

# Data Science for Smart Manufacturing

IIT Madras || University of Texas || GIAN

## Surface Characteristic Prediction Of Grinding Process

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# Need of Data Science

- In order to know the outcome of the process before undergoing it we need to take help of past data of process.
- By analyzing the data we can put forward model equation which governs the process.
- Parameters affecting the response can be controlled to get desired output.
- This can be achieved by Data Science...

# What is Data Science...?

- Scientific process of converting raw data into knowledge to support decision making.
- Science which deals with collecting, processing and analyzing the data to draw some insights which helps in decision making.
- Applications:

| Manufacturing | Defense  |
|---------------|----------|
| Healthcare    | Banking  |
| Supply chain  | Sports   |
| E- commerce   | Airlines |
| Tourism       | Retail   |

- Goal of data science is to make business more competitive and improve it.
- Data analytics approaches provide an automated and cost-effective way to
  - assure quality in manufactured products
  - Manage nation's engineering and information assets

# Classification

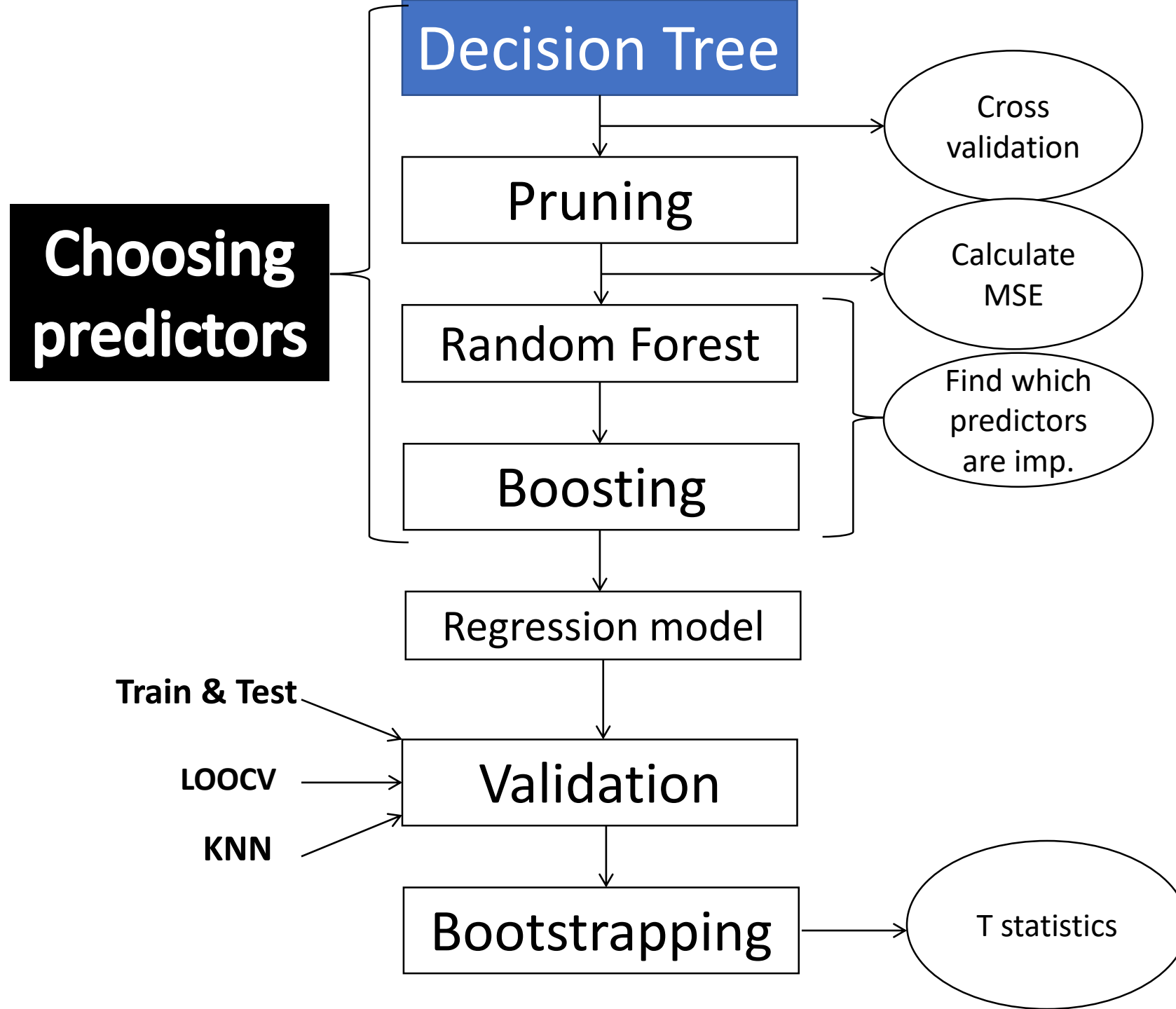
- Descriptive Analytics- It describes the data and gives information about the past.
- Predictive Analytics- Next step to descriptive analytics. It predicts the future outcome from the past data.
- Prescriptive analytics- Next step of predictive analytics. It involves the decision making and deciding the course of action.

# Surface Roughness Prediction in Grinding process

- We have a data for various speed and feed
- Accelerometers, voltage and current sensors are mounted to check vibration and power parameters.
- Total 38 workpiece are grinded using various combination of controllable parameters in four stages.
- Wheel speed= 25, 35, 45 rpm
- Work speed= 100,200,300 rpm
- Feed rate=0.01, 0.05, 0.2, 0.4, 1.2 mm/rev
- Surface profilometer measures the surface roughness in  $\mu\text{m}$ .
- From power and accelerometer sensors various parameters are extracted

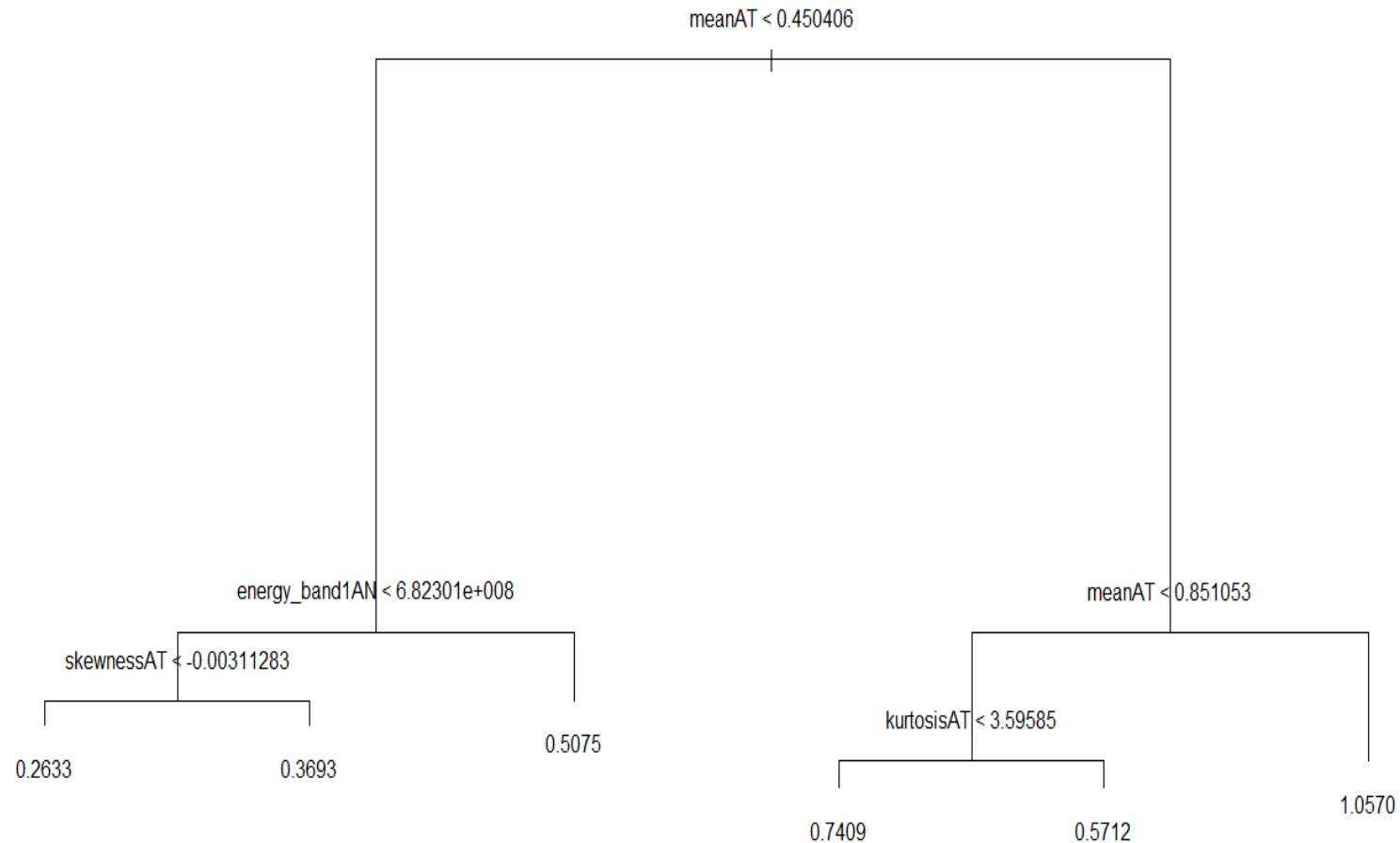
# Objective

- To design a Regression model by analyzing the collected data set which can predict the surface roughness (Ra Value) of a randomly chosen work piece.
- Dependent variable: Roughness(Ra)
- Independent variables are 24
- [Data](#)
- [Data visualization](#)



# Choosing the Right ones

- An analysis was done to judge the better prediction terms among all the given parameters using Decision Trees.





# Summary of the plot

Regression tree:

```
tree(formula = Ra ~ ., data = Final1, subset = train)
```

Variables actually used in tree construction:

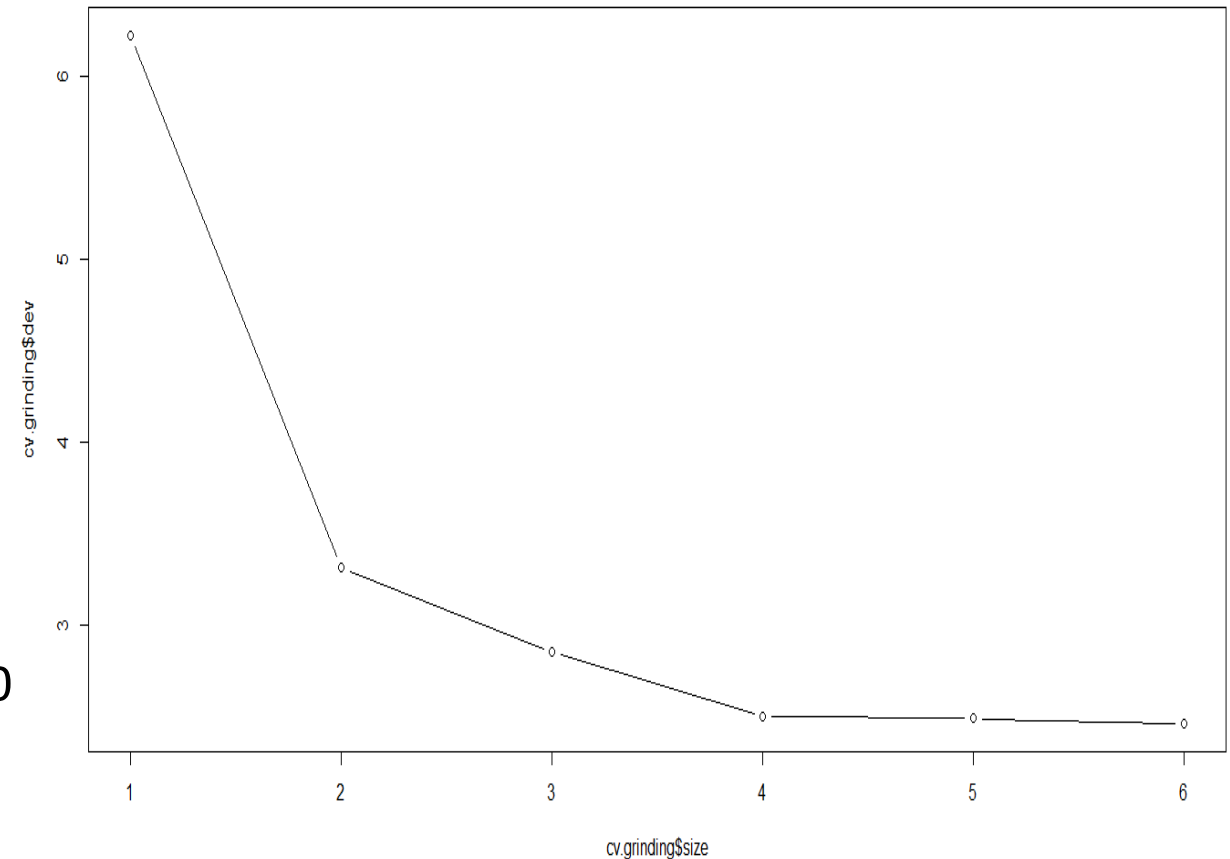
```
[1] "meanAT"      "energy_band1AN" "skewnessAT"  
"kurtosisAT"
```

Number of terminal nodes: 6

Residual mean deviance: 0.0115 = 1.081 / 94

Distribution of residuals:

| Min.       | 1st Qu.    | Median    | Mean      | 3rd Qu.   | Max.      |
|------------|------------|-----------|-----------|-----------|-----------|
| -0.2429000 | -0.0633100 | 0.0004025 | 0.0000000 | 0.0531300 | 0.4226000 |



# Pruning as an option

- **Pruning** is done to ensure the decision tree has a better performance. It makes some changes in the tree structure only for the better.
- So through **Cross Validation** we decide the size which will be best suited for pruning the tree.

## Summary of Cross Validation

```
cv.grinding
$size
[1] 6 5 4 3 2 1
$dev
[1] 2.462333 2.489448 2.503179 2.853785 3.314332 6.226398
$k
[1] -Inf 0.1483040 0.1657847 0.4142310 0.7798620 3.5092065
$method
[1] "deviance"
attr(,"class")
[1] "prune" "tree.sequence"
```

So it is to be noted that 6 is the size which we initially got. Hence no changes are to be made. We go for MSE next.

