Dimensionality reduction

Exercices

PCA

1. Load the nutrimouse data from the mixOmics R package and investigate its structure.

library(mixOmics)

A data object provided by an R package can be loaded with data. Its structure can be obtinted with str, length, dim, etc.

data("nutrimouse")
display the structure of the nutrimouse object
str(nutrimouse)

```
## List of 4
              :'data.frame':
                              40 obs. of 120 variables:
## $ gene
##
     ..$ X36b4
                  : num [1:40] -0.42 -0.44 -0.48 -0.45 -0.42 -0.43 -0.53 -0.49 -0.36
-0.5 ...
     ..$ ACAT1
                  : num [1:40] -0.65 -0.68 -0.74 -0.69 -0.71 -0.69 -0.62 -0.69 -0.66
##
-0.62 ...
     ..$ ACAT2
##
                  : num [1:40] -0.84 -0.91 -1.1 -0.65 -0.54 -0.8 -1 -0.91 -0.74 -0.79
. . .
                  : num [1:40] -0.34 -0.32 -0.46 -0.41 -0.38 -0.32 -0.44 -0.37 -0.39
##
     ..$ ACBP
-0.36 ...
    ..$ ACC1
                  : num [1:40] -1.29 -1.23 -1.3 -1.26 -1.21 -1.13 -1.22 -1.29 -1.15 -
##
1.21 ...
##
   ..$ ACC2
                  : num [1:40] -1.13 -1.06 -1.09 -1.09 -0.89 -0.79 -1 -1.06 -1.08 -0.
82 ...
## ..$ ACOTH
                  : num [1:40] -0.93 -0.99 -1.06 -0.93 -1 -0.93 -0.94 -1.05 -0.88 -0.
92 ...
##
    ..$ ADISP
                  : num [1:40] -0.98 -0.97 -1.08 -1.02 -0.95 -0.97 -0.94 -1.02 -0.98
-0.99 ...
##
     ..$ ADSS1
                  : num [1:40] -1.19 -1 -1.18 -1.07 -1.08 -1.07 -1.05 -1.16 -1.05 -1
. . .
##
    ..$ ALDH3
                  : num [1:40] -0.68 -0.62 -0.75 -0.71 -0.76 -0.75 -0.67 -0.75 -0.66
-0.69 ...
##
     ..$ AM2R
                  : num [1:40] -0.59 -0.58 -0.66 -0.65 -0.59 -0.55 -0.66 -0.66 -0.53
-0.62 ...
##
    ..$ AOX
                  : num [1:40] -0.16 -0.12 -0.16 -0.17 -0.31 -0.23 -0.09 -0.22 -0.06
-0.23 ...
##
    ..$ BACT
                  : num [1:40] -0.22 -0.32 -0.32 -0.32 -0.31 -0.29 -0.25 -0.21 -0.15
-0.2 ...
    ..$ BIEN
##
                  : num [1:40] -0.89 -0.88 -0.89 -0.77 -0.97 -0.84 -0.86 -0.9 -0.74 -
0.76 ...
##
    ..$ BSEP
                  : num [1:40] -0.69 -0.6 -0.7 -0.67 -0.68 -0.55 -0.67 -0.66 -0.6 -0.
58 ...
##
    ..$ Bcl.3
                  : num [1:40] -1.18 -1.07 -1.17 -1.12 -0.93 -1.08 -1.03 -1.01 -1.01
-1.1 ...
##
     ..$ C16SR
                 : num [1:40] 1.66 1.65 1.57 1.61 1.66 1.7 1.58 1.62 1.72 1.55 ...
##
    ..$ CACP
                  : num [1:40] -0.92 -0.87 -1.02 -0.89 -0.93 -0.97 -0.97 -0.96 -0.85
-0.95 ...
   ..$ CAR1
                  : num [1:40] -0.97 -0.92 -0.98 -0.97 -1.06 -1.03 -0.91 -1.11 -0.85
-0.99 ...
## ..$ CBS
                  : num [1:40] -0.26 -0.36 -0.4 -0.39 -0.35 -0.31 -0.32 -0.4 -0.26 -
0.39 ...
   ..$ CIDEA
                  : num [1:40] -1.21 -1.17 -1.29 -1.18 -1.15 -1.14 -1.16 -1.26 -1.12
-1.08 ...
## ..$ COX1
                  : num [1:40] -1.11 -1.06 -1.17 -1.03 -0.99 -1.03 -1.15 -1.18 -0.94
-1.07 ...
##
   ..$ COX2
                  : num [1:40] -1.18 -1.06 -1.14 -1.13 -1.1 -1.16 -1.06 -1.24 -1.23 -
1.09 ...
   ..$ CPT2
##
                  : num [1:40] -0.87 -0.87 -0.95 -0.88 -0.91 -0.92 -0.86 -0.93 -0.82
-0.88 ...
## ..$ CYP24
                  : num [1:40] -1.37 -1.14 -1.3 -1.27 -1.2 -1.11 -1.12 -1.3 -1.14 -1.
08 ...
##
    ..$ CYP26
                  : num [1:40] -1.21 -1.12 -1.22 -1.18 -1.16 -1.1 -1.07 -1.23 -1.1 -
1.1 ...
## ..$ CYP27a1 : num [1:40] -0.71 -0.62 -0.78 -0.71 -0.69 -0.6 -0.69 -0.81 -0.62 -
0.62 ...
```

```
##
     ..$ CYP27b1 : num [1:40] -1.31 -1.14 -1.29 -1.27 -1.2 -1.15 -1.17 -1.28 -1.13 -
1.15 ...
     ..$ CYP2b10 : num [1:40] -1.23 -1.2 -1.32 -1.23 -1.22 -1.1 -1.07 -1.26 -1.19 -
##
1.1 ...
##
     ..$ CYP2b13
                 : num [1:40] -1.19 -1.06 -1.25 -1.13 -1.1 -1.07 -1.2 -1.37 -1.15 -
1.11 ...
##
     ..$ CYP2c29 : num [1:40] -0.06 -0.2 -0.3 -0.07 -0.29 -0.28 -0.1 -0.1 0.18 -0.33
##
     ..$ CYP3A11
                 : num [1:40] -0.09 -0.34 -0.45 -0.11 -0.51 -0.55 -0.18 -0.25 0.06 -
0.4 ...
##
     ..$ CYP4A10
                 : num [1:40] -0.81 -0.88 -0.71 -0.65 -1.16 -0.99 -0.62 -0.82 -0.48
-0.79 ...
     ..$ CYP4A14 : num [1:40] -0.81 -0.84 -0.98 -0.41 -1.16 -1.09 -0.76 -0.87 -0.37
##
-0.95 ...
     ..$ CYP7a
                  : num [1:40] -0.77 -0.71 -0.93 -0.8 -0.71 -0.74 -0.76 -0.88 -0.77 -
##
0.77 ...
     ..$ CYP8b1
                 : num [1:40] -0.77 -0.63 -0.53 -0.73 -0.51 -0.55 -0.57 -0.63 -0.6 -
0.66 ...
##
     ..$ FAS
                  : num [1:40] -0.41 -0.37 -0.3 -0.59 -0.06 0.18 -0.16 0.04 -0.53 0.0
8 ...
                  : num [1:40] -1.03 -0.98 -1.03 -1.06 -0.99 -0.99 -0.89 -1.08 -1.04
##
     ..$ FAT
-0.91 ...
    ..$ FDFT
                  : num [1:40] -0.98 -0.92 -1.04 -1 -0.99 -1 -1.02 -0.97 -1.03 -0.95
##
. . .
##
    ..$ FXR
                  : num [1:40] -0.93 -0.87 -1 -0.9 -0.89 -0.89 -0.86 -1.01 -0.81 -0.9
1 ...
##
     ..$ G6PDH
                  : num [1:40] -1.22 -1.09 -1.28 -1.19 -1.16 -0.96 -1.15 -1.26 -1.13
-1.03 ...
##
     ..$ G6Pase
                  : num [1:40] -0.46 -0.63 -1.06 -0.71 -0.58 -0.49 -0.51 -0.61 -0.38
-0.6 ...
     ..$ GK
##
                  : num [1:40] -0.71 -0.67 -0.68 -0.75 -0.62 -0.59 -0.59 -0.66 -0.68
-0.47 ...
##
     ..$ GS
                  : num [1:40] -1.24 -1.22 -1.36 -1.21 -1.22 -1.16 -1.15 -1.31 -1.16
-1.19 ...
     ..$ GSTa
                  : num [1:40] 0 -0.05 -0.13 -0.09 -0.02 -0.11 -0.06 -0.04 0.03 -0.02
##
. . .
##
     ..$ GSTmu
                  : num [1:40] 0.02 -0.05 -0.19 0.03 -0.23 -0.05 -0.22 -0.07 0.23 -0.
14 ...
                  : num [1:40] 0.45 0.3 0.18 0.36 0.3 0.17 0.12 0.48 0.53 0.01 ...
##
     ..$ GSTpi2
##
     ..$ HMGCoAred: num [1:40] -0.95 -0.86 -0.96 -1.02 -0.7 -0.76 -1 -0.88 -0.96 -0.7
##
     ..$ HPNCL
                  : num [1:40] -0.65 -0.69 -0.75 -0.61 -0.66 -0.56 -0.61 -0.71 -0.53
-0.6 ...
     ..$ IL.2
                  : num [1:40] -0.94 -0.94 -1.16 -0.97 -0.93 -0.96 -0.96 -0.85 -0.84
##
-0.95 ...
##
     ..$ L.FABP
                  : num [1:40] 0.24 0.27 0.17 0.16 0 0.23 0.18 0.18 0.2 0.2 ...
##
     ..$ LCE
                  : num [1:40] 0.09 0.06 -0.05 0.01 -0.07 -0.1 -0.03 -0.08 0.12 -0.1
. . .
##
     ..$ LDLr
                  : num [1:40] -0.82 -0.68 -0.82 -0.94 -0.73 -0.74 -0.8 -0.83 -0.81 -
0.72 ...
##
     ..$ LPK
                  : num [1:40] -0.32 -0.39 -0.38 -0.38 -0.17 -0.14 -0.35 -0.13 -0.32
-0.24 ...
     ..$ LPL
                  : num [1:40] -1.01 -0.97 -1.11 -0.99 -1.05 -0.99 -0.93 -1.07 -0.94
##
-0.95 ...
## ..$ LXRa
                  : num [1:40] -0.82 -0.82 -0.91 -0.85 -0.83 -0.79 -0.77 -0.84 -0.75
-0.78 ...
```

```
##
   ..$ LXRb
                 : num [1:40] -1 -0.95 -1.16 -1.01 -1.01 -0.99 -0.98 -1.04 -0.98 -0.
99 ...
