

## \* HUFFMAN CODE ALGORITHM :-

Prefix Codes, means the codes (bit sequences) are assigned in such a way that the code assigned to one character is not the prefix of code assigned to any other character.

This is how huffman coding makes sure that there is no ambiguity when decoding the generated bitstream.

Example :- let there be four characters a, b, c & d and their corresponding variable length codes 00, 01, 0b1. This coding leads to ambiguity because code assigned to c is the prefix of codes assigned to 'a' and 'b'.

If the compressed bit stream is 0001

The de-compressed o/p may be →

" <u>cc</u> cd"	← 0001
or	
"cc <u>b</u> "	← 0001
or	
"a <u>cd</u> "	← 0001
or	
"a <u>b</u> "	← 0001

See this for appl.<sup>n</sup> of Huffman Coding :-

There are mainly two major parts in Huffman Coding:

- 1) Build a Huffman Tree from i/p characters.
- 2) Transverse the Huffman Tree & assign codes to characters.

→ Data Compression method.

→ lossless (without loss of information) compression.

Algorithm :-

Huffman ( $c$ ) <sup>set of n characters</sup>

- 1)  $n = |c|$
- 2)  $Q = c$  // min. Priority Queue
- 3) for  $i=1$  to  $n-1$
- 4) do allocate a new node  $z$
- 5)  $z.\text{left} \leftarrow x \leftarrow \text{Extract.min}(Q)$
- 6)  $z.\text{right} \leftarrow y \leftarrow \text{Extract.min}(Q)$
- 7)  $z.\text{freq} \leftarrow x.\text{freq} + y.\text{freq}$
- 8) Insert ( $Q, z$ )
- 9) return  $\text{Extract.min}(Q)$  // return Root of the tree

Implementation

To understand the concept of fixed & variable code:-

fixed

freq. in →  
Thousands

a	b	c	d	e	f
45	13	12	16	9	5

Total freq.  $\Rightarrow 100 \times 1000 = 1$  lakh

If each character is represented by 3 bit  $\Rightarrow$

$1 \text{ lakh} \times 3 = 3 \text{ lakh}$  bit

Storage required

variable

But in Variable Code  $\Rightarrow$

$$1 \times 45 + 3 \times 13 + 3 \times 12 + 3 \times 16 + 4 \times 9 + 4 \times 5$$

$$= 45 + 39 + 36 + 48 + 36 + 20$$
$$= 224$$

$$224 \times 1000 = 224000 \text{ bit}$$

Storage required

See sol. in next Page  $\rightarrow$

Example:-

Character	frequency	fixed code	variable length
a	45	000	0
b	13	001	101
c	12	010	100
d	16	011	111
e	9	100	1101
f	5	101	1100

Solve using Huffman Code.

In fixed Code  $\Rightarrow$  we require more ~~we~~ storage to store.

$$\text{like } 45 \times \underset{\substack{\uparrow \\ \text{bit}}}{3} = 135$$

$$13 \times 3 = 39$$

$$12 \times 3 = 36$$

⋮

for ~~less~~ <sup>reducing</sup> storage we use variable length  $\Rightarrow$  by Huffman Code.

1)  $n = 6$

2)  $Q = \begin{bmatrix} a & b & c & d & e & f \\ 45 & 13 & 12 & 16 & 9 & 5 \end{bmatrix} \leftarrow \text{min. Priority Queue.}$

3) for  $i = 1 \rightarrow 5$

4) do allocate a node (Z)

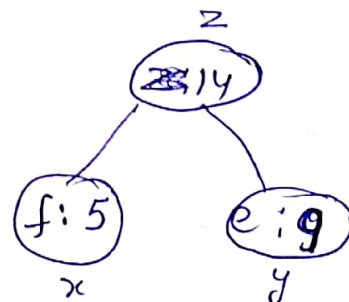
5)  $Z.\text{left} \leftarrow \text{f} \leftarrow x$

6)  $Z.\text{right} \leftarrow \text{e} \leftarrow y$

7)  $Z.\text{freq} \leftarrow x.\text{freq} + y.\text{freq}$

$Z.\text{freq} \leftarrow 5 + 9$

$Z.\text{freq} \leftarrow 14$



8) Now, Insert (Q, z)

Again go to step 3)

3)  $i = 2 - 5$

4) allocate z

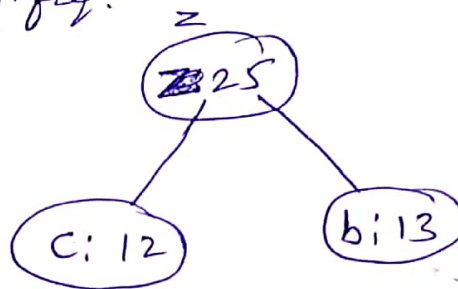
5)  $z \cdot \text{left} \leftarrow x \leftarrow c$

