

# Impact of delay between pattern presentations on memory in an attractor neural network with triple-well weights

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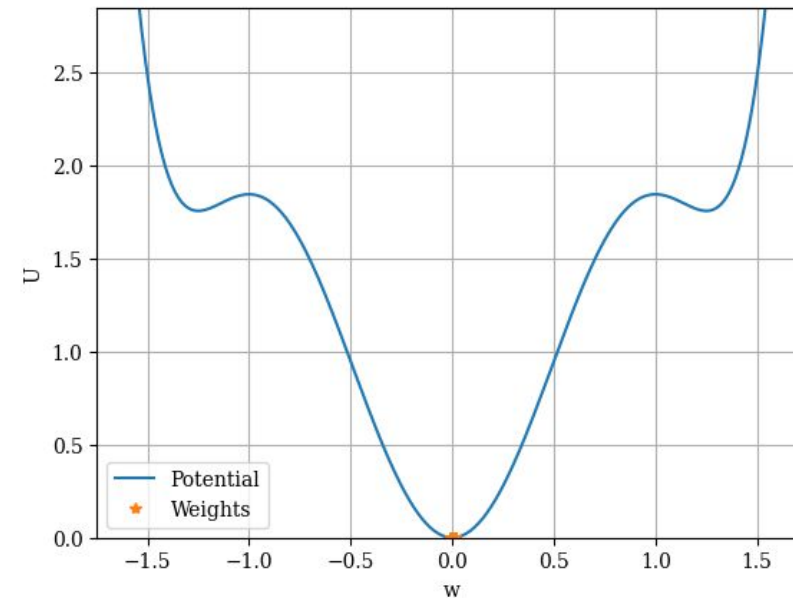
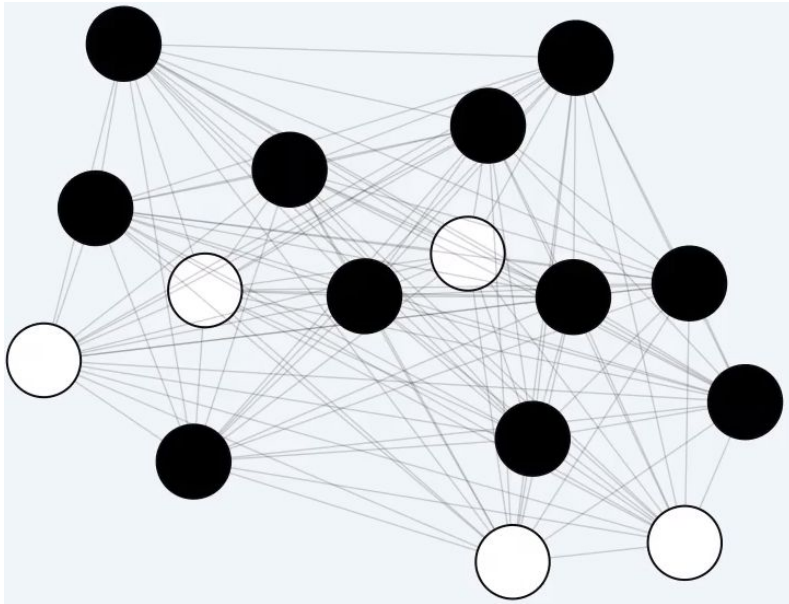


# Objectives

- **Motivation:** an attractor neural network with triple-well weights, more realistic than double-well model (Feng *et al.*, 2023) because most neurons without stimulation get disconnected
- **Objective**
  - Understand the impact of various delay durations on pattern recall (pattern completion) under given conditions using triple-well weights Hopfield model.
  - And how it affects the transition of weights to stable state (within nonzero-well) for long-term memory or to transient state (within zero-well) for short-term memory.

# Background

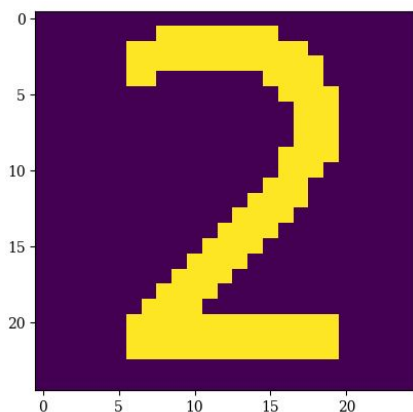
- **Model:** Triple-well weights Hopfield model:
  - A classic Hopfield model with triple-well weights potential function
  - Decay mechanism (relaxation and noise)
- When learning rate is sufficiently slow, temporal evolution depends on delay between episodes
- **Question:** How does delay duration affect recall quality and temporal evolution given a learning rate?



# Methodology

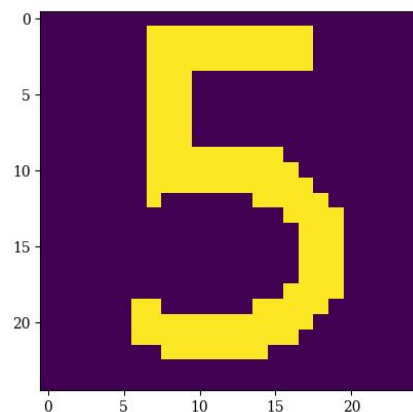
- **Model:** Triple-well Hopfield (TWH) model, 625 neurons
- **Data:** 25x25/2\_5\_combined, two digit patterns 2 and 5
- **Two episodes:** present pattern 2 at time 0, then present pattern 5 at time  $t_{\text{delay}}$ , end the process at time 1.
- **Recall quality:** let TWH model decay, at each time  $t_{\text{decay}}$  let TWH model reconstructs perturbed pattern for pattern 2, record recall quality (Pearson correlation coefficient).
- **Examine:** Set low and high learning rates (0.3, 0.7)
  - Vary  $t_{\text{delay}}$  (0.2-1, 0.1) and  $t_{\text{decay}}$  (0-7, 1), record recall quality, plot the recall quality line graph
  - Let TWH model converge, plot potential landscape and weight density distribution

