

PRACTICAL NO: -	1
PRACTICAL NAME:-	Bisection Method
STUDENT NAME: -	Simran.V.Akhade
DIV & ROLL NO:-	B(mech) - 04



Solⁿ of algebraic & Transcendental eqⁿ :-

find Root of eqⁿ

$$2x^3 + 4x^2 - 8 = 0$$

use bisection method Do 3 Iterations

consider initial guesses as 1 & 1.5

ns:

$$\text{Data } y = f(x) = 2x^3 + 4x^2 - 8 = 0$$

$$\text{Initial guess } x_1 = 1$$

$$x_2 = 1.5$$

No. of Iteration = 3

p1) apply convergence criterion to check whether initial guess are accurate or not.

$$y = f(x) = 2x^3 + 4x^2 - 8 = 0 \quad \text{--- (1)}$$

with x_1 as 1 put $x_1 = 1$ in eq (1)

$$\therefore y_1 = f(x) = 2 \times 1^3 + 4 \times 1^2 - 8 = 0$$

$$= 2 + 4 - 8$$

[= -2 Negative]

similarly, put $x_2 = 1.5$ in eq (1)

$$\therefore y_2 = f(x) = 2 \times 1.5^3 + 4 \times 1.5^2 - 8 = 0$$

[= 7.75 Positive]

Now, from eq (2) & (3) $y_1 \times y_2 = f(x_1) \times f(x_2)$

$$f(x_1) \times f(x_2) = -2 \times 7.75 = -15.5 < 0$$

Hence, convergence criterion is satisfied

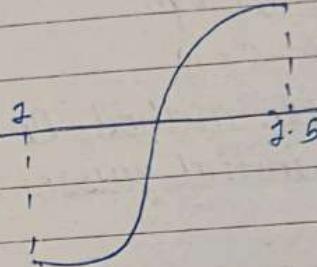


∴ Root of eqn will be calculated with initial guess

$$x_1 = 1, x_2 = 1.5$$

As per data,
we have to consider
bisection method
[i.e Brackets Method]

$$x_1 = 1, x_2 = 1.5$$



① Iteration

$$x_3 = \frac{x_1 + x_2}{2} = \frac{1+1.5}{2} = 1.25$$

$$\begin{aligned} f(x_3) &= 2x^3 + 4x^2 - 8 = 0 \\ &= 2 \times (1.25)^3 + 4 \times (1.25)^2 - 8 \\ &= 2.15 \text{ [Positive]} \end{aligned}$$

② Iteration $x_1 = 1 \neq x_2 = 2.15$

$$x_3 = \frac{x_1 + x_2}{2} = \frac{1+2.15}{2} = 1.125$$

$$\begin{aligned} f(x) &= 2 \times 1.125^3 + 4 \times 1.125^2 - 8 \\ &= -0.0898 \text{ [Negative]} \end{aligned}$$

③ Iteration $x_1 = 1.25 \quad x_2 = 1.125$

$$x = \frac{x_1 + x_2}{2} = \frac{1.25 + 1.125}{2} = 1.1875$$

$$\begin{aligned} f(x) &= 2x^3 + 4x^2 - 8 = 0 \\ &= 2 \times (1.1875)^3 + 4 \times (1.1875)^2 - 8 \\ &= 0.98 \text{ [Positive].} \end{aligned}$$

```
f = input('
x1 = input(
x2 = input(
n = input('
y1 = f(x1);
y2 = f(x2);

while (y1*y2)
    x1 = i
    x2 = i
    y1 = f
    y2 = f
end

for i = 1:
    x3 = (
    y3 = f
    if (y1
        x2
        y2
    else
        x1
        y1
    end
end

fprintf('
Output
```

```
Bisection
enter func @ (x) (2*x*
enter 1st
1
enter 1st
1.5
enter no
3
The ro
```

Bisection Method

```

f = input('enter function y = f(x) = ');
x1 = input('enter 1st initial guess x1 = ');
x2 = input('enter 1st initial guess x2 = ');
n = input('enter no of iterations n = ');
y1 = f(x1);
y2 = f(x2);

while (y1*y2 > 0)
    x1 = input('enter 1st initial guess again x1 = ');
    x2 = input('enter 1st initial guess again x2 = ');
    y1 = f(x1);
    y2 = f(x2);
end

for i = 1:n
    x3 = (x1+x2)/2;
    y3 = f(x3);
    if (y1*y3 < 0)
        x2 = x3;
        y2 = y3;
    else
        x1 = x3;
        y1 = y3;
    end
end

fprintf('\n The root of equation is = %f',x3);

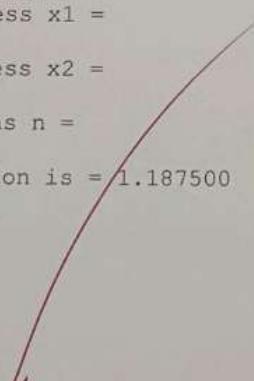
```

Output

```

Bisection28B.mlx
enter function y = f(x) =
@(x) (2*x*x*x) + (4*x*x) - 8
enter 1st initial guess x1 =
1
enter 1st initial guess x2 =
1.5
enter no of iterations n =
3
The root of equation is = 1.187500

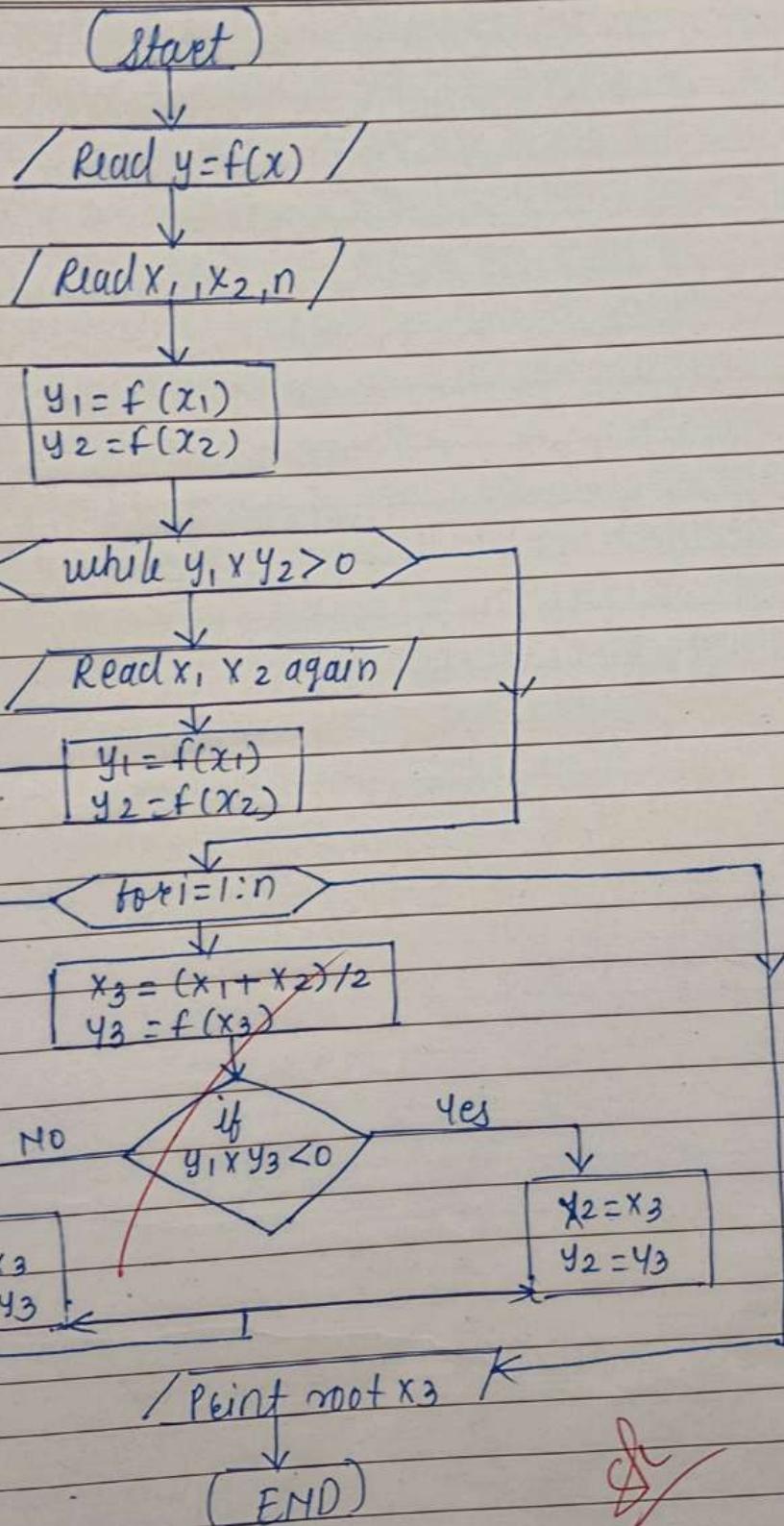
```



Shubh
 6/8/23



option





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PRACTICAL NO:-	2
PRACTICAL NAME :-	NEWTON RAPHSON METHODS
STUDENT NAME :-	SIMRAN . V. AKHADE
DIV 4 ROLL NO :-	B(mech) - 04



Newton Raphson Methods

$$y = f(x) = x^3 - 5x + 3$$

ta $y = f(x) = x^3 - 5x + 3$

Initial guess $x_1 = 0$

No. of iteration = 3

$$y = f(x) = x^3 - 5x + 3 \quad \text{--- ①}$$

$$y' = f'(x) = 3x^2 - 5 \quad \text{--- ②}$$

$$y'' = f''(x) = 6x \quad \text{--- ③}$$

$$\begin{aligned} y = f(x) &= x^3 - 5x + 3 \\ &= 0^3 - 5(0) + 3 \end{aligned}$$

$$y_1 = f(x_1) = 3$$

$$\begin{aligned} y'_1 &= f(x_1) = 3x^2 - 5 \\ &= 3(0)^2 - 5 \end{aligned}$$

$$\begin{aligned} y''_1 &= f''(x) = 6x \\ &= 6(0) \end{aligned}$$

$$y''_1 = f''(x) = 0$$

By Newton Raphson Method

Iteration 1

$$x_2 = x_1 - \frac{f(x_1)}{f'(x_1)}$$

$$\therefore x_2 = 0 - \frac{3}{-5}$$

$$x_2 = 0.6$$



place x_1 by x ,

$$x = 0.6$$

$$\begin{aligned}f(x_1) &= x^3 - 5x + 3 \\&= 0.6^3 - 5(0.6) + 3\end{aligned}$$

$$f(x) = 0.216$$

$$f'(x) = 3x^2 - 5 = 3(0.6)^2 - 5$$

$$f'(x) = -3.92$$

$$f''(x) = 6x = 6 \times 0.6$$

$$f''(x) = 3.6$$

solution 2

$$x_1 = -\frac{f(x_1)}{f'(x)}$$

$$x_2 = 0.655$$

place x_1 by x_2

= 0.6551 substitute the value from eq ①②③

$$\begin{aligned}f(x) &= x^3 - 5x + 3 \\&= 0.6551^3 - 5(0.6551) + 3 \\&= 0.0056\end{aligned}$$

$$\begin{aligned}f'(x) &= 3x^2 - 5 \\&= 3(0.6551)^2 - 5 \\&= -3.7125\end{aligned}$$

$$\begin{aligned}f''(x) &= 6x = 6 \times 0.6551 \\&= 3.9306\end{aligned}$$



solution 3

$$\therefore x_2 = x_1 - \frac{f(x)}{f'(x)}$$

$$x_2 = 0.6566$$

solution	x_1	y_1	y'	x
1	0	3	-5	0.6
2	0.6	0.216	-3.92	0.6551
3	0.6551	0.6056	-3.7125	0.6566

The root of eq is $0.6, 0.6551 \text{ & } 0.6566$
final root of eq is $= 0.6566$

```

input('enter function y = f(x) = ');
= input('enter 1st derivation = ');
if = input('enter 2nd derivation = ');
= input('enter 1st initial guess x1 = ');
= input('enter no of iteration n = ');
= f(x1);
= df(x1);
3 = ddf(x1);
= (y1*y3)/(y2*y2);
while (abs(a) > 1)

x1 = input('enter 1st initial guess again x1 = ');
y1 = f(x1);
y2 = df(x1);
y3 = ddf(x1);
a = (y1*y3)/(y2*y2);

end

for i = 1:n

x2 = x1 - (y1/y2);
fprintf('\n The root of equation is = %f',x2);
x1 = x2;
y1 = f(x1);
y2 = df(x1);

end

fprintf('\n Final root of equation is = %f',x2);

OUTPUT
newtonraphson
enter function y = f(x) =
@(x) (x*x*x)-(5*x)+3
enter 1st derivation =
@(x) (3*x*x)-5
enter 2nd derivation =
@(x) (6*x)

