



# DATA ANALYTICS

## Unit 1: Data Transformation and Data Discretization

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A function that maps the entire set of values of a given attribute to a new set of replacement values such that each old value can be identified with one of the new values

- Methods
  - Smoothing: Remove noise from data
  - Attribute/feature construction
    - New attributes constructed from the given ones
  - Aggregation: Summarization, data cube construction
  - Normalization: Scaled to fall within a smaller, specified range
    - min-max normalization
    - z-score normalization
    - normalization by decimal scaling
  - Discretization: Concept hierarchy climbing

- **Min-max normalization:** to  $[new\_min_A, new\_max_A]$

$$v' = \frac{v - min_A}{max_A - min_A} (new\_max_A - new\_min_A) + new\_min_A$$

- Ex. Let income range \$12,000 to \$98,000 normalized to  $[0.0, 1.0]$ . Then \$73,600 is mapped to  $\frac{73,600 - 12,000}{98,000 - 12,000} (1.0 - 0) + 0 = 0.716$

- **Z-score normalization** ( $\mu$ : mean,  $\sigma$ : standard deviation):

$$v' = \frac{v - \mu_A}{\sigma_A}$$

- Ex. Let  $\mu = 54,000$ ,  $\sigma = 16,000$ . Then  $\frac{73,600 - 54,000}{16,000} = 1.225$

- **Normalization by decimal scaling**

$$v' = \frac{v}{10^j} \quad \text{Where } j \text{ is the smallest integer such that } \text{Max}(|v'|) < 1$$

- Discretization: Divide the range of a continuous attribute into intervals
  - Interval labels can then be used to replace actual data values
  - Reduce data size by discretization
  - Supervised vs. unsupervised
  - Split (top-down) vs. merge (bottom-up)
  - Discretization can be performed recursively on an attribute
  - Prepare for further analysis, e.g., classification

- Typical methods: All the methods can be applied recursively
  - Binning
    - Top-down split, unsupervised
  - Histogram analysis
    - Top-down split, unsupervised
  - Clustering analysis (unsupervised, top-down split or bottom-up merge)
  - Decision-tree analysis (supervised, top-down split)
  - Correlation (e.g.,  $\chi^2$ ) analysis (unsupervised, bottom-up merge)

- **Equal-width** (distance) partitioning
  - Divides the range into  $N$  intervals of equal size: uniform grid
  - if  $A$  and  $B$  are the lowest and highest values of the attribute, the width of intervals will be:  $W = (B - A)/N$ .
  - The most straightforward, but outliers may dominate presentation
  - Skewed data is not handled well



- **Equal-depth** (frequency) partitioning
  - Divides the range into  $N$  intervals, each containing approximately same number of samples
  - Good data scaling
  - Managing categorical attributes can be tricky

- ❑ Sorted data for price (in dollars): 4, 8, 9, 15, 21, 21, 24, 25, 26, 28, 29, 34
  
- \* Partition into equal-frequency (**equi-depth**) bins:
  - Bin 1: 4, 8, 9, 15
  - Bin 2: 21, 21, 24, 25
  - Bin 3: 26, 28, 29, 34

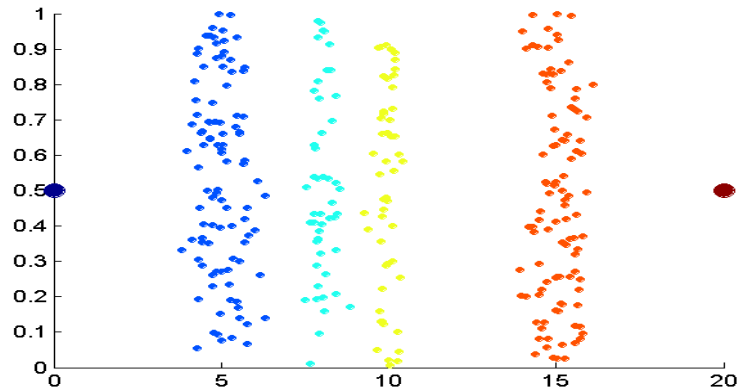
- ❑ Sorted data for price (in dollars): 4, 8, 9, 15, 21, 21, 24, 25, 26, 28, 29, 34
  
