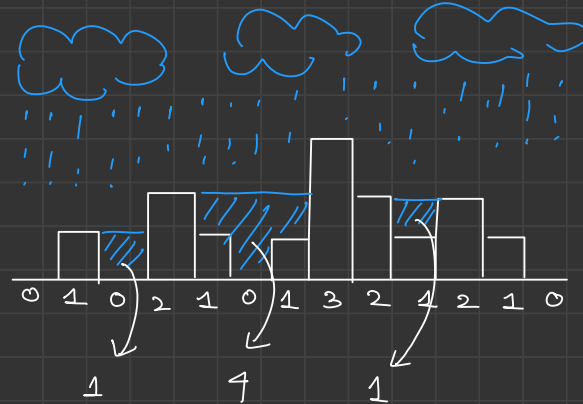


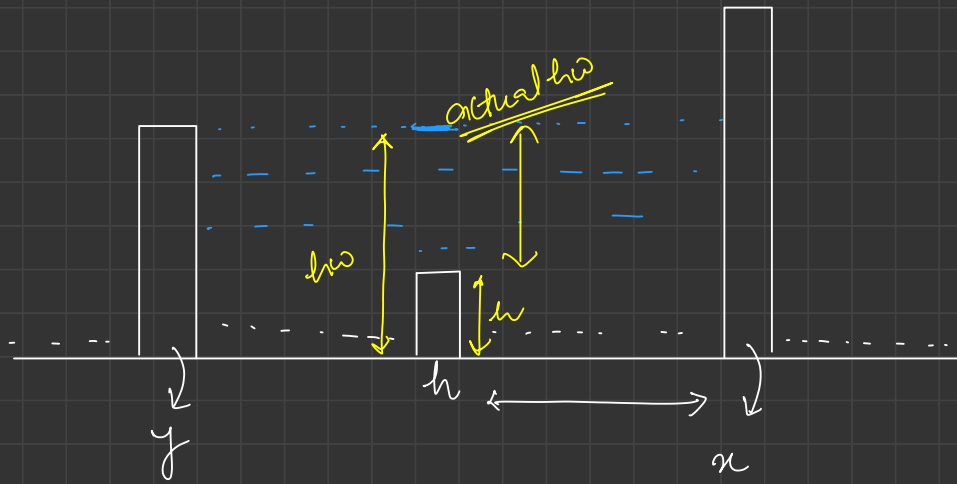


Trapping Rain Water



{ total water stored = 0 units }

How many unit of water a building can store above itself?



LB

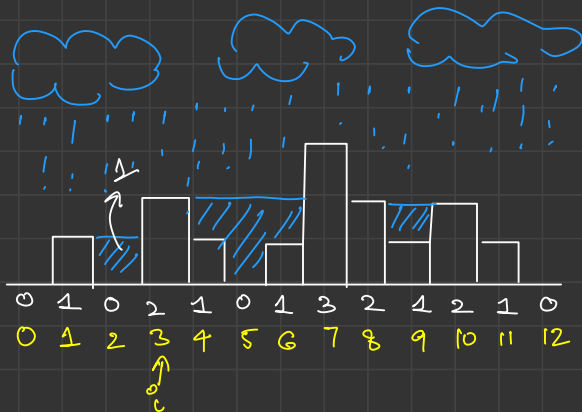
RB

max^m height
building on left
side

$$hwo = \min(LB, RB)$$

$$actual\ hwo = hwo - h$$

max height
building on
right side



$$\begin{aligned} Tc &: O(N^2) \\ SC &: O(1) \end{aligned}$$

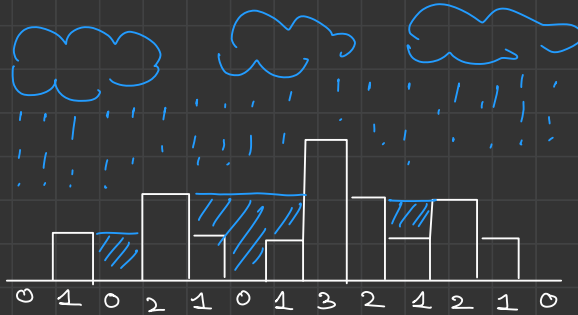
✓ Brute force

Total =

$i = 0$	<u>$RB = 3$</u>	<u>$LB = -\infty$</u>	<u>$hw = -\infty$</u>		
$i = 1$	$RB = 3$	$LB = 0$	$hw = 0$		
$i = 2$	$RB = 3$	$LB = 1$	$hw = 1$	$h = 0$	<u>$ahw = 1$</u> <u>$water = 1$</u>
$i = 3$	$RB = 3$	$LB = 1$	$hw = 1$	$h = 2$	

Can we do in $O(N)$?