```

enter 1st initial guess x_1 =

0

enter no of iteration n =

3

The root of equation is = 0.600000

The root of equation is = 0.655102

The root of equation is = 0.656619

Final root of equation is = 0.656619

S. Sankar
6/8/20



Newton-Raphson
method

(start)



Read $y = f(x)$
Read $y' = df(x)$
Read $y'' = ddf(x)$



Read x_1, n



$y_1 = f(x_1)$
 $y_2 = df(x_1)$
 $y_3 = ddf(x_1)$

$$a = \frac{y_1 \times y_3}{y_2 \times y_2}$$



while $|\text{abs}(a)| > 1$

Read x_1 , again



$y_1 = f(x_1)$
 $y_2 = df(x_1)$
 $y_3 = ddf(x_1)$

$$a = \frac{y_1 \times y_3}{y_2 \times y_2}$$

for $i=1:n$

$$x_2 = x_1 - \frac{y_1}{y_2}$$

$$x_1 = x_2$$

$$y_1 = f(x_1)$$

$$y_2 = df(x_1)$$

Print $x_0 + x_2$

(END)

8/



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PRACTICAL NO :-	3.
PRACTICAL NAME :-	GAUSS ELIMINATION
STUDENT NAME :-	SIMRAN.V.AKHADE
DIV & ROLL NO :-	B(mech)- 04



Gauss elimination

Solve the following eq's by gauss elimination

$$x + 3y + 3z = 16 \quad \text{--- } ①$$

$$x + 4y + 3z = 18 \quad \text{--- } ②$$

$$x + 3y + 4z = 19 \quad \text{--- } ③$$

: do by gauss elimination to solve eq's:

Convert given system of eq's into the matrix.

$$(Ax = B)$$

$$\left[\begin{array}{ccc|c} 1 & 3 & 3 & x \\ 1 & 4 & 3 & y \\ 1 & 3 & 4 & z \end{array} \right] = \left[\begin{array}{c} 16 \\ 18 \\ 19 \end{array} \right]$$

Convert this matrix into upper triangular matrix

$$R_2 \rightarrow R_2 - R_1$$

$$\left[\begin{array}{ccc|c} 1 & 3 & 3 & x \\ 0 & 1 & 0 & y \\ 1 & 3 & 4 & z \end{array} \right] = \left[\begin{array}{c} 16 \\ 2 \\ 19 \end{array} \right]$$

$$R_3 \rightarrow R_3 - R_1$$

$$\left[\begin{array}{ccc|c} 1 & 3 & 3 & x \\ 0 & 1 & 0 & y \\ 0 & 0 & 1 & z \end{array} \right] = \left[\begin{array}{c} 16 \\ 2 \\ 3 \end{array} \right]$$



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Therefore we get,
 $z = 3$ and
 $y = 2$

Now, put value of $z=3$ & $y=2$ in eq

$$x + 3y + 3z = 16$$

$$x + (3 \times 2) + 3(3) = 16$$

we get $x = 1$

Ans:

$$z = 3$$

$$y = 2$$

$$x = 1$$

```
Simran A
% Roll No
% Gauss
a = input('
b = input('
n = length(
% Upper T
for i = 1:n
    for k = i+1:n
        f = a(k,:)
        a(k,:) =
        b(k) =
    end
end
x = zeros(n,1
% Backward :
for i = n:-1:1
    x(i) = (b(i) -
    fprintf("\nThe
end
OUTPUT
Enter matrix a:
[1,3,3;1,4,3;1,3,
Enter matrix b:
[16;18;19]
The value of x(3
```

Simran Akhadet

% Roll No.04

% Gauss Elimination Method

```
a = input('Enter matrix a:'); % Coefficient matrix  
b = input('Enter matrix b:'); % Constant Matrix  
n = length(b);
```

in eq

% Upper Triangular Matrix

```
for i = 1:n  
    for k = i+1:n  
        f = a(k,i) / a(i,i); % Factor  
        a(k,:) = a(k,:) - f * a(i,:);  
        b(k) = b(k) - f * b(i);  
    end  
end
```

x = zeros(n,1);

% Backward Substitution

```
for i = n:-1:1  
    x(i) = (b(i) - a(i,i+1:n) * x(i+1:n)) / a(i,i);  
    fprintf("\nThe value of x(%d) = %f, i, x(i));  
end
```

OUTPUT

Enter matrix a:

[1,3,3;1,4,3;1,3,4]

Enter matrix b:

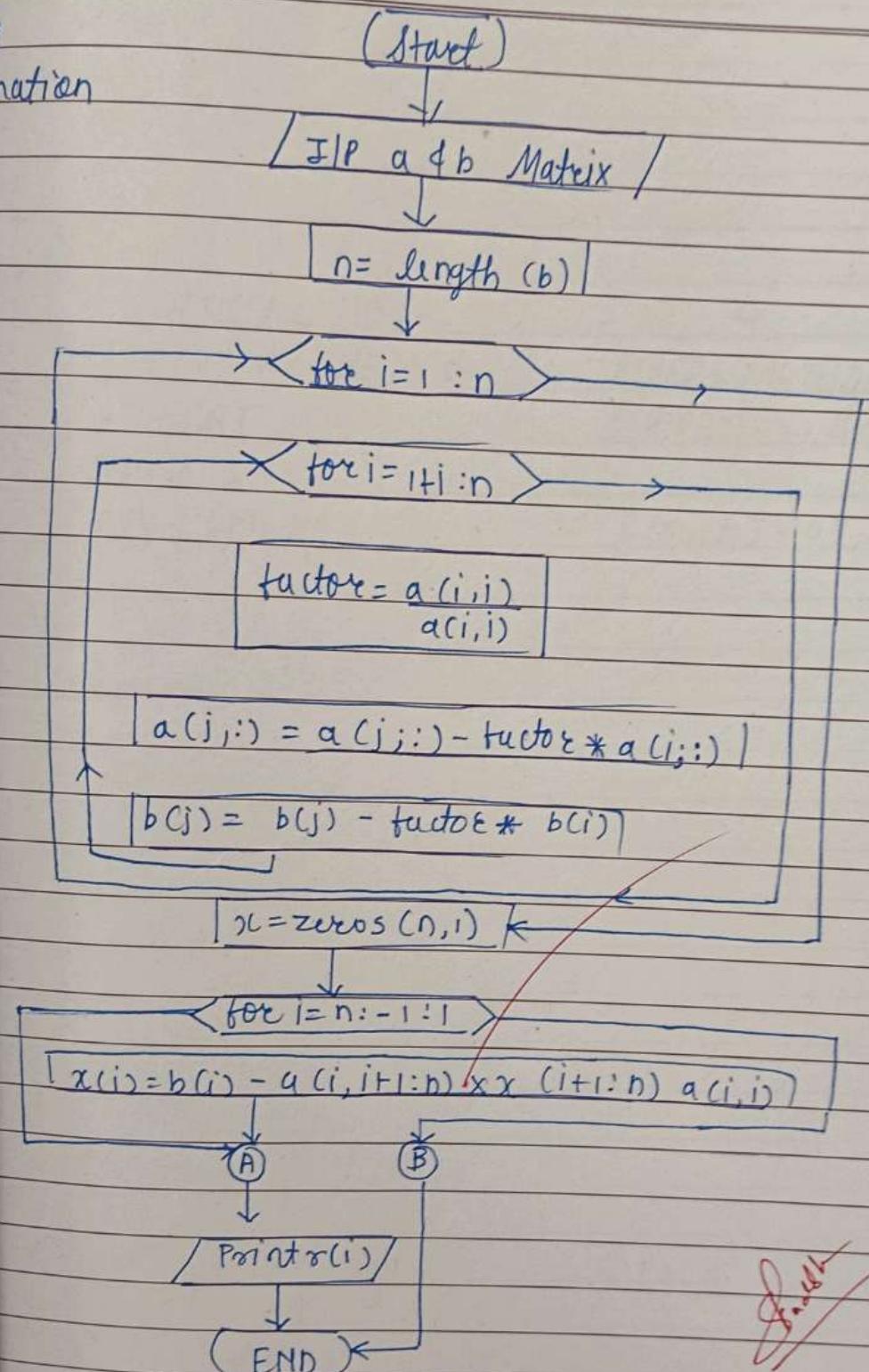
[16;18;19]

```
The value of x(3) = 3.000000  
The value of x(2) = 2.000000  
The value of x(1) = 1.000000
```



us

niation



✓



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ROLL NO :- 3290

PRACTICAL NO :-

4

PRACTICAL NAME :-

EULER'S METHOD

STUDENT

SIMRAN · V · AKHADE.

NAME :-

DIV & ROLL NO :-

B (mech) - 04



Euler's Method

$\frac{dy}{dx} = x - y^2$ for given boundary condition
that at $x_0 = 0$, $y_0 = 1$

find y_g at $x_g = 4$, take step size $h = 2$

∴ Data :- $\frac{dy}{dx} = x - y^2$

$$\text{at } x_0 = 0 \quad y_0 = 1$$

$$x_g = 4 \quad y_g = ?$$

$$\text{Here } h = 1$$

Step 1: calculate no. of iteration

$$n = \frac{x_g - x_0}{h} = \frac{4 - 0}{2} = 4$$

as per Euler's method :-

$$y_g = y_0 + h \times (f(x_0, y_0))$$

Iteration 1: at $x_0 = 0 \quad y_0 = 1$

$$\therefore y_1 = 1 + 1 \times f(x_0, y_0) \\ = 1 + 1 \times [0 - 1^2] \\ = 0$$

$$x_1 = 1 \text{ we get } y_1 = 0$$

$$\text{where } x_1 = x_0 + h$$

$$x_1 = 0 + 1$$

$$x_1 = 1$$



Iteration no: 2 Replace x_0 by x_1 & y_0 by y_1

Here $x_1 = 1$ $y_1 = 0$

$$y_g = y_1 + h \times f(x_1, y_1)$$

$$y_g = 0 + 1 \times (1 - 0^2)$$

$$y_g = 1$$

$$x_2 = x_1 + h$$

$$x_2 = 1 + 1$$

$$x_2 = 2$$

at $x_2 = 2$ we get $y_2 = 1$

Iteration 3 : Replace x_1 by x_2 & y_1 by y_2

Here $x_2 = 2$ & $y_2 = 1$

$$y_g = y_2 + h \times f(x_2, y_2)$$

$$y_g = 1 + 1 \times [2 - 1^2]$$

$$y_g = 2$$

$$x_3 = x_2 + h$$

$$x_3 = 2 + 1$$

$$x_3 = 3$$

at $x_3 = 3$ we get $y_3 = 2$

Iteration 4 : Replace x_2 by x_3 & y_2 by y_3

Here $x_3 = 3$ & $y_3 = 2$

$$y_g = y_3 + h \times f(x_3, y_3)$$

$$= 2 + 1 \times [3 - 2^2]$$

$$y_g = 1$$

$$x_4 = x_3 + h$$

$$x_4 = 3 + 1$$

$$x_4 = 4$$

at $x_4 = 4$ we get $y_4 = 1$

% Simran Akhade

% Roll No:04 Mech

% Euler Method

f = input('\n Input function (dy/dx) = '); % Input the function directly

x0 = input('\n Enter the initial value of x (x0) = ');

y0 = input('\n Enter the initial value of y (y0) = ');

h = input('\n Input step size (h) = ');

xg = input('\n Enter the final value of x (xg) = ');

n = (xg - x0) / h; % Number of steps

for i = 1:n

 yg = y0 + h * f(x0, y0); % Euler's method calculation

 x0 = x0 + h; % Increment x value

 y0 = yg; % Update y value

end

 fprintf('the final value of yg = %f', yg);

output :-

Input function (dy/dx) =

@(x,y) (x-y*y)