                  : num [1:40] -0.87 -0.97 -0.95 -1 -0.57 -0.51 -0.81 -0.83 -0.83 -0.
##
   ..$ Lpin
48 ...
##
     ..$ Lpin1
                  : num [1:40] -0.85 -0.99 -0.94 -1.02 -0.53 -0.51 -0.81 -0.87 -0.82
-0.49 ...
##
   ..$ Lpin2
                  : num [1:40] -0.85 -0.87 -0.9 -0.88 -0.72 -0.68 -0.8 -0.9 -0.68 -0.
67 ...
##
     ..$ Lpin3
                  : num [1:40] -1.23 -1.12 -1.25 -1.18 -1.12 -1.09 -1.04 -1.23 -1.13
-1.11 ...
##
     ..$ M.CPT1
                  : num [1:40] -1.15 -1.06 -1.26 -1.1 -1.11 -1.14 -1.08 -1.19 -1.06 -
1.09 ...
##
     ..$ MCAD
                  : num [1:40] -0.6 -0.62 -0.7 -0.59 -0.69 -0.66 -0.53 -0.66 -0.45 -
0.62 ...
##
     ..$ MDR1
                  : num [1:40] -1.15 -1.1 -1.26 -1.13 -1.11 -1.09 -1.09 -1.19 -1.06 -
1.1 ...
##
     ..$ MDR2
                  : num [1:40] -0.77 -0.65 -0.86 -0.77 -0.7 -0.69 -0.81 -0.81 -0.69 -
0.75 ...
##
     ..$ MRP6
                  : num [1:40] -0.99 -0.85 -0.9 -0.95 -0.91 -0.84 -0.88 -1.02 -0.83 -
0.86 ...
##
     ..$ MS
                  : num [1:40] -1.11 -1.06 -1.2 -1.09 -1.09 -1.09 -0.99 -1.16 -1.06 -
0.98 ...
     ..$ MTHFR
                  : num [1:40] -0.96 -0.99 -1.1 -0.95 -0.93 -0.96 -0.88 -1.03 -1.01 -
##
0.95 ...
##
     ..$ NGFiB
                  : num [1:40] -1.21 -1.08 -1.24 -1.12 -1.11 -1.04 -1.02 -1.21 -1.11
-1.04 ...
     ..$ NURR1
##
                  : num [1:40] -1.21 -1.1 -1.32 -1.11 -1.14 -1.18 -1.1 -1.26 -1.14 -
1.09 ...
##
                  : num [1:40] -0.49 -0.45 -0.44 -0.54 -0.47 -0.46 -0.55 -0.5 -0.44 -
     ..$ Ntcp
0.43 ...
     ..$ OCTN2
##
                  : num [1:40] -1.15 -1.15 -1.2 -1.17 -1.19 -1.11 -1.08 -1.21 -1.05 -
1.08 ...
##
     ..$ PAL
                  : num [1:40] -1.32 -1.25 -1.16 -1.25 -1.24 -1.02 -1.04 -1.27 -0.93
-0.92 ...
     ..$ PDK4
                  : num [1:40] -1.16 -1.16 -1.27 -1.16 -1.13 -1.08 -1.14 -1.24 -1.19
##
-1.04 ...
##
     ..$ PECI
                  : num [1:40] -0.68 -0.69 -0.92 -0.71 -0.83 -0.81 -0.79 -0.85 -0.58
-0.82 ...
##
    ..$ PLTP
                  : num [1:40] -1.1 -0.99 -1.03 -1.08 -0.98 -0.89 -1.05 -1.07 -1.02 -
0.85 ...
##
     ..$ PMDCI
                  : num [1:40] -0.52 -0.52 -0.6 -0.52 -0.71 -0.69 -0.55 -0.57 -0.46 -
0.69 ...
##
     ..$ PON
                  : num [1:40] -0.52 -0.55 -0.65 -0.64 -0.57 -0.63 -0.56 -0.65 -0.6 -
0.64 ...
##
     ..$ PPARa
                  : num [1:40] -0.93 -0.86 -0.95 -0.97 -0.94 -0.95 -0.9 -1.12 -0.88 -
0.95 ...
##
    ..$ PPARd
                  : num [1:40] -1.51 -1.59 -1.71 -1.57 -1.53 -1.56 -1.49 -1.57 -1.58
-1.54 ...
##
   ..$ PPARg
                  : num [1:40] -1.06 -1.02 -1.14 -1.05 -1.09 -1.01 -1 -1.13 -0.97 -1.
07 ...
##
     ..$ PXR
                  : num [1:40] -0.99 -0.96 -1.1 -0.99 -1 -1.03 -0.93 -1.07 -0.98 -0.9
6 ...
##
     ..$ Pex11a
                  : num [1:40] -1 -1.02 -1.2 -1 -0.95 -1.07 -1.05 -1.02 -1 -1.01 ...
                  : num [1:40] -1.2 -1.06 -1.16 -1.17 -1.15 -1.13 -1.09 -1.24 -1.03 -
##
     ..$ RARa
1.09 ...
##
     ..$ RARb2
                  : num [1:40] -1.19 -1.11 -1.23 -1.16 -1.14 -1.07 -1.09 -1.18 -1.12
```

```
-1.1 ...
## ..$ RXRa
                 : num [1:40] -0.67 -0.59 -0.68 -0.72 -0.78 -0.62 -0.65 -0.76 -0.55
-0.67 ...
    ..$ RXRb2
                 : num [1:40] -0.95 -0.95 -1.07 -0.95 -0.98 -0.94 -0.92 -1.03 -0.94
##
-0.95 ...
##
    ..$ RXRq1
                 : num [1:40] -1.16 -1.1 -1.21 -1.1 -1.11 -1.03 -1.07 -1.19 -1.05 -
1.04 ...
##
    ..$ S14
                 : num [1:40] -0.93 -0.86 -0.84 -1.05 -0.65 -0.4 -0.73 -0.62 -0.99 -
0.25 ...
## ..$ SHP1
                  : num [1:40] -1.1 -0.97 -1.09 -1.03 -1.13 -0.98 -0.95 -1.21 -0.93 -
0.97 ...
    ..$ SIAT4c
                : num [1:40] -1.07 -0.97 -1.04 -0.99 -0.94 -0.93 -0.89 -1.04 -0.93
##
-0.95 ...
## ..$ SPI1.1
                : num [1:40] 1.19 1.15 1.09 1.07 1.22 1.05 1.15 1.18 1.21 1.04 ...
    ..$ SR.BI
                 : num [1:40] -0.84 -0.86 -0.95 -0.95 -1.06 -0.8 -0.83 -1 -0.83 -0.7
##
7 ...
##
    ..$ THB
                 : num [1:40] -0.79 -0.85 -0.92 -0.79 -0.84 -0.86 -0.8 -0.86 -0.83 -
0.85 ...
##
    ..$ THIOL
                 : num [1:40] -0.18 -0.15 -0.24 -0.15 -0.35 -0.29 -0.22 -0.23 -0.17
-0.18 ...
    ..$ TRa
                 : num [1:40] -1.48 -1.46 -1.58 -1.54 -1.46 -1.44 -1.32 -1.56 -1.46
##
-1.35 ...
##
   ..$ TRb
                  : num [1:40] -1.07 -1 -1.16 -1.11 -1.01 -1 -0.97 -1.08 -1.02 -0.98
. . .
##
    ..$ Tpalpha : num [1:40] -0.69 -0.74 -0.81 -0.74 -0.82 -0.76 -0.72 -0.76 -0.65
-0.83 ...
##
    ..$ Tpbeta : num [1:40] -1.11 -1.09 -1.14 -1.04 -1.2 -1.05 -1 -1.16 -0.91 -1.0
7 ...
##
     .. [list output truncated]
## $ lipid :'data.frame':
                               40 obs. of 21 variables:
     ..$ C14.0 : num [1:40] 0.34 0.38 0.36 0.22 0.37 1.7 0.35 0.34 0.22 1.38 ...
##
     ..$ C16.0 : num [1:40] 26.4 24 23.7 25.5 24.8 ...
##
     ..$ C18.0 : num [1:40] 10.22 9.93 8.96 8.14 9.63 ...
##
     ..$ C16.1n.9: num [1:40] 0.35 0.55 0.55 0.49 0.46 0.66 0.36 0.29 0.44 0.9 ...
##
     ..$ C16.1n.7: num [1:40] 3.1 2.54 2.65 2.82 2.85 7.26 3.6 3.27 2.36 7.01 ...
##
     ..$ C18.1n.9: num [1:40] 17 20.1 22.9 21.9 21.4 ...
##
##
     ..$ C18.1n.7: num [1:40] 2.41 3.92 3.96 2.52 2.96 8.99 2.15 1.99 1.81 8.85 ...
##
     ..$ C20.1n.9: num [1:40] 0.26 0.23 0.26 0 0.3 0.36 0.25 0.31 0 0.21 ...
     ..$ C20.3n.9: num [1:40] 0 0 0.19 0 0.27 2.89 0 0 0 2.03 ...
##
     ..$ C18.2n.6: num [1:40] 8.93 14.98 16.06 13.89 14.55 ...
##
     ..$ C18.3n.6: num [1:40] 0 0.3 0.27 0 0.27 2.66 0 0 0 0 ...
##
     ..$ C20.2n.6: num [1:40] 0 0.3 0.33 0 0.23 0 0 0 0 ...
##
     ..$ C20.3n.6: num [1:40] 0.78 1.64 1.51 1.1 1.58 0.81 0.68 0.72 1.07 0.59 ...
##
##
     ..$ C20.4n.6: num [1:40] 3.07 15.34 13.27 3.92 11.85 ...
##
     ..$ C22.4n.6: num [1:40] 0 0.58 0.54 0 0.32 0 0 0 0 0 ...
##
     ..$ C22.5n.6: num [1:40] 0 2.1 1.77 0 0.44 0.56 0 0 0 0.39 ...
     ..$ C18.3n.3: num [1:40] 5.97 0 0 0.49 0.42 0 8.4 6.01 0.55 0 ...
##
##
     ..$ C20.3n.3: num [1:40] 0.37 0 0 0 0 0.42 0.39 0 0 ...
     ..$ C20.5n.3: num [1:40] 8.62 0 0 2.99 0.3 0 7.37 7.96 3.13 0 ...
##
     ..$ C22.5n.3: num [1:40] 1.75 0.48 0.22 1.04 0.35 2.13 2.05 2.33 1.65 0 ...
##
     ..$ C22.6n.3: num [1:40] 10.39 2.61 2.51 14.99 6.69 ...
##
            : Factor w/ 5 levels "coc", "fish", "lin", ...: 3 5 5 2 4 1 3 3 2 1 ...
##
    $ diet
##
    $ genotype: Factor w/ 2 levels "wt", "ppar": 1 1 1 1 1 1 1 1 1 1 1 ...
```

```
## check dimensions lapply(nutrimouse, dim) # apply function dim to each element in list nutrimouse
```

```
## $gene
## [1] 40 120
##
## $lipid
## [1] 40 21
##
## $diet
## NULL
##
## $genotype
## NULL
```

