Objective:

```
->Dataset from kaggle contains images, each image is of size 28*28~\mathrm{p} ixels
```

- ->Each image is of 784 dimesnions
- ->Reducing the dimensionality by using dimensionality reduction tech niques like PCA, t-SNE

In [3]:

```
#MNIST dataset from kaggle

#Importing required libraries

import numpy as np
import pandas as pd
import matplotlib.pyplot as mp
```

loading the data

In [4]:

```
data = pd.read_csv("train.csv")
```

Analyzing the data features

In [5]:

```
print(data.shape)
print(data.columns)
print(data.ndim)
print(data.head(5))
(42000, 785)
Index(['label', 'pixel0', 'pixel1', 'pixel2', 'pixel3', 'pixel4', 'pixel5',
       'pixel6', 'pixel7', 'pixel8',
       'pixel774', 'pixel775', 'pixel776', 'pixel777', 'pixel778', 'pixel77
91,
       'pixel780', 'pixel781', 'pixel782', 'pixel783'],
      dtype='object', length=785)
2
   label
         pixel0 pixel1
                           pixel2
                                    pixel3 pixel4 pixel5
                                                              pixel6
                                                                       pixel7
0
                                          0
       1
                0
                         0
                                 0
                                                   0
                                                            0
                                                                    0
                                                                             0
       0
                0
                         0
                                          0
                                                            0
                                                                             0
1
                                  0
                                                   0
                                                                    0
2
       1
                0
                         0
                                  0
                                          0
                                                   0
                                                            0
                                                                    0
                                                                             0
3
       4
                0
                         0
                                 0
                                          0
                                                   0
                                                            0
                                                                    0
                                                                             0
       0
                0
                         0
                                 0
                                          0
                                                   0
                                                            0
                                                                    0
   pixel8
                      pixel774 pixel775 pixel776
                                                       pixel777
                                                                 pixel778
                              0
                                         0
0
        0
                                                    0
                                                               0
                                                                          0
                                                    \cap
                                                               \cap
                                                                          \cap
```

2 3 4	0 0 0		0 0 0	0 0 0	0 0 0	0 0 0	0 0 0
0 1 2 3 4	pixel779 0 0 0 0 0	pixel780 0 0 0 0 0	pixel781 0 0 0 0 0	pixel782 0 0 0 0 0	pixel783 0 0 0 0 0		
[5 rows x 785 columns]							

Observations:

->The dataset contains of 42000 images each of 784 dimesnions
->Label is the class type to which the image belongs to
->So we have to seperate the label data and continue with the proces

Taking the label from the data frame and removing the label feature from the dataframe

In [8]:

S

```
l = data['label']
data = data.drop('label',axis=1)
print(l.shape)
print(data.shape)

(42000,)
(42000, 784)
```

- ->To plot the image we have to convert the datapoint which is an array from 1-d to 2-d
- ->At the same time we can check with the label for accuracy

In [10]:

```
index = 10000
grid_data = data.iloc[index].as_matrix().reshape(28,28)
mp.imshow(grid_data,interpolation='none',cmap='Blues')
mp.show()
print(l[index])
```



```
25 - 10 15 20 25
```

2D Visualization using PCA without Scikit-Learn

->Keeping in consideration about the RAM and time efficiency, taking the subset of data

In [11]:

```
label = 1.head(20000)
dataframe = data.head(20000)
print(label.shape)
print(dataframe.shape)
print(l.shape)
print(data.shape)

(20000,)
(20000, 784)
(42000,)
(42000, 784)
```

Note:

->Using sklearn is a simple process, but without sklearn we need to process bunch of steps:

->Data-preprocessing-Standardizing of data is mandatory(mean=0 a
nd variance=1)

->Computing the co-variance matrix

->Generating the top two eigen vectors to plot on the 2-dimension plane, this can be done using eigh from scipy.linalg

->This will return the eigen values in the ascending order, Sinc e we are doing on 2-d we can take top two values

In [12]:

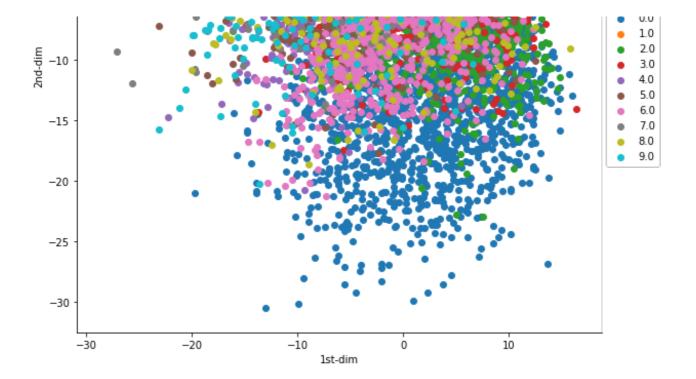
```
from sklearn.preprocessing import StandardScaler
standarad_data = StandardScaler().fit_transform(dataframe)
print(standarad_data.shape)

(20000, 784)
```