# Calculations of MSE

```
yhat=predict(tree.grinding,newdata=Final1[-train,])  
grinding.test=Final1[-train,"Ra"]  
mean((yhat-grinding.test)^2)
```

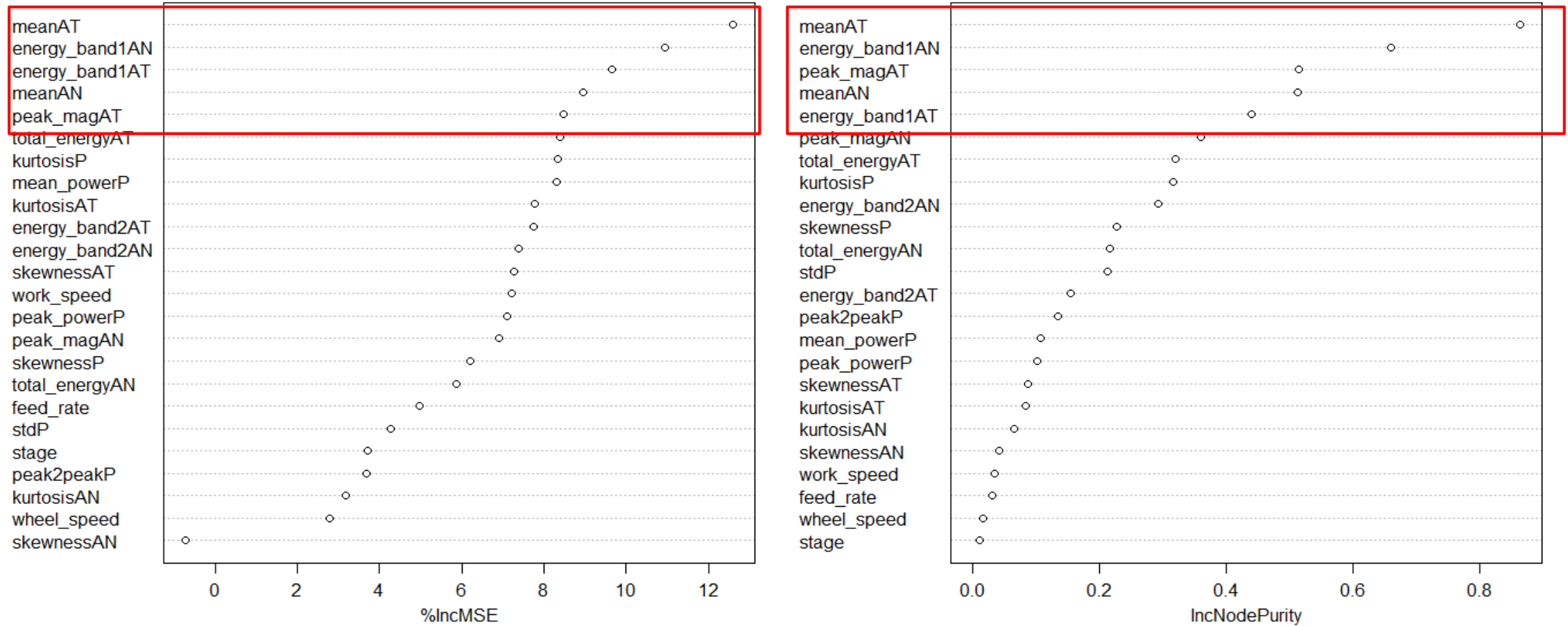
MSE: 0.01275293

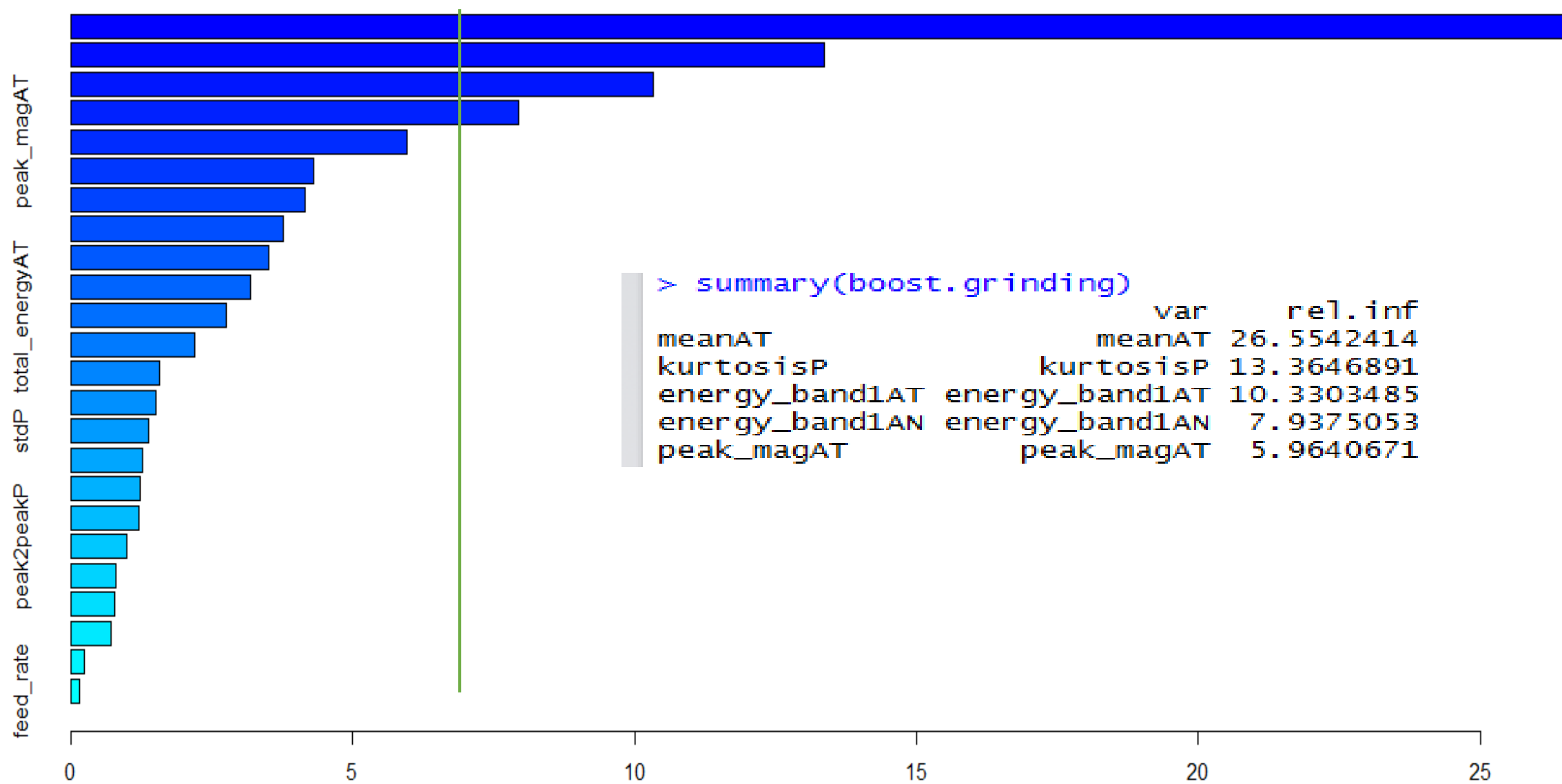
# Random Forest...

- This method is far more popular and advanced.
- `randomForest(formula = Ra ~ ., data = Final1, mtry = 5, importance = TRUE, subset = train)`
- Type of random forest: regression
- Number of trees: 500
- No. of variables tried at each split: 5
- Mean of squared residuals: 0.01500107
- % Var explained: 75.4

# Importance of each variable

rf.grinding





```
> summary(boost.grinding)
```

|                | var            | rel.inf    |
|----------------|----------------|------------|
| meanAT         | meanAT         | 26.5542414 |
| kurtosisP      | kurtosisP      | 13.3646891 |
| energy_band1AT | energy_band1AT | 10.3303485 |
| energy_band1AN | energy_band1AN | 7.9375053  |
| peak_magAT     | peak_magAT     | 5.9640671  |

# Building the Model...

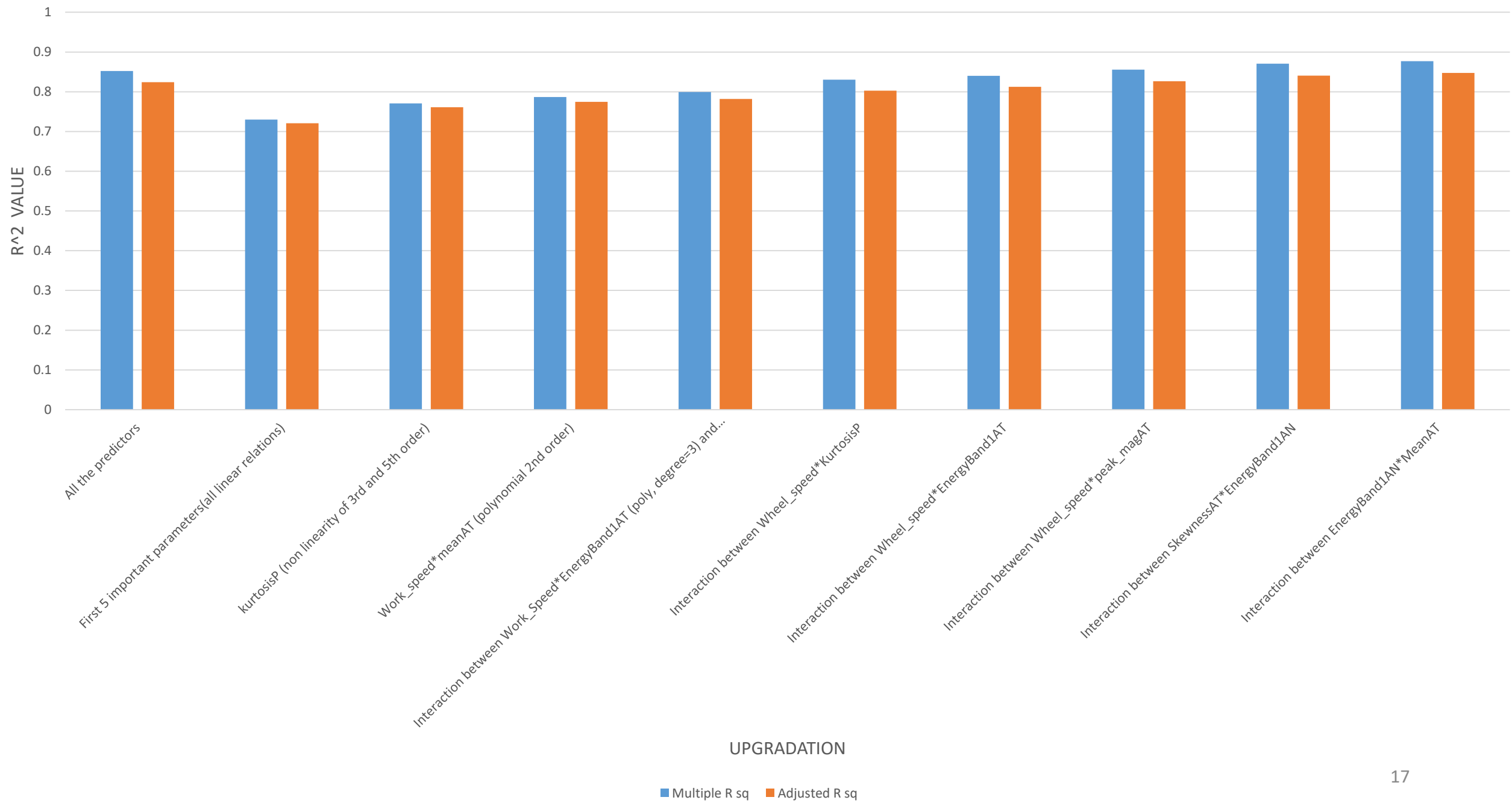
| Iteration no. | Upgradation                                                                                | Residual SE | Multiple R sq | Adjusted R sq |
|---------------|--------------------------------------------------------------------------------------------|-------------|---------------|---------------|
| 1             | All the predictors                                                                         | 0.101       | 0.8523        | 0.8239        |
| 2             | First 5 important parameters (all linear relations)                                        | 0.1273      | 0.7301        | 0.7207        |
| 3             | kurtosisP (non linearity of 3 <sup>rd</sup> and 5 <sup>th</sup> order)                     | 0.1177      | 0.7708        | 0.7612        |
| 4             | Work_speed*meanAT (polynomial 2 <sup>nd</sup> order)                                       | 0.1144      | 0.7866        | 0.7745        |
| 5             | Interaction between Work_Speed*EnergyBand1AT (poly, degree=3) and Work_speed*EnergyBand1AN | 0.1125      | 0.7994        | 0.7818        |
| 6             | Interaction between Wheel_speed*KurtosisP                                                  | 0.107       | 0.8306        | 0.8028        |
| 7             | Interaction between Wheel_speed*EnergyBand1AT                                              | 0.1043      | 0.8403        | 0.8126        |
|               |                                                                                            |             |               |               |

| Iteration no. | Upgradation                                  | Residual SE | Multiple R sq | Adjusted R sq |
|---------------|----------------------------------------------|-------------|---------------|---------------|
| 8             | Interaction between Wheel_speed*peak_magAT   | 0.1003      | 0.8556        | 0.8265        |
| 9             | Interaction between SkewnessAT*EnergyBand1AN | 0.09609     | 0.8707        | 0.8408        |
| 10            | Interaction between EnergyBand1AN*MeanAT     | 0.09413     | 0.877         | 0.8473        |

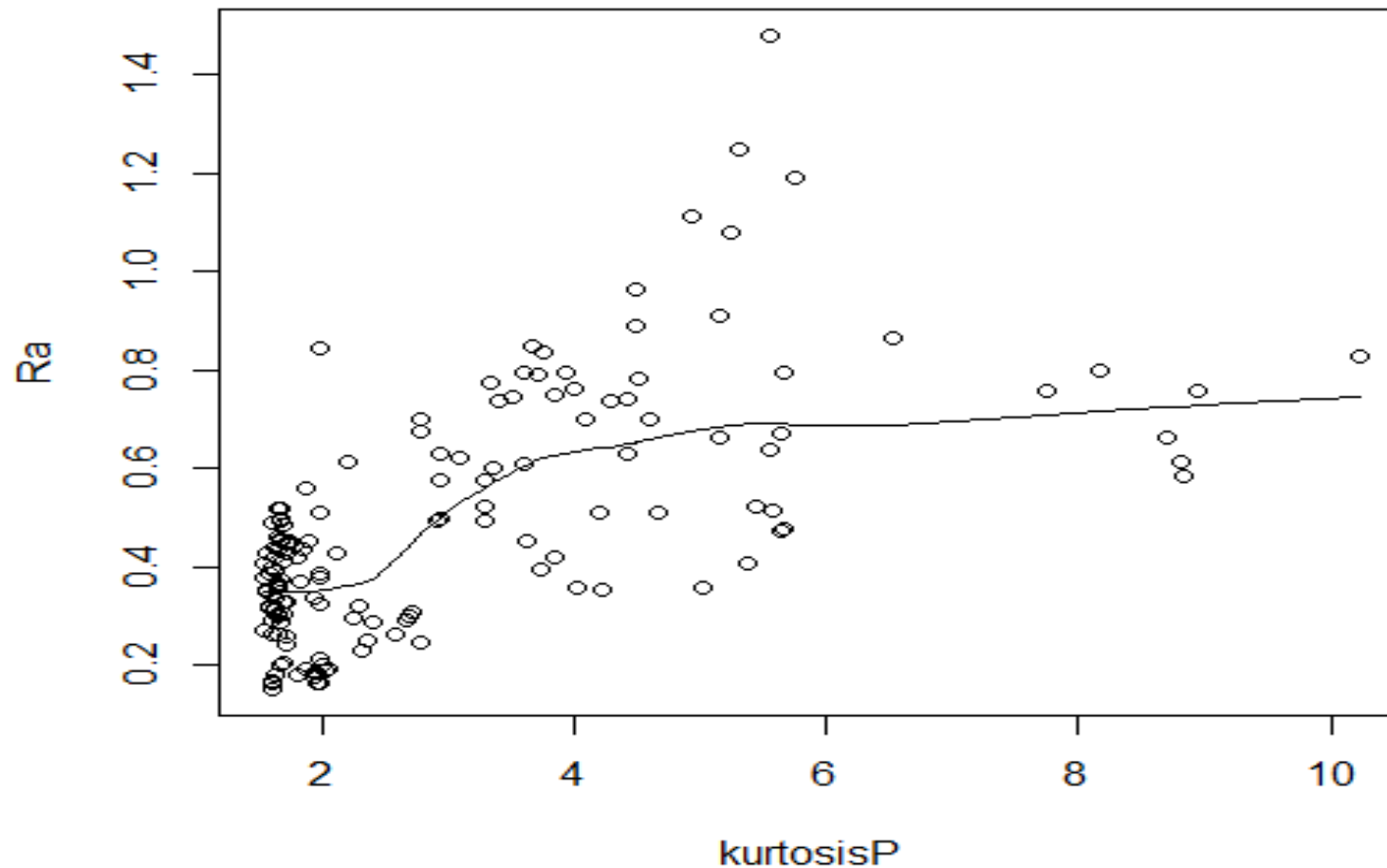
```
lm.fit=lm(Ra~meanAT+I(kurtosisP^3)+I(kurtosisP^5)+energy_band1AT+energy_band1AN+peak_magAT+poly(work_speed*meanAT,2)+poly(work_speed*energy_band1AT,3)+work_speed*energy_band1AN+poly(feed_rate*peak_magAT,5)+poly(wheel_speed*meanAT,3)+wheel_speed:kurtosisP+wheel_speed:energy_band1AT+wheel_speed*energy_band1AN+poly(wheel_speed*peak_magAT,2)+poly(skewnessAT*energy_band1AN,3)+energy_band1AN*meanAT, data=Final1)
```