lapply(nutrimouse, length) # apply function length to each element in list nutrimouse

```
## $gene
## [1] 120
##
## $lipid
## [1] 21
##
## $diet
## [1] 40
##
## $genotype
## [1] 40
```

2. Take the gene expression dataset in *samples* x *variables* matrix format. Investigate their distribution.

```
## get gene expression data structure
str(nutrimouse$gene)
```

```
##
   'data.frame':
                     40 obs. of 120 variables:
##
                       -0.42 \ -0.44 \ -0.48 \ -0.45 \ -0.42 \ -0.43 \ -0.53 \ -0.49 \ -0.36 \ -0.5 \dots
    $ X36b4
                : num
##
    $ ACAT1
                : num
                       -0.65 -0.68 -0.74 -0.69 -0.71 -0.69 -0.62 -0.69 -0.66 -0.62 ...
##
    $ ACAT2
                       -0.84 -0.91 -1.1 -0.65 -0.54 -0.8 -1 -0.91 -0.74 -0.79 ...
                : num
##
    $ ACBP
                       -0.34 -0.32 -0.46 -0.41 -0.38 -0.32 -0.44 -0.37 -0.39 -0.36 ...
                : num
##
    $ ACC1
                       -1.29 -1.23 -1.3 -1.26 -1.21 -1.13 -1.22 -1.29 -1.15 -1.21 ...
                : num
                       -1.13 -1.06 -1.09 -1.09 -0.89 -0.79 -1 -1.06 -1.08 -0.82 ...
##
    $ ACC2
                : num
##
    $ ACOTH
                       -0.93 -0.99 -1.06 -0.93 -1 -0.93 -0.94 -1.05 -0.88 -0.92 ...
                : num
                       -0.98 -0.97 -1.08 -1.02 -0.95 -0.97 -0.94 -1.02 -0.98 -0.99 ...
##
    $ ADISP
                : num
##
    $ ADSS1
                       -1.19 -1 -1.18 -1.07 -1.08 -1.07 -1.05 -1.16 -1.05 -1 ...
                : num
##
    $ ALDH3
                       -0.68 - 0.62 - 0.75 - 0.71 - 0.76 - 0.75 - 0.67 - 0.75 - 0.66 - 0.69 \dots
                : num
##
    $ AM2R
                       -0.59 -0.58 -0.66 -0.65 -0.59 -0.55 -0.66 -0.66 -0.53 -0.62 ...
                : num
##
    $ AOX
                       -0.16 -0.12 -0.16 -0.17 -0.31 -0.23 -0.09 -0.22 -0.06 -0.23 ...
                : num
##
    $ BACT
                : num
                       -0.22 -0.32 -0.32 -0.32 -0.31 -0.29 -0.25 -0.21 -0.15 -0.2 \dots
##
    $ BIEN
                       -0.89 -0.88 -0.89 -0.77 -0.97 -0.84 -0.86 -0.9 -0.74 -0.76 ...
                : num
##
    $ BSEP
                       -0.69 -0.6 -0.7 -0.67 -0.68 -0.55 -0.67 -0.66 -0.6 -0.58 ...
                : num
##
    $ Bcl.3
                       -1.18 -1.07 -1.17 -1.12 -0.93 -1.08 -1.03 -1.01 -1.01 -1.1 ...
                : num
                       1.66 1.65 1.57 1.61 1.66 1.7 1.58 1.62 1.72 1.55 ...
##
    $ C16SR
                : num
                       -0.92 - 0.87 - 1.02 - 0.89 - 0.93 - 0.97 - 0.97 - 0.96 - 0.85 - 0.95 ...
##
    $ CACP
                : num
##
    $ CAR1
                       -0.97 -0.92 -0.98 -0.97 -1.06 -1.03 -0.91 -1.11 -0.85 -0.99 ...
                : num
##
    $ CBS
                : num
                       -0.26 -0.36 -0.4 -0.39 -0.35 -0.31 -0.32 -0.4 -0.26 -0.39 ...
##
                       -1.21 -1.17 -1.29 -1.18 -1.15 -1.14 -1.16 -1.26 -1.12 -1.08 ...
    $ CIDEA
                : num
##
    $ COX1
                       -1.11 -1.06 -1.17 -1.03 -0.99 -1.03 -1.15 -1.18 -0.94 -1.07 ...
                : num
##
    $ COX2
                       -1.18 -1.06 -1.14 -1.13 -1.1 -1.16 -1.06 -1.24 -1.23 -1.09 ...
                : num
##
    $ CPT2
                       -0.87 -0.87 -0.95 -0.88 -0.91 -0.92 -0.86 -0.93 -0.82 -0.88 ...
                : num
##
                       -1.37 -1.14 -1.3 -1.27 -1.2 -1.11 -1.12 -1.3 -1.14 -1.08 ...
    $ CYP24
                : num
##
    $ CYP26
                       -1.21 -1.12 -1.22 -1.18 -1.16 -1.1 -1.07 -1.23 -1.1 -1.1 ...
                : num
    $ CYP27a1
##
                       -0.71 -0.62 -0.78 -0.71 -0.69 -0.6 -0.69 -0.81 -0.62 -0.62 ...
               : num
##
    $ CYP27b1
                       -1.31 -1.14 -1.29 -1.27 -1.2 -1.15 -1.17 -1.28 -1.13 -1.15 ...
                : num
                       -1.23 -1.2 -1.32 -1.23 -1.22 -1.1 -1.07 -1.26 -1.19 -1.1 ...
##
    $ CYP2b10
               : num
##
    $ CYP2b13
                : num
                       -1.19 -1.06 -1.25 -1.13 -1.1 -1.07 -1.2 -1.37 -1.15 -1.11 ...
##
    $ CYP2c29
                       -0.06 -0.2 -0.3 -0.07 -0.29 -0.28 -0.1 -0.1 0.18 -0.33 ...
               : num
##
    $ CYP3A11
                       -0.09 -0.34 -0.45 -0.11 -0.51 -0.55 -0.18 -0.25 0.06 -0.4 ...
                : num
##
    $ CYP4A10
                       -0.81 -0.88 -0.71 -0.65 -1.16 -0.99 -0.62 -0.82 -0.48 -0.79 ...
               : num
##
    $ CYP4A14
                       -0.81 - 0.84 - 0.98 - 0.41 - 1.16 - 1.09 - 0.76 - 0.87 - 0.37 - 0.95 ...
                : num
                       -0.77 -0.71 -0.93 -0.8 -0.71 -0.74 -0.76 -0.88 -0.77 -0.77 ...
##
    $ CYP7a
                : num
##
    $ CYP8b1
                       -0.77 -0.63 -0.53 -0.73 -0.51 -0.55 -0.57 -0.63 -0.6 -0.66 ...
                : num
##
    $ FAS
                : num
                       -0.41 -0.37 -0.3 -0.59 -0.06 0.18 -0.16 0.04 -0.53 0.08 ...
    $ FAT
                       -1.03 -0.98 -1.03 -1.06 -0.99 -0.99 -0.89 -1.08 -1.04 -0.91 ...
##
                : num
##
    $ FDFT
                : num
                       -0.98 \ -0.92 \ -1.04 \ -1 \ -0.99 \ -1 \ -1.02 \ -0.97 \ -1.03 \ -0.95 \ \dots
##
    $ FXR
                       -0.93 -0.87 -1 -0.9 -0.89 -0.89 -0.86 -1.01 -0.81 -0.91 ...
                : num
##
    $ G6PDH
                : num
                       -1.22 -1.09 -1.28 -1.19 -1.16 -0.96 -1.15 -1.26 -1.13 -1.03 ...
##
    $ G6Pase
                       -0.46 - 0.63 - 1.06 - 0.71 - 0.58 - 0.49 - 0.51 - 0.61 - 0.38 - 0.6 \dots
                : num
##
    $ GK
                       -0.71 -0.67 -0.68 -0.75 -0.62 -0.59 -0.59 -0.66 -0.68 -0.47 ...
                : num
##
    $ GS
                       -1.24 -1.22 -1.36 -1.21 -1.22 -1.16 -1.15 -1.31 -1.16 -1.19 ...
                : num
                       0 - 0.05 - 0.13 - 0.09 - 0.02 - 0.11 - 0.06 - 0.04 0.03 - 0.02 ...
##
    $ GSTa
                : num
##
    $ GSTmu
                : num
                       0.02 - 0.05 - 0.19 0.03 - 0.23 - 0.05 - 0.22 - 0.07 0.23 - 0.14 ...
                       0.45 0.3 0.18 0.36 0.3 0.17 0.12 0.48 0.53 0.01 ...
##
    $ GSTpi2
                : num
##
    $ HMGCoAred: num
                       -0.95 -0.86 -0.96 -1.02 -0.7 -0.76 -1 -0.88 -0.96 -0.7 ...
    $ HPNCL
##
                       -0.65 -0.69 -0.75 -0.61 -0.66 -0.56 -0.61 -0.71 -0.53 -0.6 ...
                : num
    $ IL.2
                       -0.94 -0.94 -1.16 -0.97 -0.93 -0.96 -0.96 -0.85 -0.84 -0.95 ...
##
                : num
##
    $ L.FABP
                       0.24 0.27 0.17 0.16 0 0.23 0.18 0.18 0.2 0.2 ...
                : num
    $ LCE
                       0.09 \ 0.06 \ -0.05 \ 0.01 \ -0.07 \ -0.1 \ -0.03 \ -0.08 \ 0.12 \ -0.1 \ \dots
##
                : num
##
    $ LDLr
                       -0.82 -0.68 -0.82 -0.94 -0.73 -0.74 -0.8 -0.83 -0.81 -0.72 ...
                : num
##
    $ LPK
                       -0.32 \ -0.39 \ -0.38 \ -0.38 \ -0.17 \ -0.14 \ -0.35 \ -0.13 \ -0.32 \ -0.24 \ \dots
                : num
```

```
##
                      -1.01 -0.97 -1.11 -0.99 -1.05 -0.99 -0.93 -1.07 -0.94 -0.95 ...
    $ LPL
               : num
##
                      -0.82 \ -0.82 \ -0.91 \ -0.85 \ -0.83 \ -0.79 \ -0.77 \ -0.84 \ -0.75 \ -0.78 \ \dots
    $ LXRa
               : num
                      -1 -0.95 -1.16 -1.01 -1.01 -0.99 -0.98 -1.04 -0.98 -0.99 ...
##
    $ LXRb
               : num
##
    $ Lpin
                      -0.87 -0.97 -0.95 -1 -0.57 -0.51 -0.81 -0.83 -0.83 -0.48 ...
               : num
    $ Lpin1
##
                      -0.85 -0.99 -0.94 -1.02 -0.53 -0.51 -0.81 -0.87 -0.82 -0.49 ...
               : num
##
    $ Lpin2
                      -0.85 -0.87 -0.9 -0.88 -0.72 -0.68 -0.8 -0.9 -0.68 -0.67 ...
               : num
##
    $ Lpin3
                      -1.23 -1.12 -1.25 -1.18 -1.12 -1.09 -1.04 -1.23 -1.13 -1.11 ...
               : num
    $ M.CPT1
##
                      -1.15 -1.06 -1.26 -1.1 -1.11 -1.14 -1.08 -1.19 -1.06 -1.09 ...
               : num
    $ MCAD
                      -0.6 -0.62 -0.7 -0.59 -0.69 -0.66 -0.53 -0.66 -0.45 -0.62 ...
##
               : num
##
    $ MDR1
               : num
                      -1.15 -1.1 -1.26 -1.13 -1.11 -1.09 -1.09 -1.19 -1.06 -1.1 ...
##
    $ MDR2
                      -0.77 -0.65 -0.86 -0.77 -0.7 -0.69 -0.81 -0.81 -0.69 -0.75 ...
               : num
                      -0.99 -0.85 -0.9 -0.95 -0.91 -0.84 -0.88 -1.02 -0.83 -0.86 ...
##
    $ MRP6
               : num
##
    $ MS
                      -1.11 -1.06 -1.2 -1.09 -1.09 -1.09 -0.99 -1.16 -1.06 -0.98 ...
               : num
##
                      -0.96 -0.99 -1.1 -0.95 -0.93 -0.96 -0.88 -1.03 -1.01 -0.95 ...
    $ MTHFR
               : num
    $ NGFiB
                      -1.21 -1.08 -1.24 -1.12 -1.11 -1.04 -1.02 -1.21 -1.11 -1.04 ...
##
               : num
##
    $ NURR1
                      -1.21 -1.1 -1.32 -1.11 -1.14 -1.18 -1.1 -1.26 -1.14 -1.09 ...
               : num
##
    $ Ntcp
               : num
                      -0.49 -0.45 -0.44 -0.54 -0.47 -0.46 -0.55 -0.5 -0.44 -0.43 ...
##
    $ OCTN2
                      -1.15 -1.15 -1.2 -1.17 -1.19 -1.11 -1.08 -1.21 -1.05 -1.08 ...
               : num
##
    $ PAL
                      -1.32 -1.25 -1.16 -1.25 -1.24 -1.02 -1.04 -1.27 -0.93 -0.92 ...
               : num
##
    $ PDK4
                      -1.16 -1.16 -1.27 -1.16 -1.13 -1.08 -1.14 -1.24 -1.19 -1.04 ...
               : num
                      -0.68 -0.69 -0.92 -0.71 -0.83 -0.81 -0.79 -0.85 -0.58 -0.82 ...
##
    $ PECI
               : num
##
    $ PLTP
                      -1.1 -0.99 -1.03 -1.08 -0.98 -0.89 -1.05 -1.07 -1.02 -0.85 ...
               : num
##
    $ PMDCI
                      -0.52 -0.52 -0.6 -0.52 -0.71 -0.69 -0.55 -0.57 -0.46 -0.69 ...
               : num
##
    $ PON
                      -0.52 -0.55 -0.65 -0.64 -0.57 -0.63 -0.56 -0.65 -0.6 -0.64 ...
               : num
                      -0.93 -0.86 -0.95 -0.97 -0.94 -0.95 -0.9 -1.12 -0.88 -0.95 ...
##
    $ PPARa
               : num
##
    $ PPARd
                      -1.51 -1.59 -1.71 -1.57 -1.53 -1.56 -1.49 -1.57 -1.58 -1.54 ...
               : num
##
    $ PPARq
                      -1.06 -1.02 -1.14 -1.05 -1.09 -1.01 -1 -1.13 -0.97 -1.07 ...
               : num
##
    $ PXR
                      -0.99 -0.96 -1.1 -0.99 -1 -1.03 -0.93 -1.07 -0.98 -0.96 ...
               : num
##
   $ Pex11a
                      -1 -1.02 -1.2 -1 -0.95 -1.07 -1.05 -1.02 -1 -1.01 ...
               : num
##
    $ RARa
                      -1.2 -1.06 -1.16 -1.17 -1.15 -1.13 -1.09 -1.24 -1.03 -1.09 ...
               : num
##
    $ RARb2
                      -1.19 -1.11 -1.23 -1.16 -1.14 -1.07 -1.09 -1.18 -1.12 -1.1 ...
               : num
##
    $ RXRa
                      -0.67 -0.59 -0.68 -0.72 -0.78 -0.62 -0.65 -0.76 -0.55 -0.67 ...
               : num
                      -0.95 -0.95 -1.07 -0.95 -0.98 -0.94 -0.92 -1.03 -0.94 -0.95 ...
##
    $ RXRb2
               : num
##
    $ RXRq1
                      -1.16 -1.1 -1.21 -1.1 -1.11 -1.03 -1.07 -1.19 -1.05 -1.04 ...
               : num
##
    $ S14
                      -0.93 -0.86 -0.84 -1.05 -0.65 -0.4 -0.73 -0.62 -0.99 -0.25 ...
               : num
                      -1.1 -0.97 -1.09 -1.03 -1.13 -0.98 -0.95 -1.21 -0.93 -0.97 ...
##
    $ SHP1
               : num
##
    $ SIAT4c
                      -1.07 - 0.97 - 1.04 - 0.99 - 0.94 - 0.93 - 0.89 - 1.04 - 0.93 - 0.95 ...
               : num
##
    $ SPI1.1
                      1.19 1.15 1.09 1.07 1.22 1.05 1.15 1.18 1.21 1.04 ...
               : num
##
    $ SR.BI
                      -0.84 -0.86 -0.95 -0.95 -1.06 -0.8 -0.83 -1 -0.83 -0.77 ...
               : num
##
    $ THB
                      -0.79 -0.85 -0.92 -0.79 -0.84 -0.86 -0.8 -0.86 -0.83 -0.85 ...
               : num
##
    $ THIOL
                      -0.18 -0.15 -0.24 -0.15 -0.35 -0.29 -0.22 -0.23 -0.17 -0.18 ...
               : num
    $ TRa
##
               : num
                      -1.48 - 1.46 - 1.58 - 1.54 - 1.46 - 1.44 - 1.32 - 1.56 - 1.46 - 1.35 ...
##
    $ TRb
                      -1.07 -1 -1.16 -1.11 -1.01 -1 -0.97 -1.08 -1.02 -0.98 ...
               : num
                      -0.69 -0.74 -0.81 -0.74 -0.82 -0.76 -0.72 -0.76 -0.65 -0.83 ...
##
    $ Tpalpha
               : num
##
    $ Tpbeta
               : num
                      -1.11 -1.09 -1.14 -1.04 -1.2 -1.05 -1 -1.16 -0.91 -1.07 ...
##
     [list output truncated]
```

