

Data Structures and Algorithms

Lecture 13

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Agenda

Data Structures

Data Structures

- ▶ What and Why

Data Structures

- ▶ What and Why
- ▶ a way to store data/information and
- ▶ a way to retrieve
- ▶ a way to delete
- ▶ a way to create relationship among data, e.g., precedence, successor, etc.

Data Structures

- ▶ Linear: Arrays, Stacks, Queues, Deques, Linked Lists
- ▶ Non-Linear: Heaps, Binary Search Trees, Graphs
- ▶ Hashing: The magic of $O(1)$ lookup

Example

A computer game that stores a deck of playing cards.
A few queries we want to answer:

Example

A computer game that stores a deck of playing cards.

A few queries we want to answer:

1. We want to add a card into the deck.
2. Which card is at the top of the deck?
3. Is the deck empty?
4. Given a card are there any higher rank cards of the same suit in the deck. E.g., Given 9♣, is there a card $C \in \{10\clubsuit, J\clubsuit, Q\clubsuit, K\clubsuit\}$ in the deck?

Stacks

Push(a)

Pop()

TopElement()

IsEmpty()

Stacks

STACK-EMPTY(S)

```
1 if  $S.top == 0$ 
2     return TRUE
3 else return FALSE
```

PUSH(S, x)

```
1 if  $S.top == S.size$ 
2     error "overflow"
3 else  $S.top = S.top + 1$ 
4      $S[S.top] = x$ 
```

POP(S)

```
1 if STACK-EMPTY( $S$ )
2     error "underflow"
3 else  $S.top = S.top - 1$ 
4     return  $S[S.top + 1]$ 
```

Queues

Enqueue(a)

Dequeue()

IsEmpty()

Queues

ENQUEUE(Q, x)

```
1  $Q[Q.tail] = x$ 
2 if  $Q.tail == Q.size$ 
3    $Q.tail = 1$ 
4 else  $Q.tail = Q.tail + 1$ 
```

DEQUEUE(Q)

```
1  $x = Q[Q.head]$ 
2 if  $Q.head == Q.size$ 
3    $Q.head = 1$ 
4 else  $Q.head = Q.head + 1$ 
5 return  $x$ 
```

Linked Lists

Node

- ▶ prev
- ▶ key
- ▶ next

Operations

- ▶ Search
- ▶ Prepend
- ▶ Insert
- ▶ Delete

Linked Lists

LIST-SEARCH(L, k)

- 1 $x = L.\text{head}$
- 2 **while** $x \neq \text{NIL}$ and $x.\text{key} \neq k$
- 3 $x = x.\text{next}$
- 4 **return** x

Linked Lists

LIST-PREPEND(L, x)

- 1 $x.next = L.head$
- 2 $x.prev = \text{NIL}$
- 3 **if** $L.head \neq \text{NIL}$
- 4 $L.head.prev = x$
- 5 $L.head = x$

Linked Lists

LIST-INSERT(x, y)

```
1   $x.next = y.next$ 
2   $x.prev = y$ 
3  if  $y.next \neq \text{NIL}$ 
4       $y.next.prev = x$ 
5   $y.next = x$ 
```

Linked Lists

LIST-DELETE(L, x)

```
1  if  $x.prev \neq NIL$ 
2       $x.prev.next = x.next$ 
3  else  $L.head = x.next$ 
4  if  $x.next \neq NIL$ 
5       $x.next.prev = x.prev$ 
```

Stacks - A deeper dive

Given $\{1, 2, \dots, n\}$, how many permutations can we generate using a stack?