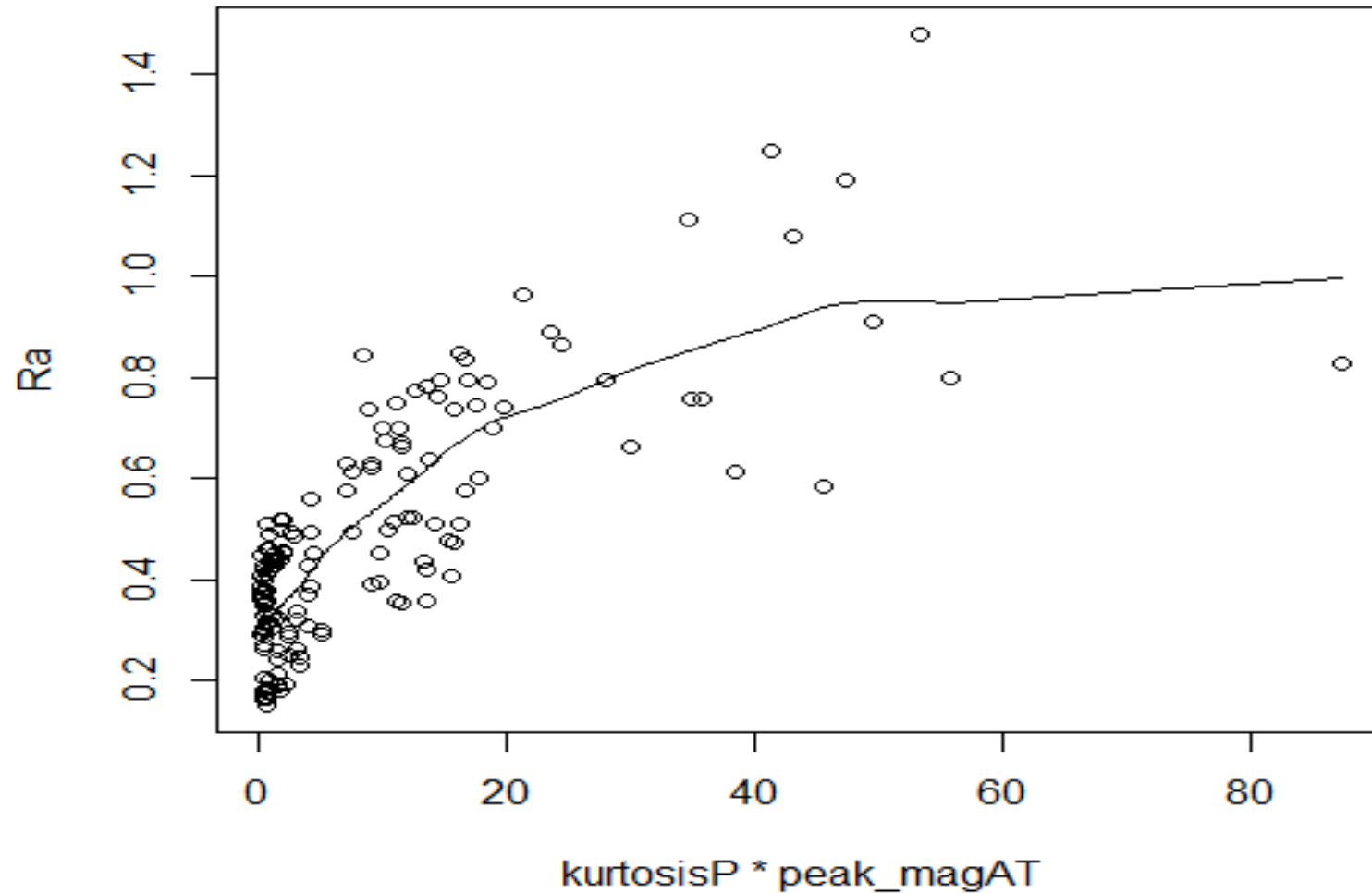
REGRESSION MODEL



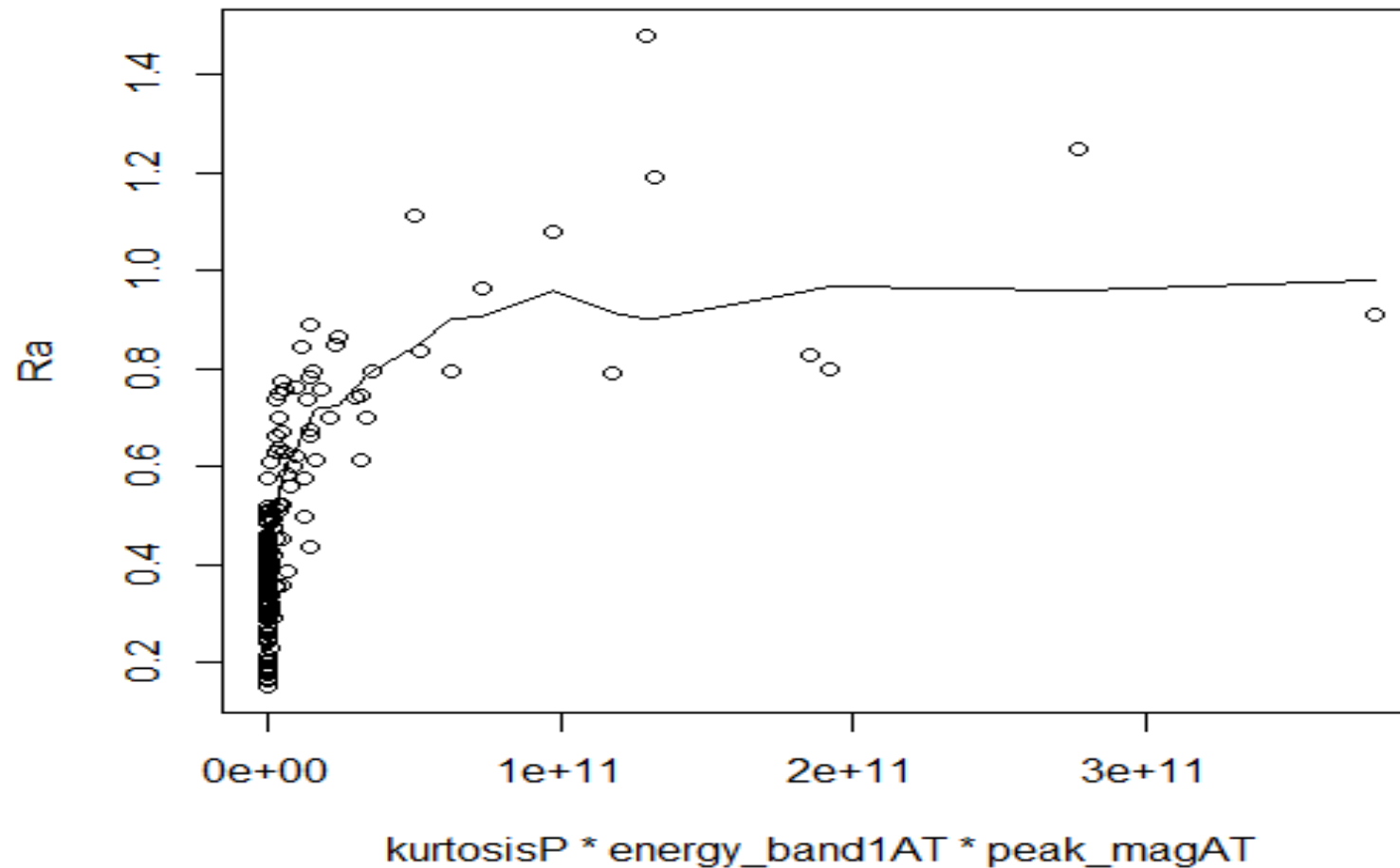
# How to decide which order polynomial will help?



# Why use interaction of predictors?



# Why reject some predictors?



# R implementation...

##validation set approach

```
library(boot)
```

##By taking sample

```
lm.fit=lm(Ra~meanAT+I(kurtosisP^3)+I(kurtosisP^5)+energy_band1AT+energy_band1AN+peak_magAT+poly(work_speed*meanAT,2)+poly(work_speed*energy_band1AT,3)+I(work_speed*energy_band1AN)+poly(feed_rate*peak_magAT,5)+poly(wheel_speed*meanAT,3)+wheel_speed:kurtosisP+wheel_speed:energy_band1AT+I(wheel_speed*energy_band1AN)+poly(wheel_speed*peak_magAT,2)+poly(skewnessAT*energy_band1AN,3)+I(energy_band1AN*meanAT),data=Final1,subset=train)
```

```
mean((Ra-predict(lm.fit,Final1))[-train]^2)
```

##LOOCV

```
glm.fit=glm(Ra~meanAT+I(kurtosisP^3)+I(kurtosisP^5)+energy_band1AT+energy_band1AN+peak_magAT+poly(work_speed*meanAT,2)+poly(work_speed*energy_band1AT,3)+I(work_speed*energy_band1AN)+poly(feed_rate*peak_magAT,5)+poly(wheel_speed*meanAT,3)+wheel_speed:kurtosisP+wheel_speed:energy_band1AT+I(wheel_speed*energy_band1AN)+poly(wheel_speed*peak_magAT,2)+poly(skewnessAT*energy_band1AN,3)+I(energy_band1AN*meanAT),data=Final1)
```

```
cv.error=cv.glm(Final1,glm.fit)
```

```
cv.error$delta
```

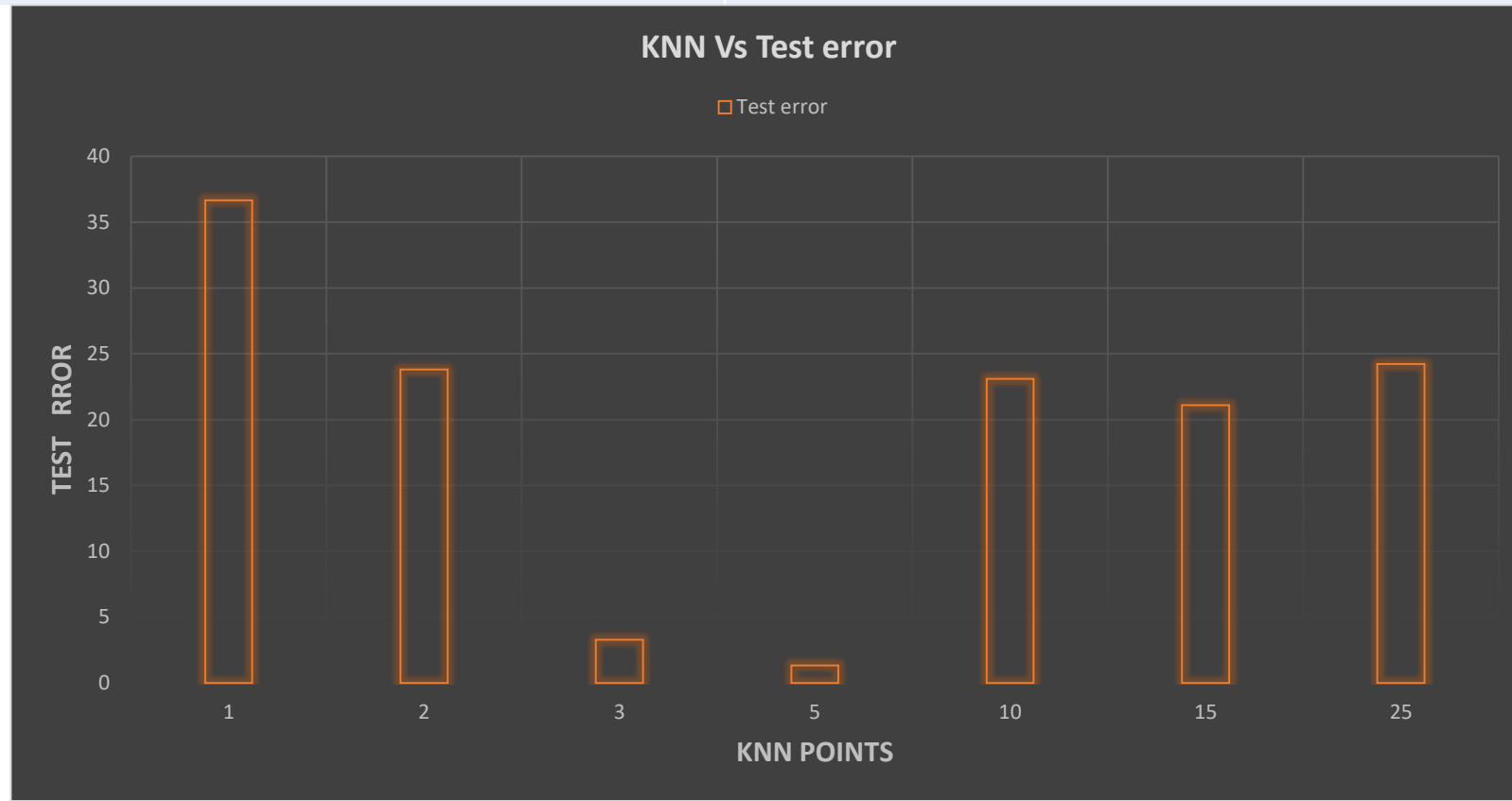
##K fold cross validation

```
cv.error.KNN=cv.glm(Final1,glm.fit,K=5)
```

```
cv.error.KNN$delta
```

# Validation

| Validation Method                    | Test Error |
|--------------------------------------|------------|
| Train & Test Validation set Approach | 0.01362    |
| LOOCV                                | 27.54      |



# Bootstrapping

**##Bootstrap**

```
boot.fn=function(Final1,index)return(coef(lm(Ra~meanAT+I(kurtosisP^3)+I(kurtosisP^5)+energy_band1AT+energy_band1AN+peak_magAT+poly(work_speed*meanAT,2)+poly(work_speed*energy_band1AT,3)+I(work_speed*energy_band1AN)+poly(feed_rate*peak_magAT,5)+poly(wheel_speed*meanAT,3)+wheel_speed:kurtosisP+wheel_speed:energy_band1AT+I(wheel_speed*energy_band1AN)+poly(wheel_speed*peak_magAT,2)+poly(skewnessAT*energy_band1AN,3)+I(energy_band1AN*meanAT),data=Final1,subset=index)))
boot.fn(Final1,1:150)
```

```
boot.fn(Final1,sample(150,150,replace=T))
boot(Final1,boot.fn,1000)
```

```
summary(lm(Ra~meanAT+I(kurtosisP^3)+I(kurtosisP^5)+energy_band1AT+energy_band1AN+peak_magAT+poly(work_speed*meanAT,2)+poly(work_speed*energy_band1AT,3)+I(work_speed*energy_band1AN)+poly(feed_rate*peak_magAT,5)+poly(wheel_speed*meanAT,3)+wheel_speed:kurtosisP+wheel_speed:energy_band1AT+I(wheel_speed*energy_band1AN)+poly(wheel_speed*peak_magAT,2)+poly(skewnessAT*energy_band1AN,3)+I(energy_band1AN*meanAT),data=Final1))$coef
```

