

(2) (a)

Implementation 1

$$T(n) = T(n-1) + T(n-2) + c$$

$$\approx T(n-1) + T(n-1) + c$$

$$\approx 2T(n-1) + c$$

$$\approx 2[2T(n-2) + c] + c$$

$$\approx 2^2 T(n-2) + 2c + c$$

$$\approx 2^2 T(n-2) + 3c$$

$$\approx 2^2 [2T(n-3)] + 3c$$

$$\approx 2^3 T(n-3) + 4c + 3c$$

$$\approx 2^3 T(n-3) + 7c$$

⋮

$$\approx 2^k T(n-k) + c$$

$$\approx 2^n (1) + c$$

$$\approx 2^n + c$$

$$\text{Complexity} = O(2^n)$$

ETC

$$T(n) = O(2^n)$$

$$T(n-k) = 0$$

$$n = k$$

$$T(n-k) = 1$$

Implementation 2

$$\begin{aligned}T(n) &= O(1) + O(1) + O(1) + O(1) + O(1) + O(n) \\&= O(5) + O(n) \\&= O(5+n)\end{aligned}$$

Complexity,  $T(n) = O(n)$

∴ Time complexity for implementation 2 is better than implementation 1.