Enter the initial value of x (x0) = 0

Enter the initial value of y (y0) = 1

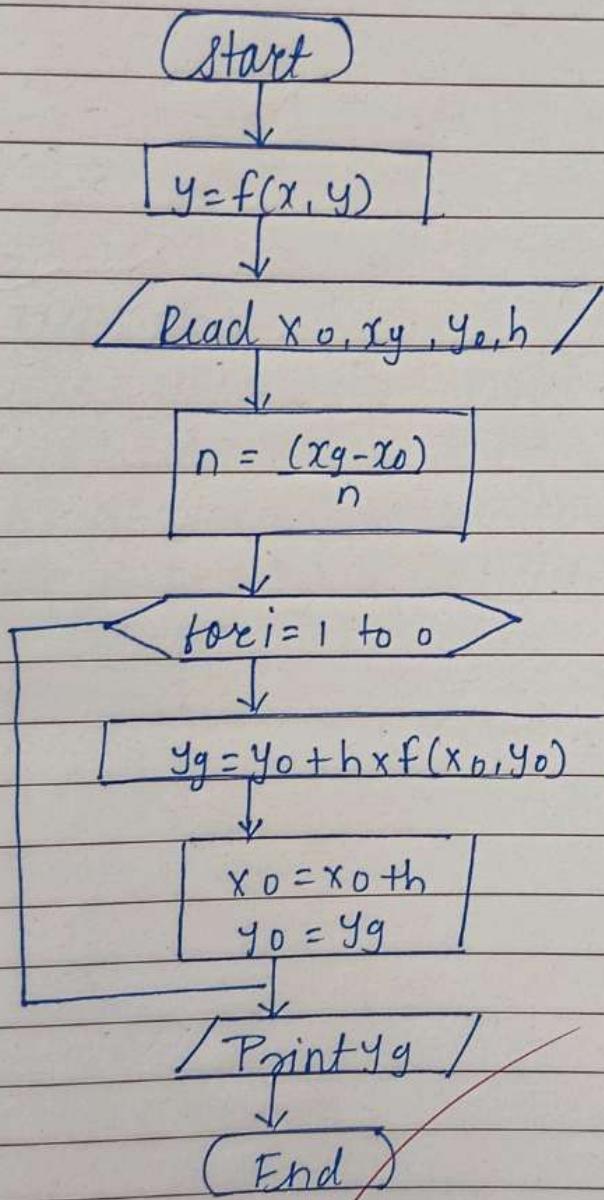
Input step size (h) = 1

Enter the final value of x (xg) = 4

the final value of yg = 1.000000



Euler's Method



S. D. M.



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PRACTICAL No :-	5
PRACTICAL NAME :-	RUNGE KUTTA 2 (RK2)
STUDENT NAME :-	SIMRAM. V. AKHADE
DIV & ROLL NO :-	B(mech) - 04



Runge - kutta (RK-2) method

$$\frac{dy}{dx} = x + y$$

where $x_0 = 0 \quad y_0 = 1$

here $h = 0.1$

find y_g at $x_g = 0.2$

Solution: Data :

$$y(0) = 1 \quad x(0) = 0$$

$$h = 0.1$$

$$\frac{dy}{dx} = f(x+y)$$

$$dx$$

Q1: To calculate no. of iteration

$$n = \frac{x_g - x_0}{h} = \frac{0.2 - 0}{0.1} = 2$$

Iteration no: 1

$$k = \frac{k_1 + k_2}{2}$$

$$= h \times f(x_0, y_0)$$

$$= 0.1 \times [0+1]$$

$$= 0.1$$

$$\text{where } x_1 = x_0 + h$$

$$x_1 = 0 + 0.1$$

$$x_1 = 0.1$$

$$= h \times f(x_0 + h, y_0 + k)$$

$$= 0.1 [0.1 + (1 + 0.1)]$$

$$= 0.12$$



$$\text{Here } k = \frac{k_1 + k_2}{2} = \frac{0.1 + 0.12}{2} = 0.11$$

$$\text{Here } y_g = y_0 + k \\ = 1 + 0.11$$

$$y_g = 1.11 \\ \text{at } x = 0.1 \text{ we get } y_g = 1.12.$$

Iteration 2 : Replace x_0 by x_1 & y_0 by y_1

$$k_1 = h \times f(x_1, y_1)$$

$$k_1 = 0.1 \times [0.1 + 1.11]$$

$$k_1 = 0.121$$

$$\text{Here } x_2 = x_1 + h$$

$$x_2 = 0.1 + 0.1$$

$$x_2 = 0.2$$

$$k_2 = h \times f(x_2, y_2 + k)$$

$$k_2 = 0.1 [(0.1 + 0.1) + (1.11 + 0.121)]$$

$$k_2 = 0.143$$

$$k = \frac{k_1 + k_2}{2} = \frac{0.121 + 0.143}{2} = 0.1320$$

$$y_g = y_1 + k$$

$$= 1.11 + 0.1320$$

$$y_g = 1.242$$

$$\text{at } x_2 = 0.2 \text{ we get } y_g = 1.242$$

```
f = input('Enter the function y= f(x):');
xo=input('enter the initial value of xo:');
yo=input('enter the initial value of yo:');
xg=input('enter the initial value of xg:');
h=input('enter the initial value of h:');
n=(xg-xo)/h;
for i=1:n
    k1=h*f(xo,yo);
    k2=h*f(xo+h,yo+k1);
    k=(k1+k2)/2;
    yg=yo+k;
    xo=xo+h;
    yo=yg;
end
fprintf('the final value of yg = %f',yg);
```

Output

Enter the function y= f(x):

@(x,y) (x+y)

enter the initial value of xo:

0

enter the initial value of yo:

1

enter the initial value of xg:

0.2

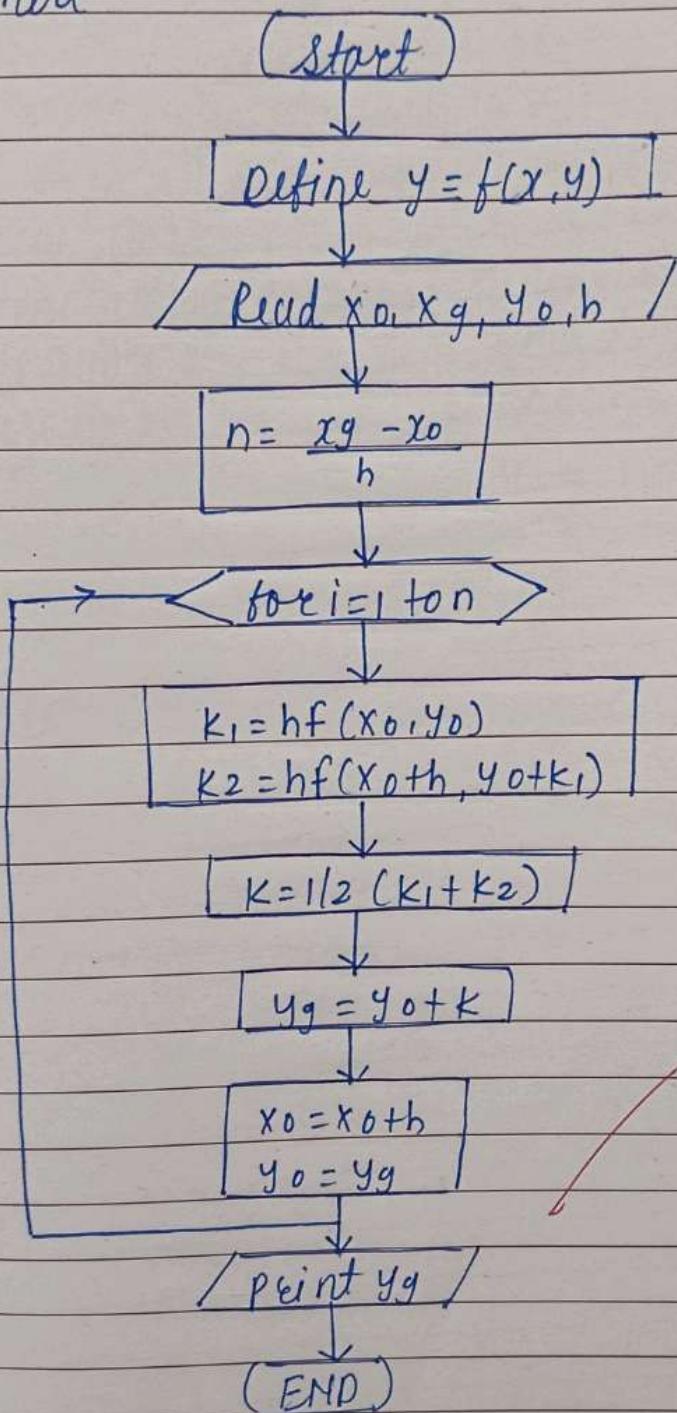
enter the initial value of h:

0.1

the final value of yg = 1.242050



RK-2 Method



S. J. Dabholkar



PRACTICAL NO :-

6

PRACTICAL NAME :-

TRAPEDIZODAL RULE

STUDENT NAME :-

SIMRAM V. AKHADÉ

DIV & ROLL NO :-

B(mech) - 04



Trapezoidal Method

Evaluate $(4x+2)$ within limits 1 to 4 by trapezoidal rule using 6 strips size.

Solution:- Data

$$y = f(x) = 4x + 2$$

$$f(x) = \int_1^4 (4x+2)$$

$$\text{Now, } h = \frac{x_n - x_0}{n}$$

$$= \frac{4-1}{6}$$

$$[h = 0.5]$$

$$\text{Therefore, } x_0 = 1$$

$$x_1 = x_0 + h = [1 + 0.5] = 1.5$$

$$x_2 = x_1 + h = [1.5 + 0.5] = 2$$

$$x_3 = x_2 + h = [2 + 0.5] = 2.5$$

$$x_4 = x_3 + h = [2.5 + 0.5] = 3$$

$$x_5 = x_4 + h = [3 + 0.5] = 3.5$$

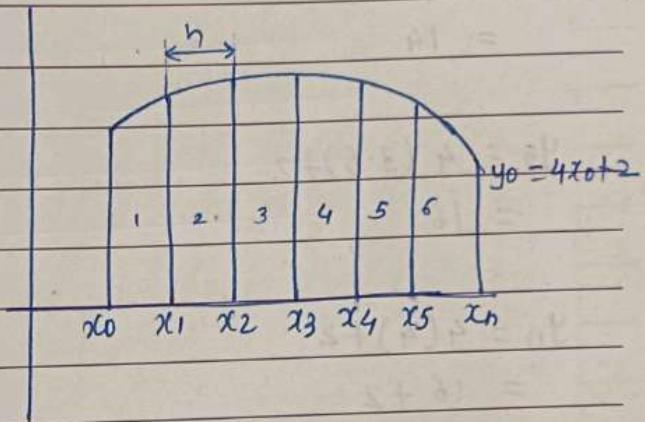
$$\text{Now, i) } y_0 = 4x_0 + 2$$

$$y_0 = 4(1) + 2$$

$$y_0 = 6$$

$$\text{ii) } y_1 = 4(1.5) + 2$$

$$= 8$$





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$$y_3 = 4(2 \cdot 5) + 2 \\ = 12$$

$$y_4 = 4(3 \cdot 5) + 2 \\ = 14$$

$$y_5 = 4(3 \cdot 5) + 2 \\ = 16$$

$$y_n = 4(4) + 2 \\ = 16 + 2 \\ = 18$$

Now, to find area

$$A = \frac{h}{2} [(y_0 + y_n) + 2(y_1 + y_2 + y_3 + y_4 + y_5)]$$

$$A = \frac{0.5}{2} [(6 + 18) + 2(8 + 10 + 12 + 14 + 16)]$$

$$\boxed{A = 36}$$

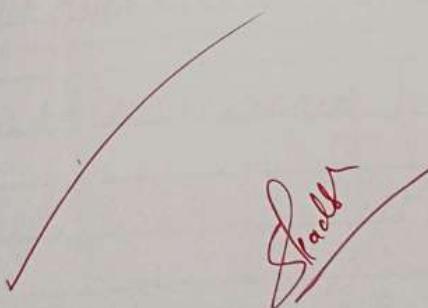
c, Nashik

Trapezodial

```
f = input('enter function y = f(x) = ');
xo = input('enter initial limit xo = ');
xn = input('enter final limit xn = ');
n = input('enter number of steps n = ');
h = (xn-xo)/n;
ans=0;
for i=1:n-1
    ans=ans+(f(xo+i*h));
end
ans=2*(ans);
ans1=f(xo)+f(xn);
area=ans+ans1;
area=area*(h/2);
fprintf('Total Area=%f',area);
```