# T-Statistics

| Prediction terms                      | Estimate      | Std. Error   | t value    | Pr(> t )     |
|---------------------------------------|---------------|--------------|------------|--------------|
| (Intercept)                           | 3.336925e-02  | 1.630400e-01 | 0.2046691  | 8.381774e-01 |
| meanAT                                | 1.360546e+00  | 5.681839e-01 | 2.3945520  | 1.818847e-02 |
| I(kurtosisP^3)                        | 2.187780e-03  | 9.565892e-04 | 2.2870635  | 2.394439e-02 |
| I(kurtosisP^5)                        | -1.428913e-05 | 8.444362e-06 | -1.6921507 | 9.321231e-02 |
| energy_band1AT                        | 3.519608e-10  | 2.077994e-10 | 1.6937531  | 9.290638e-02 |
| energy_band1AN                        | -3.039573e-10 | 8.667912e-11 | -3.5066961 | 6.390766e-04 |
| peak_magAT                            | -1.420527e-02 | 7.256045e-02 | -0.1957715 | 8.451201e-01 |
| poly(work_speed * meanAT, 2)1         | -6.586234e-01 | 7.173191e-01 | -0.9181735 | 3.603698e-01 |
| poly(work_speed * meanAT, 2)2         | 6.641240e-01  | 3.384097e-01 | 1.9624853  | 5.202031e-02 |
| poly(work_speed * energy_band1AT, 3)1 | -2.209709e+00 | 1.510211e+00 | -1.4631792 | 1.460327e-01 |
| poly(work_speed * energy_band1AT, 3)2 | 1.689080e+00  | 5.316178e-01 | 3.1772452  | 1.890785e-03 |
| poly(work_speed * energy_band1AT, 3)3 | 1.257785e-01  | 2.259181e-01 | 0.5567438  | 5.787393e-01 |
| I(work_speed * energy_band1AN)        | 6.058552e-13  | 1.730340e-13 | 3.5013661  | 6.507767e-04 |
| poly(feed_rate * peak_magAT, 5)1      | 8.597668e-02  | 4.624705e-01 | 0.1859074  | 8.528313e-01 |
| poly(feed_rate * peak_magAT, 5)2      | 6.628270e-01  | 2.691303e-01 | 2.4628482  | 1.520293e-02 |
| poly(feed_rate * peak_magAT, 5)3      | 3.999004e-01  | 1.971681e-01 | 2.0282202  | 4.475181e-02 |
| poly(feed_rate * peak_magAT, 5)4      | 4.870610e-02  | 1.875995e-01 | 0.2596281  | 7.955955e-01 |
| poly(feed_rate * peak_magAT, 5)5      | 9.250714e-02  | 1.718965e-01 | 0.5381560  | 5.914661e-01 |
| poly(wheel_speed * meanAT, 3)1        | -9.657315e-01 | 2.630368e+00 | -0.3671469 | 7.141561e-01 |
| poly(wheel_speed * meanAT, 3)2        | 7.370640e-01  | 5.833318e-01 | 1.2635416  | 2.088438e-01 |
| poly(wheel_speed * meanAT, 3)3        | -5.298450e-01 | 1.911535e-01 | -2.7718306 | 6.463545e-03 |
| I(wheel_speed * energy_band1AN)       | 7.708471e-12  | 2.290698e-12 | 3.3651183  | 1.027990e-03 |
| poly(wheel_speed * peak_magAT, 2)1    | -3.210185e-01 | 1.921859e+00 | -0.1670354 | 8.676233e-01 |
| poly(wheel_speed * peak_magAT, 2)2    | -1.207514e+00 | 4.204559e-01 | -2.8719172 | 4.825164e-03 |
| poly(skewnessAT * energy_band1AN, 3)1 | -1.050139e+00 | 2.496081e-01 | -4.2071501 | 5.014776e-05 |
| poly(skewnessAT * energy_band1AN, 3)2 | -2.055776e+00 | 5.027815e-01 | -4.0888051 | 7.877960e-05 |
| poly(skewnessAT * energy_band1AN, 3)3 | -1.071476e+00 | 3.301953e-01 | -3.2449779 | 1.522174e-03 |
| I(energy_band1AN * meanAT)            | -9.703458e-11 | 3.928192e-11 | -2.4702100 | 1.490876e-02 |
| wheel_speed:kurtosisP                 | -2.376067e-03 | 8.001043e-04 | -2.9696971 | 3.600786e-03 |
| energy_band1AT:wheel_speed            | -8.983363e-13 | 7.259787e-12 | -0.1237414 | 9.017270e-01 |



# Conclusion

- The final model presented above has 29 prediction terms.
  - $R^2$  value = 0.877   Adjusted  $R^2$  = 0.8473
  - Residual Standard Error = 0.09413
  - Mean Square Error = 0.01362

# Recap...

- Surface Roughness Prediction in Grinding process

Response- Surface roughness

Factors(24)- Process parameter(4), Acceleration and power signal(20) parameters

- Model  $R^2$  was 87% , even then process parameter where not significant.
- Need to rebuild the model

- Phenomenon of “causation”
- Quote-

*“Torture the data, and it will confess to anything.”- Ronald Coase,*  
British economist and author

- An attempt is made to rebuild the model
- Case 1: considering only process parameters
- Case 2: considering process, acceleration and power signal parameter.

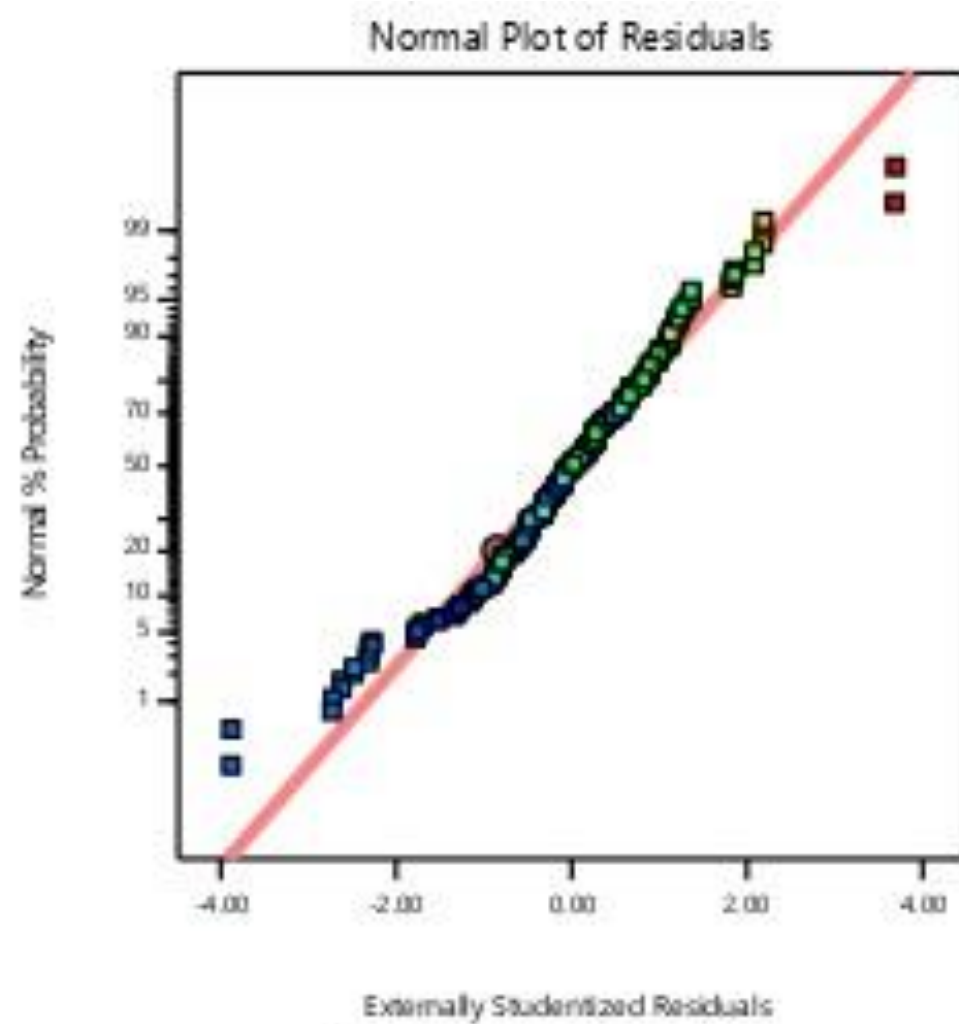
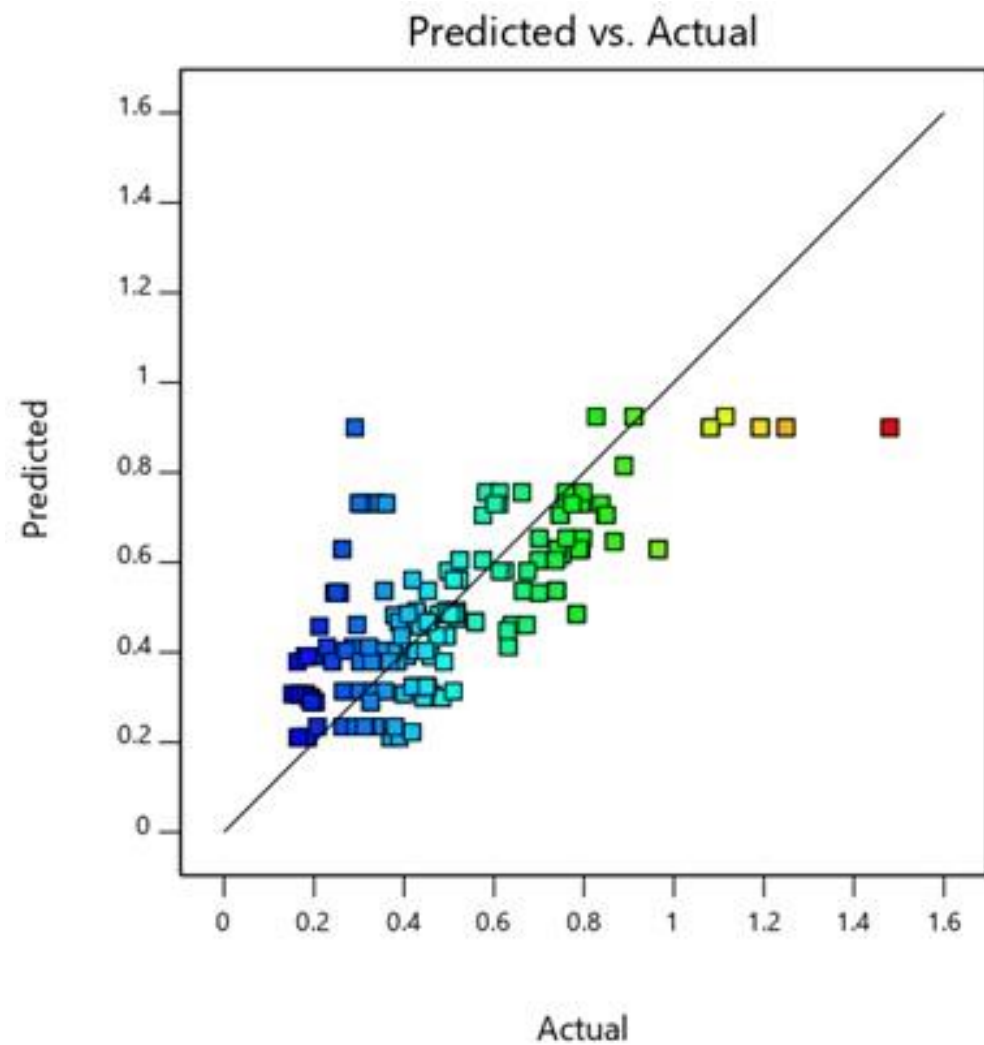
# Case 1: a] Linear model

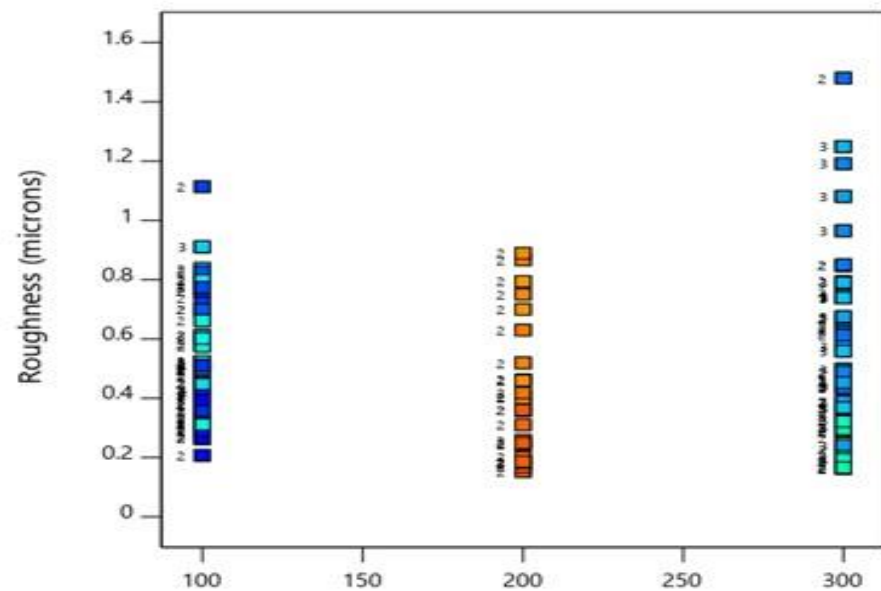
| Roughness | =           |
|-----------|-------------|
| +0.934089 |             |
| -0.008455 | wheel speed |
| -0.000127 | work speed  |
| +0.242923 | feed rate   |
| -0.076451 | stage       |

|           |        |  |                         |        |
|-----------|--------|--|-------------------------|--------|
| Std. Dev. | 0.1628 |  | R <sup>2</sup>          | 0.5691 |
| Mean      | 0.4984 |  | Adjusted R <sup>2</sup> | 0.5610 |
| C.V. %    | 32.66  |  |                         |        |

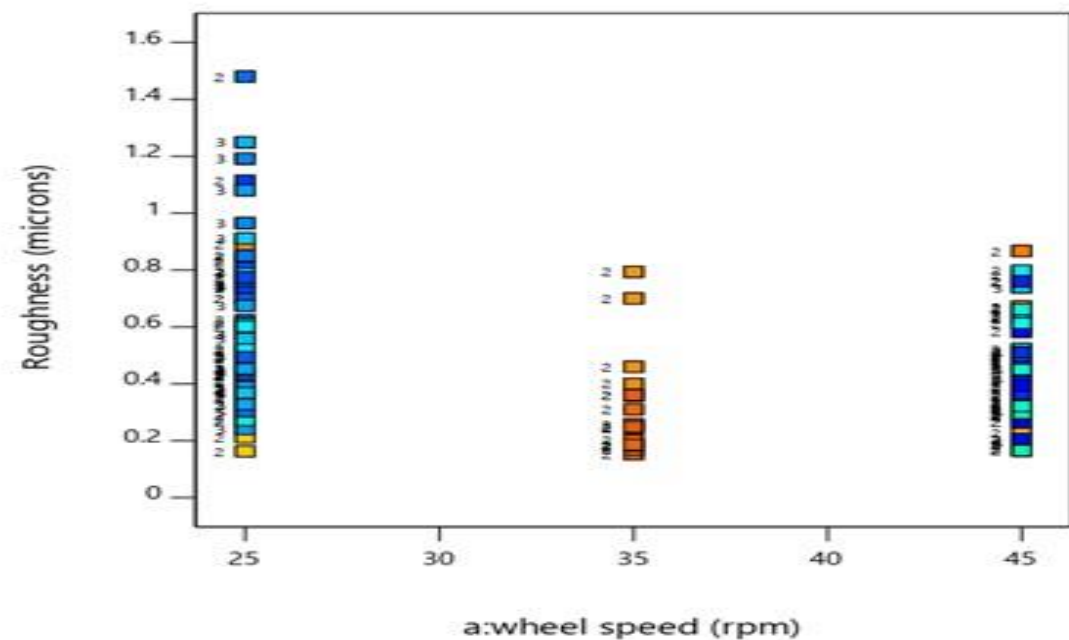
| Source        | Term df | Error df | F-value | p-value  |             |
|---------------|---------|----------|---------|----------|-------------|
| Subplot       | 4       | 315.39   | 105.13  | < 0.0001 | significant |
| a-wheel speed | 1       | 318.97   | 74.21   | < 0.0001 |             |
| B-work speed  | 1       | 291.31   | 1.37    | 0.2420   |             |
| C-feed rate   | 1       | 317.27   | 37.13   | < 0.0001 |             |
| D-stage       | 1       | 317.15   | 32.08   | < 0.0001 |             |

