

CSE 461 ASSIGNMENT 2

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SECTION: 09

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$$(3) A_i = \begin{bmatrix} \cos \theta_i & -\sin \theta_i \cos \alpha_i & \sin \theta_i \sin \alpha_i & a_i \cos \theta_i \\ \sin \theta_i & \cos \theta_i \cos \alpha_i & -\cos \theta_i \sin \alpha_i & a_i \sin \theta_i \\ 0 & \sin \alpha_i & \cos \alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0A_1 = \begin{bmatrix} \cos 30^\circ & -\sin 30^\circ \cos 0^\circ & \sin 30^\circ \sin 0^\circ & 10 \cos 30^\circ \\ \sin 30^\circ & \cos 30^\circ \cos 0^\circ & -\cos 30^\circ \sin 0^\circ & 10 \sin 30^\circ \\ 0 & \sin 0^\circ & \cos 0^\circ & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \begin{matrix} \alpha_i = 0^\circ \\ a_i = 10 \\ d_i = 0 \\ \theta_i = 30^\circ \end{matrix}$$

$${}^0A_1 = \begin{bmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} & 0 & 5\sqrt{3} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} & 0 & 5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^1A_2 = \begin{bmatrix} \cos 45^\circ & -\sin 45^\circ \cos 0^\circ & \sin 45^\circ \sin 0^\circ & 8 \cos 45^\circ \\ \sin 45^\circ & \cos 45^\circ \cos 0^\circ & -\cos 45^\circ \sin 0^\circ & 8 \sin 45^\circ \\ 0 & \sin 0^\circ & \cos 0^\circ & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \begin{matrix} \alpha_2 = 0^\circ \\ a_2 = 8 \\ d_2 = 0 \\ \theta_2 = 45^\circ \end{matrix}$$

$${}^1A_2 = \begin{bmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} & 0 & 4\sqrt{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} & 0 & 4\sqrt{2} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^1A_3 = \begin{bmatrix} \cos 10^\circ & -\sin 10^\circ \cos 0^\circ & \sin 10^\circ \sin 0^\circ & 3 \cos 10^\circ \\ \sin 10^\circ & \cos 10^\circ \cos 0^\circ & -\cos 10^\circ \sin 0^\circ & 3 \sin 10^\circ \\ 0 & \sin 0^\circ & \cos 0^\circ & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}; \begin{matrix} \alpha_3 = 0^\circ \\ \theta_3 = 10^\circ \\ d_3 = 0 \end{matrix}$$

$${}^2A_3 = \begin{bmatrix} 0.985 & -0.174 & 0 & 2.984 \\ 0.174 & 0.985 & 0 & 0.521 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0A_3 = ({}^0A_1)({}^1A_2)({}^2A_3) \Rightarrow {}^0A_3 = \begin{bmatrix} 0.0868 & -0.996 & 0 & 10.997 \\ 0.9969 & 0.0868 & 0 & 15.715 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

final position ${}^0A_3 \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 10.997 \\ 15.715 \\ 0 \\ 1 \end{bmatrix}$