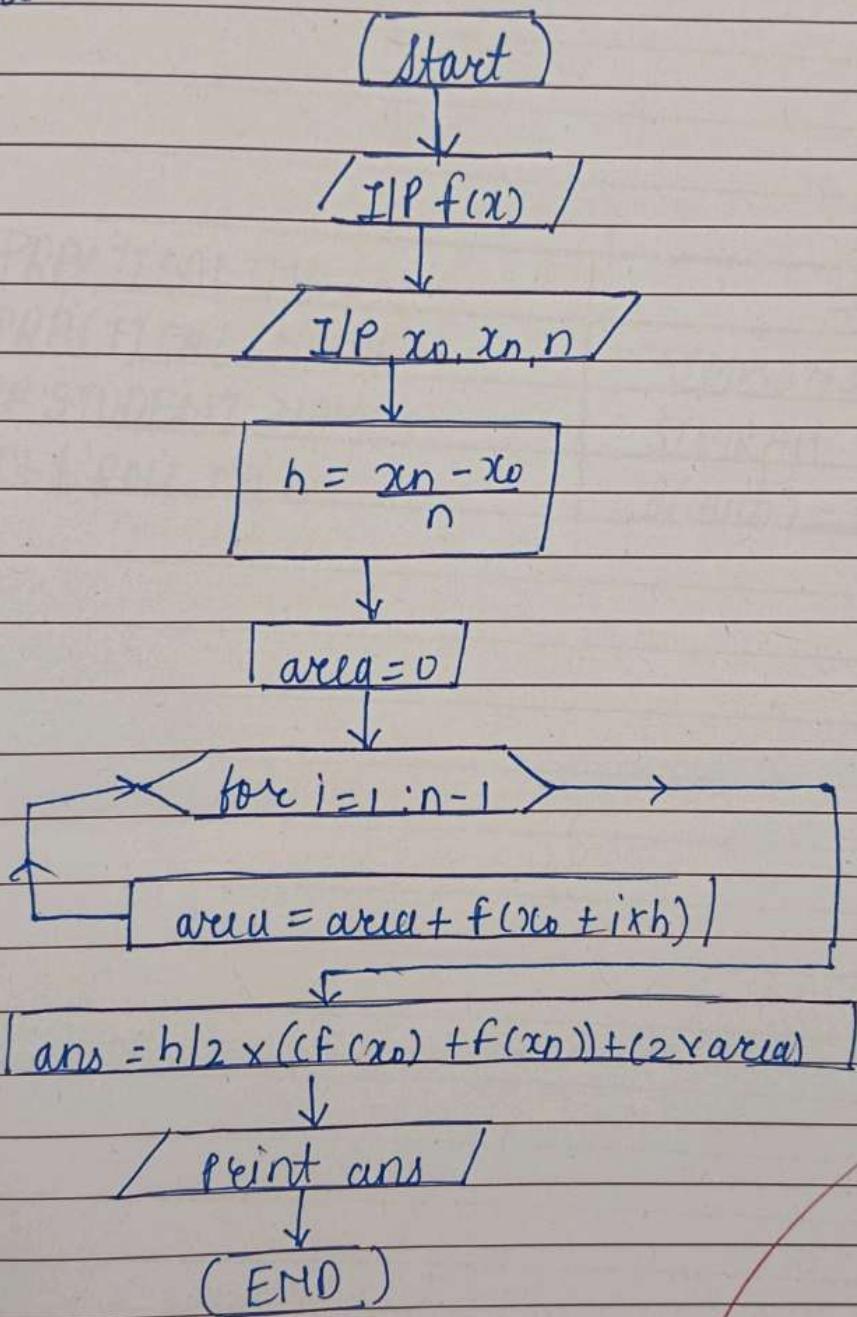
Output

```
enter function y = f(x) =
@(x) (4*x+2)
enter initial limit xo =
1
enter final limit xn =
4
enter number of steps n =
6
Total Area=36.000000
```





Trapezoidal





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PRACTICAL NO :-	7
PRACTICAL NAME :-	SIMPSON'S 1/3 RD RULE
PF STUDENT NAME :-	SIMRAN. V. AKHADE
DIV. & ROLL NO :-	B(mech) - 04

```
Simpsons1/3 rule
f = input('enter function y = f(x) = ');
xo = input('enter the value of xo: ');
xn = input('enter the value of xn: ');
n = input('enter the value of n: ');
h = (xn-xo)/n;
ans=0;

for i=1 : n-1
if(mod(i,2)~=0)
    ans=ans+4*(f(xo+i*h));
else
    ans=ans+2*(f(xo+i*h));
end
ans1=f(xo)+f(xn);
area=ans+ans1;
area=area*(h/3);
fprintf('\nTotal area = %f',area);
```

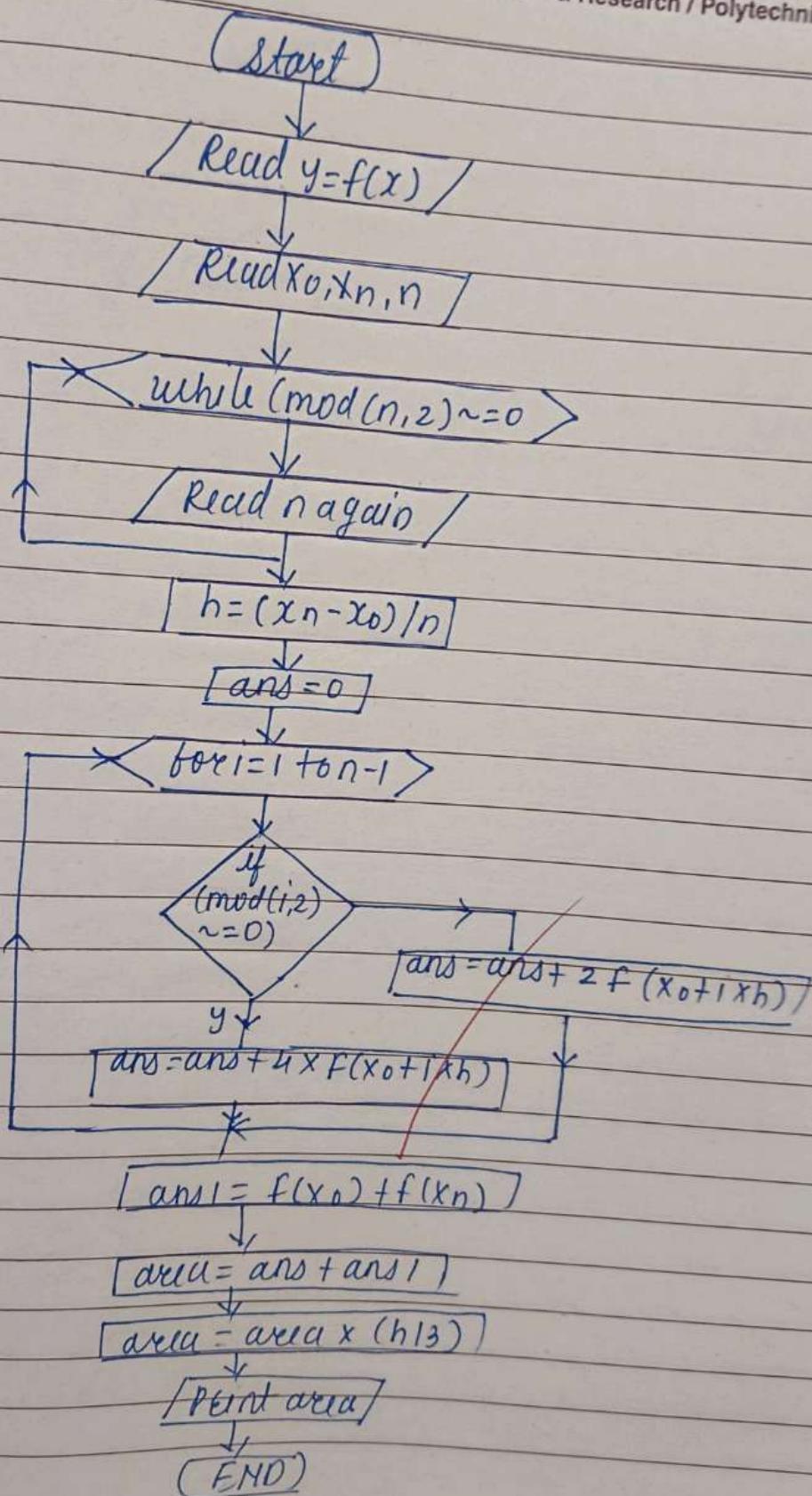
Output
simpson1
enter function y = f(x) =
 $\theta(x) \exp(x)$
enter the value of xo:
0
enter the value of xn:
4
enter the value of n:
4

Total area = 53.863846

check



Simpson 1/3





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PRACTICAL

8

PRACTICAL NAME

STRAIGHT LINE

STUDENT NAME

SIMRAN. V. AKHADE

DIV I ROLL NO

B(mech) - 04



g Straight line Eqn

x	1	2	3	4	5	6	7
y	0.5	2.5	2.0	4.0	3.5	6.0	5.5

Solution: General Eqn of line is $y = ax + b$ as we need to fit a curve which is straight line it means to find values of A & B

to find out this two unknown constant we will apply list square technique as given below.

$$y = ax + b \quad \text{--- ①}$$

we multiply by x on both side on eq ①
we get,

$$xy = ax^2 + bx \quad \text{--- ②}$$

but in a given data set there will be 'n' values of $x + y$.

while finding $a + b$ we must take summision of x summision y value.

$$y = ax \sum x + n \times b \quad \text{--- ③}$$

$$xy = a \times \sum x^2 + b \times \sum x \quad \text{--- ④}$$

in eq no. ③ + ④ we will prepare following table:



x	y	xy	x^2
1	0.5	0.5	1
2	2.5	5	4
3	2.6	6	9
4	4.0	16	16
5	3.5	17.5	25
6	6.0	36	36
7	5.5	38.5	49
28	24	114.5	140

Sustitute all submisionn value into eq no. 3 & 4
To findout constant a & b we apply cramer's rule

we will rearrange the eq ③ & ④

we get

$$a \sum x + n b = \sum y$$

$$a \sum x^2 + b \sum x = \sum xy$$

Crammer's Rule

$$a = \frac{\Delta a}{\Delta}$$

$$b = \frac{\Delta b}{\Delta}$$

$$b =$$

$$\Delta b =$$

+ calc



from eq no. ⑤ + ⑥ we will represent in terms of
matrices

$$\begin{bmatrix} \varepsilon x & n \\ \varepsilon x^2 & \varepsilon x \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} \varepsilon y \\ \varepsilon xy \end{bmatrix} \quad \rightarrow ⑦$$

from eq no. ⑦

$$\text{Here } \Delta = \begin{vmatrix} \varepsilon x & n \\ \varepsilon x^2 & \varepsilon x \end{vmatrix} = \begin{vmatrix} 28 & 7 \\ 140 & 28 \end{vmatrix}$$

$$= (28 \times 28) - (7 \times 140)$$

$$\Delta = -196$$

4

rule to prepare Δa we replace column of a i.e 1st column

$$\therefore \begin{bmatrix} \varepsilon y & n \\ \varepsilon xy & \varepsilon x \end{bmatrix} = \begin{vmatrix} 24 & 7 \\ 119.5 & 28 \end{vmatrix}$$

$$= (24 \times 28) - (7 \times 119.5)$$

$$\Delta a = -164.5$$

$$\Delta b = \begin{bmatrix} \varepsilon x & \varepsilon y \\ \varepsilon x^2 & \varepsilon xy \end{bmatrix} = \begin{vmatrix} 28 & 24 \\ 140 & 119.5 \end{vmatrix}$$

$$\Delta b = -14$$

now calculate

$$a = \frac{\Delta a}{\Delta} = \frac{-164.5}{-196} = 0.839$$



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$$b = \frac{\Delta b}{\Delta} = \frac{-14}{-196} = 0.071$$

Now put value of a + b in eq ①

$$y = ax + b$$

$$y = 0.839(x) + 0.071$$

```
n=input('\nEnter The value of given points n:');
for i=1:n
    ar2(i)=input('\nEnter the value of x:');
    ar1(i)=input('\nEnter the value of y:');
end
sum0=0;
sum1=0;
sum2=0;
sum3=0;
for i=1:n
    sum0=sum0+ar2(i);
    sum1=sum1+ar1(i);
    sum2=sum2+ar2(i)*ar1(i);
    sum3=sum3+ar2(i)*ar2(i);
end
ds=sum0*sum0-n*sum3;
da=sum1*sum0-n*sum2;
db=sum0*sum2-sum1*sum3;
a=da/ds;
b=db/ds;
fprintf('a=%f',a);
fprintf('b=%f',b);
fprintf('y=%fx+%f',a,b);
```

OUTPUT

Enter The value of given points n:7
Enter the value of x:1
Enter the value of y:0.5
Enter the value of x:2