- ❑ Smoothing by **bin means**:
  - Bin 1: 9, 9, 9, 9
  - Bin 2: 23, 23, 23, 23
  - Bin 3: 29, 29, 29, 29

- ❑ Sorted data for price (in dollars): 4, 8, 9, 15, 21, 21, 24, 25, 26, 28, 29, 34

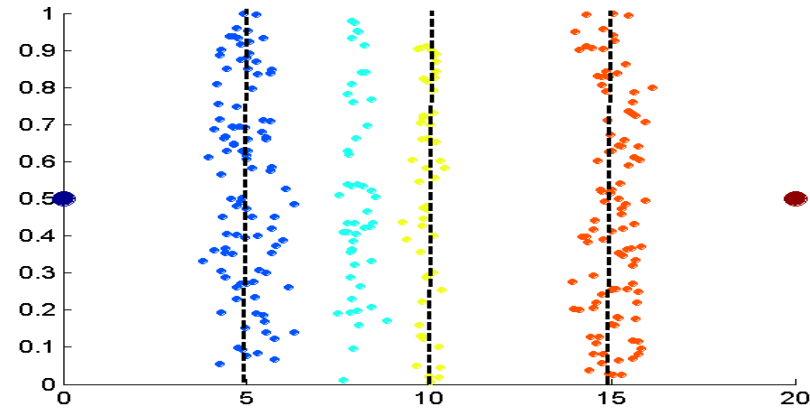
\* Smoothing by **bin boundaries**:

- Bin 1: 4, 4, 4, 15
- Bin 2: 21, 21, 25, 25
- Bin 3: 26, 26, 26, 34

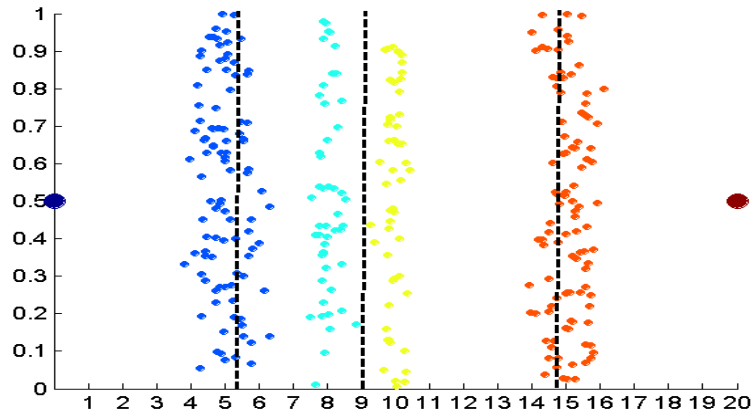
## Discretization Without Using Class Labels (Binning vs. Clustering)



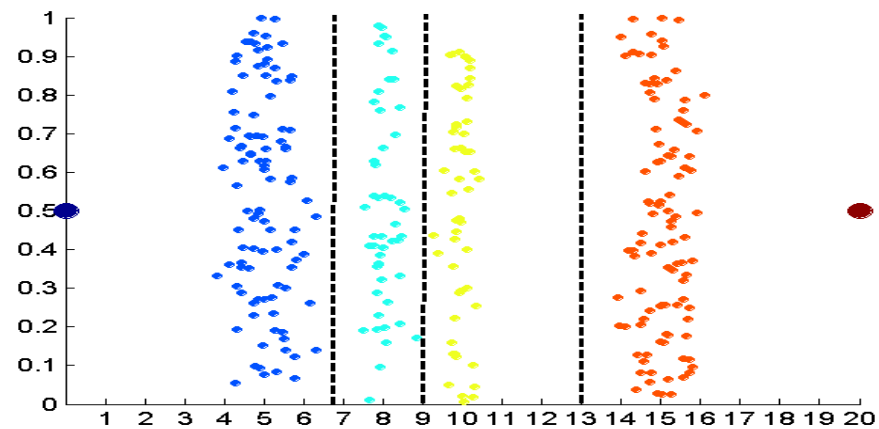
Original Data



Equal Width(binning)



Equal frequency (binning)