check if there are missing values
any(is.na(nutrimouse\$gene))

```
## investigate each variable
summary(nutrimouse$gene[, 1])
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -0.5800 -0.5025 -0.4600 -0.4552 -0.4200 -0.3000
```

```
colors <- rainbow(20, alpha=1)
plot(density(scale(nutrimouse$gene[, 1], center=T, scale=F)),
    col=colors[1], xlim=c(-0.5,0.5), ylim=c(0,8))
sapply(2:20, function(i) {
    lines(density(scale(nutrimouse$gene[, i], center=T, scale=F)), col=colors[i])
})</pre>
```

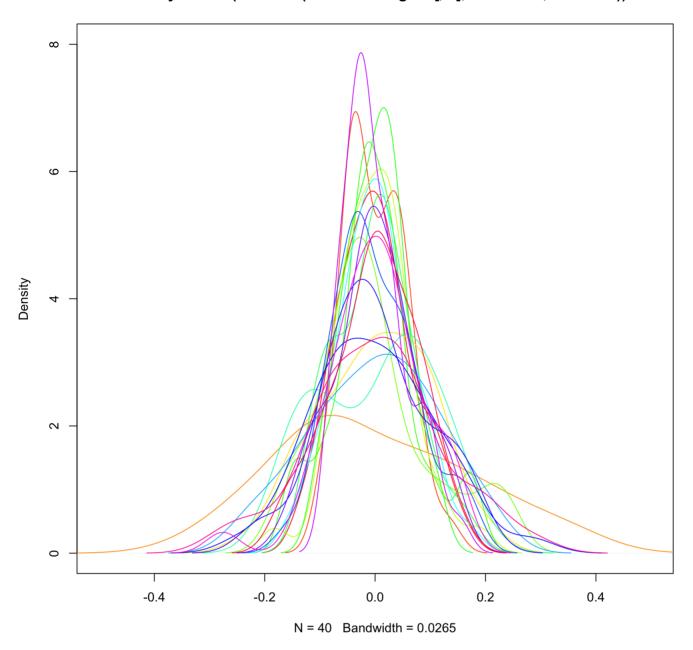
```
## [[1]]
## NULL
##
## [[2]]
## NULL
## [[3]]
## NULL
## [[4]]
## NULL
## [[5]]
## NULL
##
## [[6]]
## NULL
##
## [[7]]
## NULL
##
## [[8]]
## NULL
##
## [[9]]
## NULL
##
## [[10]]
## NULL
##
## [[11]]
## NULL
##
## [[12]]
## NULL
## [[13]]
## NULL
## [[14]]
## NULL
##
## [[15]]
## NULL
##
## [[16]]
## NULL
##
## [[17]]
## NULL
##
## [[18]]
## NULL
##
```

```
## [[19]]
## NULL
```

