




Trapping Rain Water

📅 Created	@July 28, 2024
≡ Description	Array, Two Pointers, Dynamic Programming, Stack, Monotonic Stack
🏷 Tags	Arrays


Problem Statement:

💡 You are given an array of non-negative integers `height` representing the elevation map where the width of each bar is 1 . Compute how much water it can trap after raining.

💡 Example 1:

Input: `height = [0,1,0,2,1,0,1,3,2,1,2,1]`

Output: 6

Explanation: The above elevation map (black section) is represented by array `[0,1,0,2,1,0,1,3,2,1,2,1]`. In this case, 6 units of rain water (blue section) are being trapped. 

Example 2:

Input: `height = [4,2,0,3,2,5]`

Output: 9

Constraints:

- `n == height.length`
- `1 <= n <= 2 * 10^4`
- `0 <= height[i] <= 10^5`

Code (C++)

1. Brute Force

```
#include <iostream>
#include <vector>

using namespace std;

int trap(vector<int>& height) {
    int n = height.size();
    if (n == 0) {
        return 0; // 🚫 Empty array, no water trapped
    }
    int totalWater = 0;
    for (int i = 1; i < n - 1; i++) { // 🔄 Iterate through the bars
        int leftMax = 0, rightMax = 0;
        for (int j = 0; j <= i; j++) {
            leftMax = max(leftMax, height[j]); // 📊 Find the highest bar to the left
        }
        for (int j = i; j < n; j++) {
            rightMax = max(rightMax, height[j]); // 📊 Find the highest bar to the right
        }
        totalWater += min(leftMax, rightMax) - height[i];
    }
    return totalWater;
}
```

```

    }
    for (int j = i; j < n; j++) {
        rightMax = max(rightMax, height[j]); // 📈 Find the highest bar to the right
    }
    int currentWater = min(leftMax, rightMax) - height[i]; // 💧 Calculate water trapped at
    if (currentWater > 0) {
        totalWater += currentWater; // 💧 Add to the total
    }
}
return totalWater;
}

int main() {
    vector<int> height = {0, 1, 0, 2, 1, 0, 1, 3, 2, 1, 2, 1};
    cout << "Trapped Water: " << trap(height) << endl;
    return 0;
}

```

2. Two Pointers 🎯

```

#include <iostream>
#include <vector>

using namespace std;

int trap(vector<int>& height) {
    int n = height.size();
    if (n == 0) {
        return 0; // 🚫 Empty array, no water trapped
    }
    int left = 0, right = n - 1;
    int leftMax = 0, rightMax = 0;
    int totalWater = 0;
    while (left < right) { // 🔄 Move pointers until they meet
        if (height[left] < height[right]) {
            if (height[left] >= leftMax) {
                leftMax = height[left]; // 📈 Update left maximum
            } else {
                totalWater += leftMax - height[left]; // 💧 Add water trapped at the left bar
            }
            left++; // ➡ Move left pointer
        } else {
            if (height[right] >= rightMax) {
                rightMax = height[right]; // 📈 Update right maximum
            } else {
                totalWater += rightMax - height[right]; // 💧 Add water trapped at the right bar
            }
            right--; // ⬅ Move right pointer
        }
    }
    return totalWater;
}

int main() {
    vector<int> height = {0, 1, 0, 2, 1, 0, 1, 3, 2, 1, 2, 1};
    cout << "Trapped Water: " << trap(height) << endl;
}

```

```
    return 0;
}
```

3. Dynamic Programming 📈

```
#include <iostream>
#include <vector>

using namespace std;

int trap(vector<int>& height) {
    int n = height.size();
    if (n == 0) {
        return 0; // 🚫 Empty array, no water trapped
    }
    vector<int> leftMax(n, 0); // 📈 Left maximums up to each index
    vector<int> rightMax(n, 0); // 📈 Right maximums up to each index
    leftMax[0] = height[0];
    rightMax[n - 1] = height[n - 1];
    for (int i = 1; i < n; i++) {
        leftMax[i] = max(leftMax[i - 1], height[i]); // 📈 Calculate left maximums
    }
    for (int i = n - 2; i >= 0; i--) {
        rightMax[i] = max(rightMax[i + 1], height[i]); // 📈 Calculate right maximums
    }
    int totalWater = 0;
    for (int i = 1; i < n - 1; i++) {
        int currentWater = min(leftMax[i], rightMax[i]) - height[i]; // 💧 Calculate water trapped
        if (currentWater > 0) {
            totalWater += currentWater; // 💧 Add to the total
        }
    }
    return totalWater;
}

int main() {
    vector<int> height = {0, 1, 0, 2, 1, 0, 1, 3, 2, 1, 2, 1};
    cout << "Trapped Water: " << trap(height) << endl;
    return 0;
}
```