6)  $z \cdot \text{right} \leftarrow y \leftarrow b$

7)  $z \cdot \text{freq} \leftarrow x \cdot \text{freq} + y \cdot \text{freq}$   
 $\leftarrow 12 + 13$   
 $\leftarrow 25$

8) Insert (Q, z)

a	45	
b	13	
c	12	
d	16	
e	9	
f	5	



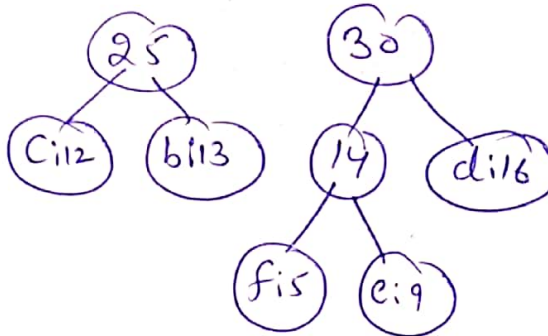
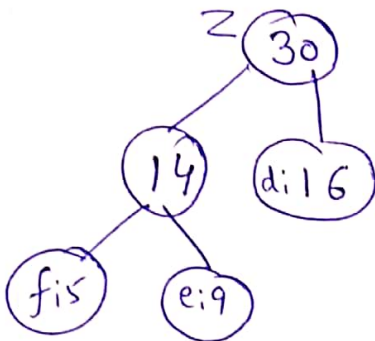
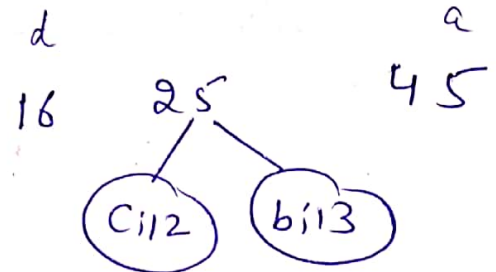
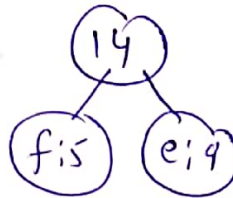
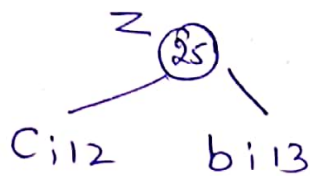
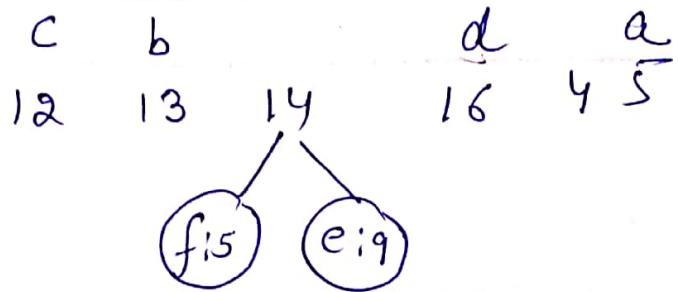
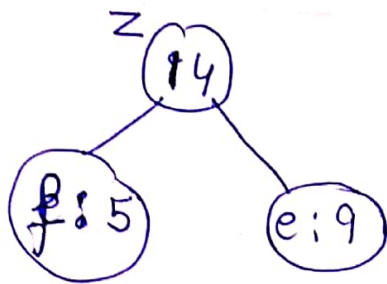
Repeat  
 until  
 1 root node  
 is found.