K-means clustering leads to  
better results

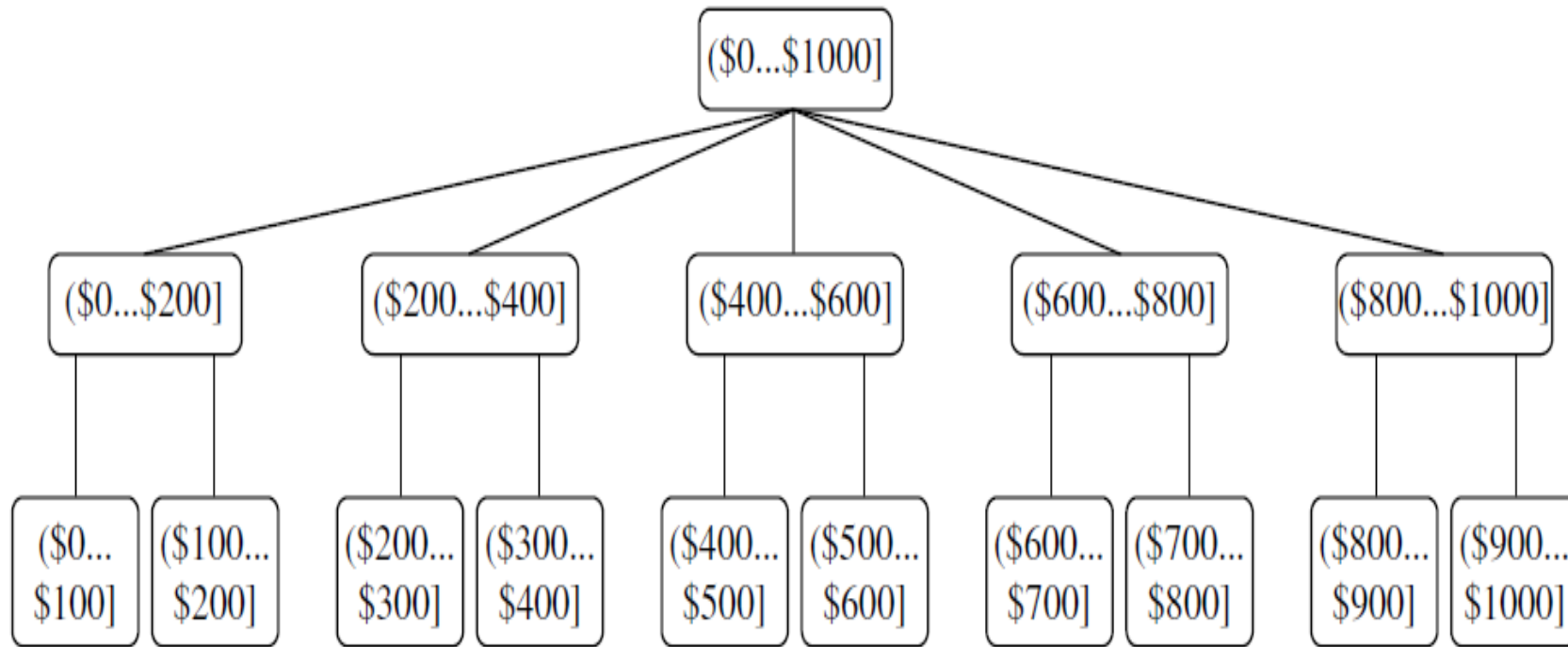
- Classification (e.g., decision tree analysis)
  - Supervised: Given class labels, e.g., cancerous vs. benign
  - Using *entropy* to determine split point (discretization point)
  - Top-down, recursive split

- Correlation analysis (e.g., Chi-merge:  $\chi^2$ -based discretization)
  - Supervised: use class information
  - Bottom-up merge: find the best neighboring intervals (those having similar distributions of classes, i.e., low  $\chi^2$  values) to merge
  - Merge performed recursively, until a predefined stopping condition

- **Concept hierarchy** organizes concepts (i.e., attribute values) hierarchically and is usually associated with each dimension in a data warehouse
- Concept hierarchies facilitate drilling and rolling in data warehouses to view data in multiple granularity