Enter the value of y:2.5

Enter the value of x:3

Enter the value of y:2

Enter the value of x:4

Enter the value of y:4

Enter the value of x:5

Enter the value of y:3.5

Enter the value of x:6

Enter the value of y:6

Enter the value of x:7

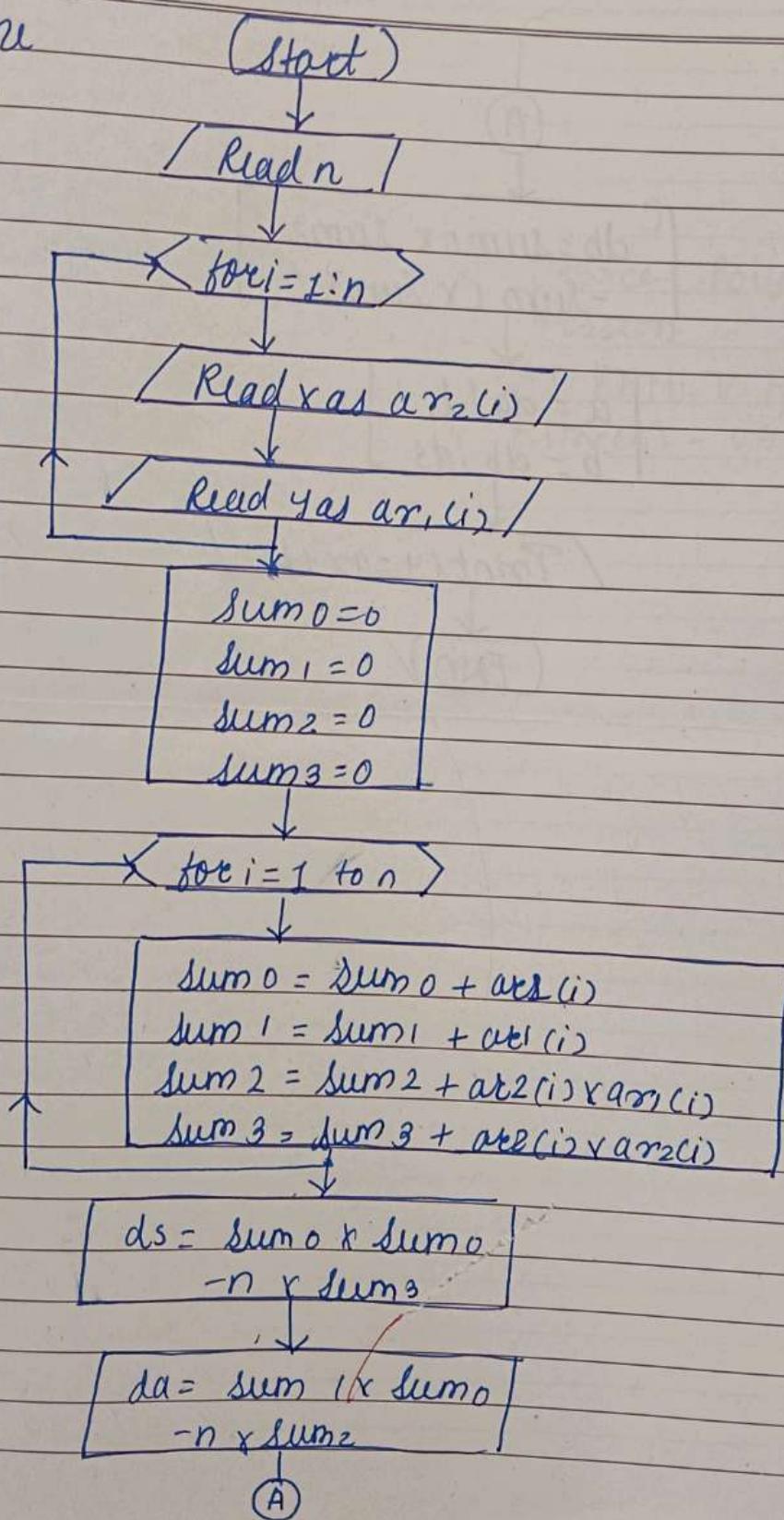
a=0.839286

b=0.071429
 $y = 0.839286x + 0.071429$

Graph

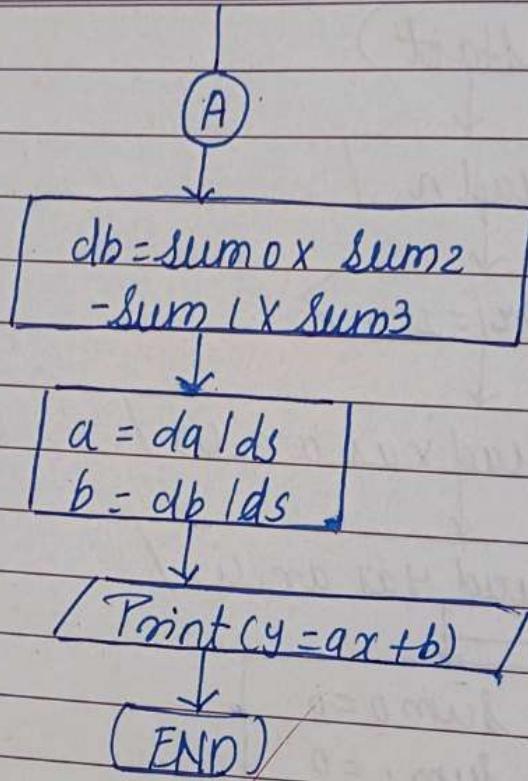


Straight line regression





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PRACTICAL NO :

9

PRACTICAL NAME

2nd Degree Polynomial Expression

STUDENT NAME :

SIMRAT· V. AKADE

DIV 9 ROLL No :

B(mech) - 04



2nd degree Polynomial Regression

Following is data given for value of $x \& y$, fit a second degree polynomial of type $ax^2 + bx + c$ where $a, b \& c$ are constant.

x	-3	-2	-1	0	1	2	3
y	12	4	1	2	7	15	30

→ General eqⁿ for 2nd degree polynomial is

$$y = ax^2 + bx + c \quad \text{--- } ①$$

we will multiply by 'x' on both sides.

$$xy = ax^3 + bx^2 + cx \quad \text{--- } ②$$

Unknowns are three

To get third eqⁿ we will multiply by x again

$$x^2y = ax^4 + bx^3 + cx^2 \quad \text{--- } ③$$

As there are 'n' no. of data points for $x \& y$ we will take

Σ - on both side ' $x \& y$ '

∴ Rewrite the eqⁿ no ① ② ③

$$\Sigma y = a \Sigma x^2 + b \Sigma x + n * b \quad \text{--- } ④$$

$$\Sigma xy = a \Sigma x^3 + b \Sigma x^2 + c \Sigma x \quad \text{--- } ⑤$$

$$\Sigma x^2y = a \Sigma x^4 + b \Sigma x^3 + c \Sigma x^2 \quad \text{--- } ⑥$$



x	y	xy	x^2	x^3	x^4	x^2y
-3	12	-36	9	-27	81	108
-2	4	-8	4	-8	16	16
-1	1	-1	1	-1	1	1
0	2	0	0	0	0	0
1	7	7	1	1	1	7
2	15	30	4	8	16	60
3	30	90	9	27	81	270

$$\begin{bmatrix} \sum x^2 & \sum x^n \\ \sum x^3 & \sum x^2 \sum x \\ \sum x^4 & \sum x^3 \sum x^2 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} \sum y \\ \sum xy \\ \sum x^2y \end{bmatrix}$$

above matrix will
solve the Gramme's
rule

$$0 \quad 71 \quad 82 \quad 28 \quad 0 \quad 196 \quad 462$$

$$\Delta = \begin{vmatrix} 28 & 0 & 7 \\ 0 & 28 & 0 \\ 196 & 0 & 28 \end{vmatrix}$$

$$= 28(28 \times 28 - 0 \times 0) - 0(0 \times 28 - 0 \times 196) + 7(0 \times 0 - 28 \times 196)$$

$$\Delta = -16464$$

$$\Delta a = \begin{vmatrix} 71 & 0 & 7 \\ 82 & 28 & 0 \\ 462 & 0 & 28 \end{vmatrix} = 71(28 \times 28 - 0 \times 0) - 0(82 \times 28 - 0 \times 196) + 7(82 \times 0 - 28 \times 462) = -34888.$$

$$\Delta b = \begin{vmatrix} 28 & 71 & 7 \\ 0 & 82 & 0 \\ 196 & 462 & 28 \end{vmatrix} = 28(82 \times 28 - 0 \times 462) - 71(0 \times 28 - 0 \times 196) + 7(0 \times 462 - 82 \times 196) \Delta b = -48216$$

$$\Delta c = \begin{vmatrix} 28 & 0 & 71 \\ 0 & 28 & 82 \\ 196 & 0 & 462 \end{vmatrix} = 28(28 \times 462 - 82 \times 0) - 0(0 \times 462 - 82 \times 196) + 71(0 \times 0 - 28 \times 196) = -27440$$



$$\therefore a = \frac{\Delta a}{\Delta} = 2.11904$$

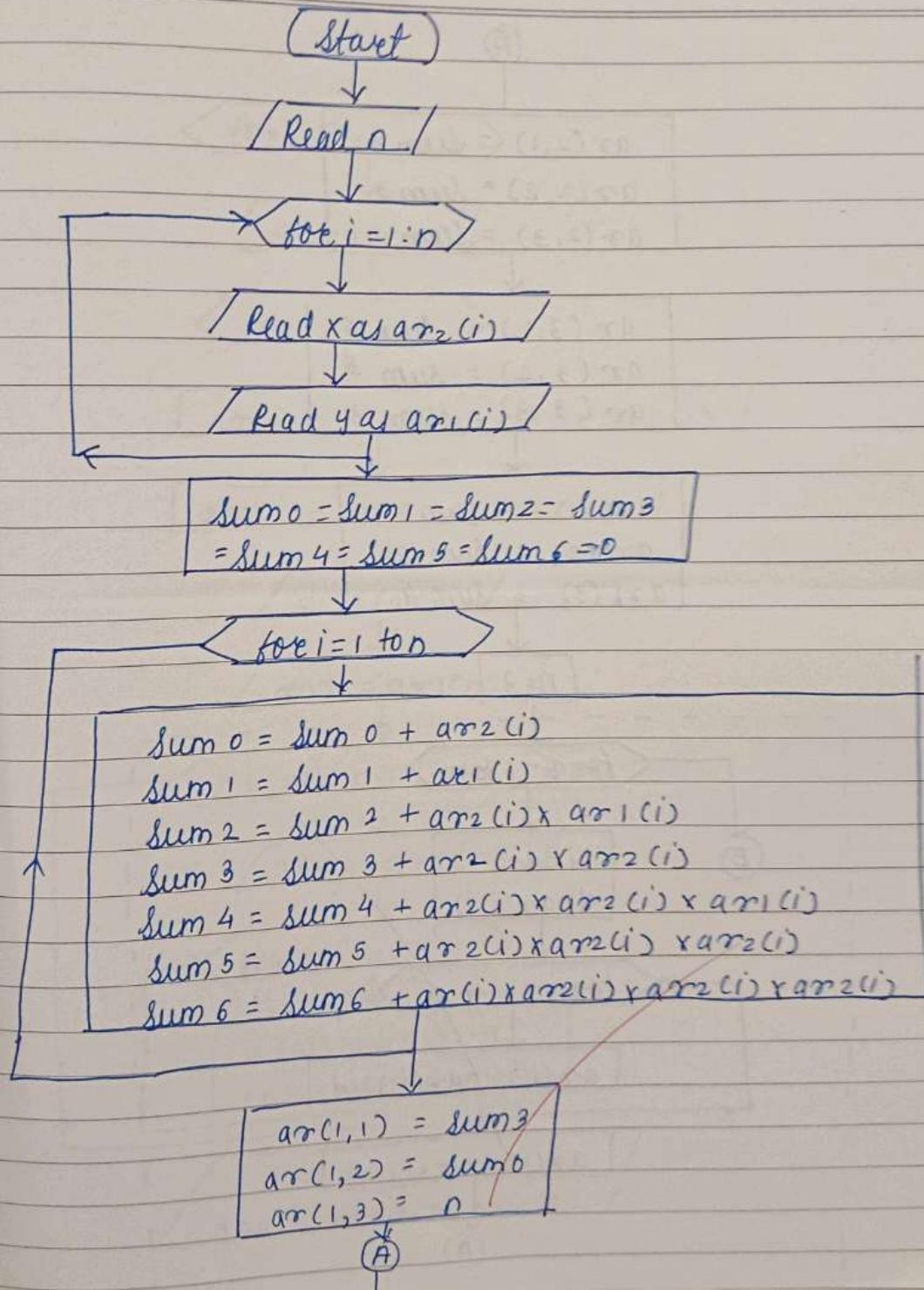
$$b = \frac{\Delta b}{\Delta} = 2.9285$$