In [13]:

```
standarad_data_1 = standarad_data
co_var_matrix = np.matmul(standarad_data_1.T, standarad_data_1)
print(co_var_matrix_shape)
```

```
httmr(co_var_martrx.smahe)
(784, 784)
In [17]:
from scipy.linalg import eigh
value, vector = eigh(co var matrix, eigvals=(782, 783))
vector = vector.T
new cord = np.matmul(vector, standarad data 1.T)
print (vector.shape)
print(standarad data 1.T.shape)
(2, 784)
(784, 20000)
In [15]:
new cord.shape
Out[15]:
(2, 20000)
Appending the label data to plot
In [18]:
new cord = np.vstack((new cord, label)).T
In [21]:
df = pd.DataFrame(data=new cord,columns=('1st-dim','2nd-dim','label'))
print(df.shape)
print(df.head(6))
import seaborn as s
s.FacetGrid(df,hue='label',size=8).map(mp.scatter,'1st-dim','2nd-dim').add
legend()
mp.show()
(20000, 3)
    1st-dim
              2nd-dim label
0 5.430697
            5.060862
                           1.0
1 -6.242999 -19.293148
                          0.0
  1.828611
             7.684498
                           1.0
                          4.0
             0.440132
3 -5.585495
4 -6.333250 -26.597773
                          0.0
5 0.659000 -1.280238
                           0.0
    10
    5
    0
```



PCA Using Scikit-Learn

- -> It becomes very easy when using Scikit-Learn library
- ->We just need to inform the number of dimesnions and then we need to add the labels to the data
- ->Should create a dataframe to plot as just as we done on above

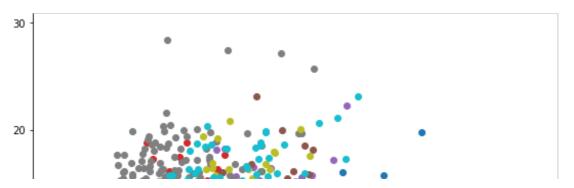
In [23]:

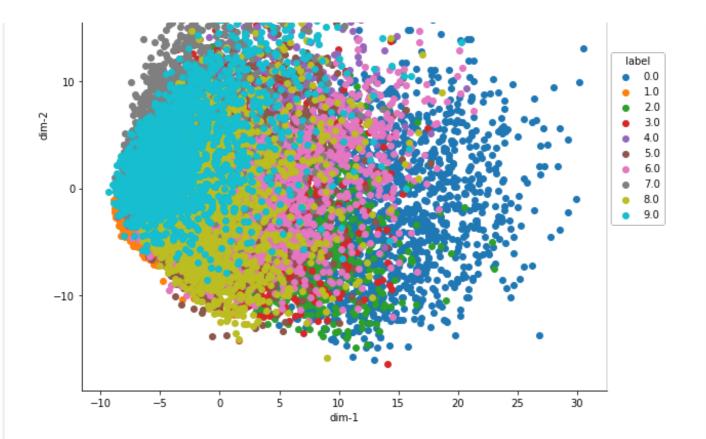
```
from sklearn import decomposition
pca = decomposition.PCA()
pca.n_components=2
pca_data = pca.fit_transform(standarad_data_1)
print(standarad_data_1.shape)
pca_data = np.vstack((pca_data.T,label)).T
print(pca_data.shape)

(20000, 784)
(20000, 3)
```

In [24]:

```
pca_data_df = pd.DataFrame(data=pca_data,columns=('dim-1','dim-2','label'))
s.FacetGrid(pca_data_df,hue='label',size=8).map(mp.scatter,'dim-1','dim-2')
.add_legend()
mp.show()
```





Note:

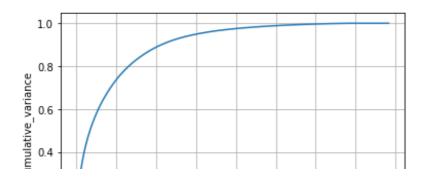
- $\mbox{->We}$ can use PCA not only for dimensionality reduction but also for picking the most useful dimensions
- ->When the dimension were 2 or 3 then it is for visualization
- ->Based on the application we can reduce our dimensions

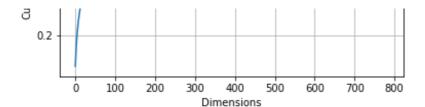
In [26]:

```
pca.n_components = 784
pca_data = pca.fit_transform(standarad_data_1)
variance_percentage =
pca.explained_variance_/np.sum(pca.explained_variance_)
cumulative_variance = np.cumsum(variance_percentage)
mp.plot(cumulative_variance)
mp.grid()
mp.xlabel('Dimensions')
mp.ylabel('Cumulative_variance')
```

