# Genetic Algorithms

[Read Chapter 9] [Exercises 9.1, 9.2, 9.3, 9.4]

- Evolutionary computation
- Prototypical GA
- An example: GABIL
- Genetic Programming
- Individual learning and population evolution

# Evoluationary Computation

- 1. Computational procedures patterned after biological evolution
- 2. Search procedure that probabilistically applies search operators to set of points in the search space

# Biological Evolution

### Lamarck and others:

• Species "transmute" over time

### Darwin and Wallace:

- Consistent, heritable variation among individuals in population
- Natural selection of the fittest

### Mendel and genetics:

- A mechanism for inheriting traits
- genotype → phenotype mapping

### $GA(Fitness, Fitness\_threshold, p, r, m)$

- Initialize:  $P \leftarrow p$  random hypotheses
- Evaluate: for each h in P, compute Fitness(h)
- While  $[\max_h Fitness(h)] < Fitness\_threshold$ 
  - 1. Select: Probabilistically select (1-r)p members of P to add to  $P_S$ .

$$Pr(h_i) = \frac{Fitness(h_i)}{\sum_{j=1}^{p} Fitness(h_j)}$$

- 2. Crossover: Probabilistically select  $\frac{r \cdot p}{2}$  pairs of hypotheses from P. For each pair,  $\langle h_1, h_2 \rangle$ , produce two offspring by applying the Crossover operator. Add all offspring to  $P_s$ .
- 3. Mutate: Invert a randomly selected bit in  $m \cdot p$  random members of  $P_s$
- 4. Update:  $P \leftarrow P_s$
- 5. Evaluate: for each h in P, compute Fitness(h)
- Return the hypothesis from P that has the highest fitness.

### Representing Hypotheses

### Represent

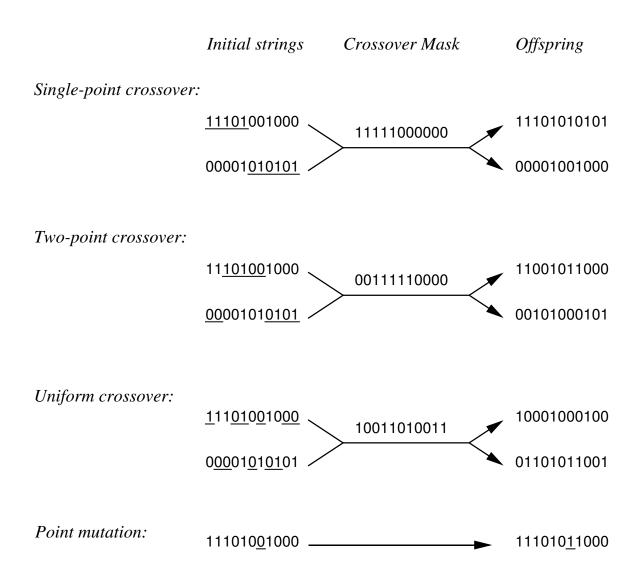
$$(Outlook = Overcast \lor Rain) \land (Wind = Strong)$$
 by

$$Outlook\ Wind$$
  $011$   $10$ 

### Represent

IF 
$$Wind = Strong$$
 THEN  $PlayTennis = yes$  by

# Operators for Genetic Algorithms



# Selecting Most Fit Hypotheses

Fitness proportionate selection:

$$Pr(h_i) = \frac{Fitness(h_i)}{\sum_{j=1}^{p} Fitness(h_j)}$$

... can lead to *crowding* 

Tournament selection:

- Pick  $h_1, h_2$  at random with uniform prob.
- With probability p, select the more fit.