Present at  $t=0$



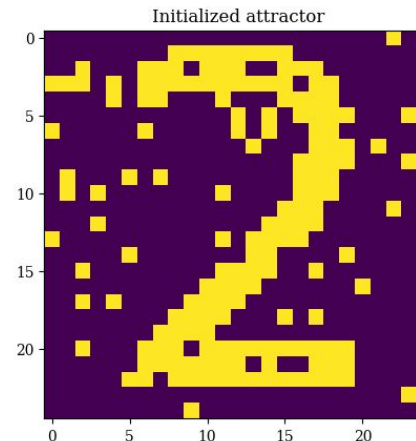
Delay ...

Present at  $t = t_{\text{delay}}$

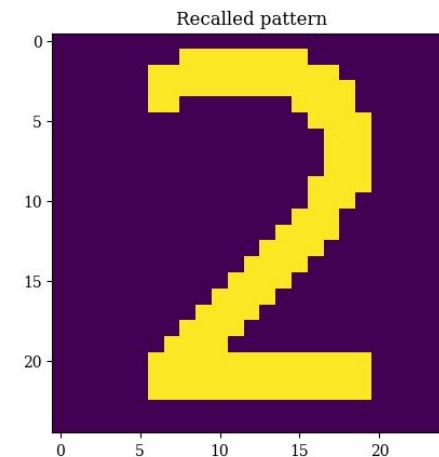


Decay  
