How they interact:

Bob learns if he can receive blood from Alice

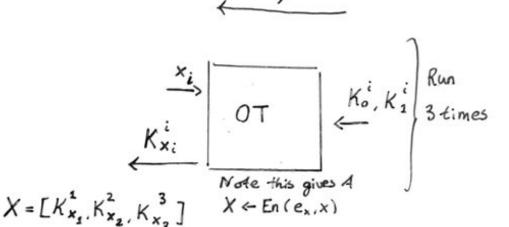
Alice

Bob

 $(F, e, d) \leftarrow Gb(1, f, T)$

F

Y - En(ex, y)



 $Z \leftarrow Ev(F(X||Y))$

 $\stackrel{\mathsf{Z}}{\longrightarrow}$

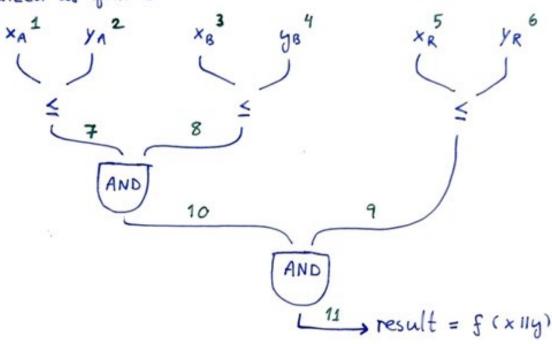
output z - De(d, Z)

we note that $e = (e_{x_A}, e_{y_A}, e_{x_B}, e_{y_B}, e_{x_R}, e_{y_R})$ where $e_x = (e_{x_A}, e_{x_B}, e_{x_R})$ and $e_y = (e_{y_A}, e_{y_B}, e_{y_R})$.

Circuit $f: \{0.13^6 \rightarrow \{0.13\}, T=11 \text{ wires} \}$ input on form f(x||y), see if y can receive blood from x.

f((xA, XB, XR), (YA, YB, YR)) = (((XA = YA) · (XB = YB)) · (XR = YR))

Visualized as follows:



Numbering of wires:

wi for i∈[1, _,6] input wires

wi for i E [7, 8, 9, 10] internal wires

wy for T = 11 output wire.

Notation: Wi = Eval (WL(i), WR(i)), where L, R:[7,11] → [1,_,11]:

Notation. $\omega_7 = \omega_1 \leq \omega_2$, $\omega_8 = \omega_3 \leq \omega_4$, $\omega_9 = \omega_5 \leq \omega_6$,

W10 = W7 N W8 , W11 = W9 N W 10

Eval is either "=" or "A". Note L(i) = R(i) < i.

$$L: 8 \rightarrow 3$$

$$Q \rightarrow 5$$

$$10 \rightarrow 7$$

$$11 \rightarrow 9$$

$$R: 8 \rightarrow 4$$

$$Q \rightarrow 6$$

$$10 \rightarrow 8$$

$$11 \rightarrow 10$$

We need to have a PRF

G: $\{0,1\}^k \times \{0,1\}^k \times [1,...,11] \rightarrow \{0,1\}^n$, use SHA-256.
"set length of wire labels to 128 bits $\rightarrow k=128$?"

Circuit generation: Want output (F, e, d)

Gb (f, 11):

For i in range (1, 12): 1 = 1, ..., 11choose $(K_0^i, K_1^i) \stackrel{\$}{\leftarrow} \{0,1\}^k \times \{0,1\}^k$

All-key-values. append (Ko, Ki) // store all keys somewhere

if i < 7: // if $i \in \{1, 2, 3, 4, 5, 6\}$

e.append((Ko, Ki)) // store keys for input wires in some way du to access

if i = 11: $d := (Z_0, Z_1) = (K_0^{11}, K_1^{11})$

Note that $e_x = \{K_o, K_1\}_{i \in \{1,3,5\}}$ will be used for Alice, and $e_y = \{K_o, K_1\}_{i \in \{2,4,6\}}$ will be used for Bob when encoding their input.

For i in range (7, 12): $// define C_{0..., C_{3}}^{i}$ for F $C_{00}^{i} = G(K_{0..., K_{0...}}^{(i)}, K_{0...}^{(i)}) \oplus (K_{\text{Eval}(0,0)}^{i}, O^{k})$ $C_{01}^{i} = G(K_{0..., K_{1...}}^{(i)}, K_{1...}^{(i)}) \oplus (K_{\text{Eval}(1,0)}^{i}, O^{k})$ $C_{10}^{i} = G(K_{1..., K_{0...}}^{(i)}, K_{0...}^{(i)}, i) \oplus (K_{\text{Eval}(1,0)}^{i}, O^{k})$ $C_{11}^{i} = G(K_{1..., K_{1...}}^{(i)}, K_{1...}^{(i)}) \oplus (K_{\text{Eval}(1,1)}^{i}, O^{k})$

choose random permutation $\Pi: \{0,1,2,3\} \rightarrow \{0,1\} \times \{0,1\}$ $(C_0, C_1, C_2, C_3) = (C_{\pi(0)}, C_{\pi(1)}, C_{\pi(2)}, C_{\pi(3)})$

F. append ((Co, Ci, Ci, Ci, Ci))

```
Encoding:
     Parse e = [[Ko, Ki], ... [Ko, Ki]]
For Alice:
    Return X = [K1 Kx2, Kx3]
   Retur Y = [ Kx1, Kx2, Kx3]
Evaluate:
       E_{V}(F,\chi,Y)
      Parse X = [K1, K3, K5], Y = [K2, K4, K6]
     K-values = [K1, K2, K3, K4, K5, K6]
     For i in range (7,11):
Access (Co, Ci, Ci, Ci, Ci)
         For j in range (4):
                 (K'_{j}, \gamma_{j}) = G(K^{L(i)}, K^{R(i)}, i) \oplus C_{j}^{i}
                        save all values, check for correct
                   result outside of loop since uniqueness
        If unique j st Jj = 04:
               K' = K' , K - values append (K')
        Else: Abort, return I
   Output Z' = K11
```

Decoding:

De(d,Z):

Parse d = (Zo, Z1)

If Z = Z .:

Return 0

If Z = Z1:

Return 1

else:

Return 1