Algorithm 😊:

Dry runs for each approach 🎉:

Input `height = [0, 1, 0, 2, 1, 0, 1, 3, 2, 1, 2, 1]` :






1. Brute Force




1. Initialization

- `totalWater = 0` 




2. Iteration 1:

- `i = 1` , `height[i] = 1`
- `leftMax = 1` , `rightMax = 3` 
- `currentWater = 0` 
- `totalWater = 0` 




3. Iteration 2:

- `i = 2` , `height[i] = 0`
- `leftMax = 1` , `rightMax = 3` 
- `currentWater = 1` 
- `totalWater = 1` 




4. Iteration 3:

- `i = 3` , `height[i] = 2`
- `leftMax = 2` , `rightMax = 3` 
- `currentWater = 1` 
- `totalWater = 2` 




5. Iteration 4:

- `i = 4` , `height[i] = 1`
- `leftMax = 2` , `rightMax = 3` 
- `currentWater = 1` 
- `totalWater = 3` 

6. Iteration 5:

- `i = 5` , `height[i] = 0`
- `leftMax = 2` , `rightMax = 3` 
- `currentWater = 2` 
- `totalWater = 5` 




7. Iteration 6:

- `i = 6` , `height[i] = 1`
- `leftMax = 2` , `rightMax = 3` 
- `currentWater = 1` 
- `totalWater = 6` 



Final Output: `totalWater = 6` 

2. Two Pointers


1. Initialization

- `left = 0` , `right = 11` 
- `leftMax = 0` , `rightMax = 1` 
- `totalWater = 0` 



2. Iteration 1:

- `height[left] = 0` , `height[right] = 1`
- `leftMax = 1`  (Update leftMax)
- `left = 1` 



3. Iteration 2:

- `height[left] = 1` , `height[right] = 1`
- `right = 10` 



4. Iteration 3:

- `height[left] = 1` , `height[right] = 2`
- `rightMax = 2`  (Update rightMax)
- `right = 9` 



5. Iteration 4:

- `height[left] = 1` , `height[right] = 1`
- `totalWater = 1`  (Add water trapped at left)
- `left = 2` 



6. Iteration 5:

- `height[left] = 0` , `height[right] = 1`
- `totalWater = 2`  (Add water trapped at left)
- `left = 3` 



7. Iteration 6:

- `height[left] = 2` , `height[right] = 1`
- `leftMax = 2`  (Update leftMax)
- `left = 4` 



8. Iteration 7:

- `height[left] = 1` , `height[right] = 1`
- `totalWater = 3`  (Add water trapped at left)
- `left = 5` 


9. Iteration 8:

- `height[left] = 0` , `height[right] = 1`
- `totalWater = 5`  (Add water trapped at left)
- `left = 6` 


10. Iteration 9:

- `height[left] = 1` , `height[right] = 1`
- `leftMax = 3`  (Update leftMax)
- `left = 7` 

1. Iteration 10:

- `height[left] = 3` , `height[right] = 1`
- `left = 8` 

1. Iteration 11:

- `height[left] = 2` , `height[right] = 1`
- `totalWater = 6`  (Add water trapped at left)

- `left = 9` ➡



1. Iteration 12:

- `height[left] = 1`, `height[right] = 1`
- `left = 10` ➡

Final Output: `totalWater = 6` 🎉

3. Dynamic Programming

1. Initialization

- `leftMax = [0, 0, 1, 1, 2, 2, 2, 2, 3, 3, 3, 3]` 
- `rightMax = [3, 3, 3, 3, 3, 3, 3, 2, 2, 2, 1, 0]` 
- `totalWater = 0` 💧