LB = ~~$- \infty$~~ ~~$\times 3$~~



RB = ~~$- \infty$~~ ~~$\times 3$~~

$\left\{ \begin{array}{l} \text{lmax}[i] = -\infty, 0, 1, 1, 2, 2, 2, 2, 3, 3, 3, 3, 3 \\ \text{rmax}[i] = 3, 3, 3, 3, 3, 3, 3, 2, 2, 2, 1, 0, -\infty \end{array} \right. \longrightarrow \text{TC: } O(N)$
 $\longrightarrow \text{TC: } O(N)$

```

for (int i = 0; i < n; i++)
{
    hws = Math.min(lmax[i], rmax[i]);
    if (hws > height[i])
    {
        int ahs = hws - height[i];
        totalWater += ahs * 1;
    }
}

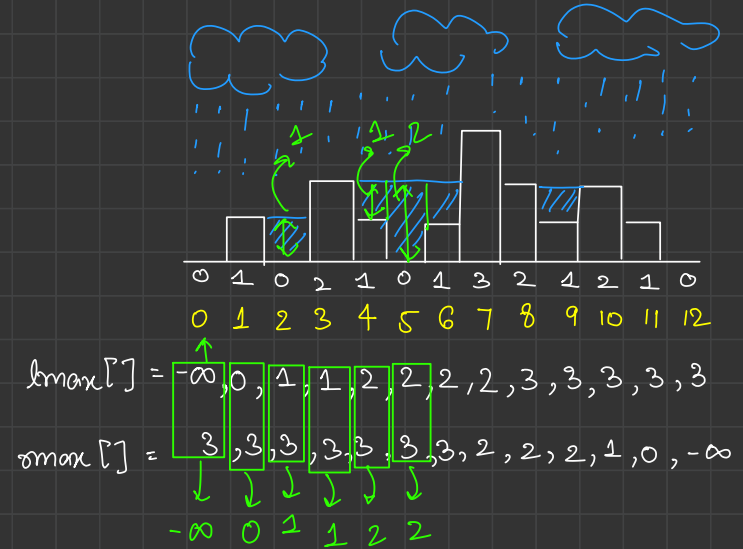
```

TC: $O(N)$
SC: $O(N)$

```
// step 3: calc. water above each building
int totalWater = 0;
for (int i = 0; i < n; i++) {
    int hw = Math.min(lmax[i], rmax[i]);
    if (arr[i] < hw) {
        int ahw = hw - arr[i];
        totalWater += (ahw * 1);
    }
}
```

Handwritten notes:
 - A green arrow points from the value 1 in the calculation $(ahw * 1)$ to the word "width" circled in green.
 - A green arrow points from the value 2 in the calculation $2 * 0 = 2$ to the word "width".

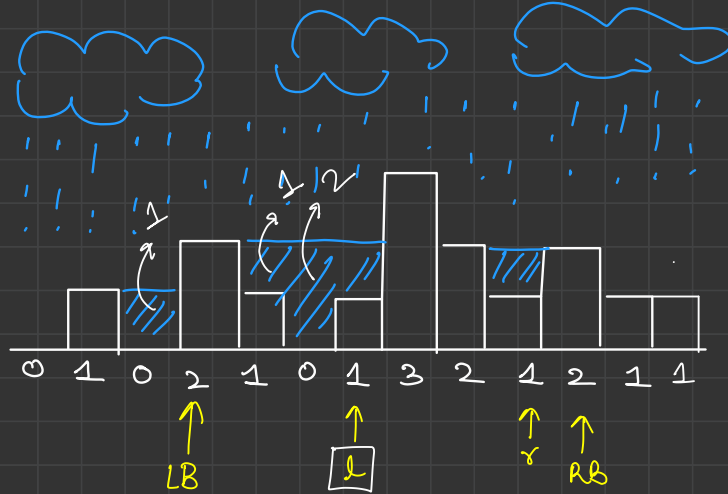
```
System.out.println(totalWater);
```



$Tc: O(N)$
 $Sc: O(N)$

Handwritten notes:
 - A green box surrounds the text $Tc: O(N)$ and $Sc: O(N)$.
 - A green checkmark is drawn next to the text.

