

Laboratorium 1: Kalkulator ISCC, podstawowe operatory na zbiorach i relacjach

Wariant 5.7

Zbiór niesparametryzowany

$S := \{ [i, j] : 1 \leq i \leq 12 \text{ and } 1 \leq j \leq i \};$

Zbiór sparametryzowany

$S := [n] \rightarrow \{ [i, j] : 1 \leq i \leq n \text{ and } 1 \leq j+12 \leq i \};$

Relacja:

$R := [n] \rightarrow \{ [i, j] \rightarrow [i, j + 12] : 0 \leq i < n \text{ and } 0 \leq j < n - 1 \};$

Zadanie 4

Wykonać dla wskazanego zbioru niesparametryzowanego i sparametryzowanego oraz relacji operacje niżej.

Zadanie 4.1

$S := \{ [i, j] : 1 \leq i \leq 12 \text{ and } 1 \leq j \leq i \}; \text{ print "S:"; } S;$

$\$0 := \{ [i, j] : 0 < i \leq 12 \text{ and } 0 < j \leq i \}$

Zadanie 4.2

$S := [n] \rightarrow \{ [i, j] : 1 \leq i \leq n \text{ and } 1 \leq j+12 \leq i \}; S;$

$\$1 := [n] \rightarrow \{ [i, j] : 0 < i \leq n \text{ and } -11 \leq j \leq -12 + i \}$

Zadanie 4.3

$R := [n] \rightarrow \{ [i, j] \rightarrow [i, j + 12] : 0 \leq i < n \text{ and } 0 \leq j < n - 1 \}; R;$

$\$2 := [n] \rightarrow \{ [i, j] \rightarrow [i, 12 + j] : 0 \leq i < n \text{ and } 0 \leq j \leq -2 + n \}$

Zadanie 4.4

CARD – oblicza liczbę elementów zbioru

$q := \text{card } S; q;$

Niesparametryzowany: $\$3 := \{ 78 \}$

Sparametryzowany: $\$3 := [n] \rightarrow \{ (1/2 * n + 1/2 * n^2) : n > 0 \}$

Zadanie 4.5

$D := \text{domain } R; \text{ //obliczenie dziedziny relacji } D;$

$\$4 := [n] \rightarrow \{ [i, j] \rightarrow [i, 12 + j] : 0 \leq i < n \text{ and } 0 \leq j \leq -2 + n \}$

Zadanie 4.6

$RA := \text{range } R; \text{ //obliczenie zakresu relacji } RA;$

$\$5 := [n] \rightarrow \{ [i0, i1] : 0 \leq i0 < n \text{ and } 12 \leq i1 \leq 10 + n \}$

Zadanie 4.7

$m := \text{identity } S; \text{ // tworzy relację tożsamości } m;$

Niesparametryzowany: $\$7 := \{ [i, j] \rightarrow [i' = i, j' = j] : 0 < i \leq 12 \text{ and } 0 < j \leq i \}$

Sparametryzowany: $\$8 := [n] \rightarrow \{ [i, j] \rightarrow [i' = i, j' = j] : 0 < i \leq n \text{ and } -11 \leq j \leq -12 + i \}$

Zadanie 4.8

$I := \text{pow } R; \text{ // oblicza potęgę relacji } m$

$\$9 := ([n] \rightarrow \{ [k] \rightarrow [[i, j] \rightarrow [i, 12k + j]] : k > 0 \text{ and } 0 \leq i < n \text{ and } 0 \leq j \leq 10 + n - 12k \}, \text{True})$

Zadanie 4.9

$S2 := \text{scan } S; //$ przebiera elementy skończonego zbioru – zbiór musi być niesparametryzowany
 $S2;$

