You have to use the designated spaces for your answers. No extra pages will be provided.

Problem 1: The CYK Algorithm (10 points)

Consider the following context-free grammar.

$$S \to AB \mid BC$$

$$A o CB \mid$$
 a

$$B \to AC \mid \mathbf{b}$$

$$C o AB \mid \mathtt{a}$$

Now run the CYK algorithm to decide whether the string abbab can be derived in the grammar above. You must fill in the entire CYK table below.

| 1,5 | | | | |
|-----|------|------|-----|------|
| 1,4 | 2, 5 | | | |
| 1,3 | 2,4 | 3,5 | | |
| 1,2 | 2, 3 | 3, 4 | 4,5 | |
| 1,1 | 2, 2 | 3, 3 | 4,4 | 5, 5 |