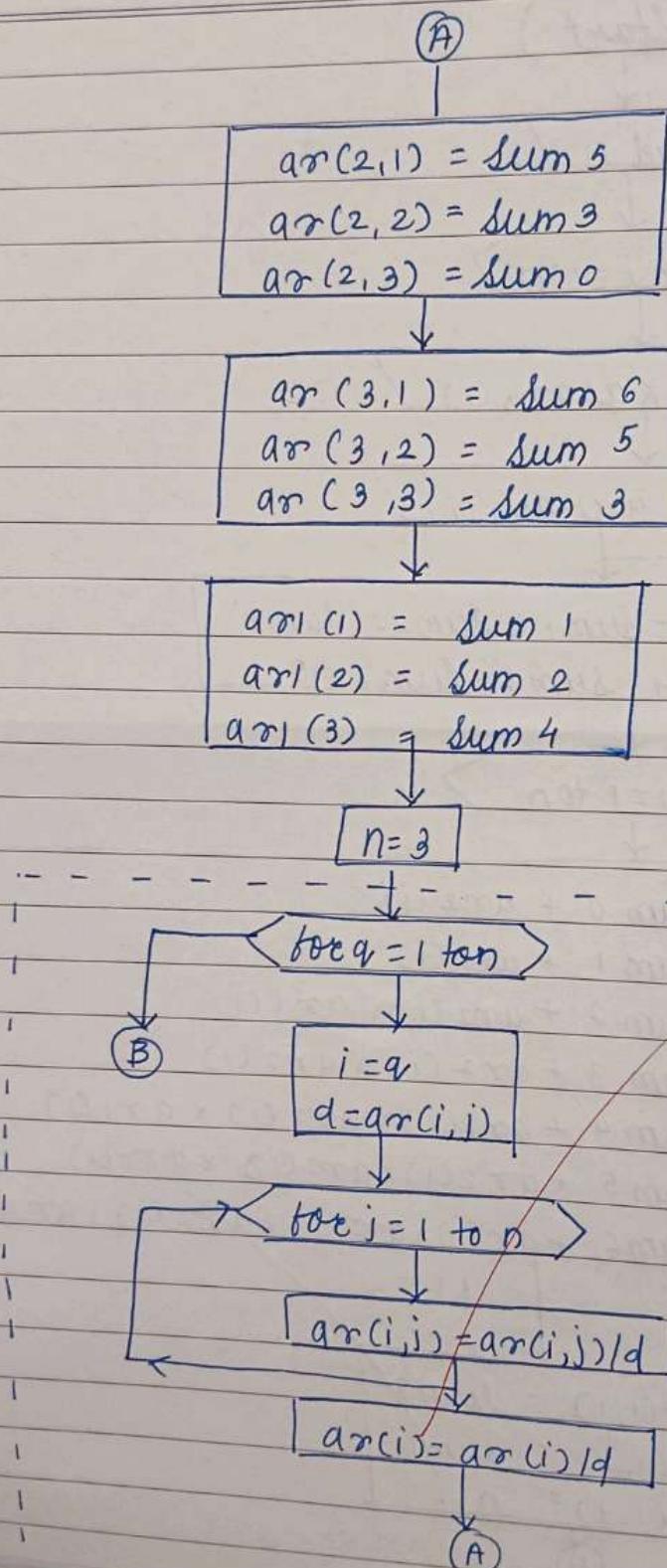
$$c = \frac{\Delta c}{\Delta} = 1.6667$$

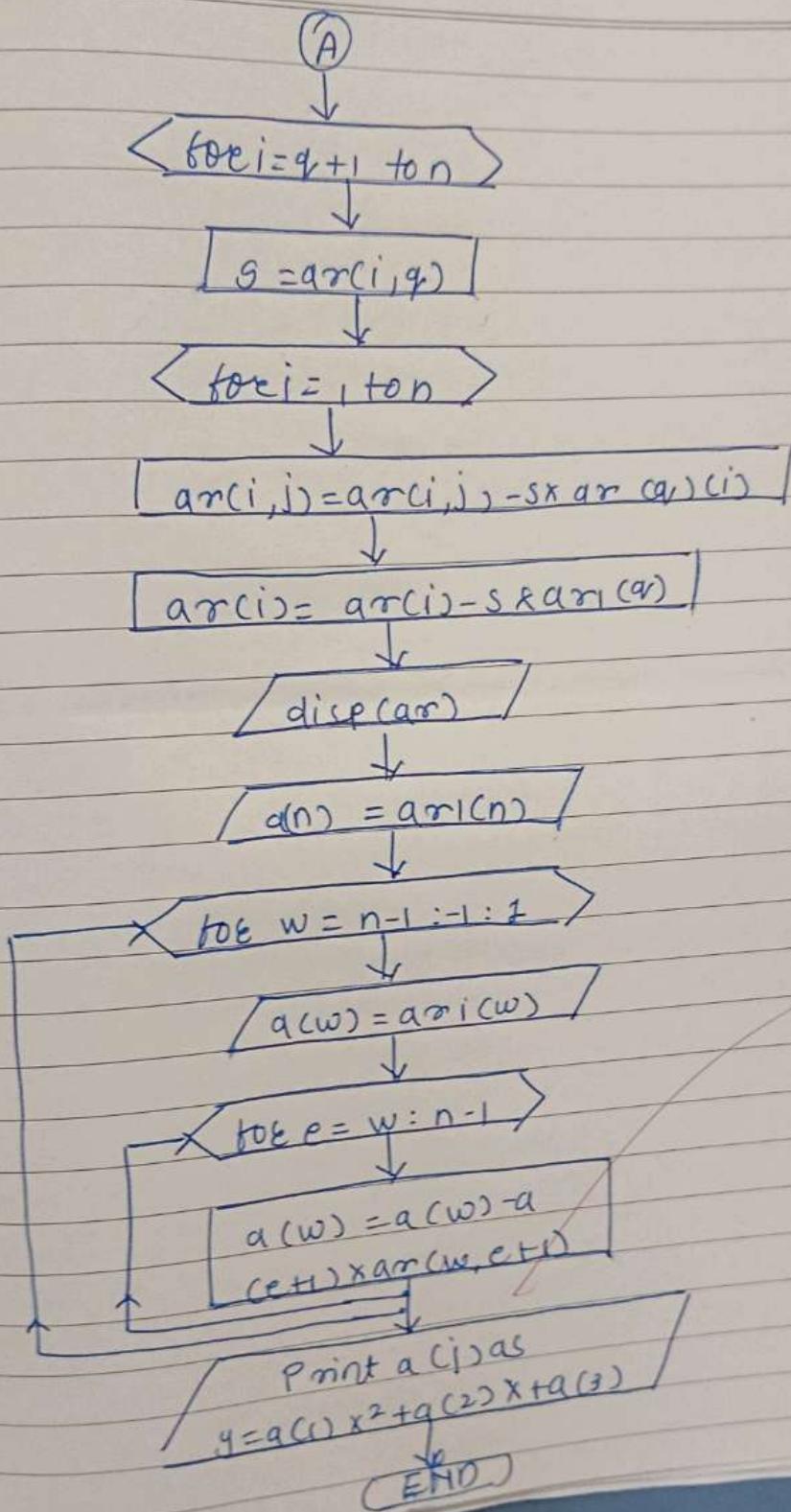
\therefore the value of $a, b \& c$ is $a = 2.11904$,

$$b = 2.9285$$

$$c = 1.6667$$







Simran Akhade

Roll.no :4

```
n=input('\nEnter the value of given points n');
for i=1:n
    ar2(i)=input('\nEnter the value of x:');
    ar1(i)=input('\nEnter the value of y
    :'); end
sum0=0;
sum1=0;
sum2=0;
sum3=0;
sum4=0;
sum5=0;
sum6=0;
for i=1:n
    sum0=sum0+ar2(i);
    sum1=sum1+ar1(i);
    sum2=sum2+ar2(i)*ar1(i);
    sum3=sum3+ar2(i)*ar2(i);
    sum4=sum4+ar2(i)*ar2(i)*ar1(i);
    sum5=sum5+ar2(i)*ar2(i)*ar2(i);
    sum6=sum6+ar2(i)*ar2(i)*ar2(i)*ar2(i);
end
ar(1,1)=sum3;
ar(1,2)=sum0;
ar(1,3)=n;
ar(2,1)=sum5;
ar(2,2)=sum3;
ar(2,3)=sum0;
ar(3,1)=sum6;
ar(3,2)=sum5;
```

```
ar(3,3)=sum3;  
ar1(1)=sum1;  
ar1(2)=sum2;  
ar1(3)=sum4;  
n=3;  
for q=1:n  
    i=q;  
    d=ar(i,i);  
    for j=1:n  
        ar(i,j)=ar(i,j)/d;  
    end  
    ar1(i)=ar1(i)/d;  
    for i=q+1:n  
        s=ar(i,q);  
        for j=1:n  
            ar(i,j)=ar(i,j)-s*ar(q,j);  
        end  
        ar1(i)=ar1(i)-s*ar1(q);  
    end  
    disp(ar);  
    a(n)=ar1(n);  
    for w=n-1:-1:1  
        a(w)=ar1(w);  
        for e=w:n-1  
            a(w)=a(w)-(a(e+1)*ar(w,e+1));  
        end  
    end  
    fprintf('\n\n y=%fx*x+%f*x+%\nf',a(1),a(2),a(3));
```

OUTPUT

Enter the value of given points n

7

Enter the value of x:

-3

Enter the value of y :

12

Enter the value of x:

-2

Enter the value of y :

4

Enter the value of x:

-1

Enter the value of y :

1

Enter the value of
x:

0

Enter the value of y :

2

Enter the value of
x:

1

Enter the value of y :

7

Enter the value of
x:

2

Enter the value of y :

15

Enter the value of
x:

3

Enter the value of y :

30

1.0000 0 0.2500

0 1.0000 0

0 0 1.0000

$$y=2.119048x^2+2.928571x+1.666667$$

/ f



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PRACTICAL NO :

PRACTICAL NAME :

10

LAGRANGE'S OF STATIC

STUDENT NAME :

SIMRAM V. AKHADE.

DIV & ROLL NO :

B(mech) - 04



find interpolating polynomial for following data

x	0	1	2	5
$y = f(x)$	2	3	12	147

find value of y at $x = 1.5$ by using
Lagranges Interpolation

$$\begin{array}{lll} x_0 = 0 & y_0 = 2 & x_g = 1.5 \\ x_1 = 1 & y_1 = 3 & y_g = ? \\ x_2 = 2 & y_2 = 12 \\ x_3 = 5 & y_3 = 147 \end{array}$$

$$\therefore y_g = y_0 L_0 + y_1 L_1 + y_2 L_2 + y_3 L_3$$

$$\therefore L_0 = \frac{(x_g - x_1)(x_g - x_2)(x_g - x_3)}{(x_0 - x_1)(x_0 - x_2)(x_0 - x_3)}$$

$$\therefore L_0 = \frac{(1.5 - 1)(1.5 - 2)(1.5 - 5)}{(0 - 1)(0 - 2)(0 - 5)}$$

$$L_0 = -0.0875$$

$$L_1 = \frac{(x_g - x_0)(x_g - x_2)(x_g - x_3)}{(x_1 - x_0)(x_1 - x_2)(x_1 - x_3)}$$

$$L_1 = 0.6562$$



$$L_2 = \frac{(x_g - x_0) (x_g - x_1) (x_g - x_3)}{(x_2 - x_0) (x_2 - x_1) (x_2 - x_3)}$$

$$L_2 = 0.4375$$

$$L_3 = \frac{(x_g - x_0) (x_g - x_1) (x_g - x_2)}{(x_3 - x_0) (x_3 - x_1) (x_3 - x_2)}$$