2. Calculate Water Trapped 💧:

- For each `i` from `1` to `len(height) - 1`:
 - `i = 1`, `currentWater = min(leftMax[1], rightMax[1]) - height[1] = 0 - 1 = -1` (Since it's negative, no water is trapped here.)
 - `i = 2`, `currentWater = min(leftMax[2], rightMax[2]) - height[2] = 1 - 0 = 1`, `totalWater = 1`
 - `i = 3`, `currentWater = min(leftMax[3], rightMax[3]) - height[3] = 1 - 2 = -1` (No water trapped.)
 - `i = 4`, `currentWater = min(leftMax[4], rightMax[4]) - height[4] = 2 - 1 = 1`, `totalWater = 2`
 - `i = 5`, `currentWater = min(leftMax[5], rightMax[5]) - height[5] = 2 - 1 = 1`, `totalWater = 3`
 - `i = 6`, `currentWater = min(leftMax[6], rightMax[6]) - height[6] = 2 - 0 = 2`, `totalWater = 5`
 - `i = 7`, `currentWater = min(leftMax[7], rightMax[7]) - height[7] = 2 - 1 = 1`, `totalWater = 6`
 - `i = 8`, `currentWater = min(leftMax[8], rightMax[8]) - height[8] = 2 - 3 = -1` (No water trapped.)
 - `i = 9`, `currentWater = min(leftMax[9], rightMax[9]) - height[9] = 2 - 2 = 0` (No water trapped.)
 - `i = 10`, `currentWater = min(leftMax[10], rightMax[10]) - height[10] = 2 - 1 = 1`, `totalWater = 7`
 - `i = 11`, `currentWater = min(leftMax[11], rightMax[11]) - height[11] = 2 - 2 = 0` (No water trapped.)

Final Output: `totalWater = 7` 🎉

Java

```
import java.util.Arrays;

public class TrappingRainWater {

    // 1. Brute Force 🛠️
    public static int trap1(int[] height) {
        int n = height.length;
        if (n == 0) {
            return 0; // 🚫 Empty array, no water trapped
        }
        int totalWater = 0;
        for (int i = 1; i < n - 1; i++) { // 🔄 Iterate through the bars
            int leftMax = 0, rightMax = 0;
            for (int j = 0; j <= i; j++) {
```

```

        leftMax = Math.max(leftMax, height[j]); // 📈 Find the highest bar to the left
    }
    for (int j = i; j < n; j++) {
        rightMax = Math.max(rightMax, height[j]); // 📈 Find the highest bar to the right
    }
    int currentWater = Math.min(leftMax, rightMax) - height[i]; // 💧 Calculate water trapped at index i
    if (currentWater > 0) {
        totalWater += currentWater; // 💧 Add to the total
    }
}
return totalWater;
}

// 2. Two Pointers 🎯
public static int trap2(int[] height) {
    int n = height.length;
    if (n == 0) {
        return 0; // 🚫 Empty array, no water trapped
    }
    int left = 0, right = n - 1;
    int leftMax = 0, rightMax = 0;
    int totalWater = 0;
    while (left < right) { // 🔄 Move pointers until they meet
        if (height[left] < height[right]) {
            if (height[left] >= leftMax) {
                leftMax = height[left]; // 📈 Update left maximum
            } else {
                totalWater += leftMax - height[left]; // 💧 Add water trapped at the left bar
            }
            left++; // ➡ Move left pointer
        } else {
            if (height[right] >= rightMax) {
                rightMax = height[right]; // 📈 Update right maximum
            } else {
                totalWater += rightMax - height[right]; // 💧 Add water trapped at the right bar
            }
            right--; // ⬅ Move right pointer
        }
    }
    return totalWater;
}

// 3. Dynamic Programming 📈
public static int trap3(int[] height) {
    int n = height.length;
    if (n == 0) {
        return 0; // 🚫 Empty array, no water trapped
    }
    int[] leftMax = new int[n]; // 📈 Left maximums up to each index
    int[] rightMax = new int[n]; // 📈 Right maximums up to each index
    leftMax[0] = height[0];
    rightMax[n - 1] = height[n - 1];
    for (int i = 1; i < n; i++) {
        leftMax[i] = Math.max(leftMax[i - 1], height[i]); // 📈 Calculate left maximums
    }
    for (int i = n - 2; i >= 0; i--) {
        rightMax[i] = Math.max(rightMax[i + 1], height[i]); // 📈 Calculate right maximums
    }
}