apply(nutrimouse\$gene, 2, summary)

```
##
                                          ACBP
                                                  ACC1
                                                          ACC2
                                                                  АСОТН
              X36b4
                       ACAT1
                                ACAT2
                                                                            ADTSP
           -0.58000 -0.75000 -1.10000 -0.66000 -1.4400 -1.2000 -1.06000 -1.08000
## Min.
## 1st Qu. -0.50250 -0.69000 -0.88000 -0.50250 -1.3000 -1.0900 -0.95000 -1.02000
## Median
          -0.46000 -0.66000 -0.79500 -0.42500 -1.2600 -1.0450 -0.92000 -0.97000
## Mean
           -0.45525 -0.65525 -0.76675 -0.43375 -1.2585 -1.0280 -0.91075 -0.97825
## 3rd Qu. -0.42000 -0.62000 -0.64500 -0.35500 -1.2200 -0.9875 -0.88000 -0.94000
           -0.30000 -0.52000 -0.39000 -0.24000 -1.0700 -0.7900 -0.73000 -0.87000
## Max.
##
                      ALDH3
                              AM2R
                                       AOX
                                               BACT
                                                        BIEN
                                                                BSEP
              ADSS1
                                                                        Bc1.3
           -1.19000 -0.9900 -0.780 -0.4800 -0.44000 -1.16000 -0.9000 -1.22000
## Min.
## 1st Qu. -1.14000 -0.9100 -0.670 -0.3175 -0.32250 -0.99000 -0.7600 -1.10250
          -1.07500 -0.7850 -0.630 -0.2300 -0.30000 -0.92000 -0.7000 -1.06500
           -1.07575 -0.8100 -0.628 -0.2505 -0.28275 -0.92125 -0.6910 -1.05875
## 3rd Qu. -1.03500 -0.7475 -0.590 -0.1675 -0.23500 -0.85500 -0.6275 -1.01000
## Max.
           -0.91000 -0.6200 -0.460 -0.0400 -0.11000 -0.64000 -0.5100 -0.91000
                                                       COX1
##
                                       CBS
                                            CIDEA
                                                              COX2
             C16SR
                      CACP
                              CAR1
                                                                      СРТ2
                                                                              CYP24
## Min.
           1.55000 -1.2600 -1.1900 -0.5600 -1.3300 -1.18000 -1.280 -1.2000 -1.3700
## 1st Ou. 1.59000 -1.0325 -0.9900 -0.4450 -1.2325 -1.09250 -1.180 -1.0100 -1.2600
## Median 1.61000 -0.9800 -0.9100 -0.4000 -1.1700 -1.05500 -1.130 -0.9450 -1.1800
           1.62675 - 0.9845 - 0.9135 - 0.3995 - 1.1840 - 1.04975 - 1.135 - 0.9565 - 1.1925
## Mean
## 3rd Qu. 1.65250 -0.9375 -0.8475 -0.3375 -1.1400 -1.01000 -1.090 -0.8800 -1.1375
## Max.
           1.78000 - 0.8300 - 0.6300 - 0.2600 - 1.0700 - 0.88000 - 1.040 - 0.8200 - 1.0500
             CYP26 CYP27a1 CYP27b1 CYP2b10 CYP2b13 CYP2c29 CYP3A11 CYP4A10
##
## Min.
           -1.3200 -0.88000 -1.350 -1.32000 -1.37000 -0.52000 -1.02000 -1.33000
## 1st Qu. -1.2225 -0.78500 -1.245 -1.23000 -1.19250 -0.28250 -0.71250 -1.15250
          -1.1500 -0.73000 -1.180 -1.20000 -1.14000 -0.14000 -0.53000 -1.05000
## Median
           -1.1560 -0.72725 -1.200 -1.18475 -1.14575 -0.14725 -0.50825 -0.97975
## Mean
## 3rd Qu. -1.1000 -0.67000 -1.150 -1.15000 -1.09750 -0.03000 -0.38500 -0.81750
## Max.
           -0.9600 -0.59000 -0.990 -1.04000 -0.96000 0.18000 0.06000 -0.48000
##
           CYP4A14
                     CYP7a
                             CYP8b1
                                         FAS
                                                 FAT
                                                         FDFT
                                                                   FXR
                                                                          G6PDH
           -1.2900 -0.9300 -1.01000 -1.05000 -1.0900 -1.17000 -1.0600 -1.30000
## Min.
## 1st Ou. -1.1500 -0.8000 -0.76000 -0.67000 -1.0400 -1.02000 -0.9525 -1.20250
## Median -1.0800 -0.7700 -0.67000 -0.49000 -0.9950 -0.99000 -0.9000 -1.15000
           -0.9930 -0.7695 -0.68225 -0.45175 -0.9910 -0.98075 -0.9105 -1.15125
## Mean
## 3rd Qu. -0.8925 -0.7400 -0.59000 -0.22500 -0.9475 -0.93750 -0.8775 -1.10750
## Max.
           -0.1500 -0.6100 -0.50000 0.18000 -0.7500 -0.81000 -0.7600 -0.96000
##
                         GK
                                 GS
                                       GSTa GSTmu GSTpi2 HMGCoAred
           -1.06000 -0.9600 -1.3800 -0.4300 -0.440 0.00000
## Min.
                                                             -1.0700 -0.97000
                                                            -0.9700 -0.75000
## 1st Qu. -0.82000 -0.8000 -1.3025 -0.1525 -0.200 0.12000
          -0.69000 -0.7000 -1.2250 -0.0900 -0.140 0.21000
                                                             -0.9300 -0.69000
## Mean
           -0.69825 -0.7145 -1.2325 -0.1030 -0.119 0.22975
                                                            -0.9135 -0.69375
## 3rd Qu. -0.53500 -0.6200 -1.1675 -0.0350 -0.050 0.33250
                                                             -0.8750 -0.60750
## Max.
           -0.38000 -0.4600 -1.1200 0.0400 0.230 0.55000
                                                             -0.7000 -0.53000
##
              IL.2 L.FABP
                                LCE
                                       LDLr
                                               LPK
                                                        _{
m LPL}
                                                               LXRa
                                                                       LXRb
## Min.
           -1.1600 -0.4600 -0.26000 -0.9600 -0.570 -1.11000 -0.9100 -1.1600
## 1st Qu. -1.0025 -0.0750 -0.10000 -0.8525 -0.395 -1.03000 -0.8400 -1.0225
          -0.9450 0.0600 -0.06000 -0.8200 -0.350 -0.99000 -0.8150 -0.9900
## Median
## Mean
           -0.9505 0.0340 -0.05275 -0.8195 -0.344 -0.99075 -0.8115 -0.9960
## 3rd Qu. -0.8975 0.1825 0.00000 -0.7675 -0.295 -0.95000 -0.7775 -0.9675
## Max.
           -0.8200 0.2800 0.12000 -0.6800 -0.130 -0.86000 -0.6500 -0.8400
##
                       Lpin1 Lpin2
                                      Lpin3
                                              M.CPT1
                                                        MCAD
                                                                 MDR1
               Lpin
                                                                          MDR 2
           -1.13000 -1.10000 -1.140 -1.2900 -1.29000 -0.7300 -1.30000 -0.92000
## Min.
## 1st Qu. -0.85500 -0.87000 -0.910 -1.1975 -1.16500 -0.6600 -1.16250 -0.83000
## Median -0.72500 -0.76000 -0.855 -1.1450 -1.12000 -0.6200 -1.12000 -0.78000
           -0.75325 -0.76475 -0.849 -1.1475 -1.12575 -0.6050 -1.13425 -0.77875
## Mean
## 3rd Qu. -0.61500 -0.64000 -0.775 -1.0975 -1.09000 -0.5575 -1.09000 -0.71750
```

```
## Max.
           -0.48000 \ -0.49000 \ -0.670 \ -0.9800 \ -0.96000 \ -0.4200 \ -0.99000 \ -0.65000
##
               MRP6
                          MS
                               MTHFR
                                         NGFiB
                                                  NURR1
                                                           Ntcp
                                                                    OCTN2
                                                                              PAT
## Min.
           -1.09000 -1.20000 -1.1000 -1.29000 -1.32000 -0.6500 -1.28000 -1.3200
## 1st Ou. -1.00250 -1.11000 -1.0025 -1.20000 -1.21000 -0.4925 -1.19000 -1.2550
## Median
           -0.95500 -1.06500 -0.9700 -1.12000 -1.14000 -0.4400 -1.15000 -1.2000
## Mean
           -0.94775 -1.06075 -0.9720 -1.12925 -1.16125 -0.4370 -1.13925 -1.1445
## 3rd Ou. -0.87750 -1.00750 -0.9300 -1.07750 -1.10750 -0.3675 -1.08000 -1.0075
## Max.
           -0.83000 \ -0.88000 \ -0.8800 \ -0.91000 \ -0.95000 \ -0.2500 \ -1.04000 \ -0.8900
##
               PDK4
                        PECI
                                  PLTP
                                          PMDCI
                                                    PON
                                                          PPARa
                                                                   PPARd PPARg
## Min.
           -1.28000 -1.11000 -1.15000 -1.07000 -0.7100 -1.1400 -1.7100 -1.190
## 1st Ou. -1.17250 -0.92250 -1.09250 -0.94250 -0.6325 -1.0225 -1.5900 -1.090
          -1.13000 -0.84000 -1.05000 -0.76500 -0.5800 -0.9500 -1.5600 -1.055
## Mean
           -1.13525 -0.84725 -1.03625 -0.76725 -0.5825 -0.9660 -1.5595 -1.052
## 3rd Qu. -1.08000 -0.79750 -0.99750 -0.60000 -0.5375 -0.9000 -1.5100 -1.010
           -1.01000 -0.58000 -0.85000 -0.44000 -0.4500 -0.8300 -1.4300 -0.900
## Max.
##
                PXR Pex11a
                                RARa
                                      RARb2
                                                 RXRa RXRb2
                                                               RXRq1
## Min.
           -1.13000 -1.2000 -1.30000 -1.3000 -0.7800 -1.070 -1.2300 -1.05000
## 1st Qu. -1.03000 -1.0500 -1.18250 -1.1900 -0.6725 -1.000 -1.1425 -0.98000
## Median
           -0.99000 -1.0200 -1.13000 -1.1350 -0.6350 -0.960 -1.1000 -0.85500
## Mean
           -0.99225 -1.0220 -1.13325 -1.1445 -0.6360 -0.964 -1.0955 -0.80675
## 3rd Qu. -0.94750 -0.9875 -1.07500 -1.0900 -0.5875 -0.935 -1.0500 -0.65750
## Max.
           -0.84000 -0.9000 -0.97000 -0.9900 -0.4900 -0.780 -0.9000 -0.25000
                      SIAT4c SPI1.1 SR.BI
##
                                                 THB THIOL
                                                               TRa
                                                                         TRb
               SHP1
## Min.
           -1.21000 -1.16000 0.96000 -1.060 -0.9200 -0.900 -1.670 -1.22000
## 1st Qu. -1.07500 -0.99000 1.03750 -0.920 -0.8500 -0.590 -1.510 -1.11000
          -0.99000 -0.96000 1.07500 -0.830 -0.8200 -0.345 -1.460 -1.06000
## Median
           -1.00675 -0.96225 1.09075 -0.843 -0.8170 -0.411 -1.457 -1.05425
## Mean
## 3rd Qu. -0.94750 -0.92750 1.15000 -0.800 -0.7875 -0.230 -1.395 -0.99750
## Max.
           -0.78000 -0.84000 1.23000 -0.610 -0.6900 -0.030 -1.220 -0.92000
##
            Tpalpha Tpbeta
                              UCP2
                                        UCP3
                                                  VDR
                                                         VLDLr
                                                                   Waf1
                                                                            ap2
## Min.
           -1.00000 -1.310 -1.0800 -1.27000 -1.30000 -1.19000 -1.3000 -1.3700
## 1st Qu. -0.86000 -1.200 -1.0025 -1.15250 -1.18000 -1.09250 -1.1500 -1.2225
## Median -0.83000 -1.140 -0.9800 -1.11000 -1.12000 -1.05500 -1.1300 -1.1900
           -0.81825 -1.130 -0.9660 -1.10775 -1.13175 -1.05325 -1.1235 -1.1880
## Mean
## 3rd Qu. -0.76000 -1.065 -0.9275 -1.05000 -1.08000 -1.01000 -1.0875 -1.1475
## Max.
           -0.65000 \ -0.910 \ -0.7600 \ -0.92000 \ -0.94000 \ -0.91000 \ -0.9400 \ -1.0800
##
           apoA.I
                              apoC3
                                       apoE
                                               c.fos cHMGCoAS
                                                               cMOAT eif2g
                     apoB
## Min.
           0.5400 - 0.2700 - 0.49000 \ 0.86000 - 1.22000 - 1.24000 - 1.0200 - 1.230
## 1st Qu. 0.6575 -0.2000 -0.39000 0.98000 -1.15000 -1.10250 -0.8950 -1.100
           0.7200 - 0.1700 - 0.34000 \ 1.04000 - 1.11000 - 1.03000 - 0.8700 - 1.055
## Median
## Mean
           0.7295 - 0.1675 - 0.34075 \ 1.02825 - 1.10525 - 1.01375 - 0.8485 - 1.058
## 3rd Qu. 0.8100 -0.1450 -0.30000 1.07000 -1.06000 -0.91000 -0.7875 -1.020
           0.9200 0.0100 -0.18000 1.18000 -0.98000 -0.78000 -0.6900 -0.840
## Max.
##
              hABC1 i.BABP
                                i.BAT i.FABP
                                               i.NOS
                                                       mABC1 mHMGCoAS
           -1.25000 -0.8900 -1.89000 -1.300 -1.4300 -0.9800
## 1st Qu. -1.17250 -0.8325 -1.74250 -1.170 -1.2850 -0.9200
                                                              -0.3000
## Median -1.13500 -0.8000 -1.69000 -1.140 -1.2400 -0.8700
## Mean
           -1.13825 -0.7935 -1.69775 -1.122 -1.2460 -0.8765
                                                              -0.2210
## 3rd Qu. -1.09750 -0.7475 -1.66000 -1.075 -1.2075 -0.8375
                                                             -0.1275
           -0.98000 -0.6700 -1.55000 -0.930 -1.0900 -0.8000
## Max.
                                                               0.0600
```



