

## LAB 6

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Section -A

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### **1.Nodes in binary tree**

```
#include<stdio.h>

#include <stdlib.h>

int opcount=0;

typedef struct node *Nodeptr;

struct node{

int data;

Nodeptr rchild;

Nodeptr lchild;

}NODE;


int number_of_nodes(Nodeptr root){

    opcount++;

    if(root)

        return 1+ number_of_nodes(root->lchild)+number_of_nodes(root->rchild);

    return 0;

}

Nodeptr getnode(){

    return ((Nodeptr)malloc (sizeof(NODE)));

}
```

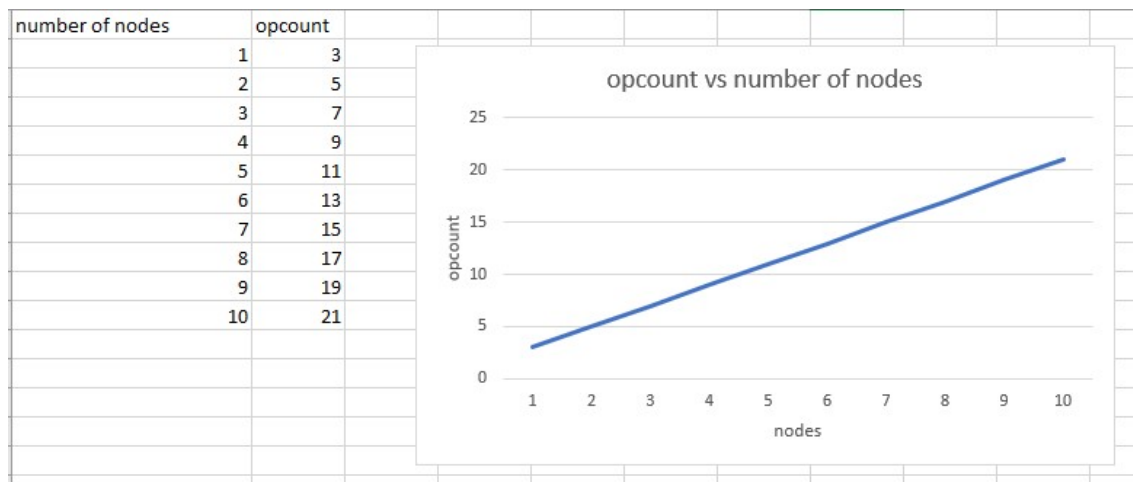
```
Nodeptr CreateBinaryTree(int item){  
    int x;  
    if (item!=-1) { //until input is not equal to -1
```

```
  
        Nodeptr temp=getnode() ;  
        temp->data = item;  
        printf("Enter the lchild of %d :",item);  
        scanf("%d",&x);  
        temp->lchild = CreateBinaryTree(x);  
        printf("Enter the rchild of %d :",item);  
        scanf("%d",&x);  
        temp->rchild = CreateBinaryTree(x);  
        return temp;  
    }  
    return NULL;  
}
```

```
  
int main()  
{  
    Nodeptr root = NULL;  
    int item;  
    printf("Creating the tree : \n");  
    printf("Enter the root :");  
    scanf("%d",&item);  
    root=CreateBinaryTree(item);  
  
    int nodes=number_of_nodes(root);  
  
    printf("number of nodes=%d",nodes);  
    printf("number of operations=%d",opcount);
```

}

```
PS C:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6> cd "C:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6\" ; if ($?) { gcc binarytree.c -o binarytree } ; if ($?) { .\binarytree }  
Creating the tree :  
Enter the root :2  
Enter the lchild of 2 :1  
Enter the lchild of 1 :-1  
Enter the rchild of 1 :-1  
Enter the rchild of 2 :-1  
number of nodes=2number of operations=5
```



## TIME COMPLEXITY ANALYSIS

The algorithm visits every nodes including nodes pointing to NULL values thereby for n nodes the algorithm works for  $2n+1$  iterations(opcount) because n nodes with have  $n+1$  null nodes

Thereby time complexity =  $O(2n+1)=O(n)$

## 2.quick sort

```
#include<stdio.h>

#include <stdlib.h>

int opcount=0;

void swap(int arr[],int i,int j){
    int temp;
    temp=arr[i];
    arr[i]=arr[j];
    arr[j]=temp;
}

int partition(int arr[],int start,int end){
    int pivot=arr[end];
    int i=start;
    for(int j=start;j<end;++j){
        opcount++;
        if(arr[j]<=pivot){
            swap(arr,i,j);
            i++;
        }
    }
    swap(arr,i,end);
    return i;
}

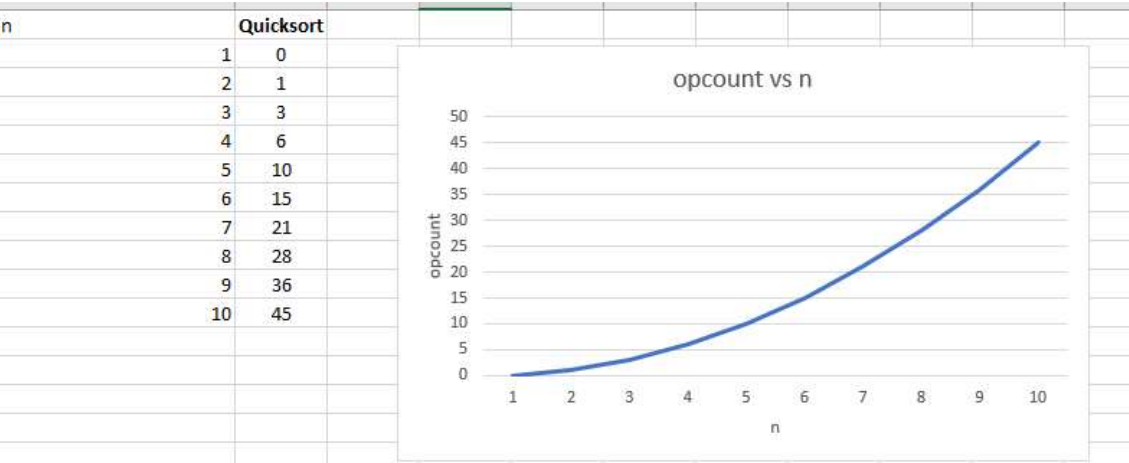
void quicksort(int arr[],int start ,int end){
    if(start<end){
        int p=partition(arr,start,end);
        quicksort(arr,start,p-1);
```

```
    quicksort(arr,p+1,end);  
  }  
}
```

```
void main(){  
    //int arr[5]={1,2,3,4,-1};  
    int n;  
    printf("enter the number of elements");  
    scanf("%d",&n);  
    int arr[n];  
    for (int i = 0; i < n; ++i)  
        scanf(" %d", &arr[i]);
```

```
  
    quicksort(arr,0,n-1);  
    for(int i=0;i<n;++i)  
        printf("%d ",arr[i]);  
    printf("opcount=%d",opcount);  
  
}
```

```
PS C:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6> cd "c:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6\" ; if ($?) { gcc quicksort.c -o quicksort } ; if ($?) { .\quicksort }  
enter the number of elements5  
7 6 5 4 3  
3 4 5 6 7 opcount=10  
PS C:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6> 
```



## Analysis of Quicksort

$$T(n) = T(k) + T(n-k-1) + f(n)$$

where  $k$  number of elements smaller than pivot

### Worst Case

Occurs when we pick the greatest or smallest as pivot

$$\begin{aligned} T(n) &= T(0) + T(n-1) + f(n) \\ &= T(n-1) + f(n) \\ &\approx \frac{n(n+1)}{2} \approx O(n^2) \end{aligned}$$

### Best Case

We use partition takes middle element

$$\begin{aligned} T(n) &= 2T(n/2) + f(n) \\ &= n \log n \text{ (Master's Theorem)} \end{aligned}$$

### Average Case

We take the average case to be  $O(n \log n)$

### 3.mergesort

```
#include<stdlib.h>
```

```
#include<stdio.h>
```

```
int opcount=0;
```

```
void merge(int arr[], int l, int m, int r)
```

```
{
```

```
    int i, j, k;
```

```
    int n1 = m - l + 1;
```

```
    int n2 = r - m;
```

```
    /* create temp arrays */
```

```
    int L[n1], R[n2];
```

```
    /* Copy data to temp arrays L[] and R[] */
```

```
    for (i = 0; i < n1; i++)
```

```
        L[i] = arr[l + i];
```

```
    for (j = 0; j < n2; j++)
```

```
        R[j] = arr[m + 1 + j];
```

```
    /* Merge the temp arrays back into arr[l..r]*/
```

```
    i = 0; // Initial index of first subarray
```

```
    j = 0; // Initial index of second subarray
```

```
    k = l; // Initial index of merged subarray
```

```
    while (i < n1 && j < n2)
```

```
    {    opcount++;
```

```
        if (L[i] <= R[j])
```

```
        {
```

```
            arr[k] = L[i];
```

```
            i++;
```

```
        }
```



```

        else
        {
            arr[k] = R[j];

            j++;
        }

        k++;
    }

    /* Copy the remaining elements of L[], if there
    are any */
    while (i < n1)

    { opcount++;
        arr[k] = L[i];

        i++;
        k++;
    }

    /* Copy the remaining elements of R[], if there
    are any */
    while (j < n2)
    { opcount++;
        arr[k] = R[j];

        j++;
        k++;
    }
}

/* l is for left index and r is right index of the
sub-array of arr to be sorted */
void mergeSort(int arr[], int l, int r)

```

```

{
    if (l < r)
    {
        // Same as (l+r)/2, but avoids overflow for
        // large l and h
        int m = l+(r-l)/2;

        // Sort first and second halves
        mergeSort(arr, l, m);
        mergeSort(arr, m+1, r);

        merge(arr, l, m, r);
    }
}

```

```

/* UTILITY FUNCTIONS */
/* Function to print an array */
void printArray(int A[], int size)
{
    int i;
    for (i=0; i < size; i++)
        printf("%d ", A[i]);
    printf("\n");
}

```

```

/* Driver program to test above functions */
void main(){
    //int arr[5]={1,2,3,4,-1};
    int n;
    printf("enter the number of elements");
    scanf("%d",&n);
}

```

```

int arr[n];

for (int i = 0; i < n; ++i)

    scanf("%d", &arr[i]);


mergeSort(arr,0,n-1);

for(int i=0;i<n;++i)

    printf("%d",arr[i]);

printf("opcount=%d",opcount);

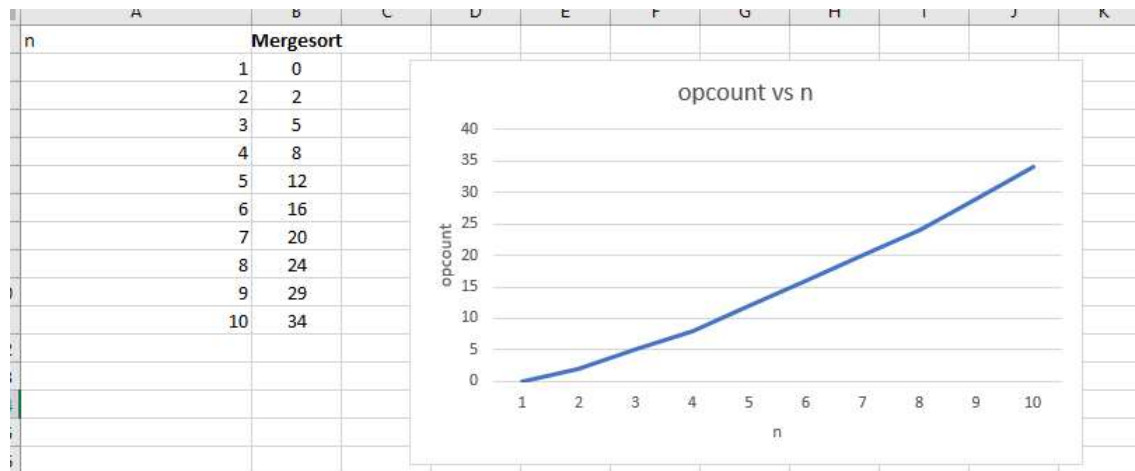
}

```

```

PS C:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6> cd "c:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6\" ; if ($?) { gcc merge.c -o
merge } ; if ($?) { .\merge }
enter the number of elements5
6 5 4 3 2
23456opcount=12
PS C:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6> cd "c:\Users\aniket\Desktop\desktop\sem4\daa\lab\daa\week6\" ; if ($?) { gcc tempCodeRu
nnerFile.c -o tempCodeRunnerFile } ; if ($?) { .\tempCodeRunnerFile }
enter the number of elements4
6 5 4 3
3456opcount=8

```



## Analysis of Merge Sort

We always divide the array in two halves so we get the best, average, worst case time complexity

$$\begin{aligned} T(n) &= 2T(n/2) + f(n) \\ &= n \log n \quad (\text{Master's theorem}) \end{aligned}$$