Niesparametryzowany: $\$10 := \{ [i = 12, j = 12]; [i = 12, j = 11]; [i = 11, j = 11]; [i = 12, j = 10]; [i = 11, j = 10]; [i = 10, j = 10]; [i = 12, j = 9]; [i = 11, j = 9]; [i = 10, j = 9]; [i = 9, j = 9]; [i = 12, j = 8]; [i = 11, j = 8]; [i = 10, j = 8]; [i = 9, j = 8]; [i = 8, j = 8]; [i = 12, j = 7]; [i = 11, j = 7]; [i = 10, j = 7]; [i = 9, j = 7]; [i = 8, j = 7]; [i = 7, j = 7]; [i = 12, j = 6]; [i = 11, j = 6]; [i = 10, j = 6]; [i = 9, j = 6]; [i = 8, j = 6]; [i = 7, j = 6]; [i = 6, j = 6]; [i = 12, j = 5]; [i = 11, j = 5]; [i = 10, j = 5]; [i = 9, j = 5]; [i = 8, j = 5]; [i = 7, j = 5]; [i = 6, j = 5]; [i = 5, j = 5]; [i = 12, j = 4]; [i = 11, j = 4]; [i = 10, j = 4]; [i = 9, j = 4]; [i = 8, j = 4]; [i = 7, j = 4]; [i = 6, j = 4]; [i = 5, j = 4]; [i = 4, j = 4]; [i = 12, j = 3]; [i = 11, j = 3]; [i = 10, j = 3]; [i = 9, j = 3]; [i = 8, j = 3]; [i = 7, j = 3]; [i = 6, j = 3]; [i = 5, j = 3]; [i = 4, j = 3]; [i = 3, j = 3]; [i = 12, j = 2]; [i = 11, j = 2]; [i = 10, j = 2]; [i = 9, j = 2]; [i = 8, j = 2]; [i = 7, j = 2]; [i = 6, j = 2]; [i = 5, j = 2]; [i = 4, j = 2]; [i = 3, j = 2]; [i = 2, j = 2]; [i = 12, j = 1]; [i = 11, j = 1]; [i = 10, j = 1]; [i = 9, j = 1]; [i = 8, j = 1]; [i = 7, j = 1]; [i = 6, j = 1]; [i = 5, j = 1]; [i = 4, j = 1]; [i = 3, j = 1]; [i = 2, j = 1]; [i = 1, j = 1] \}$

Zadanie 4.10

$R2 := \text{scan}(R * [n] \rightarrow \{n=6\}); //$ przebiera elementy skończonej relacji, relacja musi być niesparametryzowana
 $R2;$

$\$11 := [n] \rightarrow \{ [i = 5, j = 4] \rightarrow [5, 16] : n = 6; [i = 4, j = 4] \rightarrow [4, 16] : n = 6; [i = 3, j = 4] \rightarrow [3, 16] : n = 6; [i = 2, j = 4] \rightarrow [2, 16] : n = 6; [i = 1, j = 4] \rightarrow [1, 16] : n = 6; [i = 0, j = 4] \rightarrow [0, 16] : n = 6; [i = 5, j = 3] \rightarrow [5, 15] : n = 6; [i = 4, j = 3] \rightarrow [4, 15] : n = 6; [i = 3, j = 3] \rightarrow [3, 15] : n = 6; [i = 2, j = 3] \rightarrow [2, 15] : n = 6; [i = 1, j = 3] \rightarrow [1, 15] : n = 6; [i = 0, j = 3] \rightarrow [0, 15] : n = 6; [i = 5, j = 2] \rightarrow [5, 14] : n = 6; [i = 4, j = 2] \rightarrow [4, 14] : n = 6; [i = 3, j = 2] \rightarrow [3, 14] : n = 6; [i = 2, j = 2] \rightarrow [2, 14] : n = 6; [i = 1, j = 2] \rightarrow [1, 14] : n = 6; [i = 0, j = 2] \rightarrow [0, 14] : n = 6; [i = 5, j = 1] \rightarrow [5, 13] : n = 6; [i = 4, j = 1] \rightarrow [4, 13] : n = 6; [i = 3, j = 1] \rightarrow [3, 13] : n = 6; [i = 2, j = 1] \rightarrow [2, 13] : n = 6; [i = 1, j = 1] \rightarrow [1, 13] : n = 6; [i = 0, j = 1] \rightarrow [0, 13] : n = 6; [i = 5, j = 0] \rightarrow [5, 12] : n = 6; [i = 4, j = 0] \rightarrow [4, 12] : n = 6; [i = 3, j = 0] \rightarrow [3, 12] : n = 6; [i = 2, j = 0] \rightarrow [2, 12] : n = 6; [i = 1, j = 0] \rightarrow [1, 12] : n = 6; [i = 0, j = 0] \rightarrow [0, 12] : n = 6 \}$

Zadanie 4.11

$S1 := \{ [i, j] : 1 \leq i \leq 3 \text{ and } 1 \leq j \leq i \};$
 $S3 := S + S1; //$ suma zbiorów, zbiór $S1$ utworzyć samemu
 $S3;$
 $\$12 := \{ [i, j] : i \leq 12 \text{ and } 0 < j \leq i \}$