PLS

1. Perform PLS (mixOmics::pls) and investigate the output, sample distribution and variable relationship with plots.

```
pls.res <- pls(X=nutrimouse$gene, Y=nutrimouse$lipid, ncomp=2, scale=TRUE, mode="cano
nical")
max(abs(scale(nutrimouse$gene, center=T, scale=T) - pls.res$X))

## [1] 0

max(abs(scale(nutrimouse$lipid, center=T, scale=T) - pls.res$Y))</pre>
```

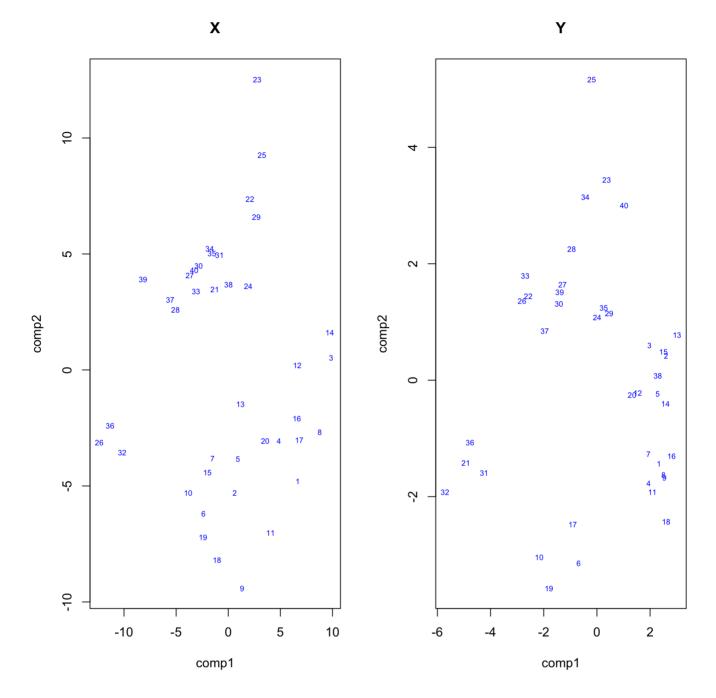
[1] 0

The sample distribution plot can be performed with **variates**, sample coordinates in the new reference (rotated axes) for each of the two blocks.

```
str(pls.res$variates)
```

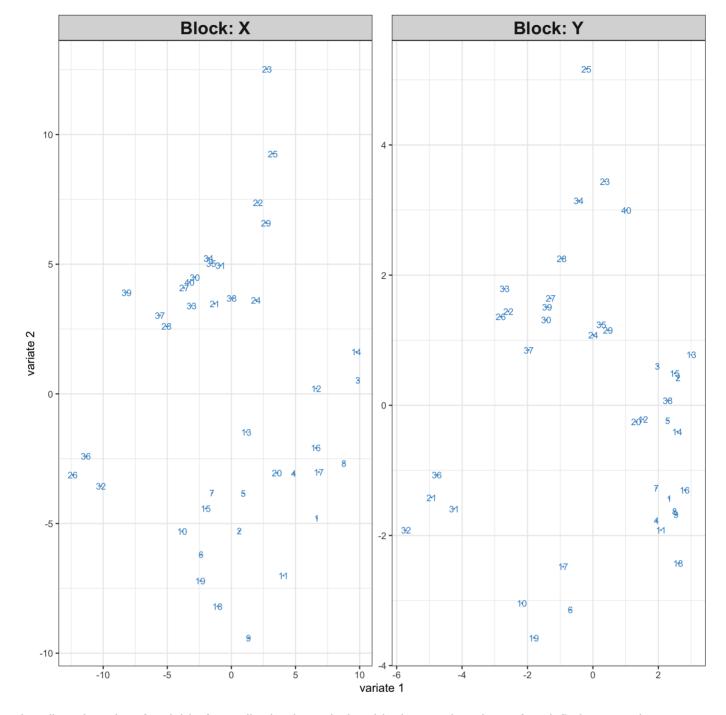
```
## List of 2
## $ X: num [1:40, 1:2] 6.659 0.614 9.876 4.864 0.934 ...
## ... attr(*, "dimnames")=List of 2
## ...$ : chr [1:40] "1" "2" "3" "4" ...
## ...$ : chr [1:2] "comp1" "comp2"
## $ Y: num [1:40, 1:2] 2.33 2.6 1.98 1.94 2.29 ...
## ... attr(*, "dimnames")=List of 2
## ...$ : chr [1:40] "1" "2" "3" "4" ...
## ...$ : chr [1:2] "comp1" "comp2"
```

```
PCx <- "comp1"
PCy <- "comp2"
par(mfrow=c(1,2))
plot(pls.res$variates$X[, PCx], pls.res$variates$X[, PCy], xlab=PCx, ylab=PCy, main
="X", type='n')
text(pls.res$variates$X[, PCx], pls.res$variates$X[, PCy], rownames(pls.res$variates
$X), col='blue', cex=0.6)
plot(pls.res$variates$Y[, PCx], pls.res$variates$Y[, PCy], xlab=PCx, ylab=PCy, main
="Y", type='n')
text(pls.res$variates$Y[, PCx], pls.res$variates$Y[, PCy], rownames(pls.res$variates
$Y), col='blue', cex=0.6)</pre>
```



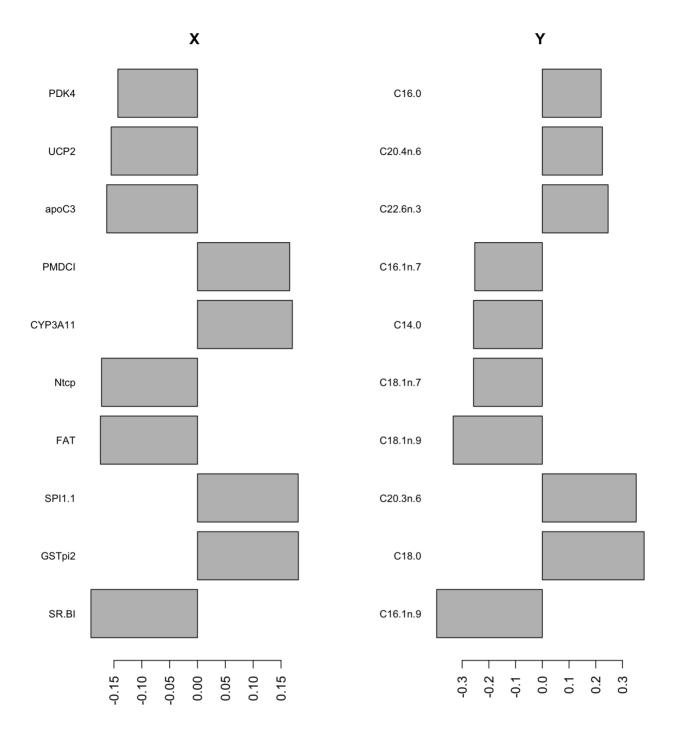
which is also produced with plotIndiv.

```
plotIndiv(pls.res)
```



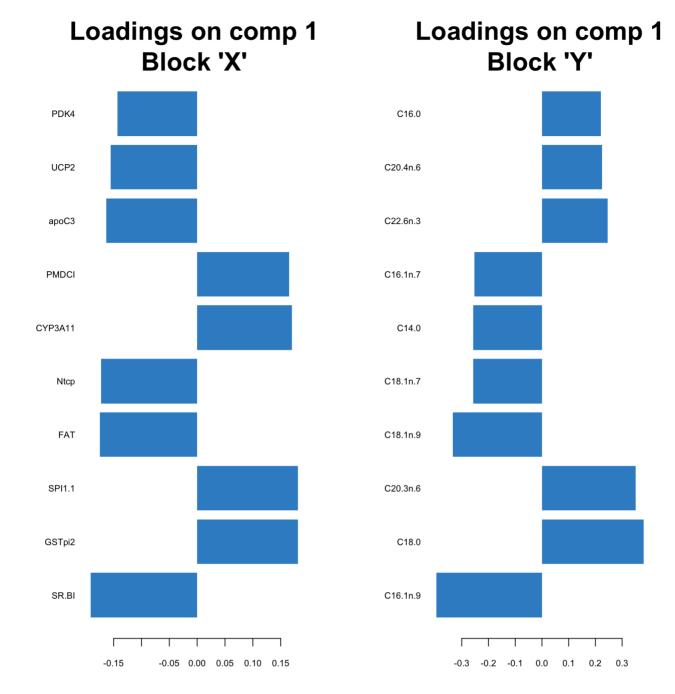
Loading plot: plot of variables' contribution in each data block to each variate, after deflating more *important* variates.

```
par(mfrow=c(1,2), las=2, mar=c(4,8,1,1))
loadings.ind.X <- order(abs(pls.res$loadings$X[, "comp1"]), decreasing = T)
barplot(head(pls.res$loadings$X[loadings.ind.X, "comp1"], 10), main="X", horiz = T, c
ex.names=0.8)
loadings.ind.Y <- order(abs(pls.res$loadings$Y[, "comp1"]), decreasing = T)
barplot(head(pls.res$loadings$Y[loadings.ind.Y, "comp1"], 10), main="Y", horiz = T, c
ex.names=0.8)</pre>
```



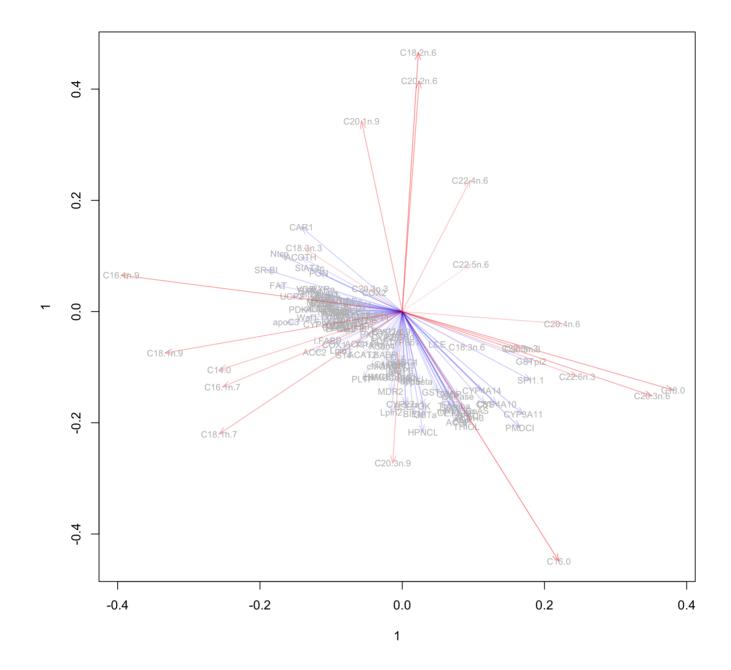
which is the same as with ${\tt plotLoadings}$.

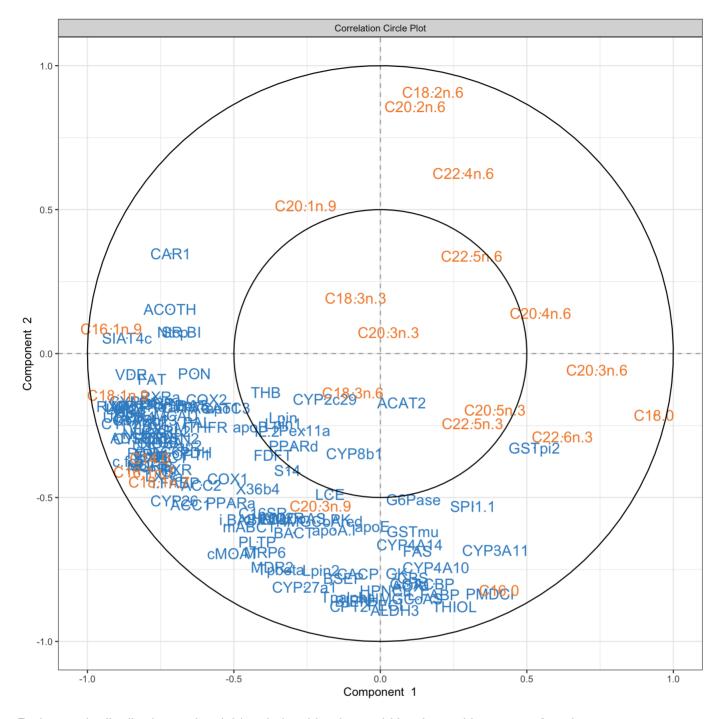
```
plotLoadings(pls.res, ndisplay = 10)
```



The plot of variable relationship could be obtained from **loadings.star**.

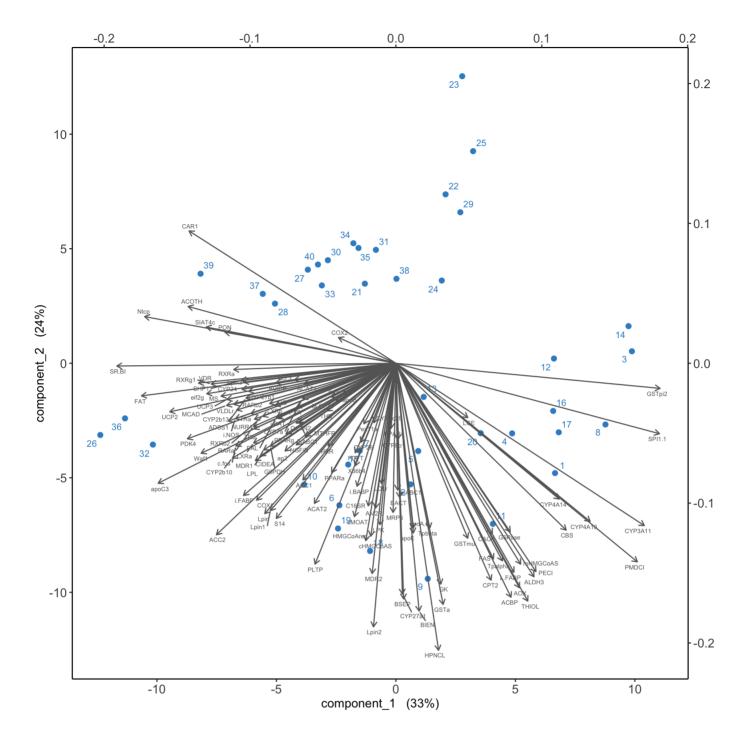
```
names(pls.res$loadings.star) <- c("X", "Y")</pre>
colnames(pls.res$loadings.star$X) <- colnames(pls.res$loadings.star$Y) <- c(PCx, PCy)</pre>
plot(1,1,type='n',
     xlim=range(c(pls.res$loadings.star$X[, PCx],pls.res$loadings.star$Y[, PCx])),
     ylim=range(c(pls.res$loadings.star$X[, PCy],pls.res$loadings.star$Y[, PCy])))
arrows(0, 0, pls.res$loadings.star$X[, PCx], pls.res$loadings.star$X[, PCy],
       length=0.1, angle=20, col=rgb(0,0,1,alpha=apply(pls.res$loadings.star$X[, c(PC
x, PCy)], 1, norm, "2")))
text(pls.res$loadings.star$X[, PCx],
     pls.res$loadings.star$X[, PCy],
     rownames(pls.res$loadings.star$X), col='grey', cex=0.7)
arrows(0, 0, pls.res$loadings.star$Y[, PCx], pls.res$loadings.star$Y[, PCy],
       length=0.1, angle=20, col=rgb(1,0,0,alpha=apply(pls.res$loadings.star$Y[, c(PC
x, PCy)], 1, norm, "2")))
text(pls.res$loadings.star$Y[, PCx],
     pls.res$loadings.star$Y[, PCy],
     rownames(pls.res$loadings.star$Y), col='grey', cex=0.7)
plotVar(pls.res)
```

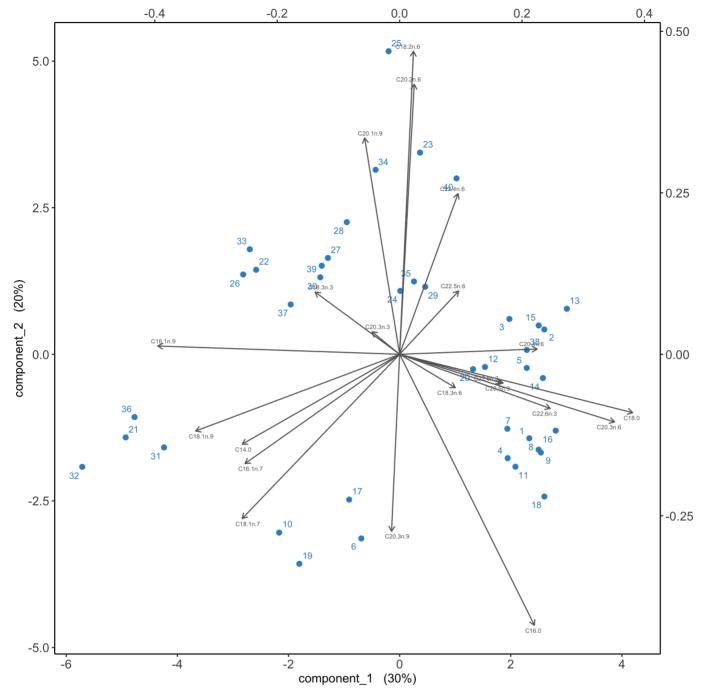




Both sample distribution and variable relationship plot could be done with biplot function.

```
biplot(pls.res, block="X", ind.names.size=3, var.names.size=2)
biplot(pls.res, block="Y", ind.names.size=3, var.names.size=2)
```





2. Observe the difference between the two modes regression and canonical of PLS.

```
pls.reg.res <- pls(X=nutrimouse$gene, Y=nutrimouse$lipid, ncomp=2, scale=TRUE, mode
="regression")</pre>
```

CCA

1. Perform CCA (mixOmics::rcc) between 20 genes and all lipids. Investigate correlations, sample distribution and variable relationship with plots.

The gene expression data is reduced to 20 genes so that the number of variables is less than the number of samples, to perform an unregularized CCA.

```
nutrimouse$gene_selected <- as.matrix(nutrimouse$gene[, 1:20])
str(nutrimouse$gene_selected)</pre>
```

```
## num [1:40, 1:20] -0.42 -0.44 -0.48 -0.45 -0.42 -0.43 -0.53 -0.49 -0.36 -0.5 ...
## - attr(*, "dimnames")=List of 2
## ..$ : chr [1:40] "1" "2" "3" "4" ...
## ..$ : chr [1:20] "X36b4" "ACAT1" "ACAT2" "ACBP" ...
```

cca.res <- rcc(X=nutrimouse\$gene_selected, Y=as.matrix(nutrimouse\$lipid), ncomp=2)
max(abs(nutrimouse\$gene - cca.res\$X))</pre>

```
## [1] 2.9
```

max(abs(nutrimouse\$lipid - cca.res\$Y))

[1] 0

str(cca.res)

```
## List of 11
## $ call
                   : language rcc(X = nutrimouse$gene selected, Y = as.matrix(nutrimo
use\prescript{slipid}), ncomp = 2)
                   : num [1:40, 1:20] -0.42 -0.44 -0.48 -0.45 -0.42 -0.43 -0.53 -0.49
## $ X
-0.36 -0.5 ...
    ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:40] "1" "2" "3" "4" ...
##
    ....$ : chr [1:20] "X36b4" "ACAT1" "ACAT2" "ACBP" ...
## $ Y
                   : num [1:40, 1:21] 0.34 0.38 0.36 0.22 0.37 1.7 0.35 0.34 0.22 1.3
8 ...
   ..- attr(*, "dimnames")=List of 2
    ...$: chr [1:40] "1" "2" "3" "4" ...
##
    ....$ : chr [1:21] "C14.0" "C16.0" "C18.0" "C16.1n.9" ...
## $ ncomp
                   : num 2
                  : chr "ridge"
##
   $ method
##
   $ cor
                   : Named num [1:20] 1 1 0.999 0.996 0.981 ...
     ..- attr(*, "names")= chr [1:20] "1" "2" "3" "4" ...
##
                  :List of 2
##
   $ loadings
     ..$ X: num [1:20, 1:2] 1.408 4.802 3.235 -7.373 -0.724 ...
##
##
     .. ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:20] "X36b4" "ACAT1" "ACAT2" "ACBP" ...
##
     .. .. ..$ : NULL
##
##
     ..$ Y: num [1:21, 1:2] 1.111 -0.143 -0.462 -1.02 -0.09 ...
     ... - attr(*, "dimnames")=List of 2
##
     ....$ : chr [1:21] "C14.0" "C16.0" "C18.0" "C16.1n.9" ...
##
##
     .. .. ..$ : NULL
   $ variates
##
                  :List of 2
     ..$ X: num [1:40, 1:2] -1.203 -1.25 -0.831 0.338 -0.119 ...
##
##
     .. ..- attr(*, "dimnames")=List of 2
     ....$: chr [1:40] "1" "2" "3" "4" ...
##
##
     .. .. ..$ : NULL
     ..$ Y: num [1:40, 1:2] -1.203 -1.25 -0.831 0.338 -0.119 ...
##
##
     .. ..- attr(*, "dimnames")=List of 2
##
     ....$: chr [1:40] "1" "2" "3" "4" ...
     .. .. ..$ : NULL
##
##
   $ names
                  :List of 4
     ..$ sample : chr [1:40] "1" "2" "3" "4" ...
##
##
     ..$ colnames:List of 2
     .. ..$ X: chr [1:20] "X36b4" "ACAT1" "ACAT2" "ACBP" ...
##
     .. ..$ Y: chr [1:21] "C14.0" "C16.0" "C18.0" "C16.1n.9" ...
     ..$ blocks : chr [1:2] "X" "Y"
##
     ..$ data : chr [1:2] "nutrimouse$gene selected" "as.matrix(nutrimouse$lipid)"
   $ lambda
                  : Named num [1:2] 0 0
    ..- attr(*, "names")= chr [1:2] "lambda1" "lambda2"
##
   $ prop expl var:List of 2
    ..$ X: Named num [1:2] 0.00132 0.0024
##
     .... attr(*, "names")= chr [1:2] "comp1" "comp2"
##
    ..$ Y: Named num [1:2] 0.0184 0.0299
##
     .... attr(*, "names")= chr [1:2] "comp1" "comp2"
##
   - attr(*, "class")= chr "rcc"
##
```

```
## 1 2 3 4 5 6 7
## 1.00000000 1.00000000 0.99922446 0.99607902 0.98142435 0.95641141 0.89083472
## 8 9 10 11 12 13 14
## 0.88959894 0.78648273 0.76470925 0.75189350 0.66984945 0.63240310 0.53662009
## 15 16 17 18 19 20
## 0.49948385 0.34852831 0.33274136 0.27818295 0.22569639 0.03783839
```