**A, C, D significant**

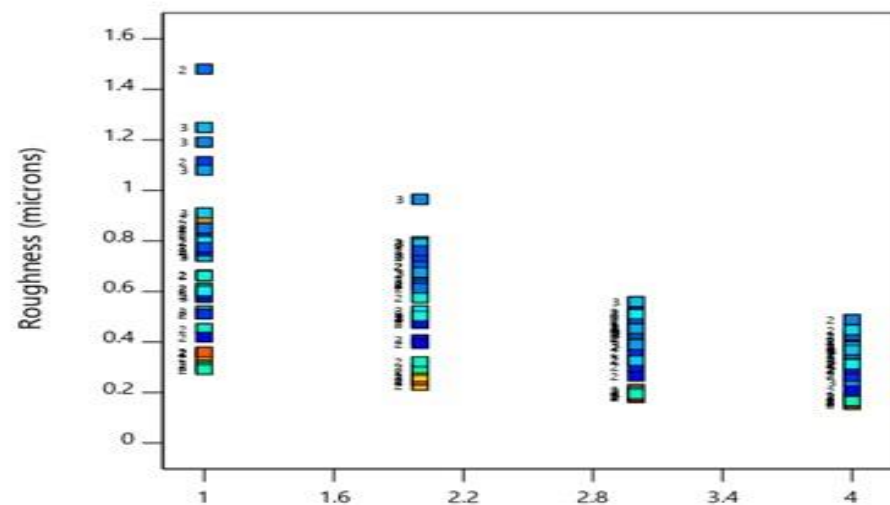




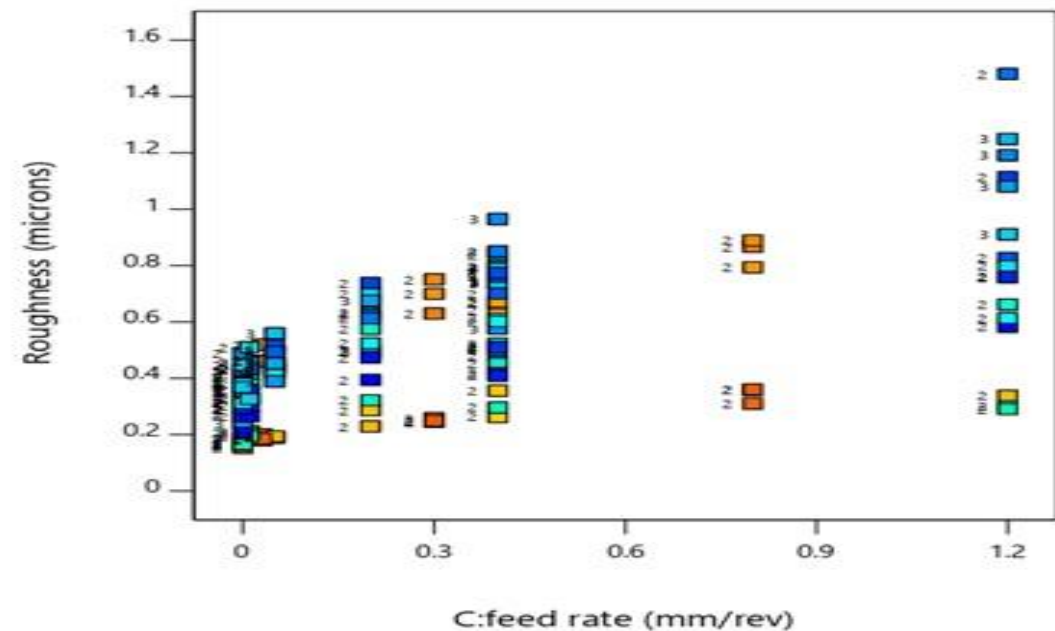
B:work speed (rpm)



a:wheel speed (rpm)



D:stage



C:feed rate (mm/rev)

- Linear model is significant as all data points lie near the line plotted on predicted vs actual data points.
- Outliers in the normal probability plot are the significant factors
- Optimized factors to minimize roughness:

Feed rate: 0 to 0.3

Wheel speed: 35 rpm

Work speed: 200 rpm

Stage: 4

## 2] Quadratic:

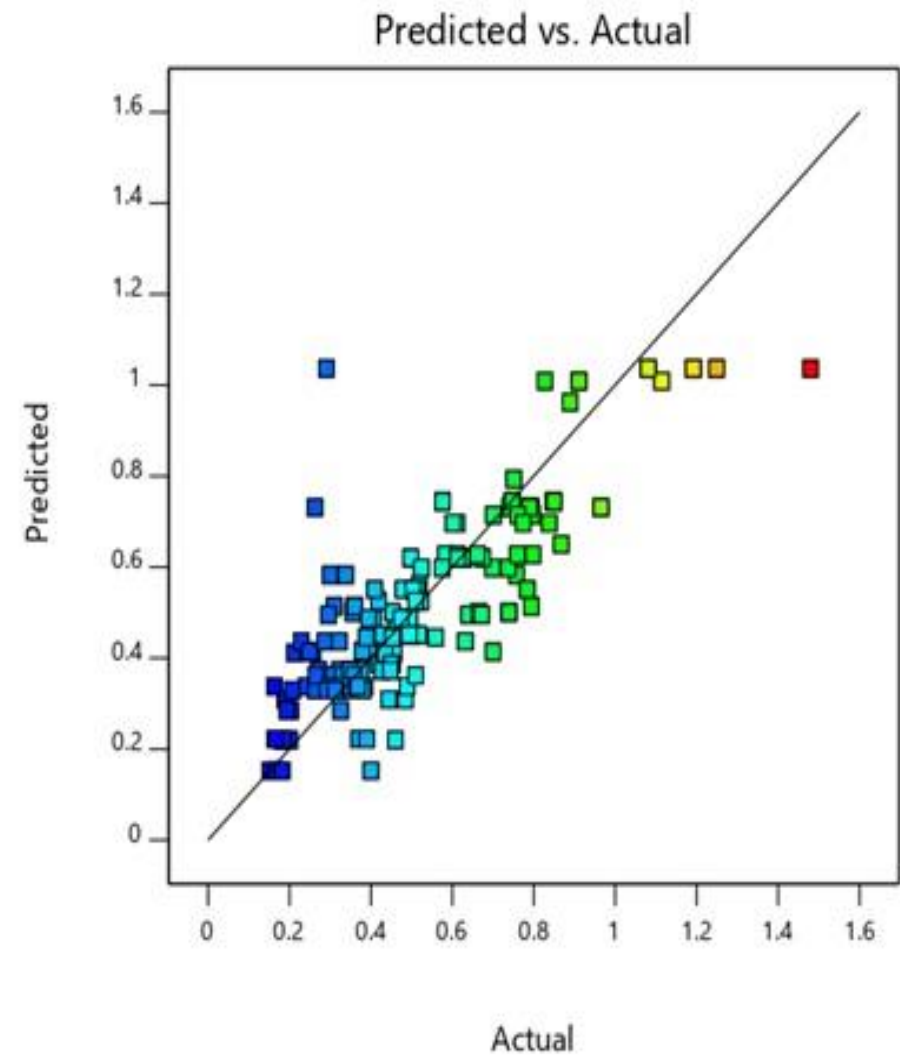
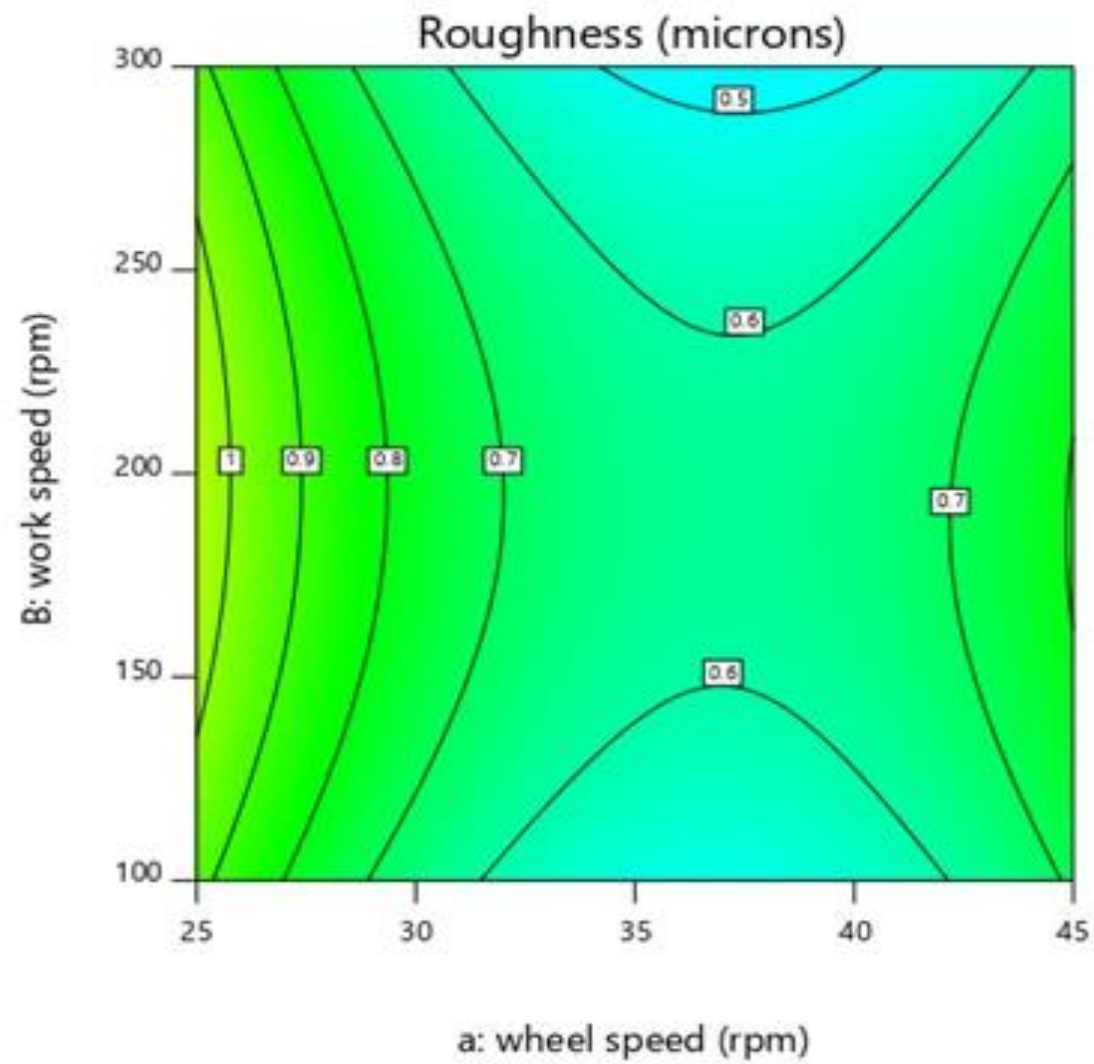
|           |        |  |                         |        |
|-----------|--------|--|-------------------------|--------|
| Std. Dev. | 0.1392 |  | R <sup>2</sup>          | 0.6941 |
| Mean      | 0.4984 |  | Adjusted R <sup>2</sup> | 0.6782 |
| C.V. %    | 27.94  |  |                         |        |

