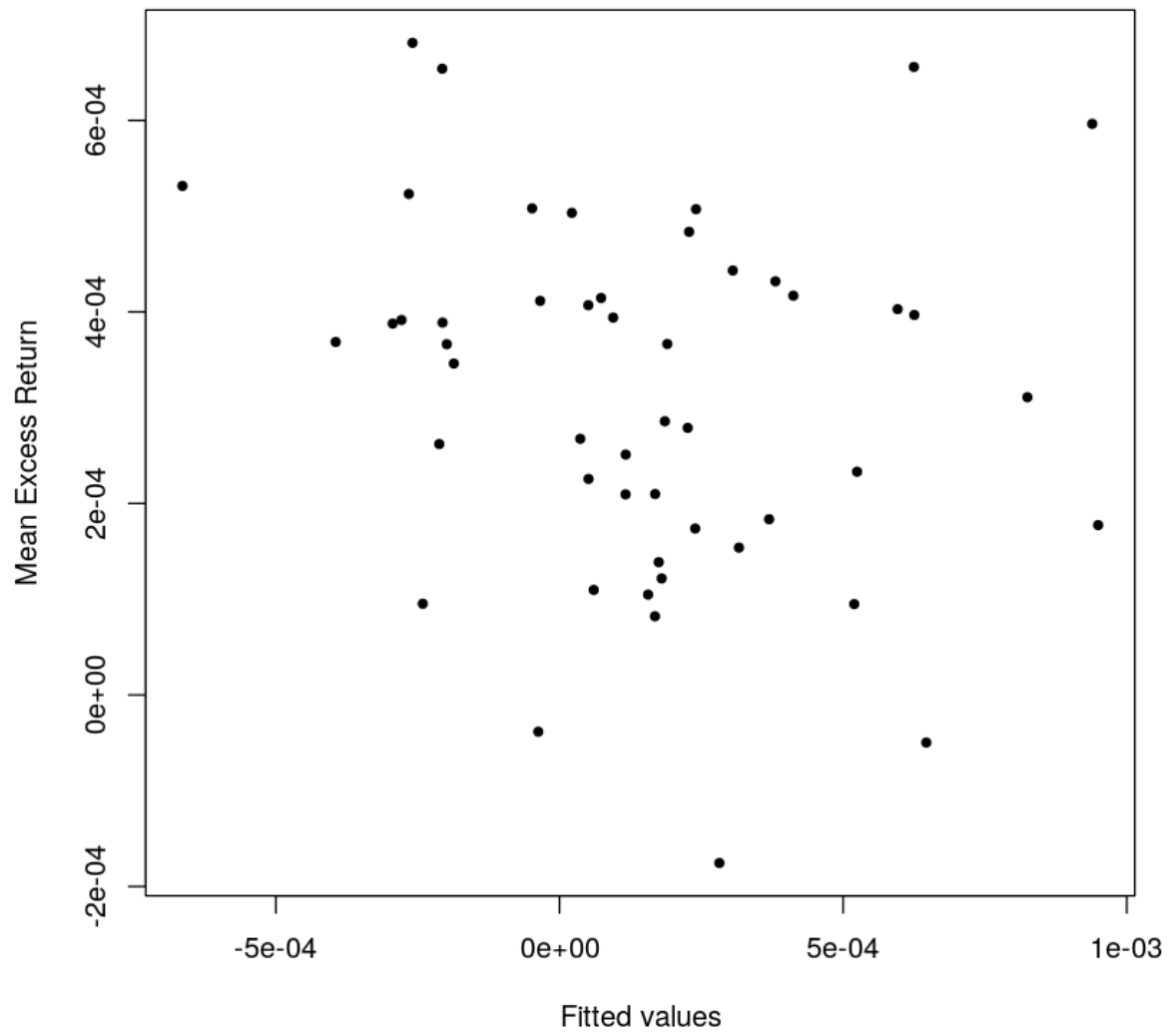
```
In [607]: beta_storage <- matrix(rep(0), nrow = 30, ncol = 1448) #For storing betas. Every three rows represents the rolling betas for a given security
for (j in 0:9) {
  ri_minus_rf <- stock_returns[,random_stocks][,(j+1)] - ffddata[,4]
  rm_minus_rf <- ffddata[,1] - ffddata[,4]
  SMB <- ffddata[,2]
  HML <- ffddata[,3]
  beta_M <- c(rep(0,1448))
  beta_SMB <- c(rep(0,1448))
  beta_HML <- c(rep(0,1448))
  for (i in 1:1448) { #iterate through each rolling window
    ols <- lm(ri_minus_rf[i:(i+62)] ~ rm_minus_rf[i:(i+62)] + SMB[i:(i+62)] + HML[i:(i+62)]) #OLS to find betas at each rolling window
    beta_M[i] <- ols$coefficients[2] # assign coefficients
    beta_SMB[i] <- ols$coefficients[3]
    beta_HML[i] <-ols$coefficients[4]
  }
  beta_storage [(3*j+1),] <- beta_M # assign coefficients to broader beta_storage
  beta_storage [(3*j+2),] <- beta_SMB
  beta_storage [(3*j+3),] <- beta_HML}
```



Market Model 12/31/2007 Fitted Values vs. Mean Excess Return



Market Model 12/31/2009 Fitted Values vs. Mean Excess Return



In []: