Identifying Gradient Fields and Exact Differentials

1. Determine whether each of the vector fields below is conservative.

a)
$$\mathbf{F} = \langle xe^x + y, x \rangle$$

b)
$$\mathbf{F} = \langle xe^x + y, x + 2 \rangle$$

c)
$$\mathbf{F} = \langle xe^x + y + x, x \rangle$$

- **2.** Show $(xe^x + y) dx + x dy$ is exact.
- $\bf 3$. Compute the two dimensional curl of $\bf F$ for each of the vector fields below.

a)
$$\mathbf{F} = \langle x, xe^x + y \rangle$$

b)
$$\mathbf{F} = \mathbf{i} + \mathbf{j}$$

c)
$$\mathbf{F} = \langle xy^2, x^2y \rangle$$

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