Student Information

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Answer 1

a) $G_1 = (V, \Sigma, R, S) \text{ where}$ $V = \{S, a, b\} ,$ $\Sigma = \{a, b\} ,$ S is the start symbol , $R = \{S \to SaSbSbS|SbSaSbS|SbSaSs|\epsilon\}$ such that $L(G_1) = L_1$.

b)

$$G_2 = (V, \Sigma, R, S)$$
 where

$$\begin{split} V &= \{S, a, b\} \ , \\ \Sigma &= \{a, b\} \ , \\ S \text{ is the start symbol } , \\ R &= \{S \rightarrow aSb|aaSb|\epsilon\} \end{split}$$

such that $L(G_2) = L_2$.

 $\mathbf{c})$

Let's introduce a Nondeterministic Pushdown Automaton M such that $L(M) = L_1$

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\begin{split} M &= (K, \Sigma, V, \Delta, s, F) \text{ where }, \\ K &= \{p, q\} \\ \Sigma &= \{a, b\} \\ V &= \{a, b, S\} \\ s &= p \\ F &= \{q\} \end{split} \Delta = \quad \{ & ((p, \epsilon, \epsilon), (q, S)), \\ & ((q, \epsilon, S), (q, SaSbSbS)), \\ & ((q, \epsilon, S), (q, SbSaSbS)), \\ & ((q, \epsilon, S), (q, SbSbSaS)), \\ & ((q, \epsilon, S), (q, \epsilon)), \\ & ((q, a, a), (q, \epsilon)), \\ & ((q, b, b), (q, \epsilon)) \\ & \} \end{split}
```

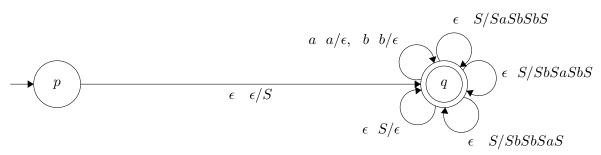


Figure: State Diagram of M

Be careful that $(a - a/\epsilon)$ and $(b - b/\epsilon)$ has been shown on the same loop for simplicity!

d)

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\begin{split} G_3 &= (V, \Sigma, R, S) \text{ where} \\ V &= \{S, S_1, S_2, a, b\} \ , \\ \Sigma &= \{a, b\} \ , \\ S \text{ is the start symbol }, \\ R &= \{ \\ S &\rightarrow S_1 | S_2, \\ S_1 &\rightarrow S_1 a S_1 b S_1 b S_1 | S_1 b S_1 a S_1 b S_1 | S_1 b S_1 a S_1 | \epsilon, \\ S_2 &\rightarrow a S_2 b | a a S_2 b | \epsilon \\ \} \\ \text{such that } L(G_3) &= L_3 = L_1 \cup L_2 \ . \end{split}
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Answer 2

a)

Consider the string $w = 00111 \in L(G_1)$:

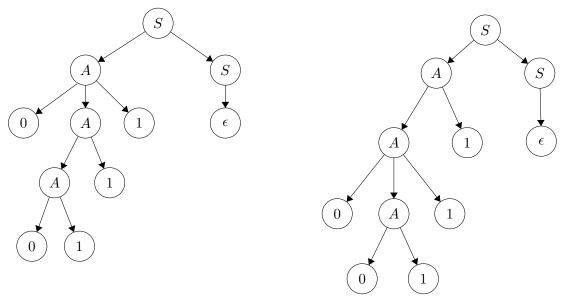


Figure 1 - 2: Two different parse trees for W

Since G_1 has two distinct parse trees, which are drawn above, for the string w = 00111. The grammar G_1 is ambiguous.

b)

Let's introduce an unambiguous grammar G_2 such that $L(G_1) = L(G_2)$:

```
G_2 = (V, \Sigma, R, S) \text{ where}
V = \{S, A, B, 0, 1\},
\Sigma = \{0, 1\},
S \text{ is the start symbol },
R = \{
S \to AS | \epsilon,
A \to A1 | B,
B \to 0B1 | 01
\}
```

 $\mathbf{c})$

Left-most derivation :

$$S \implies AS \implies A1S \implies B1S \implies 0B11S \implies 00111S \implies 00111$$

Corrsponding parse tree:

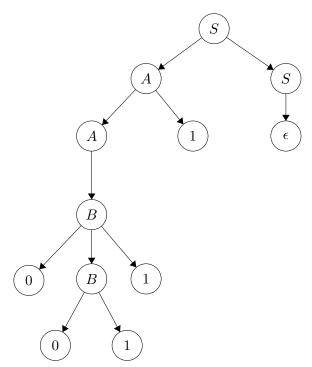


Figure: Corresponding parse tree