And Convergence

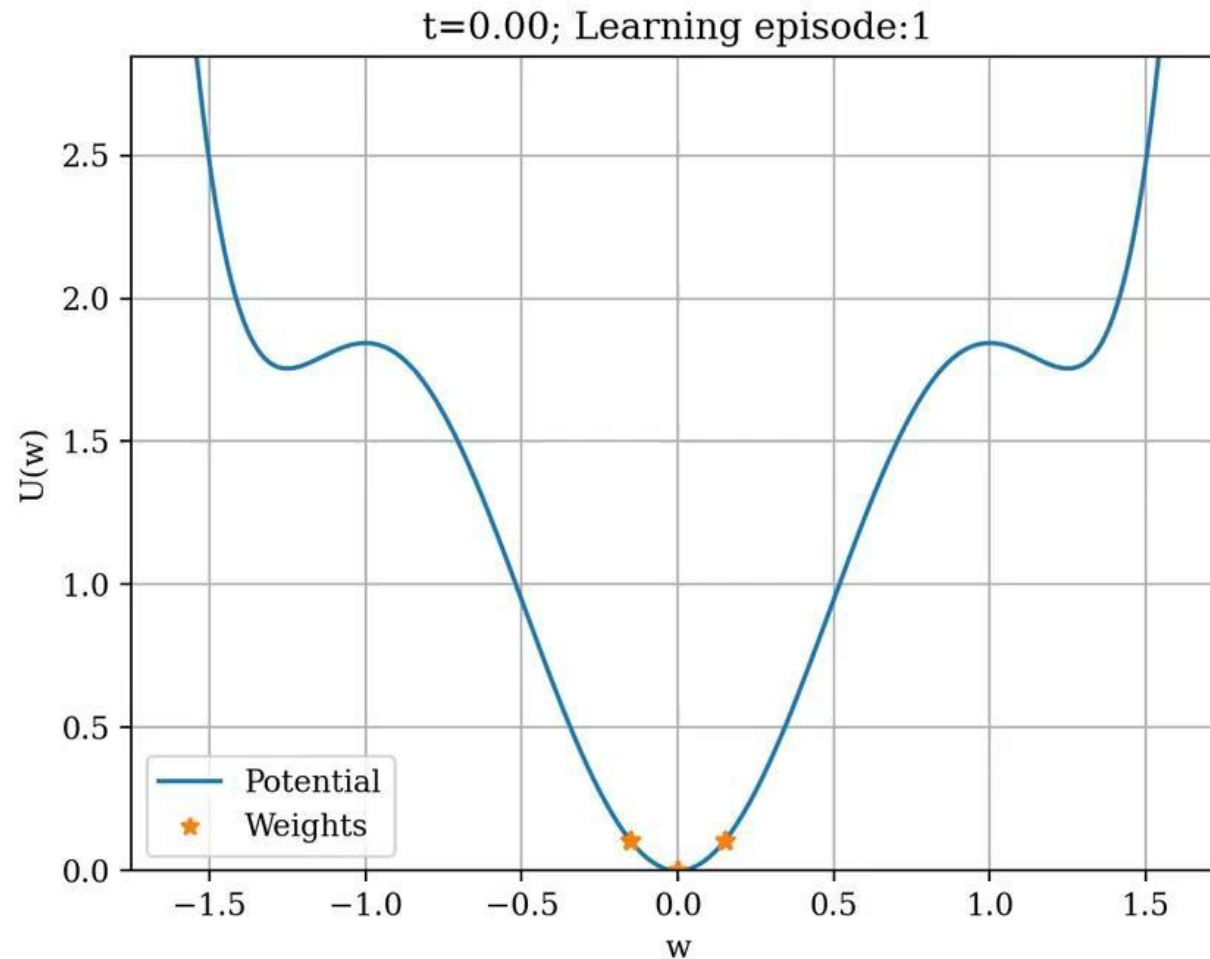
Initialize



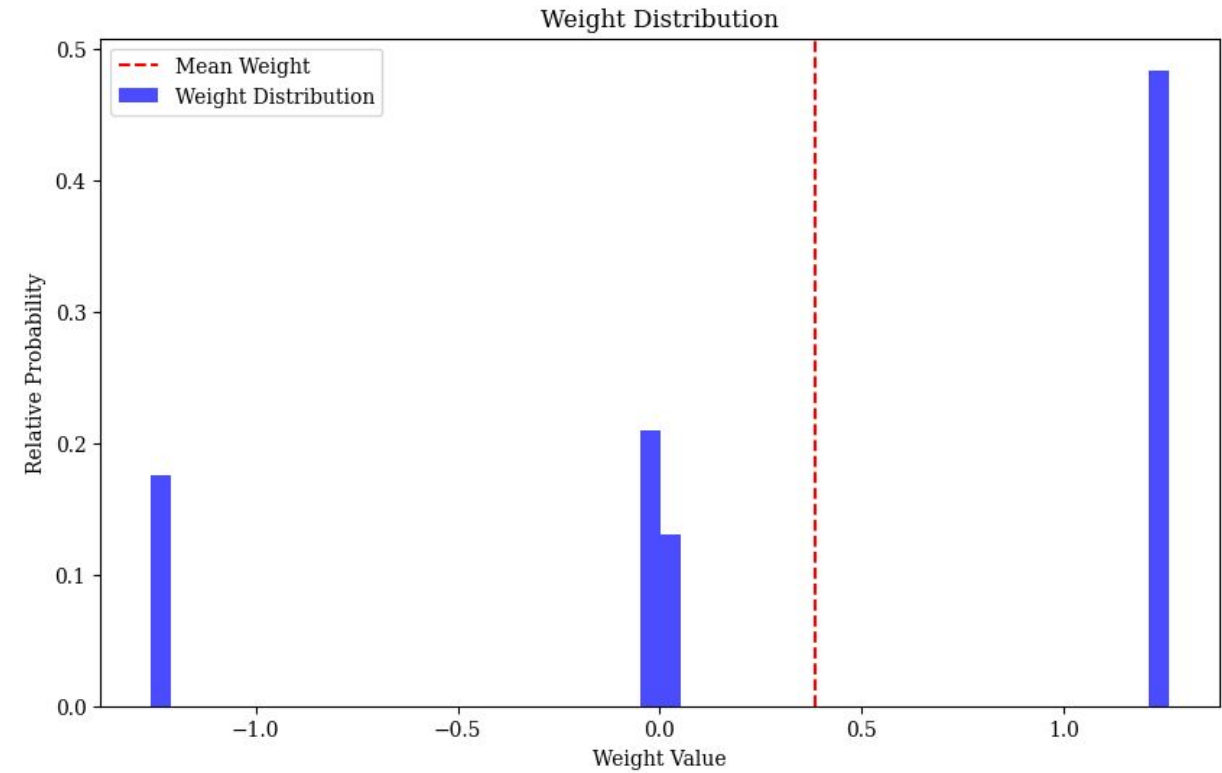
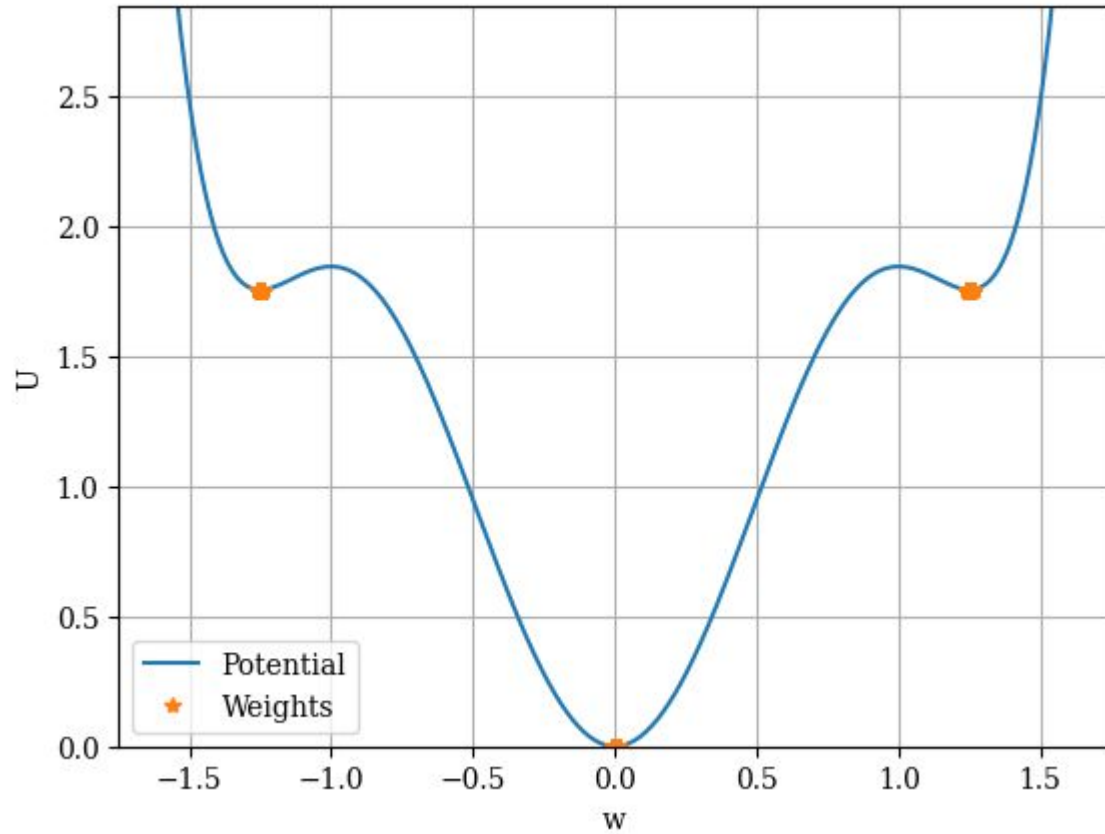
Recall