```

```

    int totalWater = 0;
    for (int i = 1; i < n - 1; i++) {
        int currentWater = Math.min(leftMax[i], rightMax[i]) - height[i]; // 💧 Calculate water trapped at current index
        if (currentWater > 0) {
            totalWater += currentWater; // 💧 Add to the total
        }
    }
    return totalWater;
}

public static void main(String[] args) {
    int[] height = {0, 1, 0, 2, 1, 0, 1, 3, 2, 1, 2, 1};
    System.out.println("Approach 1: " + trap1(height));
    System.out.println("Approach 2: " + trap2(height));
    System.out.println("Approach 3: " + trap3(height));
}
}

```

Python 🐍

```

def trap1(height):
    """
    Approach 1: Brute Force 🛠️
    """
    n = len(height)
    if n == 0:
        return 0 # 🚫 Empty array, no water trapped
    totalWater = 0
    for i in range(1, n - 1): # 🔄 Iterate through the bars
        leftMax = 0
        rightMax = 0
        for j in range(i + 1):
            leftMax = max(leftMax, height[j]) # 📈 Find the highest bar to the left
        for j in range(i, n):
            rightMax = max(rightMax, height[j]) # 📈 Find the highest bar to the right
        currentWater = min(leftMax, rightMax) - height[i] # 💧 Calculate water trapped at current index
        if currentWater > 0:
            totalWater += currentWater # 💧 Add to the total
    return totalWater

def trap2(height):
    """
    Approach 2: Two Pointers 🎯
    """
    n = len(height)
    if n == 0:
        return 0 # 🚫 Empty array, no water trapped
    left = 0
    right = n - 1
    leftMax = 0
    rightMax = 0
    totalWater = 0
    while left < right: # 🔄 Move pointers until they meet
        if height[left] < height[right]:
            if height[left] >= leftMax:
                leftMax = height[left] # 📈 Update left maximum
            else:
                currentWater = leftMax - height[left]
                totalWater += currentWater
            left += 1
        else:
            if height[right] >= rightMax:
                rightMax = height[right] # 📈 Update right maximum
            else:
                currentWater = rightMax - height[right]
                totalWater += currentWater
            right -= 1
    return totalWater

```



```

        totalWater += leftMax - height[left] # 💧 Add water trapped at the left bar
        left += 1 # ➡ Move left pointer
    else:
        if height[right] >= rightMax:
            rightMax = height[right] # 📈 Update right maximum
        else:
            totalWater += rightMax - height[right] # 💧 Add water trapped at the right bar
            right -= 1 # ⬅ Move right pointer
    return totalWater

def trap3(height):
    """
    Approach 3: Dynamic Programming 📈
    """
    n = len(height)
    if n == 0:
        return 0 # 🚫 Empty array, no water trapped
    leftMax = [0] * n # 📈 Left maximums up to each index
    rightMax = [0] * n # 📈 Right maximums up to each index
    leftMax[0] = height[0]
    rightMax[n - 1] = height[n - 1]
    for i in range(1, n):
        leftMax[i] = max(leftMax[i - 1], height[i]) # 📈 Calculate left maximums
    for i in range(n - 2, -1, -1):
        rightMax[i] = max(rightMax[i + 1], height[i]) # 📈 Calculate right maximums
    totalWater = 0
    for i in range(1, n - 1):
        currentWater = min(leftMax[i], rightMax[i]) - height[i] # 💧 Calculate water trapped at i
        if currentWater > 0:
            totalWater += currentWater # 💧 Add to the total
    return totalWater

if __name__ == "__main__":
    height = [0, 1, 0, 2, 1, 0, 1, 3, 2, 1, 2, 1]
    print("Approach 1:", trap1(height))
    print("Approach 2:", trap2(height))
    print("Approach 3:", trap3(height))

```