Zadanie 4.12

$R1 := [n] \rightarrow \{ [i, j] \rightarrow [i+1, j] : 0 \leq i < n \text{ and } 0 \leq j < n - 1 \};$
 $R3 := R + R1; //$ suma relacji, relację $R1$ utworzyć samemu
 $R3;$
 $\$13 := [n] \rightarrow \{ [i, j] \rightarrow [i, 12 + j] : 0 \leq i < n \text{ and } 0 \leq j \leq -2 + n; [i, j] \rightarrow [1 + i, j] : 0 \leq i < n \text{ and } 0 \leq j \leq -2 + n \}$

Zadanie 4.13

$S3 := S - S1$; //różnica zbiorów

\$22 := { };

Zadanie 4.14

$R3 := R - R1$; //różnica relacji

\$27 := [n] -> { [i, j] -> [i, 12 + j] : $0 \leq i < n$ and $0 \leq j \leq -2 + n$ }

Zadanie 4.15

$S3 := S * S1$; // intersekcja zbiorów

\$23 := { [i, j] : $i \leq 12$ and $0 < j \leq i$ }

Zadanie 4.16

$R2 := R * S$ // intersekcja dziedziny relacji R ze zbiorem S

\$24 := [n] -> { [i, j] -> [i, 12 + j] : $0 \leq i \leq 12$ and $i < n$ and $0 < j \leq i$ and $j \leq -2 + n$ }

Zadanie 4.17

$R2 := R(S)$; // aplikacja relacji S na zbiorze S

\$15 := [n] -> { [i0, i1] : $0 \leq i0 \leq 12$ and $i0 < n$ and $13 \leq i1 \leq 12 + i0$ and $i1 \leq 10 + n$ }

Zadanie 4.18

$R3 := R \circ R1$; // kompozycja relacji R i R1

\$16 := [n] -> { [i, j] -> [1 + i, 12 + j] : $0 \leq i < n$ and $0 \leq j \leq -14 + n$ }

Zadanie 4.19

$R2 := R^i$; //relacja R do potęgi i, gdzie i jest stała

i := 2;

\$25 := [n] -> { [i, j] -> [i, 24 + j] : $0 \leq i < n$ and $0 \leq j \leq -14 + n$ }

Zadanie 4.20

$I := R^+$; // obliczenie tranzytywnego domknięcia relacji R

\$23 := ([n] -> { [i, j] -> [i, o1] : $(-j + o1) \bmod 12 = 0$ and $0 \leq i < n$ and $0 \leq j \leq -2 + n$ and $o1 \geq 12 + j$ and $12 \leq o1 \leq 10 + n$ }, True)

Zadanie 4.21

b := S = S1; //sprawdzenie czy zbiory S i S1 są identyczne

\$17 := False

Zadanie 4.22

b := R = R1; //sprawdzenie czy relacje R i R1 są identyczne

\$18 := False

Zadanie 4.23

b := S ≤ S1; //sprawdzenie czy zbiór S jest podzbiorem S1

\$19 := False

Zadanie 4.24

b := R ≤ R1; //sprawdzenie czy relacja R jest podzbiorem R1

\$20 := False

Zadanie 4.25

$m := S \ll S$; //tworzenie relacji, której elementy dziedziny są // leksykograficznie ściśle mniejsze niż elementy zakresu.

$\$21 := \{ [i, j] \rightarrow [i', j'] : i \leq 12 \text{ and } 0 < j \leq i \text{ and } i < i' \leq 12 \text{ and } 0 < j' \leq i';$
 $[i, j] \rightarrow [i' = i, j'] : i \leq 12 \text{ and } 0 < j \leq i \text{ and } j' > j \text{ and } 0 < j' \leq i \}$

Zadanie 4.26

$m := S \gg S$; //tworzenie relacji, dla której elementy dziedziny są // leksykograficznie ściśle większe niż elementy zakresu.

$\$22 := \{ [i, j] \rightarrow [i', j'] : i \leq 12 \text{ and } 0 < j \leq i \text{ and } i' \leq 12 \text{ and } i' < i \text{ and } 0 < j' \leq i';$
 $[i, j] \rightarrow [i' = i, j'] : i \leq 12 \text{ and } 0 < j \leq i \text{ and } 0 < j' < j \text{ and } j' \leq i \}$