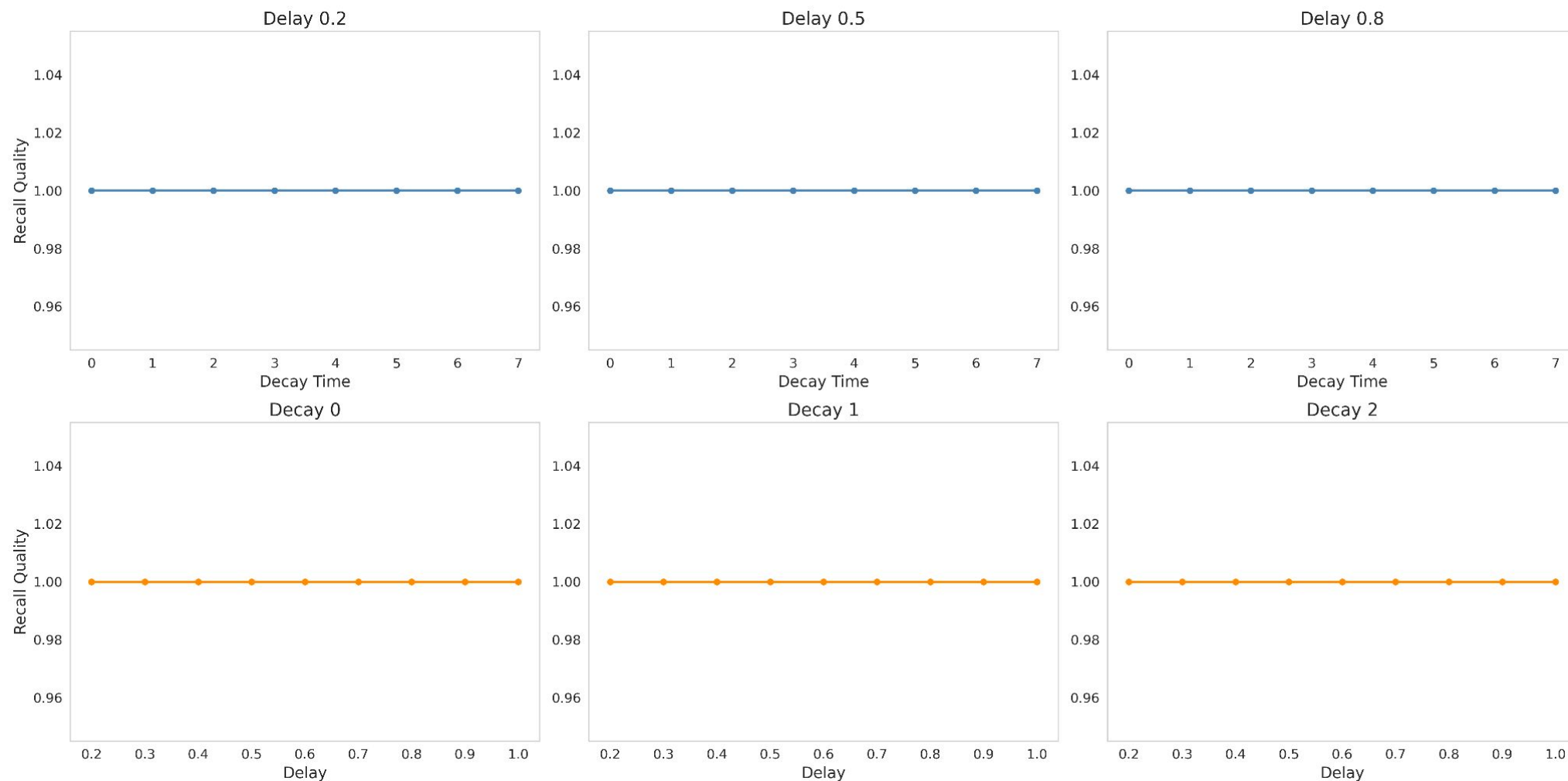
# Weight dynamics of an attractor neural network with triple-well weights