Out[26]:

Text(0,0.5,'Cumulative variance')





Observation:

- ->If we go for 100-dimensions then 77 percent of data spread is used .
- $\operatorname{\mathsf{->}If}$ we want 90 of data to be used then we have to choose 200-dimens ions

t-SNE using Scikit-Learn:

- $\ \ \ ->$ We just need to mention the number of components required
- ->Perplexity to understand complexity which gives better \dot{z} n the range from 30 to 50
 - ->Number of Iterations for optimaztion
- $\ \ ->$ We train the model with 2 components and then fit our data to that model
- $\ \ ->$ Then we add our label to the modeled data and then we c reate our normal dataframe

with column names

->By using seaborn we can plot our tsne results

1

In [28]:

```
from sklearn.manifold import TSNE
print(standarad_data_1.shape)
print(label.shape)

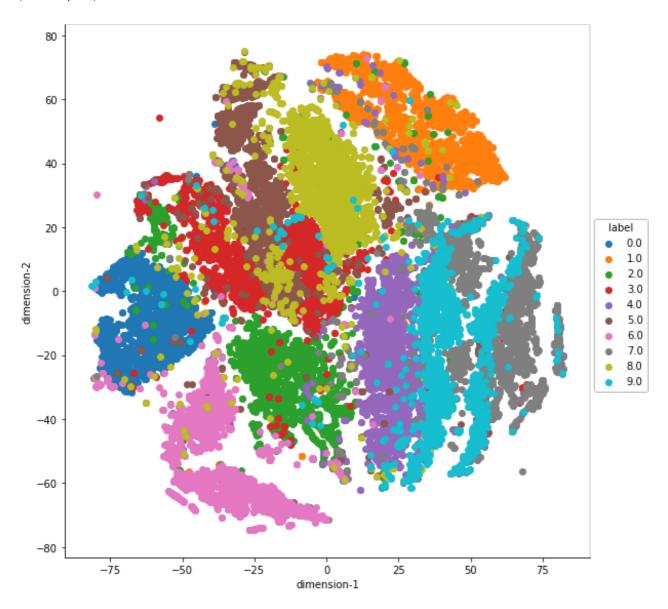
(20000, 784)
(20000,)
```

In [36]:

```
model = TSNE (n_components=2)
tsne_data = model.fit_transform(standarad_data_1)
print(tsne_data.shape)
print(label.shape)
tsne_data_model_= np_vstack((tsne_data_T_label))_T
```

```
print(tsne_data_model.shape)
tsne_model_df = pd.DataFrame(data=tsne_data_model,columns=('dimension-1','d
imension-2','label'))
s.FacetGrid(tsne_model_df,hue='label',size=8).map(mp.scatter,'dimension-1',
'dimension-2').add_legend()
mp.show()
```

```
(20000, 2)
(20000,)
(20000, 3)
```



Note:

->We have to try this same model for different perplexity values and number of iterations

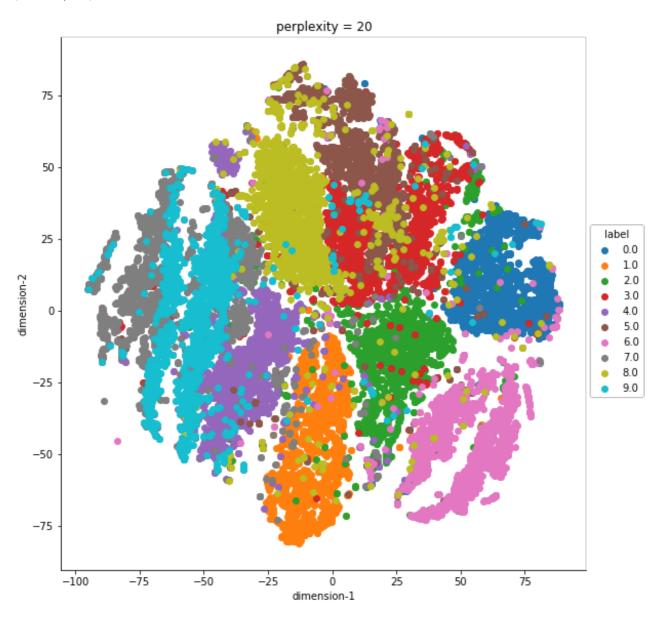
 $\ -> Getting$ the best from t-SNE mean that by analyzing multiple graphs with different perplexity values

t-SNE with perplexity of 20

In [37]:

```
model = TSNE(n_components=2,random_state=998,perplexity=20)
tsne_model = model.fit_transform(standarad_data_1)
tsne_model = np.vstack((tsne_model.T,label)).T
print(tsne_model.shape)
tsne_model_df = pd.DataFrame(data=tsne_model,columns=('dimension-1','dimension-2','label'))
s.FacetGrid(tsne_model_df,hue='label',size=8).map(mp.scatter,'dimension-1',
'dimension-2').add_legend()
mp.title('perplexity = 20')
mp.show()
```