✓ TC: O(N) SC: O(1)



LB <= RB

```

hws = LB;
if (hws > arr[l])
{
    totalWater += (hws - arr[l]) * 1;
}
LB = Math.max(LB, arr[l]);
l++;

```

RB < LB

```

hws = RB;
if (hws > arr[r])
{
    totalWater += (hws - arr[r]) * 1;
}
RB = Math.max(RB, arr[r]);
r--;

```

Sum of Subarray Minimums

Brute force : $TC: O(N^2)$
 $SC: O(1)$

$arr[] = \{ 3, 2, 4, 1, 5, 2 \}$

$$\text{Total Subarray} = \frac{N * (N + 1)}{2}$$

Subarrays

(3) (3, 2) (3, 2, 4) (3, 2, 4, 1) (3, 2, 4, 1, 5) (3, 2, 4, 1, 5, 2)

(2) (2, 4) (2, 4, 1) (2, 4, 1, 5) (2, 4, 1, 5, 2)

(4) (4, 1) (4, 1, 5) (4, 1, 5, 2)

(1) (1, 5) (1, 5, 2)

(5) (5, 2) (2)

Sum = 36

$$TC: O(N) \quad SC: O(N)$$

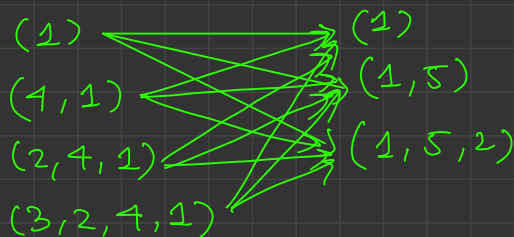
arr[] = { ⁰3, ¹2, ²4, ³1, ⁴5, ⁵2 }

✓ nseli = { -1, -1, 1, -1, 3, 3 }

✓ nseri = { 1, 3, 3, 6, 5, 6 }

✓ 1 * 1

2 * 2
= 4



$$(i - nseli[i]) * (nseri[i] - i)$$

↓
No. of subarrays where
i is min!

{ (1) (1,5) (1,5,2) (1,1) (1,1,5)
(1,1,5,2) (2,4,1) (2,4,1,5)
(2,4,1,5,2)
(3,2,4,1) (3,2,4,1,5) (3,2,4,1,5,2)

```
// step 3: calc number of subarray where arr[i] is min, and then calc there sum
long totalSum = 0;
for (int i = 0; i < n; i++) {
    long num = ((i - nseli[i]) * (nseri[i] - i)) % mod;
    long sum = (num * a[i]) % mod;
    totalSum = (totalSum + sum) % mod;
}
```

$$\begin{array}{l} \text{nseli} \\ \text{nseri} \end{array} \begin{array}{c} \begin{array}{ccc} 0 & 1 & 2 \\ \{ & 1, 2, 1 \} \\ \{ & -1, 0, -1 \} \\ \{ & 2, 2, 3 \} \end{array} \end{array}$$

$$(2 - (-1)) \times (3 - 2) = 3$$

(1) (2,1) (1,2,1)

(1) (1,2)

$$(2 - 1) \times (1 - (-1)) = 2$$

$$(1 - 0) \times (2 - 1) = 1$$

(2)

Minimum Stack

→ push

→ pop

→ getMin

↪ returns minEle. present in stack.

eg:

st.push(1)

st.getMin() ~ 1

st.push(20)

st.getMin() ~ 1

st.push(-10)

st.getMin() ~ -10



st

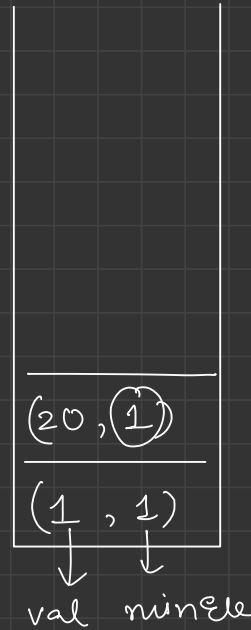
st.pop()

st.getMin() ~ 1

$st.push(1) \rightarrow TC \ O(1)$
 $st.getMin() \rightsquigarrow 1$
 $st.push(20) \rightarrow TC \ O(N)$
 $st.getMin() \rightsquigarrow 1$
 $st.push(-10)$
 $st.getMin() \rightsquigarrow -10$
 $st.pop() \rightarrow -10$
 $st.getMin() \rightsquigarrow 1$

$TC \ O(N)$
 $\hookrightarrow \underline{O(1)}?$

class Pair
 {
 int val;
 int minEle;
 }
 *



minEle = ~~0~~ ~~1~~ -10

✓ `st.push(100)`
`st.getMin()` → 100
 ✓ `st.push(200)`
`st.getMin()` → 100
 ✓ `st.push(10)`
 ✓ `st.getMin()` → 10 ✓
 ✓ `st.push(5)`
 ✓ `st.getMin()` → 5
`st.pop()` → 5
`getMin()` → 10
`pop()` →
`getMin()`



$$\text{minEle} = \cancel{100} 10$$

$$x = \text{val} - \text{minEle}$$

$$\begin{aligned}
 \text{prevMin} &= \text{minEle} - \text{peek} \\
 &= 10 - (-90) \\
 &= \boxed{100}
 \end{aligned}$$