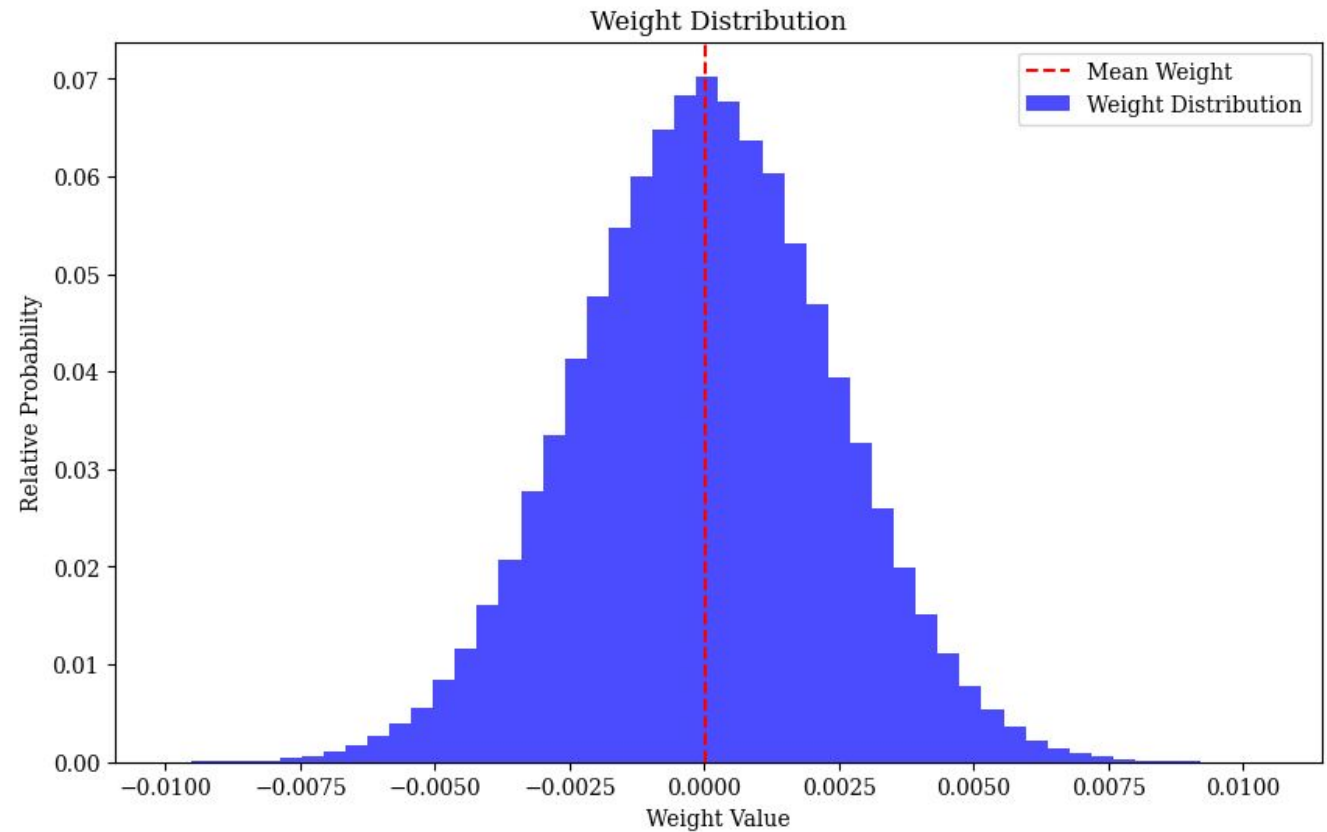
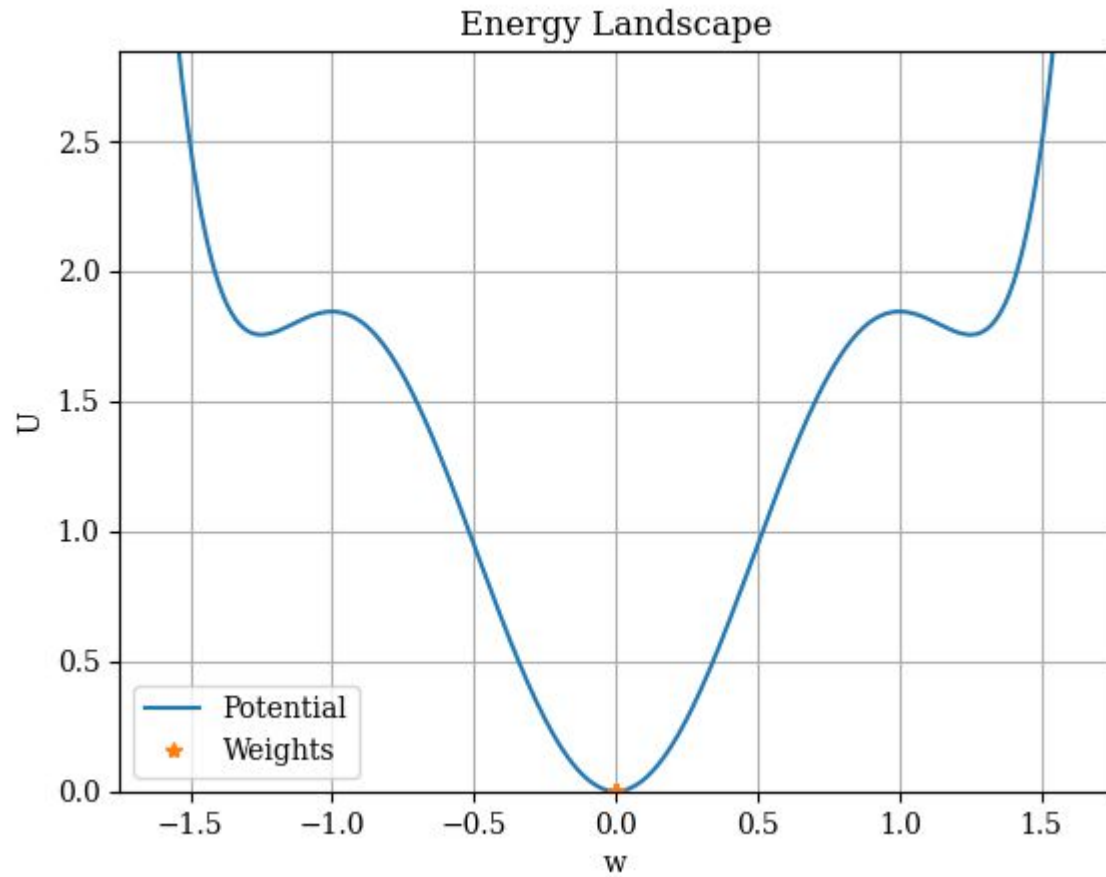
# Weights converge to stable states with high learning rate