$$L_3 = -0.00625$$

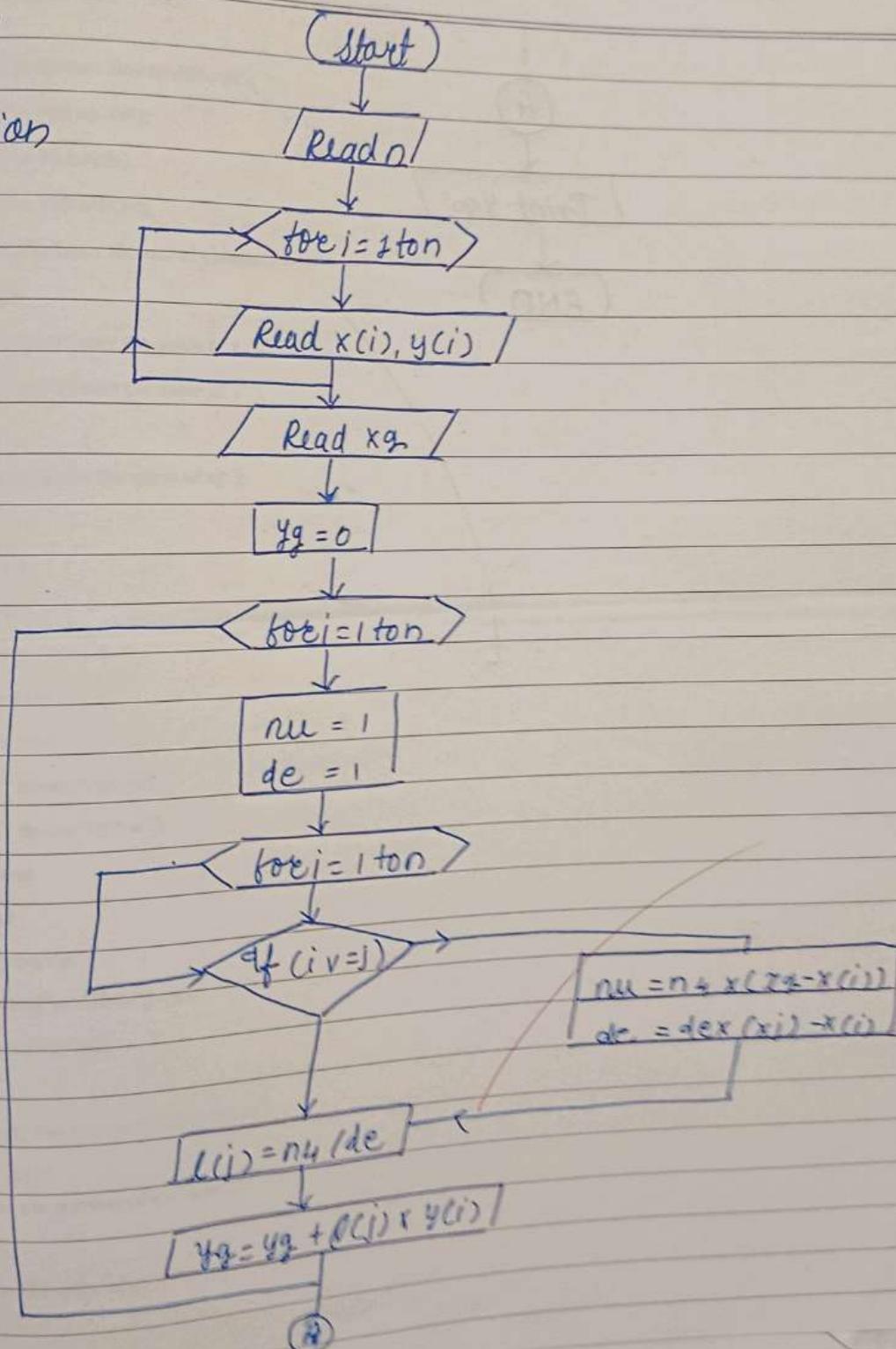
$$y_g = y_0 L_0 + y_1 L_1 + y_2 L_2 + y_3 L_3$$

$$y_g = 2 \times (-0.6875) + 3 \times (0.6562) + 12 \times 0.4375 + 147 \times (-0.00625)$$

The final value of $y_g = 6.125$

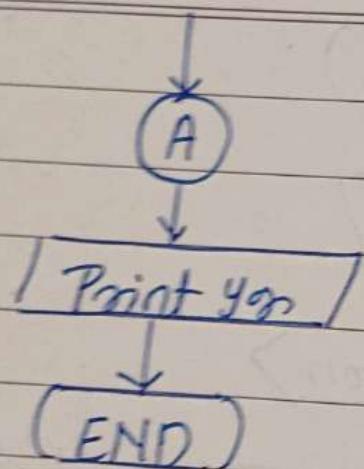


Newchent:
george's
interpolation





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Lagranges method

INPUT

```
fprintf('\n Name : Simran Akhade');
fprintf('\n Roll no. 04');
fprintf('\n B1 batch');
fprintf('\n TYB MECH');
n=input('\n Enter the no. of elements n:');
for i=1:n
```

```
    x(i)=input('Enter the value of x:');
    y(i)=input('Enter the value of y:');
end
```

```
xg=input('Enter the value of xg:');
yg=0;
```

```
for j=1:n
```

```
    nu=1;
```

```
    de=1;
```

```
    for i=1:n
```

```
        if (i==j)
```

```
            nu=nu*(xg-x(i));
            de=de*(x(j)-x(i));
        end
    end
```

```
i(j)=nu/de;
```

```
fprintf('\n L%f=%f',j,i(j));
yg=yg+i(j)*y(j);
end
```

```
fprintf('The final value of yg %f', yg');
```

OUTPUT

Enter the number of elements n:

4

Enter the value of x :

0

Enter the value of y :

2

Enter the value of x :

1

Enter the value of y :

3

Enter the value of x :

2

Enter the value of y :

12

Enter the value of x :

5

Enter the value of y :

147

Enter the value of xg :

1.5

L1.000000=-0.087500

L2.000000=0.656250

L3.000000=0.437500

L4.000000=-0.006250 The final value of yg 6.125000

91



K. K. Wagh Institute of Engineering Edu. & Research / Polytechnic, Nashik - 3

PRACTICAL NO :
PRACTICAL NAME :
STUDENT NAME :
DIV ROLL NO :

II
MEAN, MEDIAN, MODE
SIMRAN. AKADE
B(Mech) - 04



x	f	x	$x \cdot f$	of	x^2	$f \cdot x^2$	f^2
0-10	13	5	65	13	25	325	169
10-20	20	15	300	33	225	4500	400
20-30	30	25	750	63	625	18750	900
30-40	25	35	875	88	1225	30625	625
40-50	12	45	540	100	2025	24300	144
		100	125	2530	4125	78500	2238

1) Arithmetic mean:

$$\bar{x} = \frac{\sum fx}{\sum f} = \frac{2530}{100} = 25.3$$

2) Median

$$M = \frac{100}{2} = 50$$

Median is 20-30 span

$$\text{median} = 25$$

$$\text{Mode } l + \frac{h f_i - f_0}{2f_i - f_0 - f_0}$$

$$f_0 = 20$$

$$f_1 = 36$$

$$f_2 = 25$$

$$l = 20$$

$$h = 10$$

$$= 20 + 10(30 - 20)$$

$$2 \times 30 - 20 - 25$$

$$\text{mode} = 26.67$$



4) Standard deviation

$$\sigma = \sqrt{\frac{\sum f(x)^2}{N} - \left(\frac{\sum fx}{N}\right)^2}$$

$$= \sqrt{\frac{(78500)}{100} - \left(\frac{2530}{100}\right)^2}$$

$$= 12.037$$

5) Karl Pearson coeff. of skewness

$$Sk = \frac{\text{mean} - \text{mode}}{\sigma}$$

$$= \frac{25.3 - 26.67}{12.037}$$

$$= -0.1138.$$

6) Karl Pearson's correlation coeff.

$$\sum x = 125$$

$$\sum y = 100$$

$$\sum xy = 2530$$

$$\sum x^2 = 1425$$

$$\sum y^2 = 2238$$

$$\rho = \frac{\sqrt{[5(2530) - (125)(100)]}}{\sqrt{[5(1425) - (125)^2][5(2238) - (100)^2]}}$$

$$\rho = 0.06144$$



(start)
↓
Input no. of
data point (n)

Initiating arrays x & f
frequency with sign n

↓
Rearrange x & f

calculate weight sum of
 $x = \text{sum}(x \times f)$

calculate sum of f frequency

$$\text{mean} = \frac{\text{sum}(x \times f)}{\text{sum } f}$$

```
n = input('Enter the Value of n: ');
l = input('\nEnter the value of l (lower limit of modal class): ');
h = input('\nEnter the value of h (class width):');
```

```
for i = 1:n
```

```
    x(i) = input('\nEnter the value of x: ');
    f(i) = input('\nEnter the value of f: ');
end
```

```
sumx = 0;
```

```
sumf = 0;
```

```
sumfx = 0;
```

```
for i = 1:n
```

```
    sumf = sumf + f(i);
    sumx = sumx + x(i);
    sumfx = sumfx + x(i) * f(i);
end
```

```
mean_value = sumfx / sumf;
fprintf('Arithmetic Mean: %f\n', mean_value);
```

```
values = repelem(x, f);
std_dev = std(values);
fprintf('Standard Deviation: %f\n', std_dev);
```

```
% Mode calculation
```

```
[fm, mode_idx] = max(f);
```

```
if mode_idx > 1 && mode_idx < n  
    f1 = f(mode_idx - 1);  
    f2 = f(mode_idx + 1);  
    mode_val = l + h * ((fm - f1) / (2 * fm - f1 - f2));  
    fprintf('Mode: %f\n', mode_val);  
else  
    fprintf('Mode calculation is not possible due to insufficient class intervals.\n');  
end
```

% Skewness calculation

```
skew_val = (mean_value - mode_val) / (std_dev) ;  
fprintf('Skewness: %f\n', skew_val);  
Output
```

Enter the Value of n: 5

Enter the value of l (lower limit of modal class): 20

Enter the value of h (class width): 10

Enter the value of x: 5

Enter the value of f: 13

Enter the value of x: 15

Enter the value of f: 20

Enter the value of x: 25

Enter the value of f: 30

Enter the value of x: 35

Enter the value of f: 25

Enter the value of x: 45

Enter the value of f: 12

Arithmetic Mean: 25.300000

Standard Deviation: 12.098501

Mode: 26.666667

Skewness: -0.112962

✓
SK ✓



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PRACTICAL NO : 12
PRACTICAL NAME : DATA SETS
STUDENT NAME : SIMRAN AKHADE
ROLL NOIV : B(mech) - 04

New Session from File

Data set

Data Set Variable
Energy_consumption 1000x11 table

Response
EnergyConsumption double 53.2633 ...

Predictors

	Name	Type	Range
<input type="checkbox"/>	Timestamp	datetime	< unsuitable >
<input checked="" type="checkbox"/>	Temperature	double	20.0076 - 29.9987
<input checked="" type="checkbox"/>	Humidity	double	30.016 - 59.9891
<input checked="" type="checkbox"/>	SquareFootage	double	1000.51 - 1999.08
<input checked="" type="checkbox"/>	Occupancy	double	0 - 9
<input checked="" type="checkbox"/>	HVACUsage	categorical	2 unique

Add All Remove All

[How to prepare data](#)

Validation

Validation Scheme
Cross-Validation

Protects against overfitting. For data not set aside for testing, the app partitions the data into folds and estimates the accuracy on each fold.

Cross-validation folds 5

[Read about validation](#)