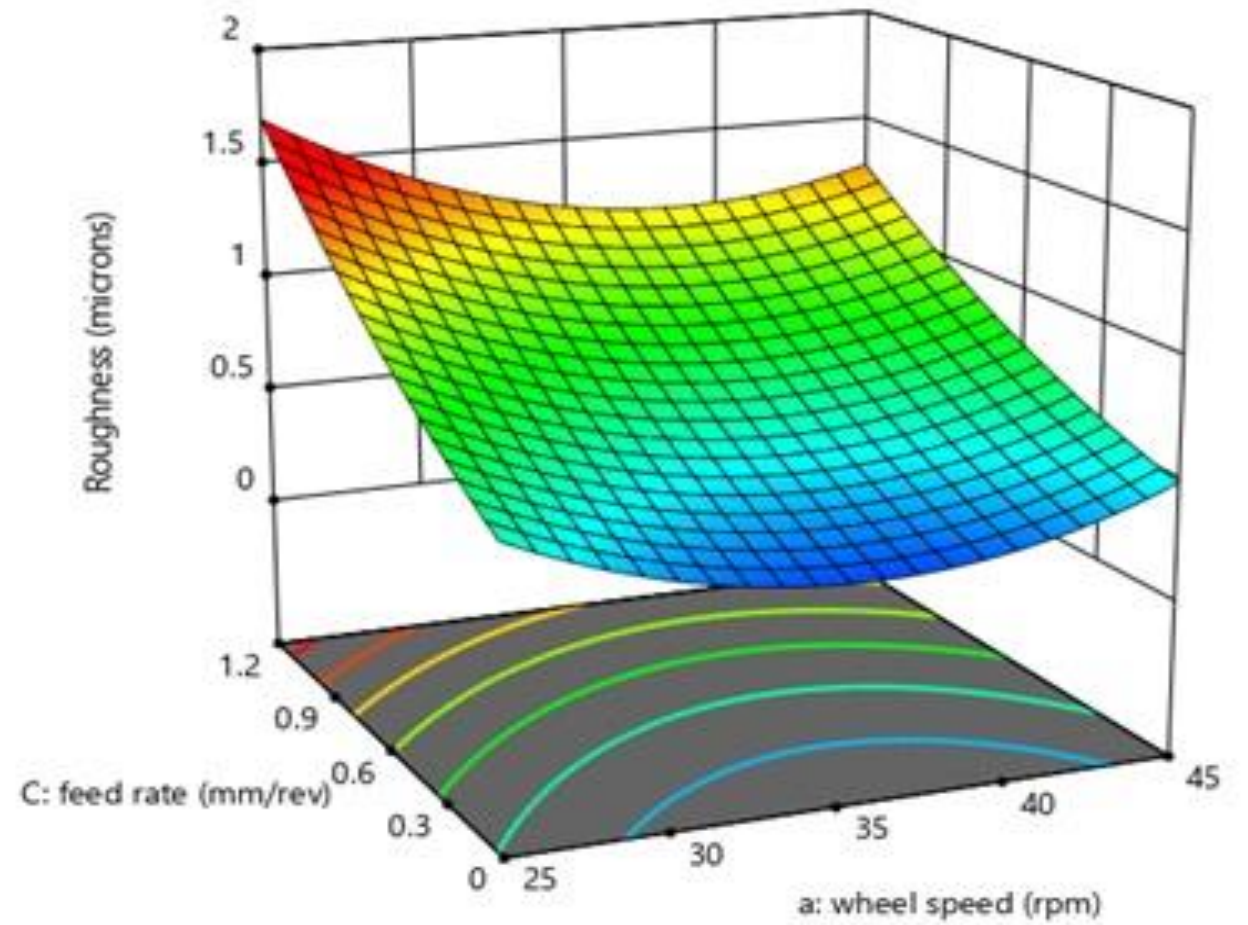
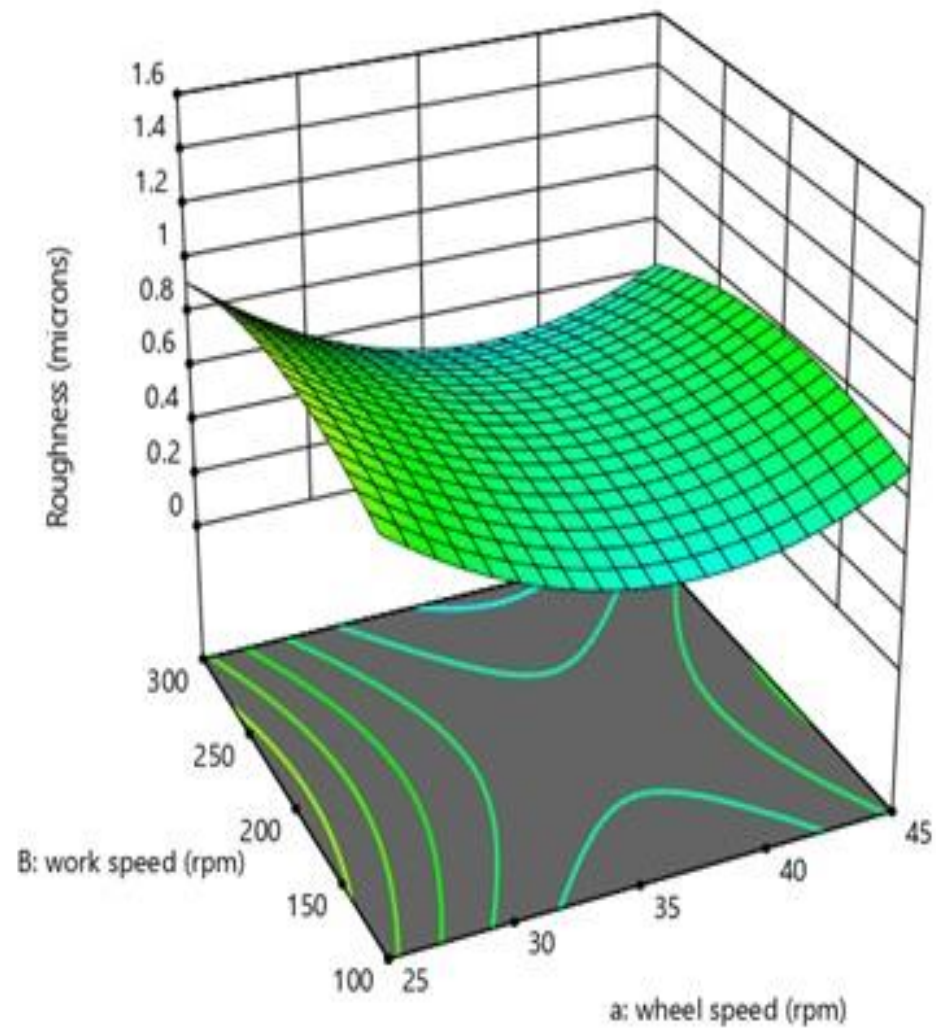
| Roughness | =                        |
|-----------|--------------------------|
| +3.77855  |                          |
| -0.206723 | wheel speed              |
| +0.006080 | work speed               |
| -0.089405 | feed rate                |
| -0.240050 | stage                    |
| -0.000018 | wheel speed * work speed |
| -0.013116 | wheel speed * feed rate  |
| +0.000379 | wheel speed * stage      |
| -0.000124 | work speed * feed rate   |
| -0.000154 | work speed * stage       |
| +0.432729 | feed rate * stage        |
| +0.002926 | wheel speed <sup>2</sup> |
| -0.000013 | work speed <sup>2</sup>  |
| +0.241883 | feed rate <sup>2</sup>   |
| +0.030276 | stage <sup>2</sup>       |
|           |                          |

**A, C, AB, AC, A<sup>2</sup>, B<sup>2</sup> are significant**

| Source         | Term df | Error df | F-value | p-value  |             |
|----------------|---------|----------|---------|----------|-------------|
| Subplot        | 14      | 309.00   | 50.08   | < 0.0001 | significant |
| a-wheel speed  | 1       | 309.00   | 76.75   | < 0.0001 |             |
| B-work speed   | 1       | 309.00   | 1.92    | 0.1671   |             |
| C-feed rate    | 1       | 309.00   | 9.96    | 0.0018   |             |
| D-stage        | 1       | 309.00   | 2.35    | 0.1264   |             |
| aB             | 1       | 309.00   | 4.42    | 0.0363   |             |
| aC             | 1       | 309.00   | 13.52   | 0.0003   |             |
| aD             | 1       | 309.00   | 0.0990  | 0.7533   |             |
| BC             | 1       | 309.00   | 0.1191  | 0.7303   |             |
| BD             | 1       | 309.00   | 1.58    | 0.2094   |             |
| CD             | 1       | 309.00   | 3.37    | 0.0674   |             |
| a <sup>2</sup> | 1       | 309.00   | 47.11   | < 0.0001 |             |
| B <sup>2</sup> | 1       | 309.00   | 11.71   | 0.0007   |             |
| C <sup>2</sup> | 1       | 309.00   | 0.7085  | 0.4006   |             |
| D <sup>2</sup> | 1       | 309.00   | 1.20    | 0.2745   |             |



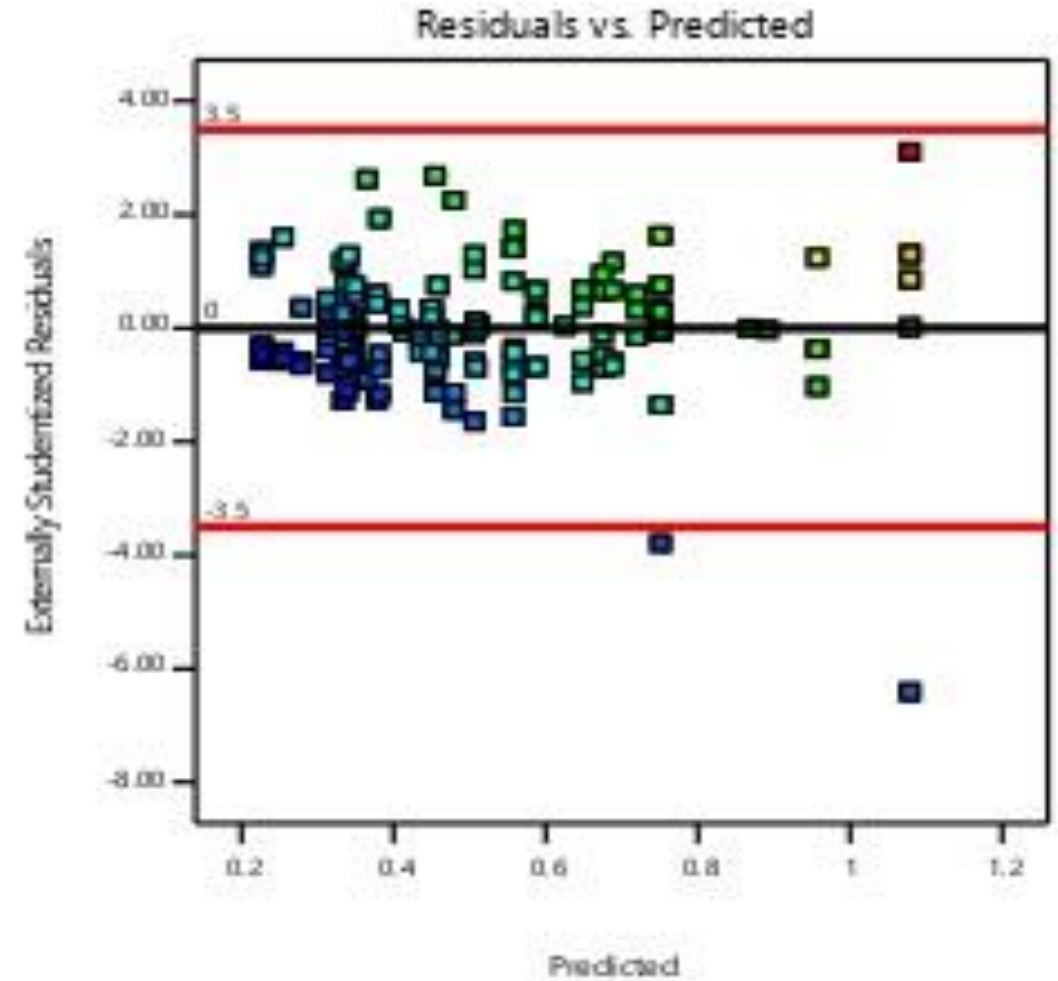
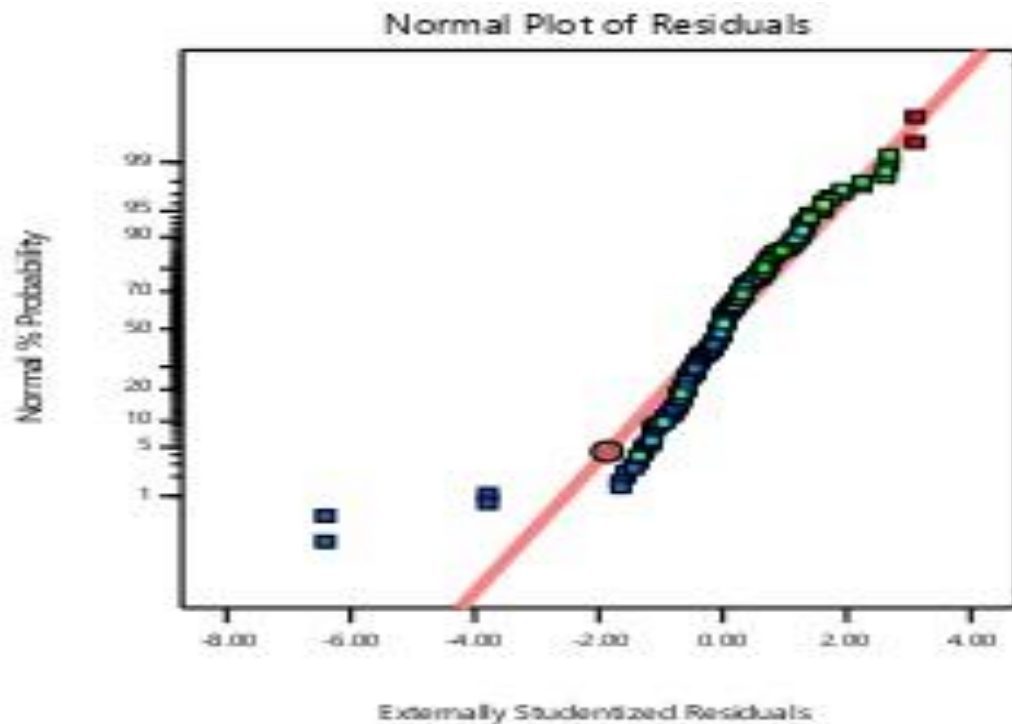




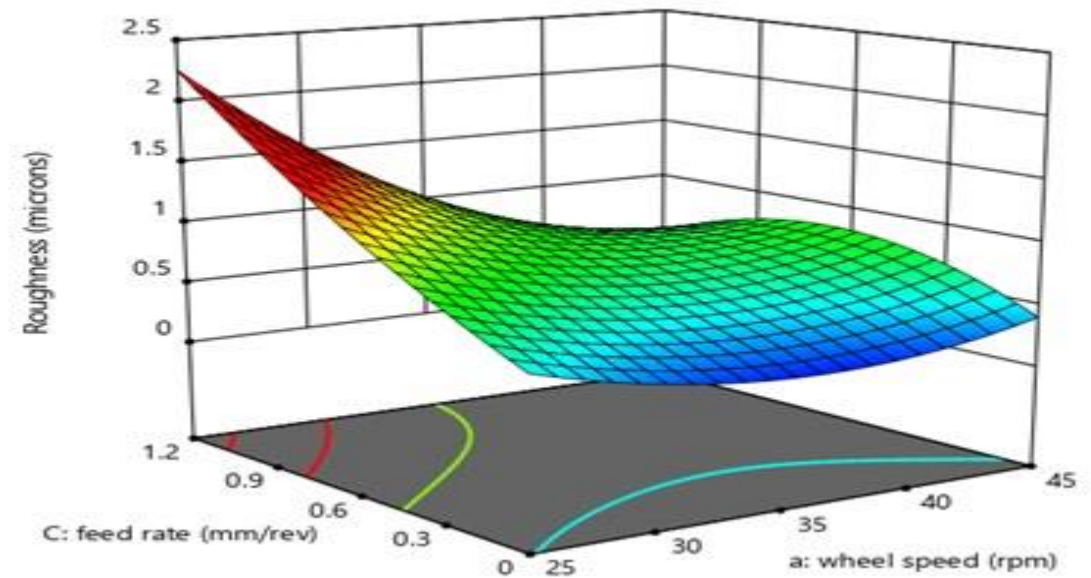
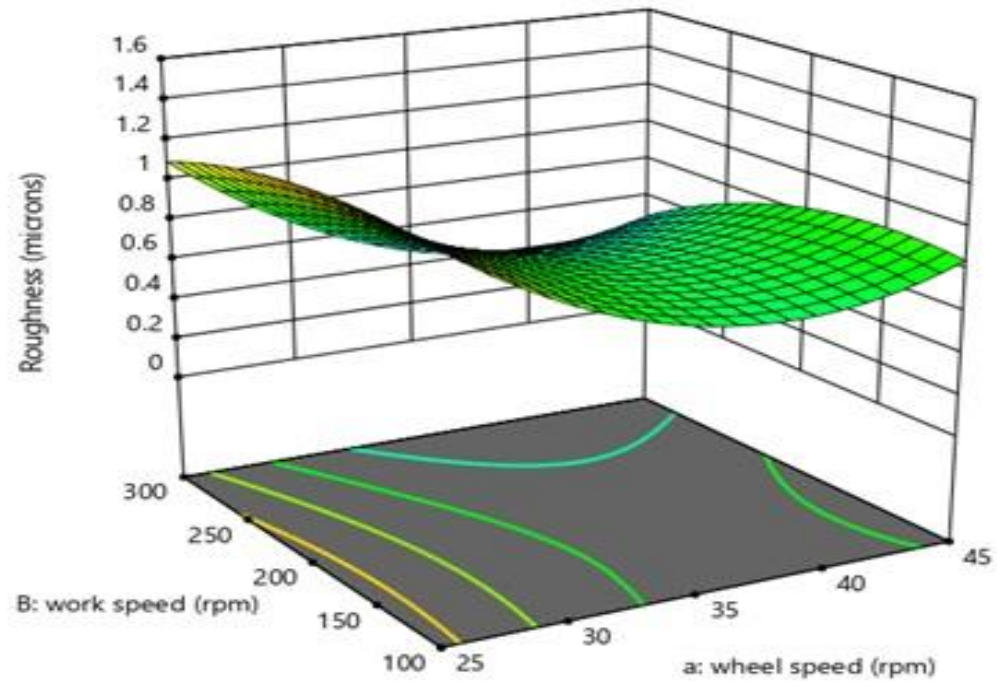
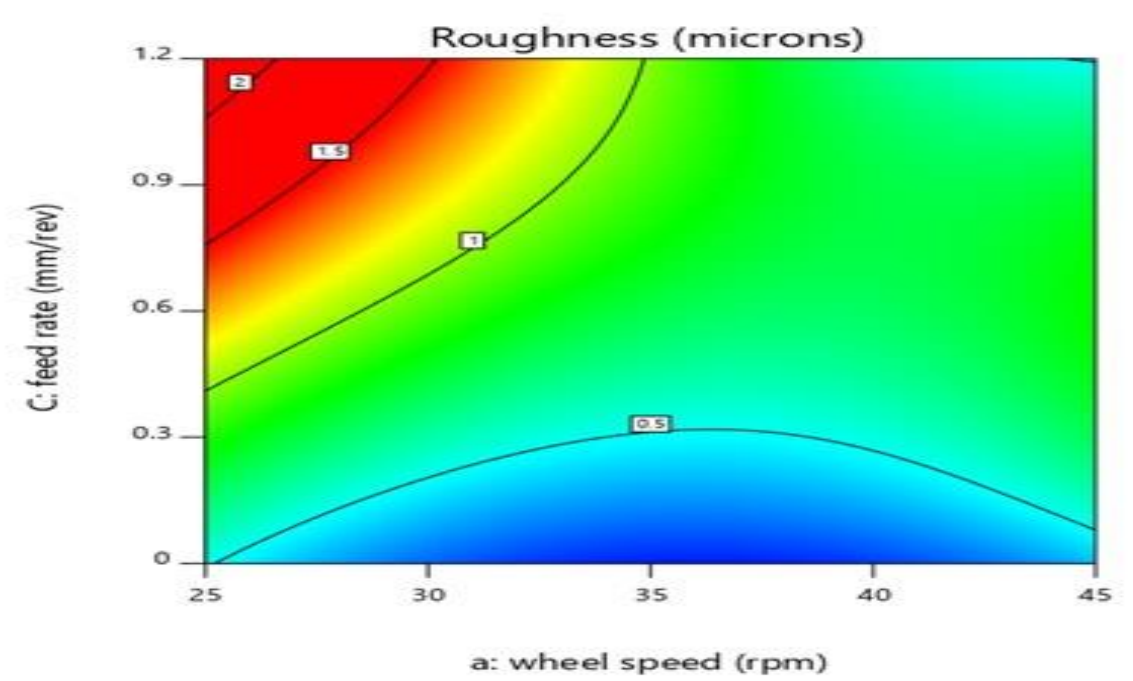
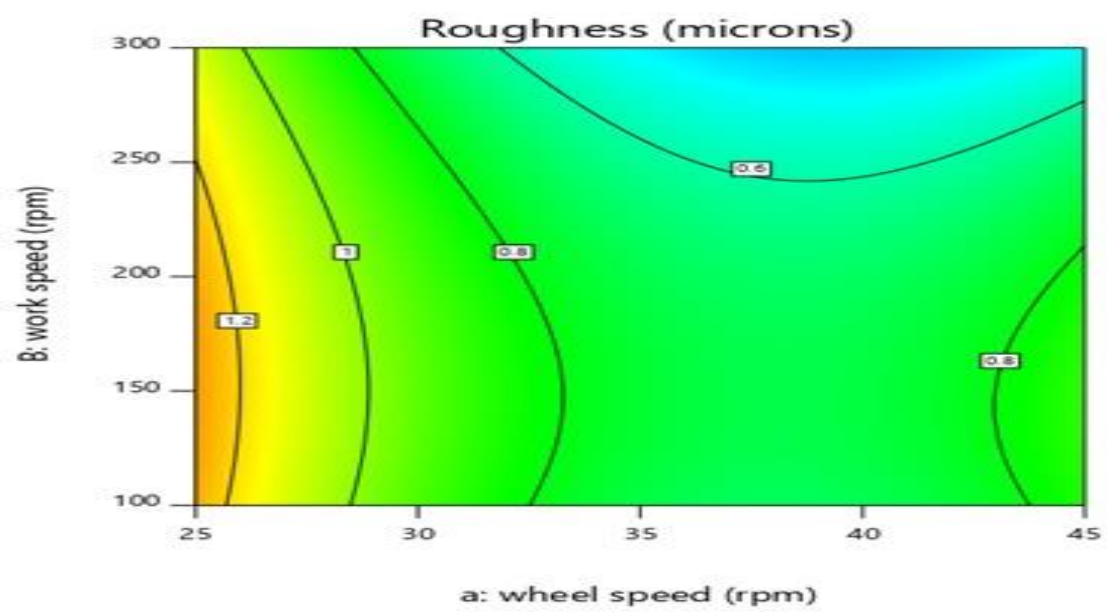
### 3] Cubic