# Memory recall sustains with a high learning rate

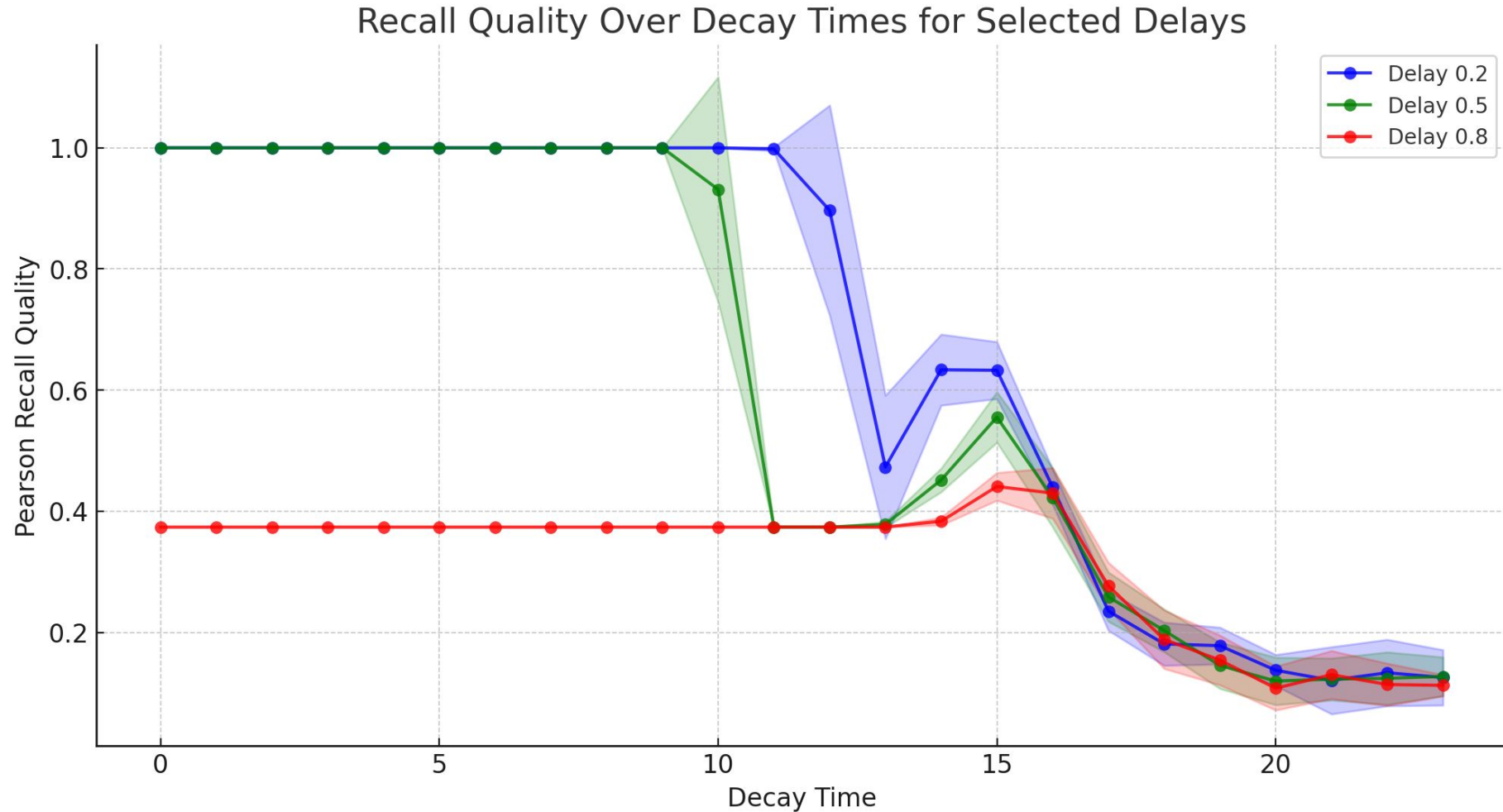


# Weights converge to transient states with a low learning rate