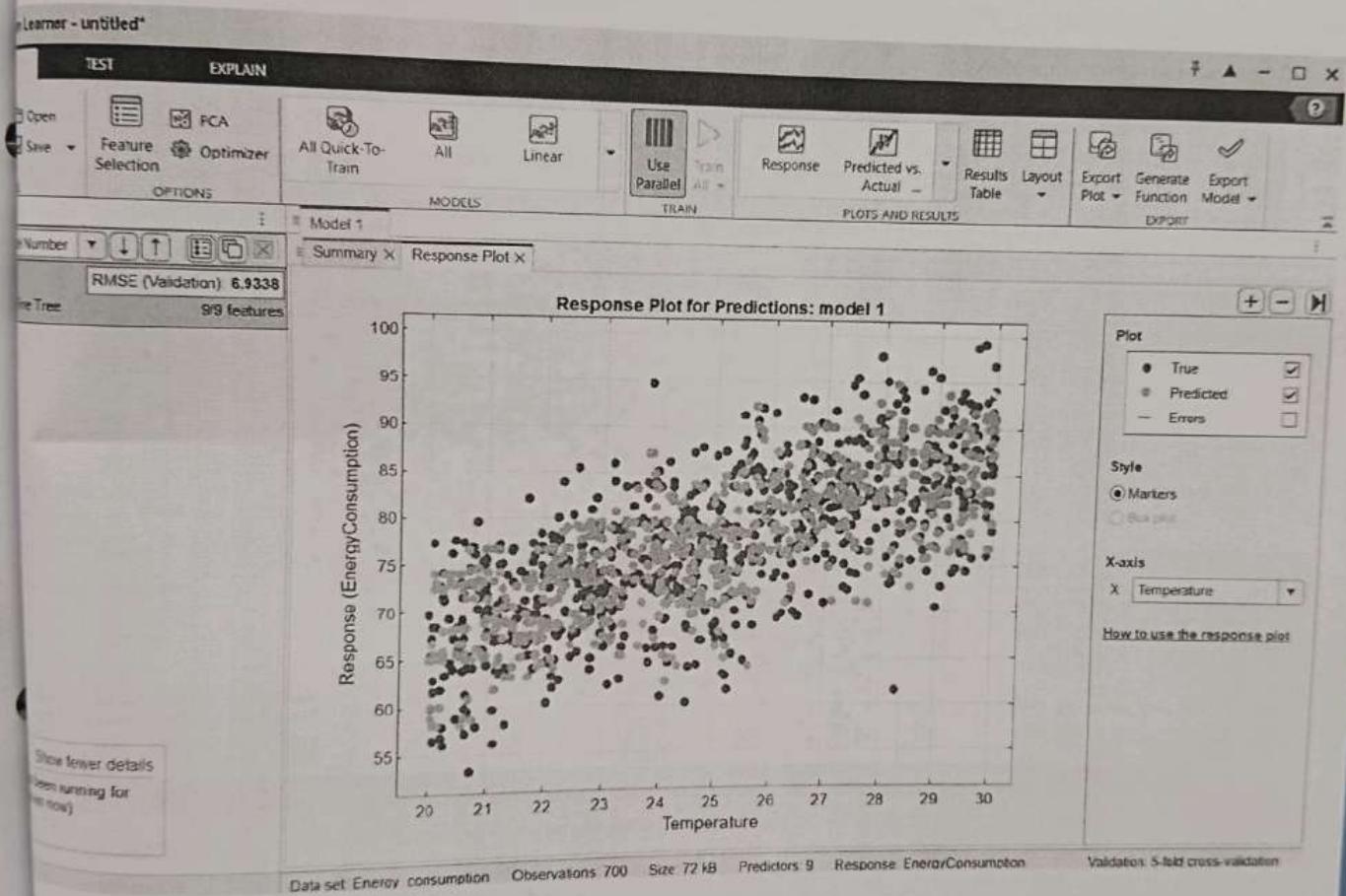
Test

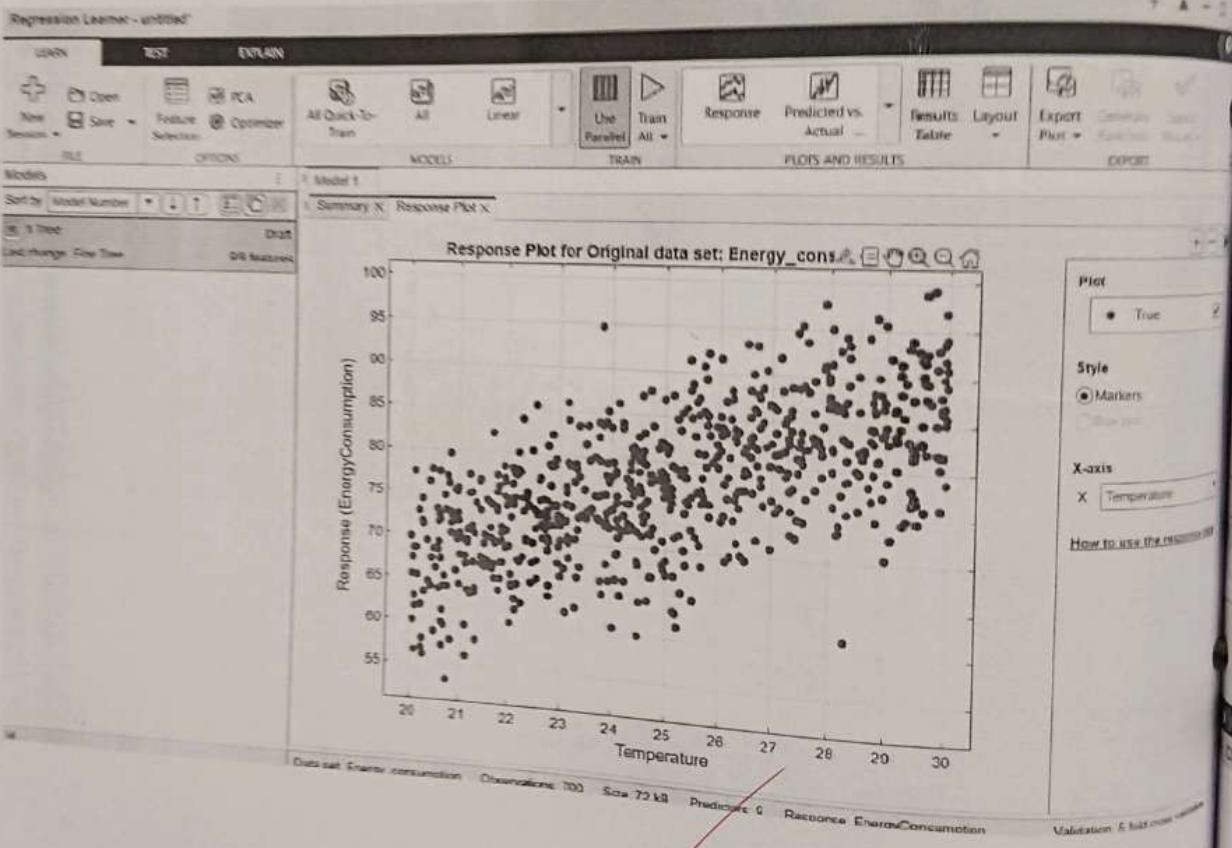
Set aside a test data set
Percent set aside 30

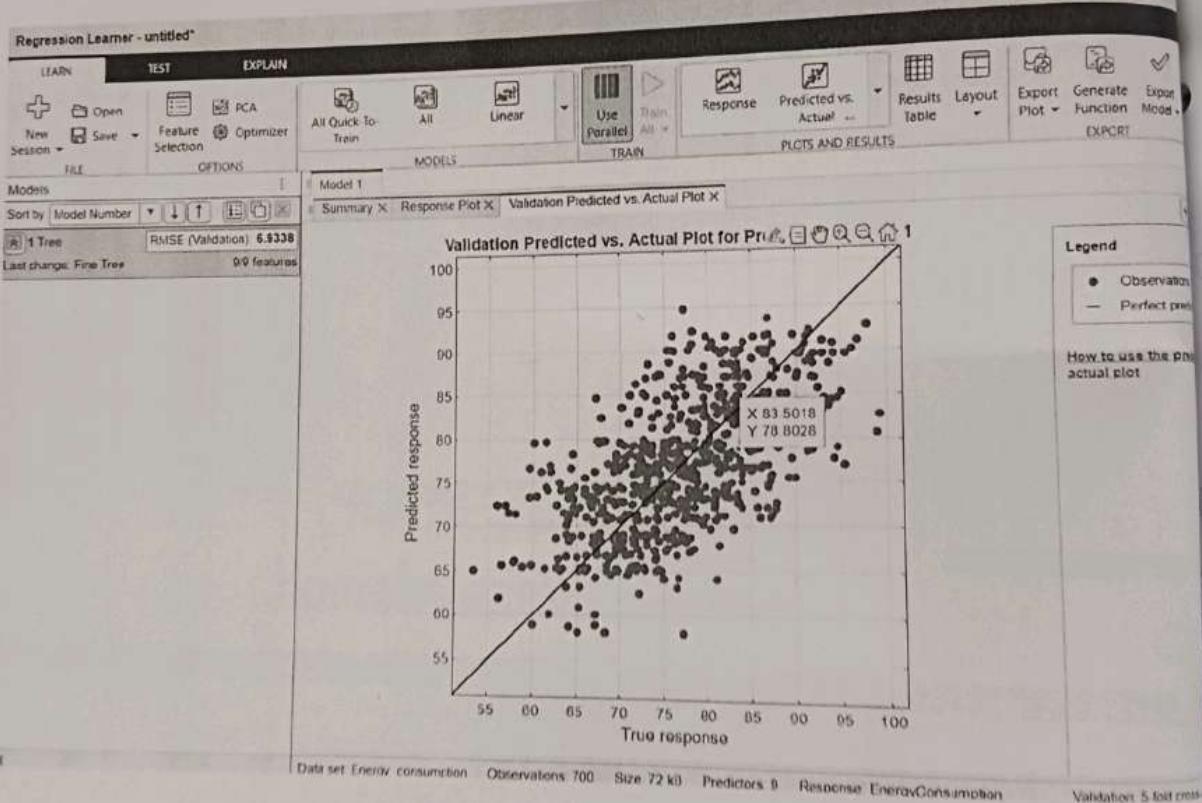
Use a test set to evaluate model performance after tuning and training models. To import a separate test set instead of partitioning the current data set, use the Test Data button after starting an app session.

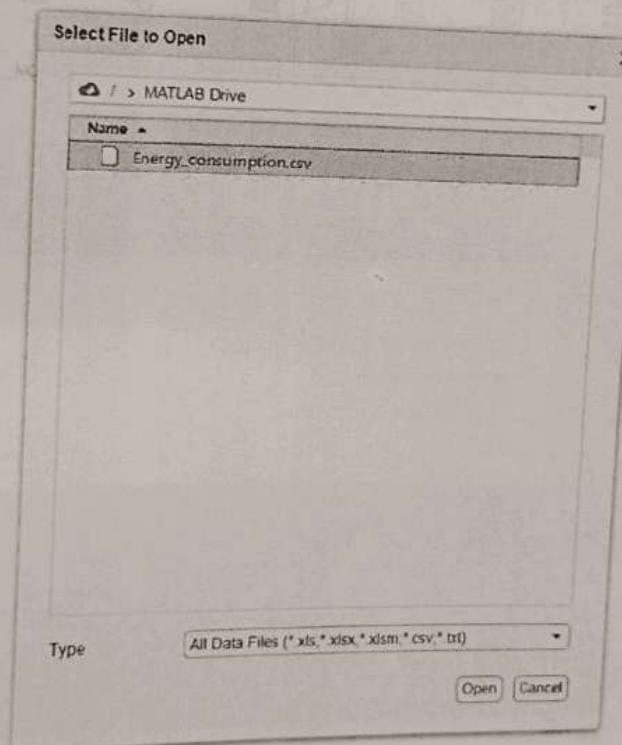
[Read about test data](#)

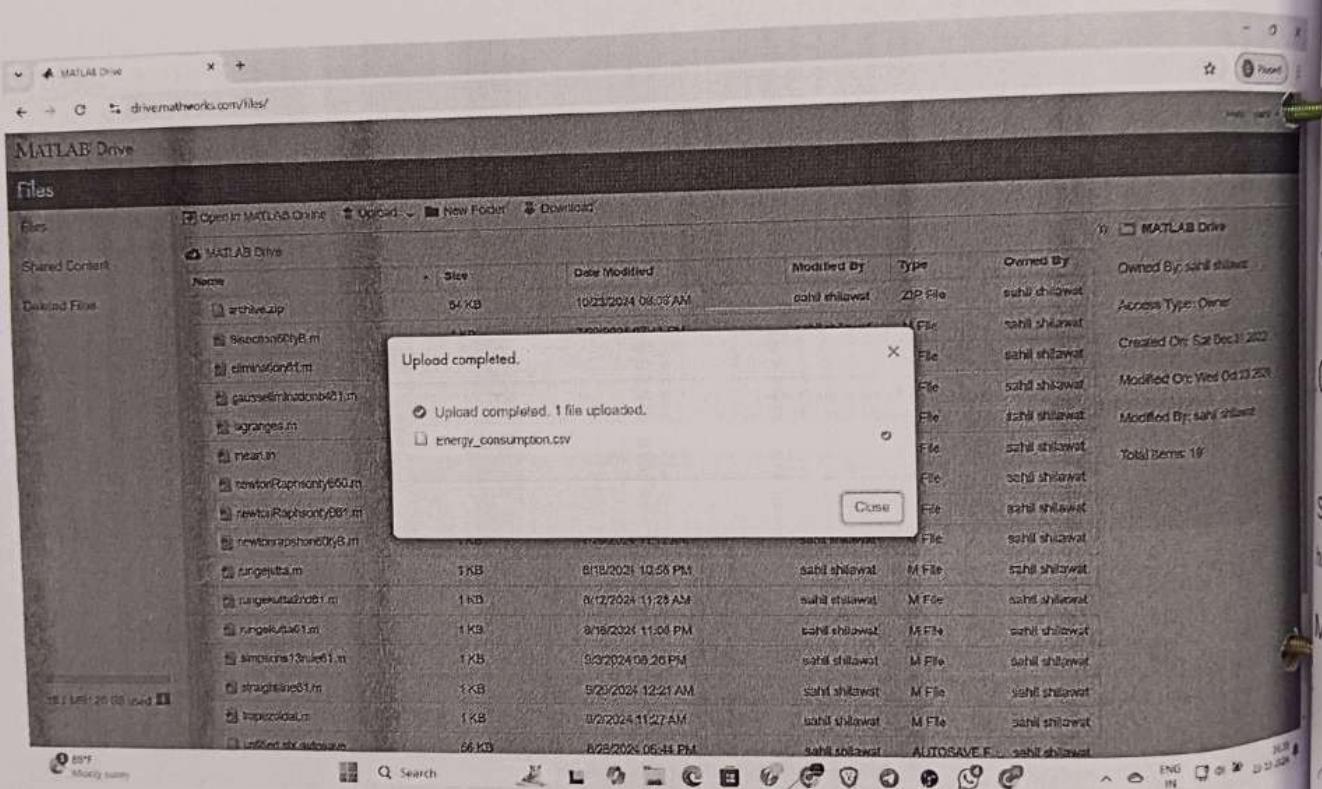
Start Session Cancel

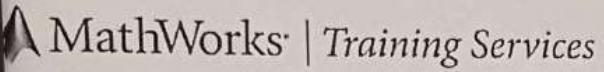










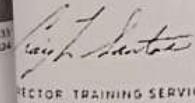


Course Completion Certificate

Mirran Akhade

has successfully completed **100%** of the self-paced training course

ATLAB Fundamentals


Mirran Akhade

20 October 2024

VECTOR TRAINING SERVICES