SHORT CUT :- a b c d e f  
 45 13 12 16 9 5

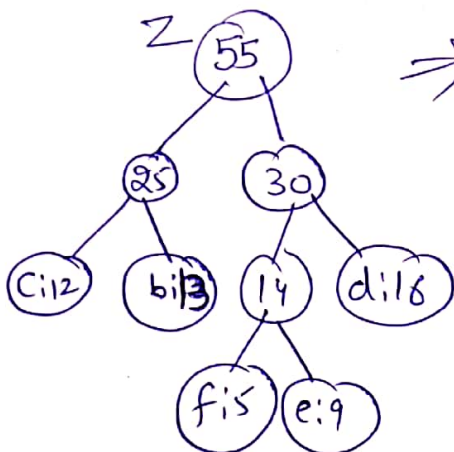
Arrange in ascending order:-

~~a b c d e f~~  
 f e c b d a  
 5 9 12 13 16 45

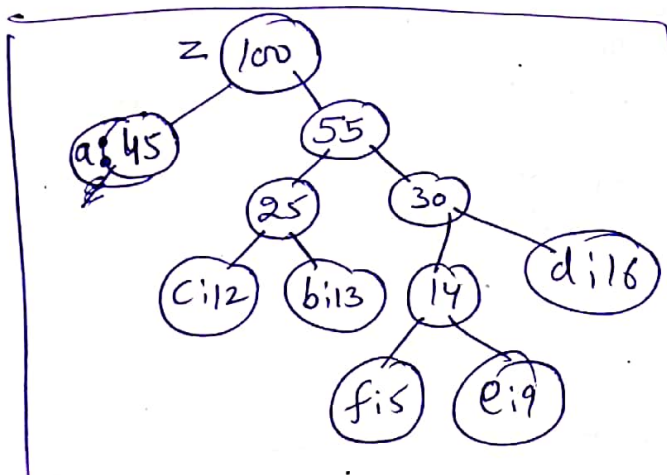
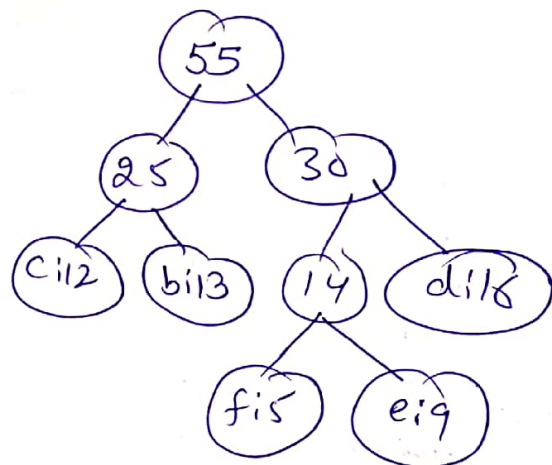




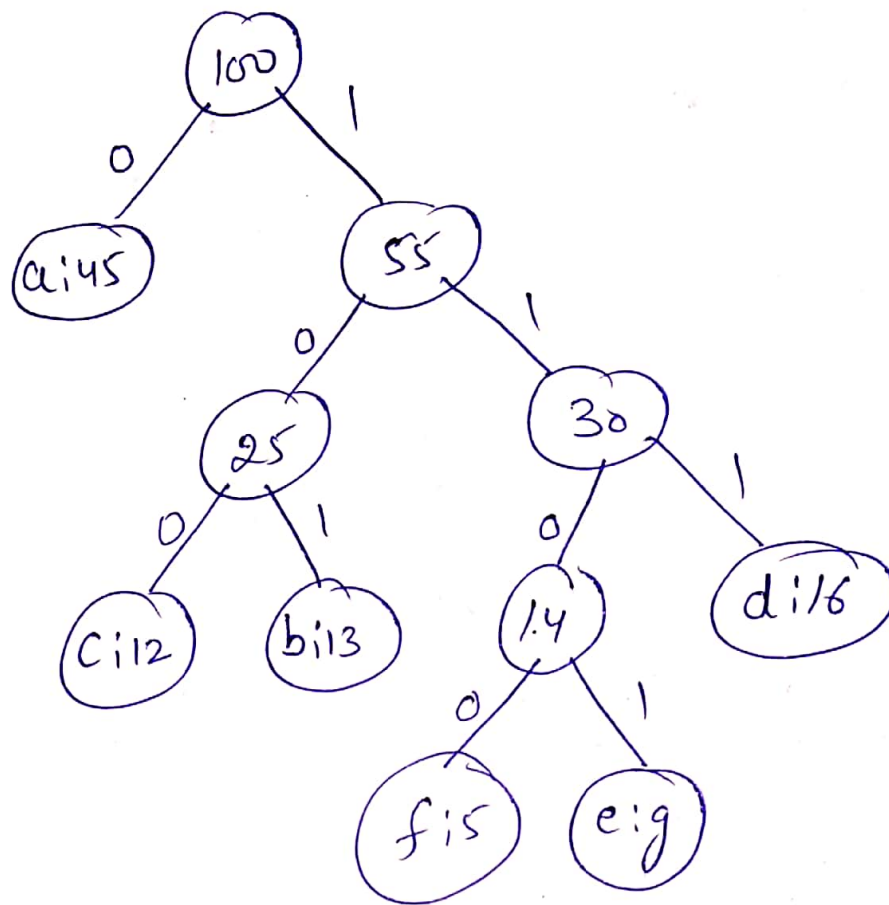
a  
4 5



a  
4 5



← New Assign 0 to left node & 1 to right node



Now New Code :-  
Variable Code

Ans ⇒

a	0
b	101
c	100
d	111
e	1101
f	1100