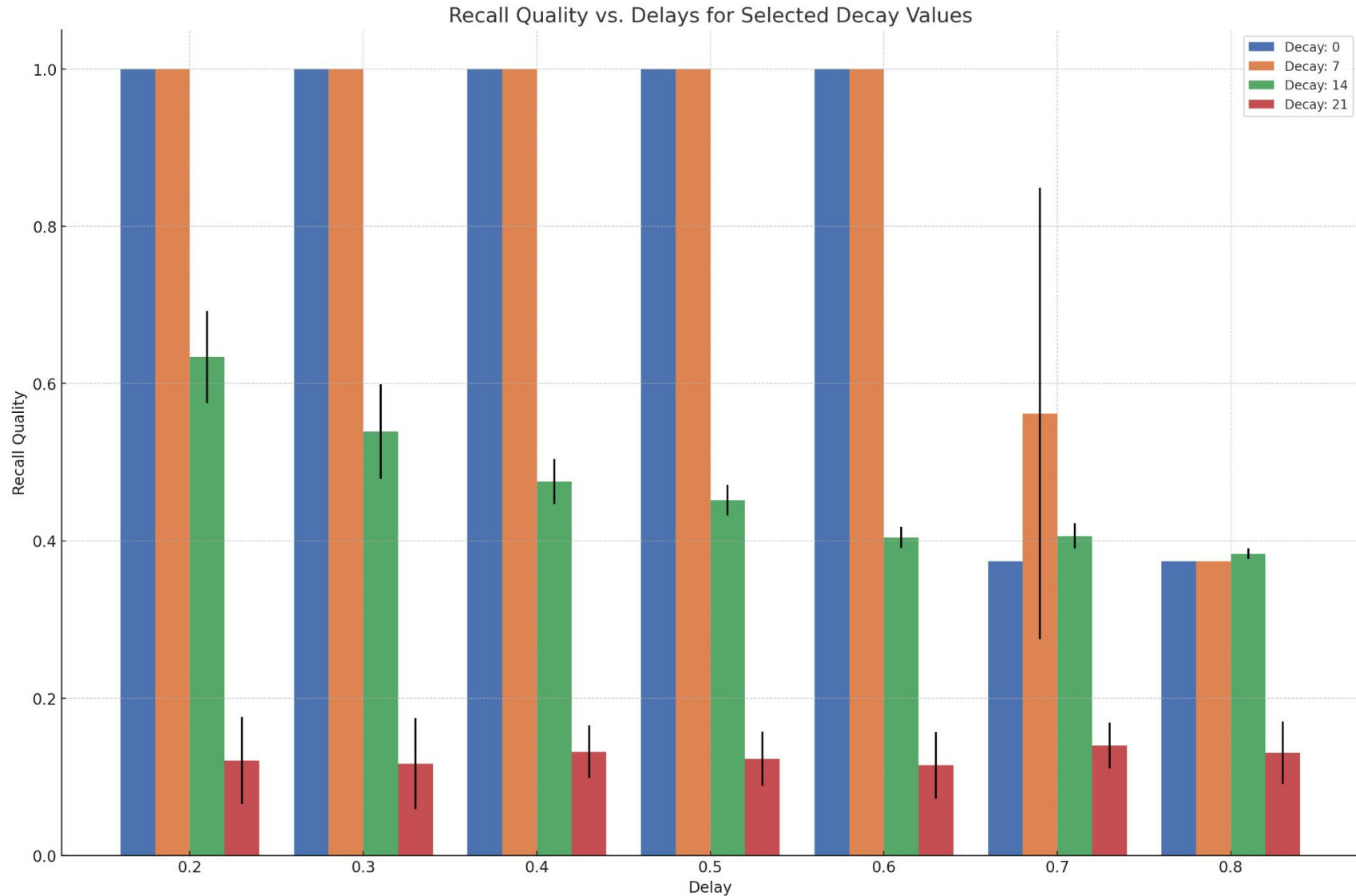




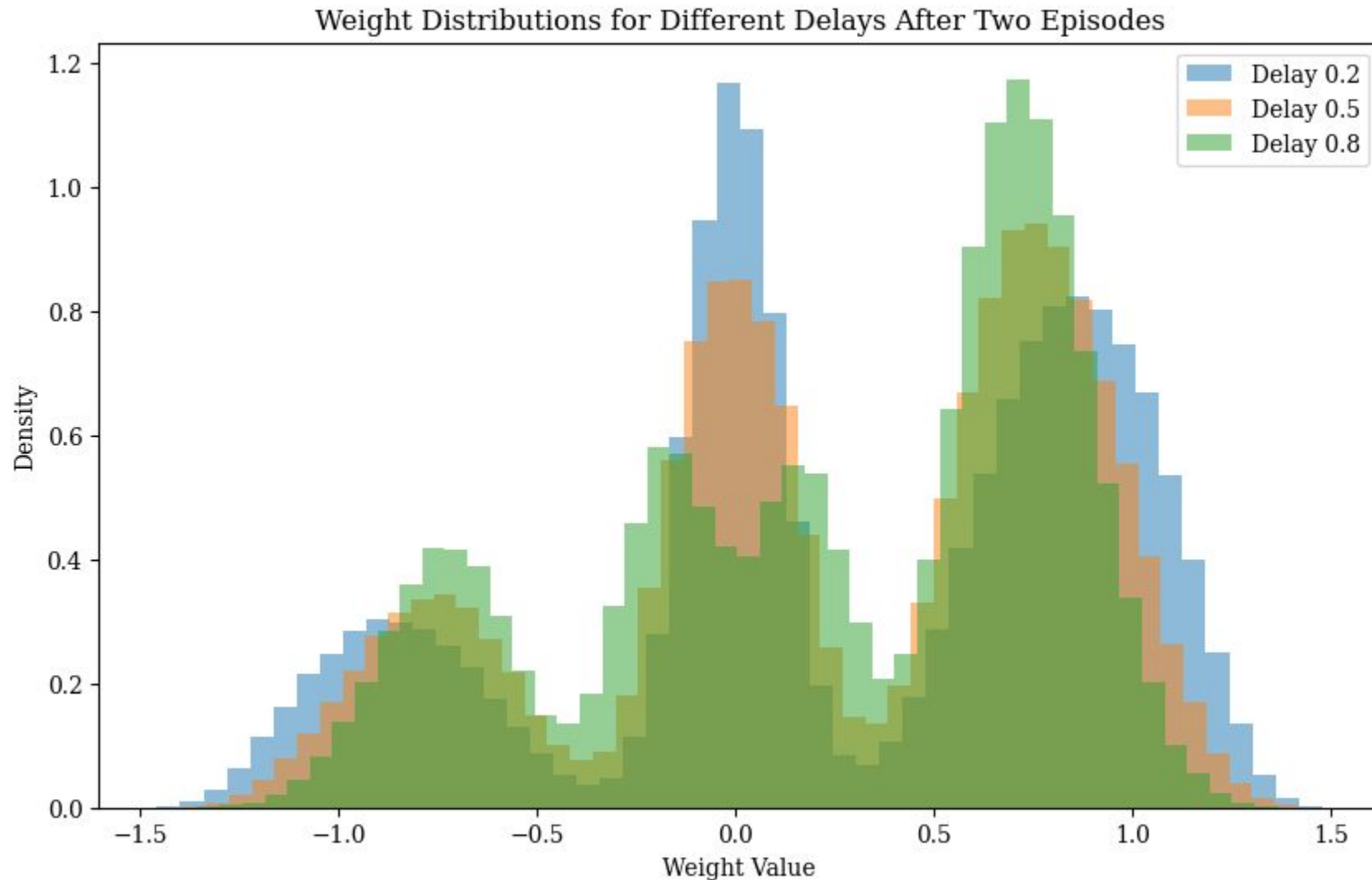
# Memory recall efficacy diminishes over extended decay intervals