### Rank selection:

- Sort all hypotheses by fitness
- Prob of selection is proportional to rank

# GABIL [DeJong et al. 1993]

Learn disjunctive set of propositional rules, competitive with C4.5

#### Fitness:

$$Fitness(h) = (correct(h))^2$$

### Representation:

IF  $a_1 = T \wedge a_2 = F$  THEN c = T; IF  $a_2 = T$  THEN c = F represented by

### Genetic operators: ???

- want variable length rule sets
- want only well-formed bitstring hypotheses

# Crossover with Variable-Length Bitstrings

Start with

$$h_2: 01 \ 11 \ 0 \ 10 \ 01 \ 0$$

- 1. choose crossover points for  $h_1$ , e.g., after bits 1, 8
- 2. now restrict points in  $h_2$  to those that produce bitstrings with well-defined semantics, e.g.,  $\langle 1, 3 \rangle$ ,  $\langle 1, 8 \rangle$ ,  $\langle 6, 8 \rangle$ .

if we choose  $\langle 1, 3 \rangle$ , result is

### GABIL Extensions

Add new genetic operators, also applied probabilistically:

- 1. AddAlternative: generalize constraint on  $a_i$  by changing a 0 to 1
- 2. DropCondition: generalize constraint on  $a_i$  by changing every 0 to 1

And, add new field to bitstring to determine whether to allow these

So now the learning strategy also evolves!

### GABIL Results

Performance of GABIL comparable to symbolic rule/tree learning methods C4.5, ID5R, AQ14

Average performance on a set of 12 synthetic problems:

- GABIL without AA and DC operators: 92.1% accuracy
- GABIL with AA and DC operators: 95.2% accuracy
- symbolic learning methods ranged from 91.2 to 96.6

### Schemas

How to characterize evolution of population in GA? Schema = string containing 0, 1, \* ("don't care")

- Typical schema: 10\*\*0\*
- Instances of above schema: 101101, 100000, ...

Characterize population by number of instances representing each possible schema

• m(s,t) = number of instances of schema s in pop at time t

### Consider Just Selection

- $\bar{f}(t)$  = average fitness of pop. at time t
- m(s,t) = instances of schema s in pop at time t
- $\hat{u}(s,t)$  = ave. fitness of instances of s at time t

Probability of selecting h in one selection step

$$\Pr(h) = \frac{f(h)}{\sum_{i=1}^{n} f(h_i)}$$
$$= \frac{f(h)}{n\overline{f}(t)}$$

Probabilty of selecting an instance of s in one step

$$\Pr(h \in s) = \sum_{h \in s \cap p_t} \frac{f(h)}{n\overline{f}(t)}$$
$$= \frac{\hat{u}(s,t)}{n\overline{f}(t)} m(s,t)$$

Expected number of instances of s after n selections

$$E[m(s,t+1)] = \frac{\hat{u}(s,t)}{\bar{f}(t)}m(s,t)$$

### Schema Theorem

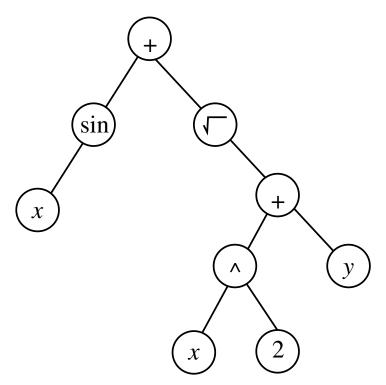
$$E[m(s,t+1)] \ge \frac{\hat{u}(s,t)}{\bar{f}(t)} m(s,t) \left(1 - p_c \frac{d(s)}{l-1}\right) (1 - p_m)^{o(s)}$$

- m(s,t) = instances of schema s in pop at time t
- $\bar{f}(t)$  = average fitness of pop. at time t
- $\hat{u}(s,t)$  = ave. fitness of instances of s at time t
- $p_c$  = probability of single point crossover operator
- $p_m$  = probability of mutation operator
- l = length of single bit strings
- o(s) number of defined (non "\*") bits in s
- d(s) = distance between leftmost, rightmost defined bits in s