(20000, 3)



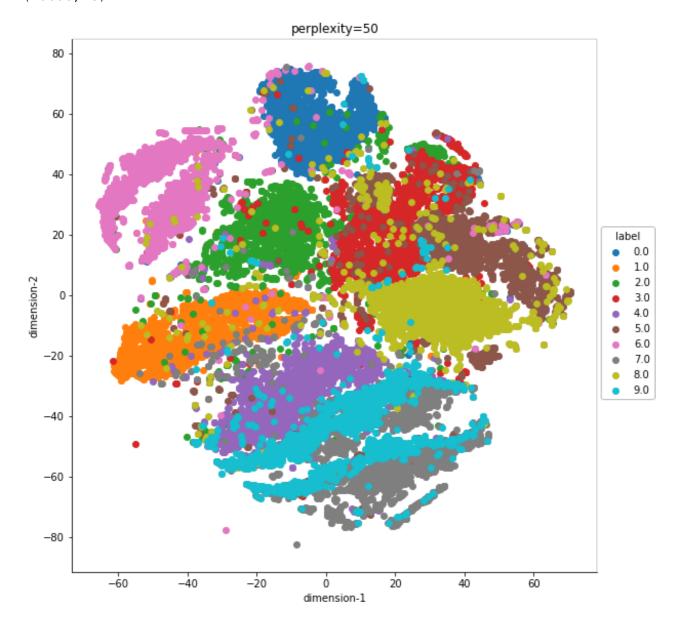
t-SNE with perplexity of 50

In [38]:

```
model = TSNE(n_components=2,random_state=997,perplexity=50)
tsne_model = model.fit_transform(standarad_data_1)
tsne_model = np.vstack((tsne_model.T,label)).T
print(tsne_model.shape)
tsne_model_df = pd.DataFrame(data=tsne_model,columns=('dimension-1','dimension-2','label'))
s.FacetGrid(tsne_model_df,hue='label',size=8).map(mp.scatter,'dimension-1',
'dimension-2').add_legend()
```

```
mp.title("perplexity=50")
mp.show()
```

(20000, 3)



t-SNE with perplexity 50 and number of iterations as 2000

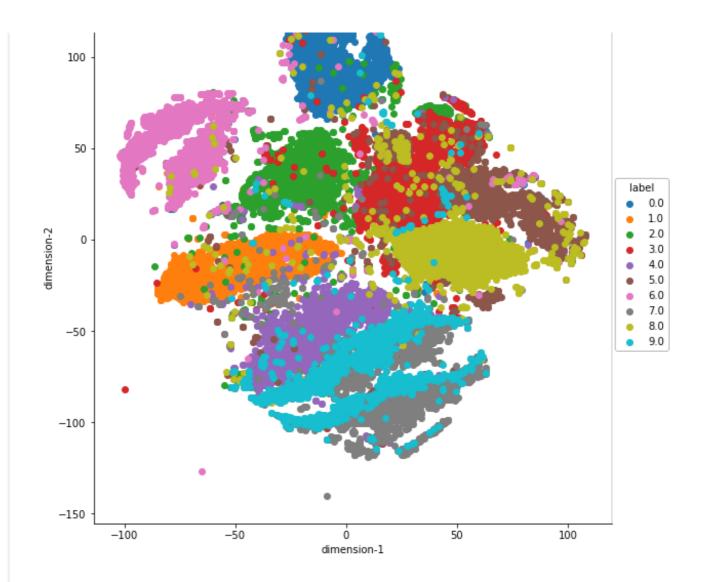
In [39]:

(20000, 3)

```
model = TSNE(n_components=2,random_state=997,perplexity=50,n_iter=2000)
tsne_model = model.fit_transform(standarad_data_1)
tsne_model = np.vstack((tsne_model.T,label)).T
print(tsne_model.shape)
tsne_model_df = pd.DataFrame(data=tsne_model,columns=('dimension-1', 'dimension-2', 'label'))
s.FacetGrid(tsne_model_df,hue='label',size=8).map(mp.scatter,'dimension-1',
'dimension-2').add_legend()
mp.title("perplexity=50 and iterations=2000")
mp.show()
```



perplexity=50 and iterations=2000



Conclusion:

- -> PCA will tries to preserve the global shape of the data
- $\mbox{-->}\mbox{ t-SNE}$ will tries to preserve the local shape of the data and it tries to preserve the
 - global shape of the data
- $\mbox{-->}\mbox{ t-SNE}$ tries to embed the points from high dimensionality to low d imesnionality by
 - preserving the distance of local clusters