|           |        |                         |        |
|-----------|--------|-------------------------|--------|
| Std. Dev. | 0.1363 | R <sup>2</sup>          | 0.7210 |
| Mean      | 0.4984 | Adjusted R <sup>2</sup> | 0.6914 |
| C.V. %    | 27.36  |                         |        |

**A, AB, A<sup>2</sup>, ABC are significant**



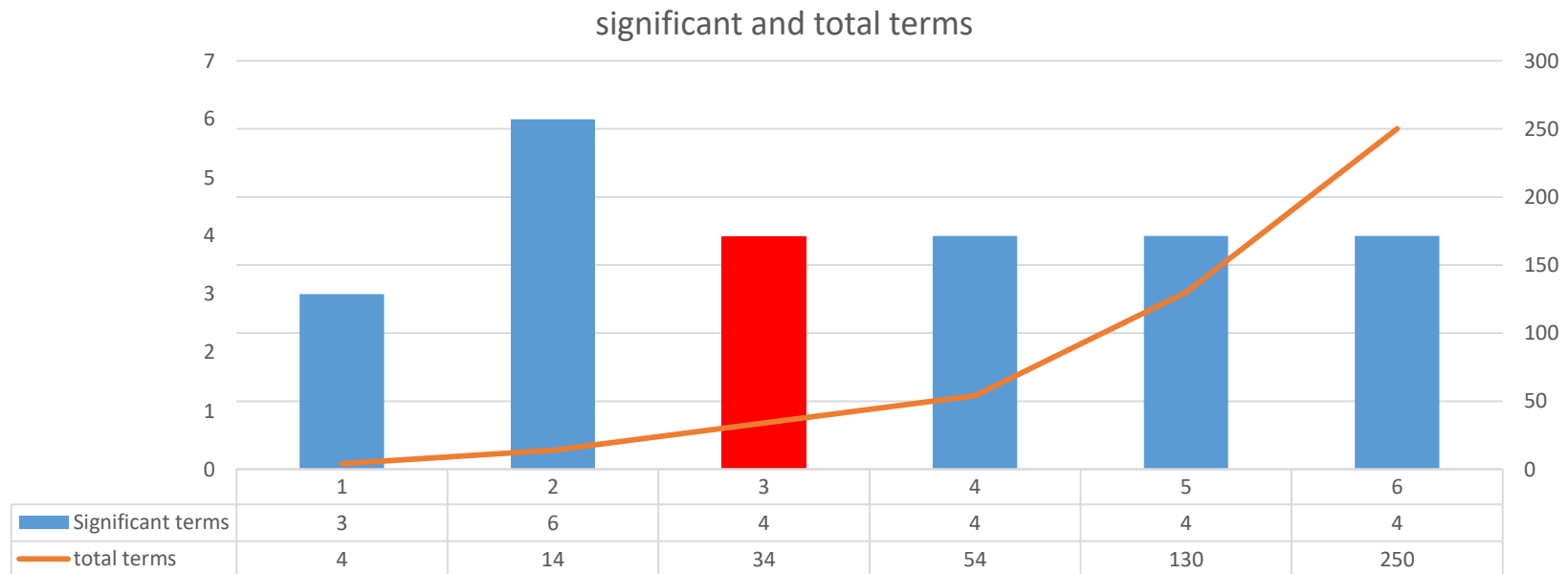
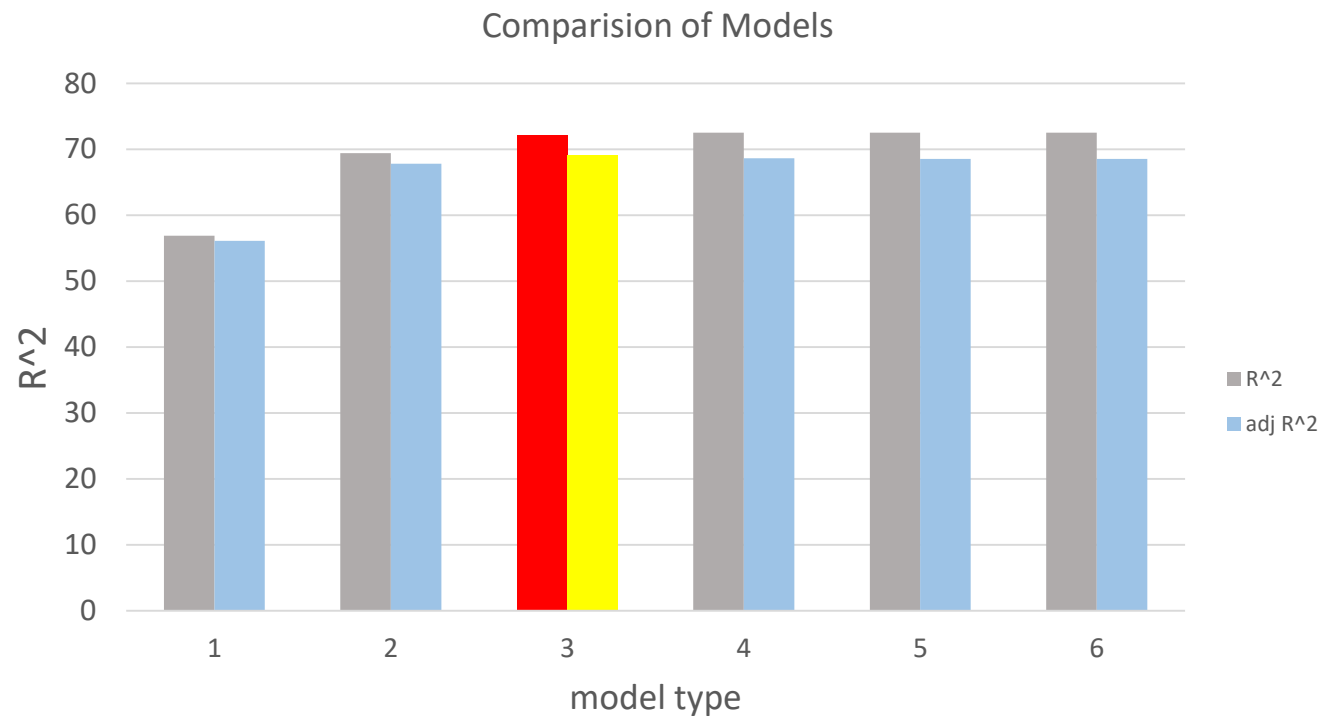




## Comparison of various models

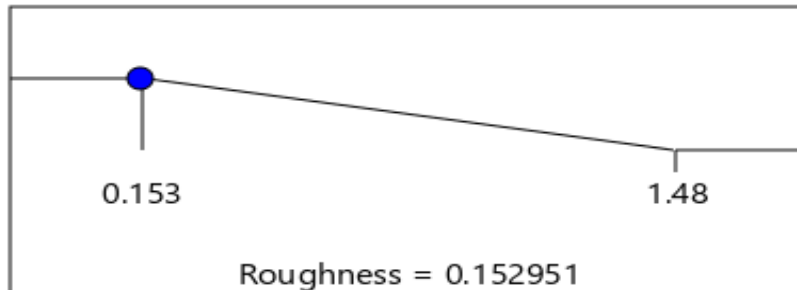
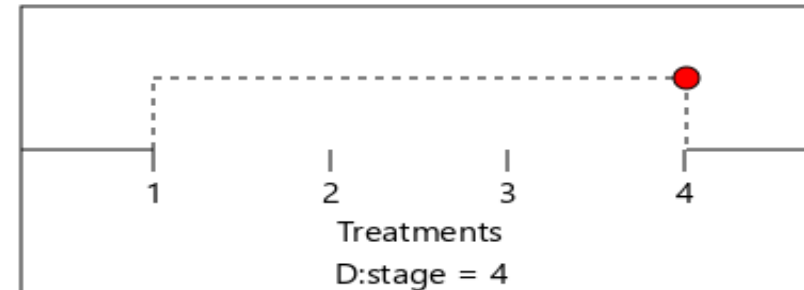
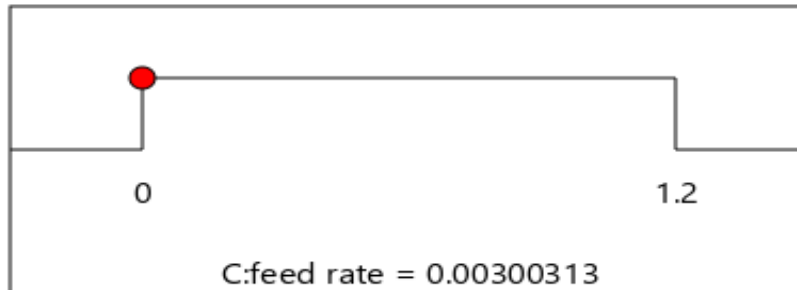
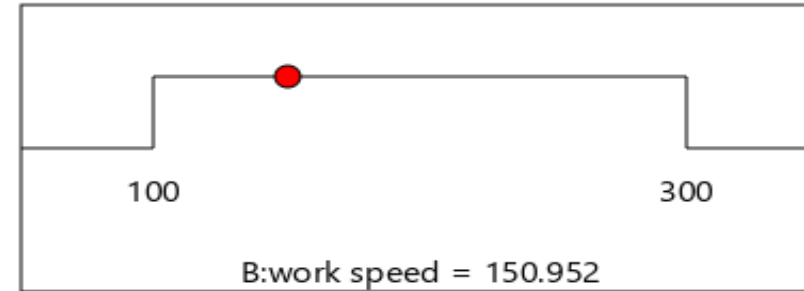
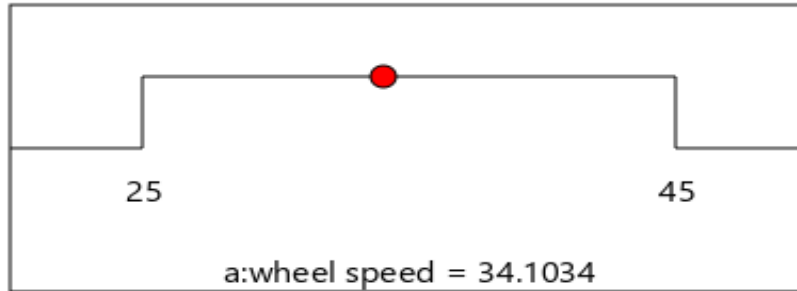
| A          | Wheel speed      |                       |                   |             |                                               |
|------------|------------------|-----------------------|-------------------|-------------|-----------------------------------------------|
| B          | work speed       |                       |                   |             |                                               |
| C          | feed rate        |                       |                   |             |                                               |
| D          | Stage            |                       |                   |             |                                               |
| MODEL TYPE | R <sup>2</sup> % | adj. R <sup>2</sup> % | Significant terms | Total terms | Significant factors                           |
| Linear     | 56.91            | 56.1                  | 3                 | 4           | A, C, D                                       |
| Quadratic  | 69.41            | 67.82                 | 6                 | 14          | A, C, AB, AC, A <sup>2</sup> , B <sup>2</sup> |
| Cubic      | 72.1             | 69.14                 | 4                 | 34          | A, AB, A <sup>2</sup> , ABC                   |
| Quartile   | 72.52            | 68.64                 | 4                 | 54          | A, AB, A <sup>2</sup> , ABC                   |
| fifth      | 72.52            | 68.53                 | 4                 | 130         | A, AB, A <sup>2</sup> , ABC                   |
| sixth      | 72.52            | 68.53                 | 4                 | 250         | A, AB, A <sup>2</sup> , ABC                   |

- Cubic model is the best model as it gives best R<sup>2</sup> value
- As model level increases more number of insignificant terms are added with no improvement in R<sup>2</sup> and significant terms.

