# Report 1 (Week 1)

# 1. Introduction

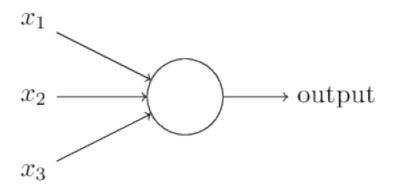
A brief introduction about neural networks. What does it do, what place it has in machine learning studies etc.

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### 1.1 Perceptrons

Basic things about perceptrons. This is an actual introduction to neural networks. It has a input and output scheme like this.

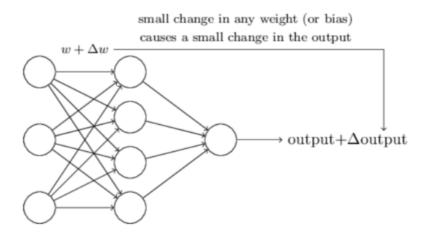


It has weights for the importance of the  $X_j$ . For example, if  $X_2$  has more importance than  $X_3$  or  $X_1$ , it has bigger weight and it directly affects the output.

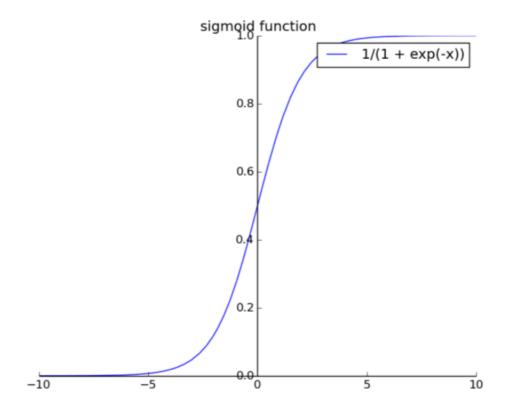
output = 
$$\begin{cases} 0 & \text{if } \sum_{j} w_{j} x_{j} \leq \text{ threshold} \\ 1 & \text{if } \sum_{j} w_{j} x_{j} > \text{ threshold} \end{cases}$$

## 1.2 Sigmoid neurons

This scheme explains the effects of changing weights to the output.

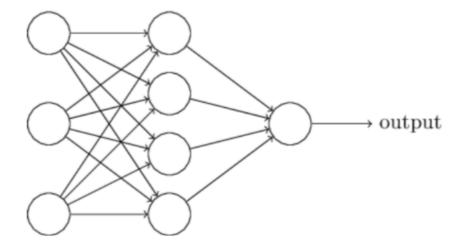


But this is not a healthy example with perceptrons. Little weight change can cause the output from 0 to 1 or from 1 to 0. And this is not a good thing to happen us. Therefore we are introduced with a new neuron that is called sigmoid neuron. It can have a value of any number in the range of from 0 to 1. Not just 0 or 1.

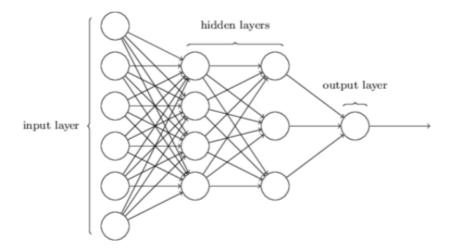


$$\frac{1}{1+exp(-\sum_j w_j x_j - b)}$$

## 1.3 The architecture of neural networks



This is a simple architecture of neural networks.



More complicated one with hidden layers etc.

## 1.4 Gradient Descent Algorithm

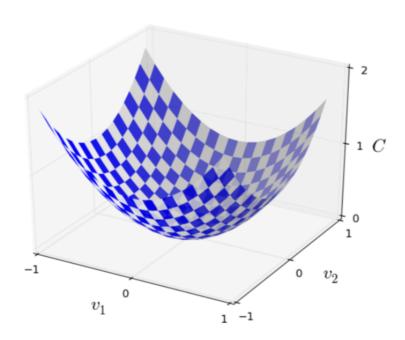
Gradient descent is a first-order optimization algorithm. To find a local minimum of a function using gradient descent, one takes steps proportional to the negative of the gradient (or of the approximate gradient) of the function at the current point.

Hypothesis: 
$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

Parameters: 
$$\theta_0, \theta_1$$

Cost Function: 
$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^{m} \left( h_{\theta}(x^{(i)}) - y^{(i)} \right)^2$$

Goal: 
$$\min_{\theta_0, \theta_1} \text{minimize } J(\theta_0, \theta_1)$$



Sample cost function with two variables.

#### 1.5 Implementing our network to classify digits

Get the codes from https://github.com/mnielsen/neural-networks-and-deep-learning It has an output like this:

```
Epoch 0: 9129 / 10000

Epoch 1: 9295 / 10000

Epoch 2: 9348 / 10000

...

Epoch 27: 9528 / 10000

Epoch 28: 9542 / 10000

Epoch 29: 9534 / 10000
```

Codes will be added.