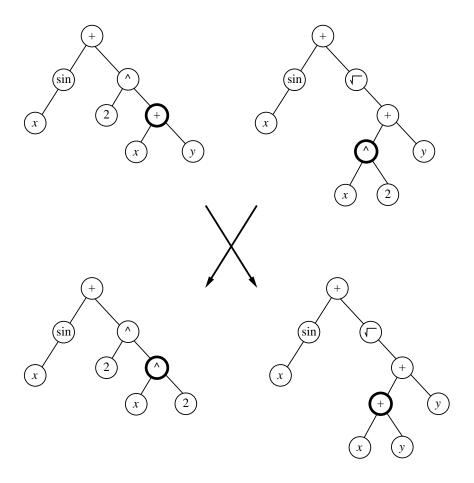
# Genetic Programming

Population of programs represented by trees

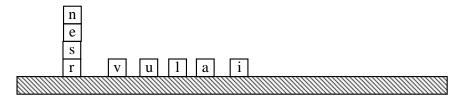
$$\sin(x) + \sqrt{x^2 + y}$$



# Crossover



### Block Problem



Goal: spell UNIVERSAL

### Terminals:

- CS ("current stack") = name of the top block on stack, or F.
- TB ("top correct block") = name of topmost correct block on stack
- NN ("next necessary") = name of the next block needed above TB in the stack

#### Primitive functions:

- (MS x): ("move to stack"), if block x is on the table, moves x to the top of the stack and returns the value T. Otherwise, does nothing and returns the value F.
- (MT x): ("move to table"), if block x is somewhere in the stack, moves the block at the top of the stack to the table and returns the value T. Otherwise, returns F.
- (EQ x y): ("equal"), returns T if x equals y, and returns F otherwise.
- (NOT x): returns T if x = F, else returns F
- (DU x y): ("do until") executes the expression x repeatedly until expression y returns the value T

# Learned Program

Trained to fit 166 test problems

Using population of 300 programs, found this after 10 generations:

(EQ (DU (MT CS)(NOT CS)) (DU (MS NN)(NOT NN)) )

### Genetic Programming

More interesting example: design electronic filter circuits

- Individuals are programs that transform begining circuit to final circuit, by adding/subtracting components and connections
- Use population of 640,000, run on 64 node parallel processor
- Discovers circuits competitive with best human designs

# GP for Classifying Images

[Teller and Veloso, 1997]

Fitness: based on coverage and accuracy

### Representation:

- Primitives include Add, Sub, Mult, Div, Not, Max, Min, Read, Write, If-Then-Else, Either, Pixel, Least, Most, Ave, Variance, Difference, Mini, Library
- Mini refers to a local subroutine that is separately co-evolved
- Library refers to a global library subroutine (evolved by selecting the most useful minis)

### Genetic operators:

- Crossover, mutation
- Create "mating pools" and use rank proportionate reproduction

# Biological Evolution

Lamark (19th century)

- Believed individual genetic makeup was altered by lifetime experience
- But current evidence contradicts this view

What is the impact of individual learning on population evolution?

### Baldwin Effect

#### Assume

- Individual learning has no direct influence on individual DNA
- But ability to learn reduces need to "hard wire" traits in DNA

#### Then

- Ability of individuals to learn will support more diverse gene pool
  - Because learning allows individuals with various "hard wired" traits to be successful
- More diverse gene pool will support faster evolution of gene pool
- $\rightarrow$  individual learning (indirectly) increases rate of evolution

### Baldwin Effect

### Plausible example:

- 1. New predator appears in environment
- 2. Individuals who can learn (to avoid it) will be selected
- 3. Increase in learning individuals will support more diverse gene pool
- 4. resulting in faster evolution
- 5. possibly resulting in new non-learned traits such as instintive fear of predator

# Computer Experiments on Baldwin Effect

[Hinton and Nowlan, 1987]

Evolve simple neural networks:

- Some network weights fixed during lifetime, others trainable
- Genetic makeup determines which are fixed, and their weight values

#### Results:

- With no individual learning, population failed to improve over time
- When individual learning allowed
  - Early generations: population contained many individuals with many trainable weights
  - Later generations: higher fitness, while number of trainable weights decreased

# Summary: Evolutionary Programming

- ullet Conduct randomized, parallel, hill-climbing search through H
- Approach learning as optimization problem (optimize fitness)
- Nice feature: evaluation of Fitness can be very indirect
  - consider learning rule set for multistep decision making
  - no issue of assigning credit/blame to indiv. steps