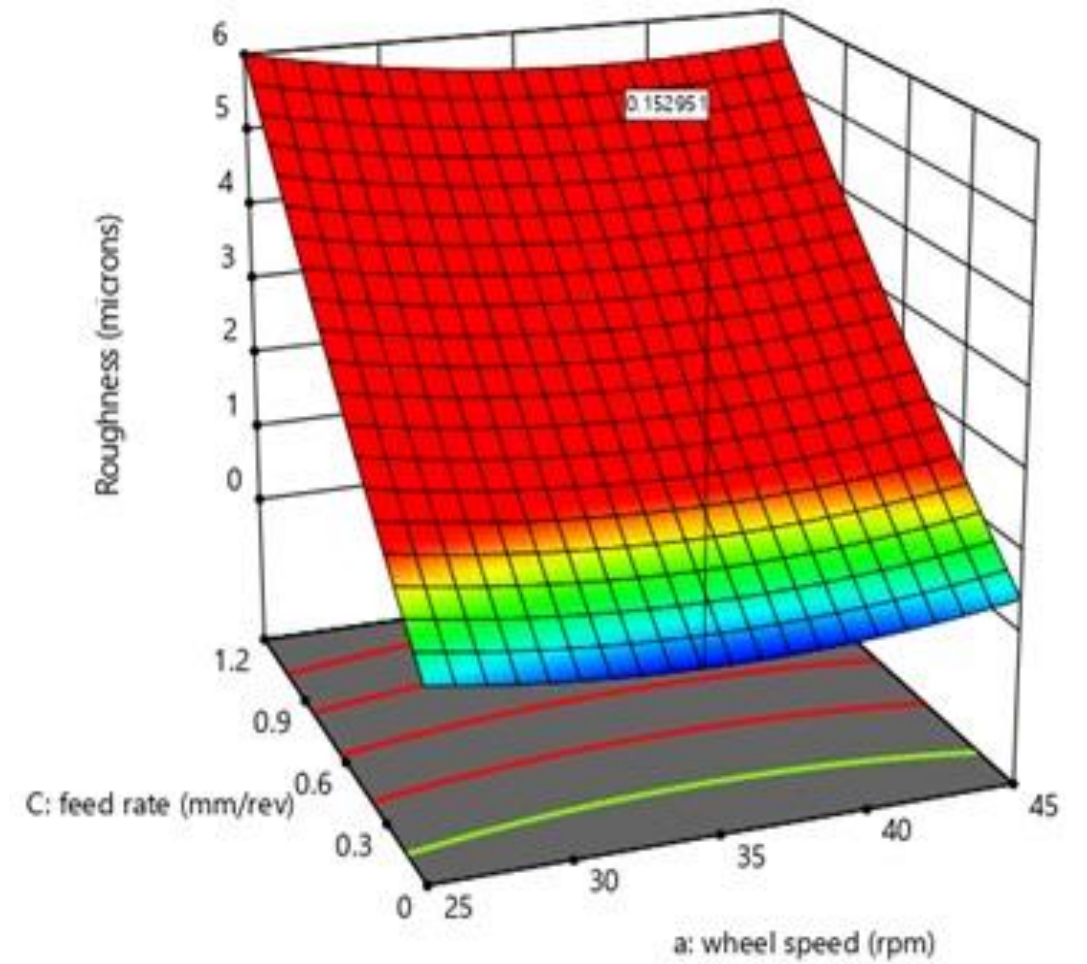
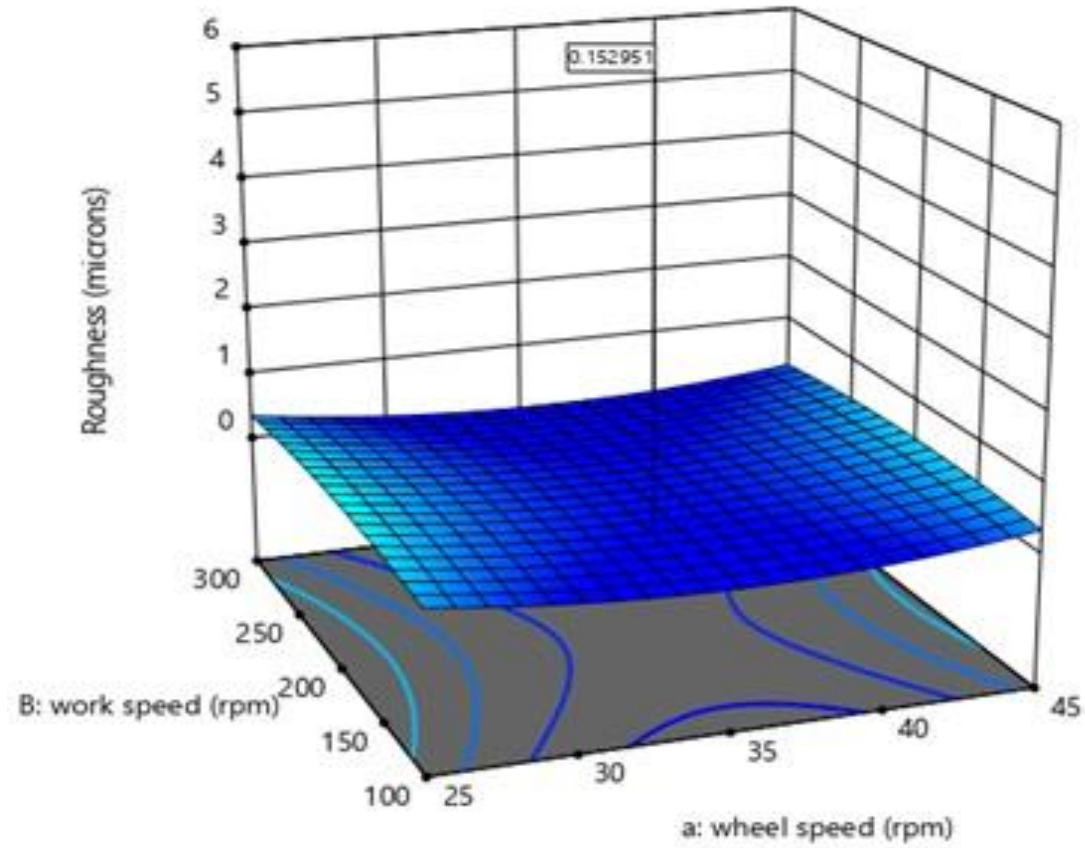


# Optimization

| wheel speed | work speed | feed rate | stage   |
|-------------|------------|-----------|---------|
| 40.2699     | 296.959    | 1.02722   | 1.71848 |



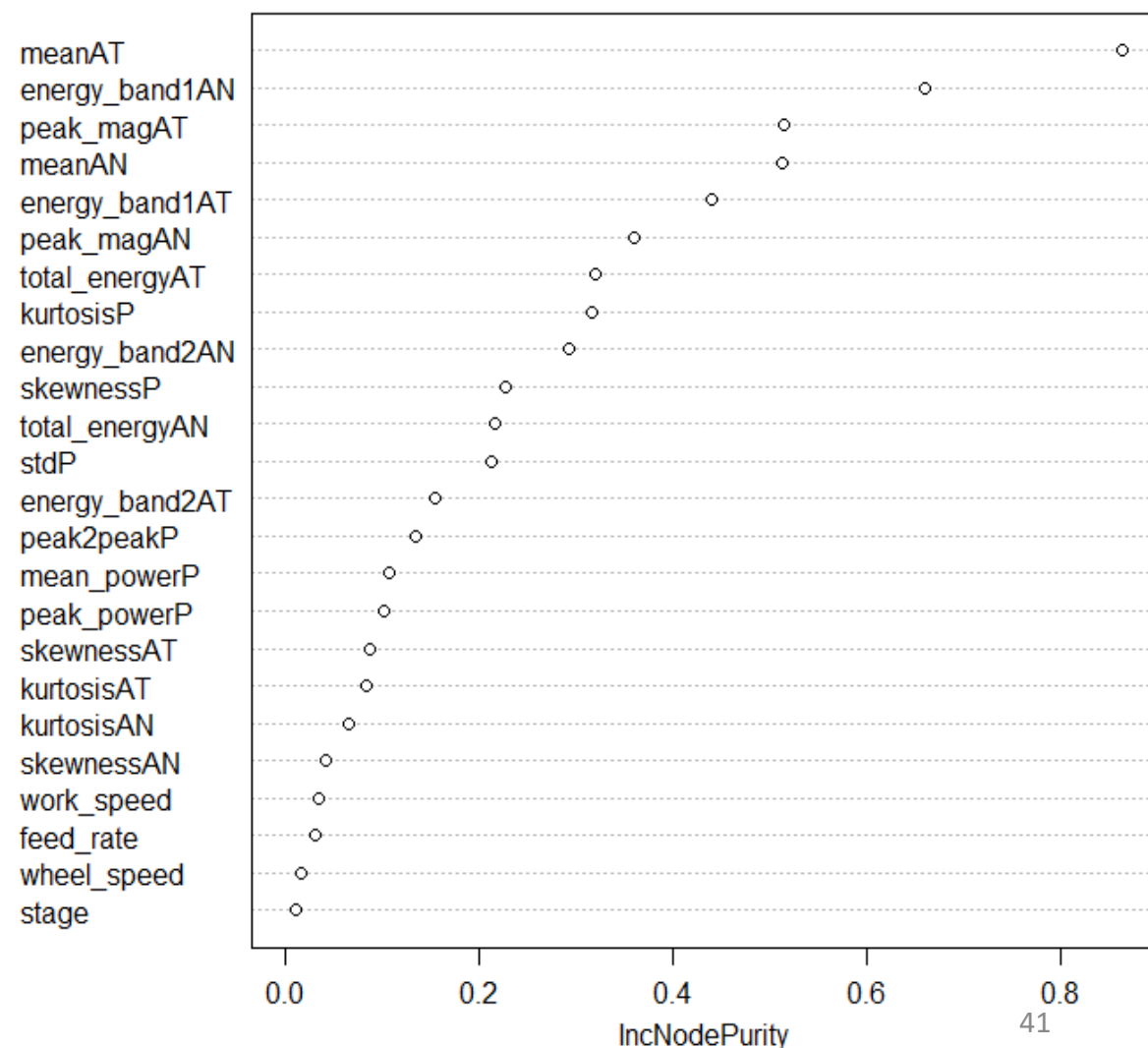
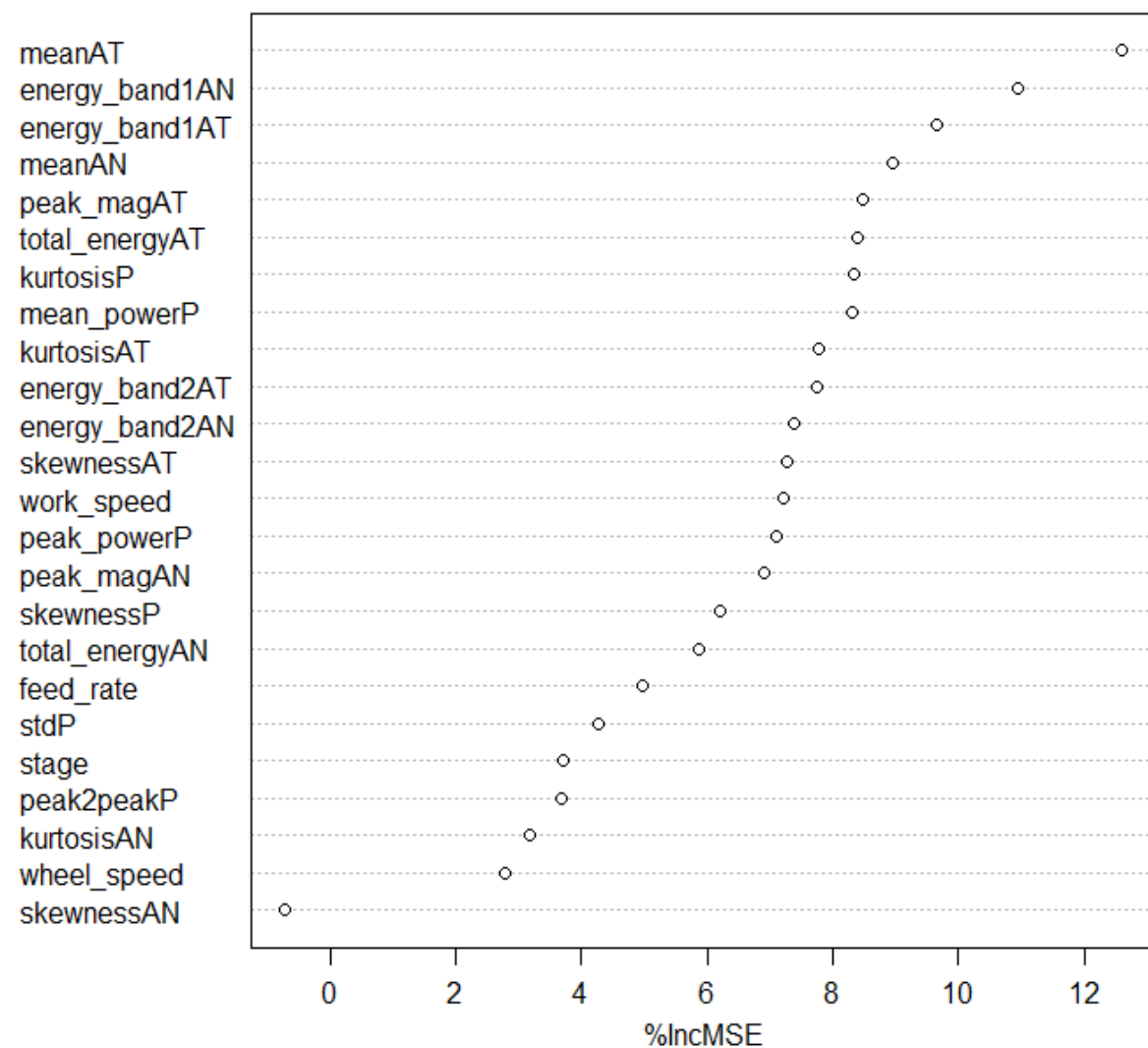
Desirability = 1.000  
Solution 1 out of 100





# Case 2

rf.grinding



# Conclusion

| Model                                      | Significant Parameters                  |                |            |
|--------------------------------------------|-----------------------------------------|----------------|------------|
| Only process parameter                     | Wheel speed, (wheel speed) <sup>2</sup> |                |            |
|                                            | Wheel speed* work speed                 |                |            |
|                                            | Wheel speed* work speed*feed rate       |                |            |
| Process, Acceleration and Power Parameters | Process                                 | Acceleration   | Power      |
|                                            | Work speed                              | Mean AT        | Kurtosis   |
|                                            | Feed rate                               | Energy band AN | Mean power |
|                                            | Stage                                   | Mean AN        |            |
|                                            | Wheel speed                             | Energy band AN |            |

# Quotes

- *Every company has big data in its future and every company will eventually be in the data business.”- **Thomas H. Davenport***
- *“Big data will replace the need for 80% of all doctors”- **Vinod Khosla***
- *“Information is the oil of the 21st century, and analytics is the combustion engine”- **Peter Sondergaard**, Senior Vice President at Gartner*
- *“Data are becoming the new raw material of business.”- **Craig Mundie**, Senior Advisor to the CEO at Microsoft.*

# Learnings

- Implementation of algorithms in R and Python
- Modelling in design expert
- Optimization
- Approach to solve the big data problem

Thank you