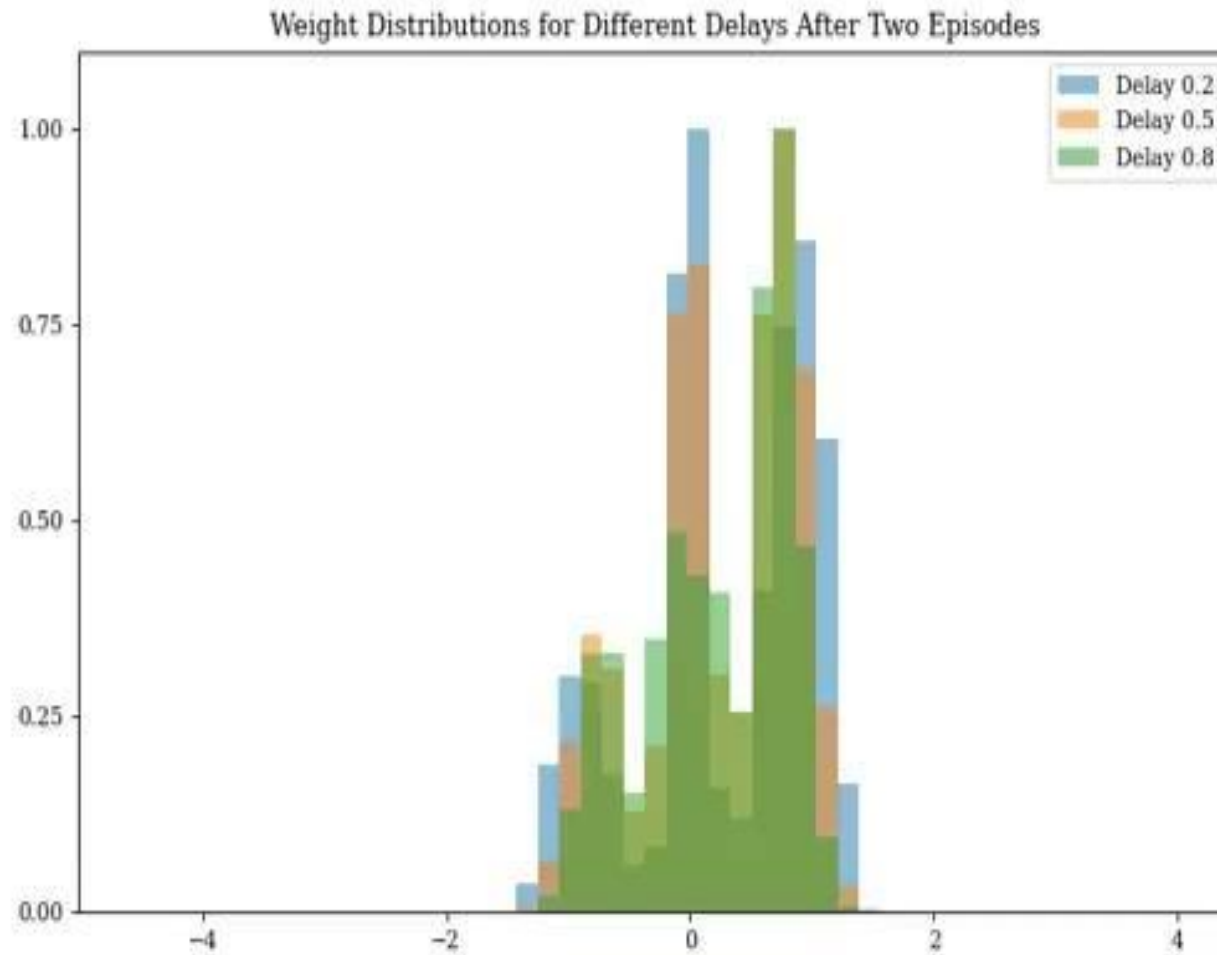
# Degradation of memory recall with increasing delay at low learning rates



# Shorter delays prompt quicker weight shifts to nonzero-well for stable memory states



# A slower transition to zero-well at low delays to transient memory states



# Future Work Planned

- Similar approach for sparser patterns
- Similar approach with an increasing number of patterns
- Test the qualitative prediction of TWH model on cognitive experiments