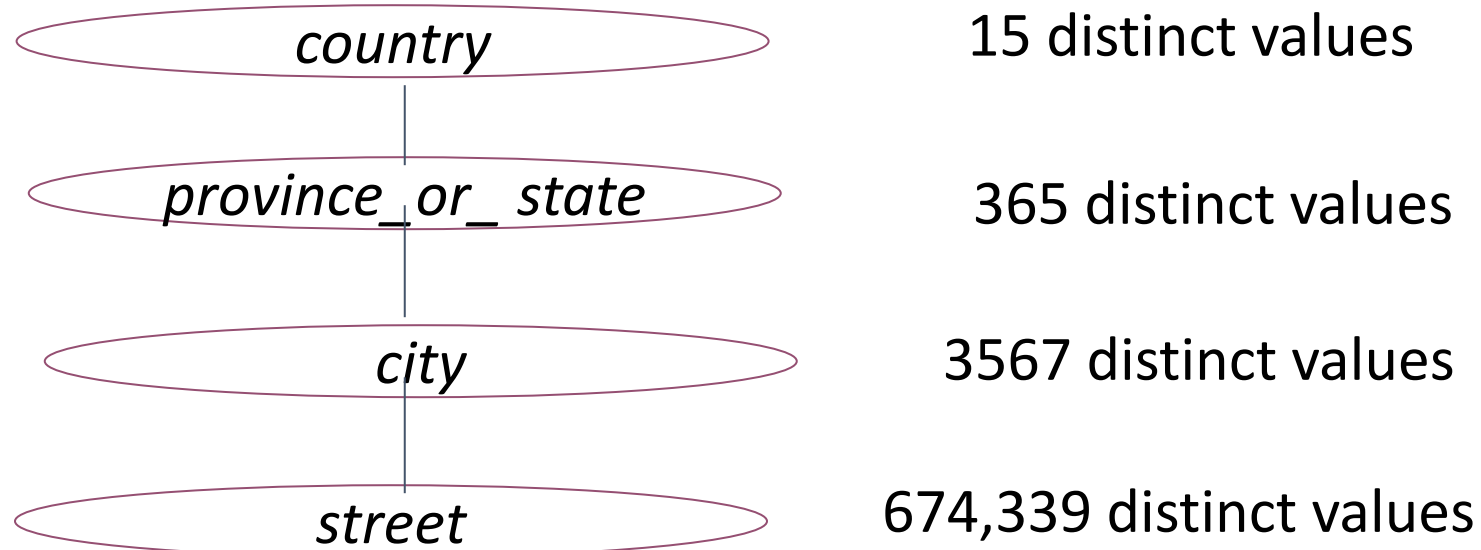
- Concept hierarchy formation: Recursively reduce the data by collecting and replacing low level concepts (such as numeric values for *age*) by higher level concepts (such as *youth*, *adult*, or *senior*)
- Concept hierarchies can be explicitly specified by domain experts and/or data warehouse designers
- Concept hierarchy can be automatically formed for both numeric and nominal data. For numeric data, use discretization methods shown.



- Specification of a partial/total ordering of attributes explicitly at the schema level by users or experts
  - *street < city < state < country*
- Specification of a hierarchy for a set of values by explicit data grouping
  - {Urbana, Champaign, Chicago} < Illinois
- Specification of only a partial set of attributes
  - E.g., only *street < city*, not others
- Automatic generation of hierarchies (or attribute levels) by the analysis of the number of distinct values
  - E.g., for a set of attributes: {*street, city, state, country*}

## Automatic Concept Hierarchy Generation

- Some hierarchies can be automatically generated based on the analysis of the number of distinct values per attribute in the data set
  - The attribute with the most distinct values is placed at the lowest level of the hierarchy
  - Exceptions, e.g., weekday, month, quarter, year



# DATA ANALYTICS

## Exercise

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- ☐ Mention and explain the different data normalization techniques.
- ☐ How classification and correlation analysis is used in data discretization.

### Text Book:

- [Data Mining: Concepts and Techniques](#) by Jiawei Han, Micheline Kamber and Jian Pei, The Morgan Kaufmann Series in Data Management Systems, 3rd Edition.



## THANK YOU

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