The sample distribution plot can be performed with **variates**, sample coordinates in the new reference (rotated axes) for each of the two blocks.

```
str(cca.res$variates)
```

```
## List of 2
## $ X: num [1:40, 1:2] -1.203 -1.25 -0.831 0.338 -0.119 ...
## ... attr(*, "dimnames")=List of 2
## ...$ : chr [1:40] "1" "2" "3" "4" ...
## $ Y: num [1:40, 1:2] -1.203 -1.25 -0.831 0.338 -0.119 ...
## ... attr(*, "dimnames")=List of 2
## ...$ : chr [1:40] "1" "2" "3" "4" ...
## ...$ : NULL
```

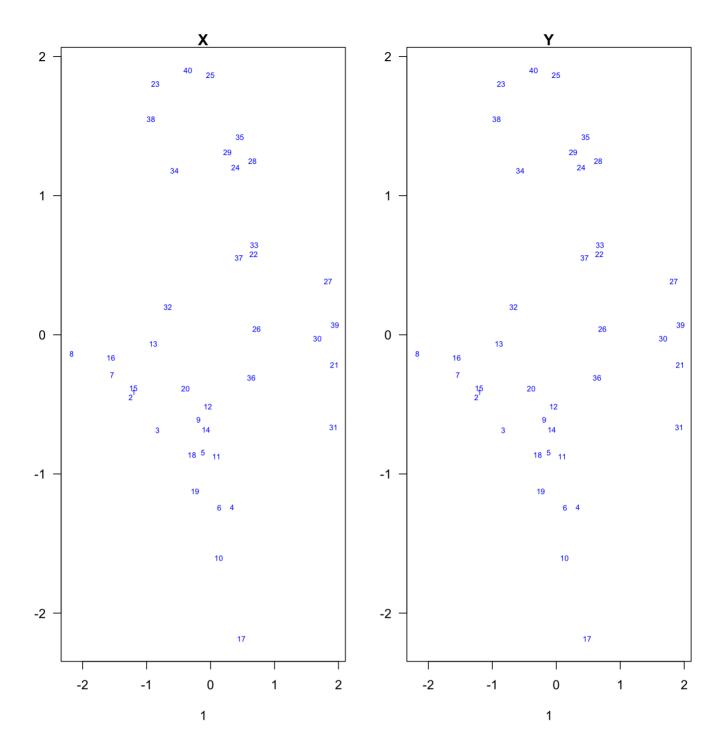
```
PCx <- 1
PCy <- 2
par(mfrow=c(1,2), las=1, mar=c(4,3,1,1))
plot(cca.res$variates$X[, PCx], cca.res$variates$X[, PCy], xlab=PCx, ylab=PCy, main
="X", type='n')
text(cca.res$variates$X[, PCx], cca.res$variates$X[, PCy], rownames(cca.res$variates
$X), col='blue', cex=0.6)
plot(cca.res$variates$Y[, PCx], cca.res$variates$Y[, PCy], xlab=PCx, ylab=PCy, main
="Y", type='n')
text(cca.res$variates$Y[, PCx], cca.res$variates$Y[, PCy], rownames(cca.res$variates
$Y), col='blue', cex=0.6)
cor(cca.res$variates$X[,1], cca.res$variates$Y[,1])</pre>
```

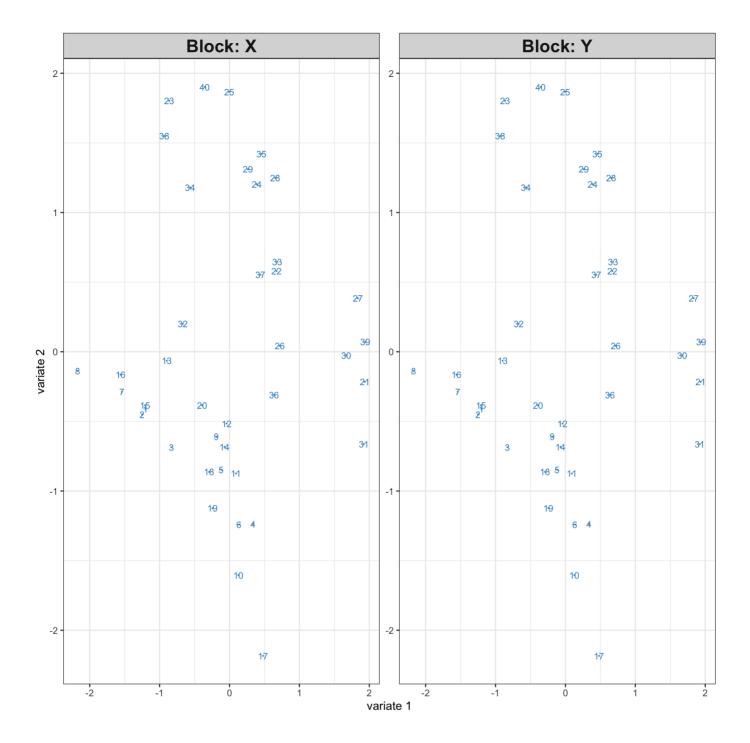
```
## [1] 1
```

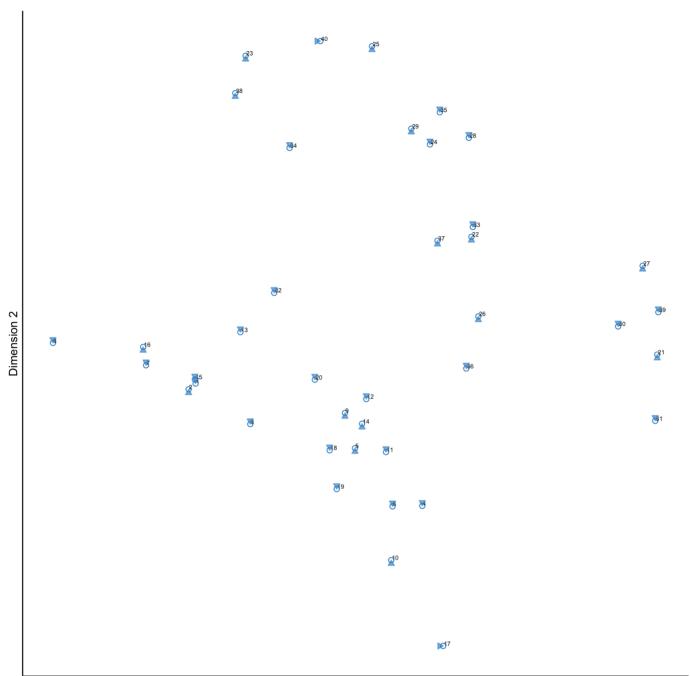
```
cor(cca.res$variates$X[,2], cca.res$variates$Y[,2])
```

```
## [1] 1
```

```
plotIndiv(cca.res)
plotArrow(cca.res)
```







Dimension 1

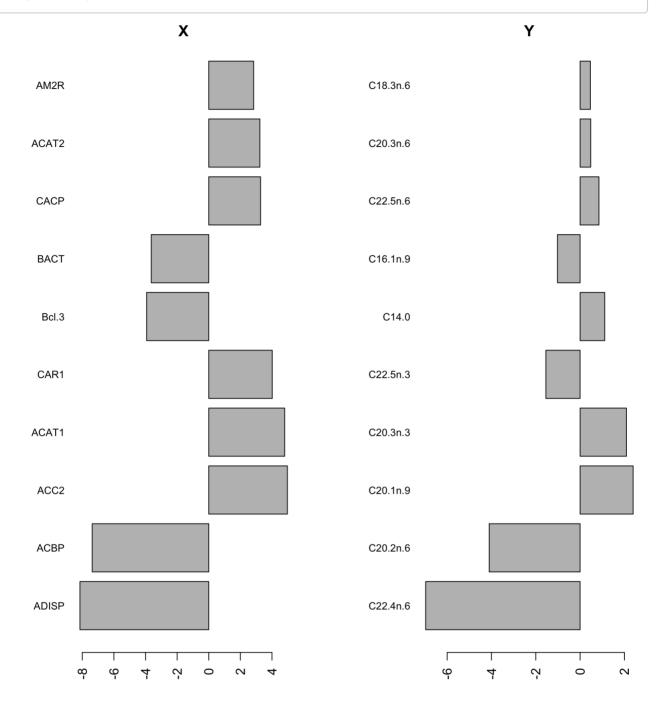
Variable relationship is obtained from loadings or with plotVar.

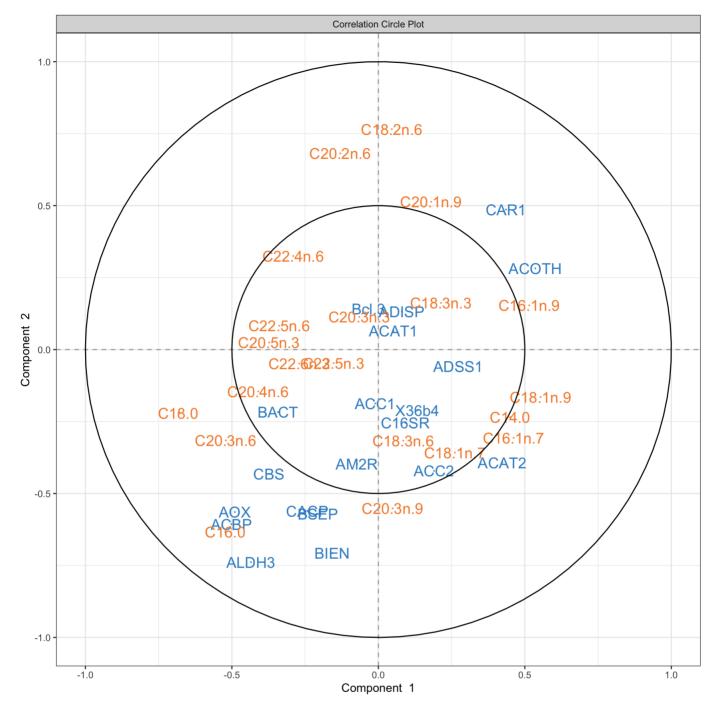
```
par(mfrow=c(1,2), las=2, mar=c(4,8,1,1))
loadings.ind.X <- order(abs(cca.res$loadings$X[, 1]), decreasing = T)
barplot(head(cca.res$loadings$X[loadings.ind.X, 1], 10), main="X", horiz = T, cex.nam
es=0.8)
loadings.ind.Y <- order(abs(cca.res$loadings$Y[, 1]), decreasing = T)
barplot(head(cca.res$loadings$Y[loadings.ind.Y, 1], 10), main="Y", horiz = T, cex.nam
es=0.8)
max(abs(cca.res$variates$X - scale(cca.res$X, center=T, scale=F) %*% cca.res$loadings
$X))</pre>
```

```
## [1] 0
```

```
\label{lem:max_abs_cca.res} $$\max(abs(cca.res\$Y, center=T, scale=F) %*% cca.res\$loadings \$Y))$
```

plotVar(cca.res)





2. Perform CCA with scaled datasets and observe the difference

```
## [1] 0.4797719
```

```
max(abs(cca.res.scale$variates$X - cca.res$variates$X))
```

```
## [1] 3.631284
```

```
max(abs(cca.res.scale$variates$Y - cca.res$variates$Y))
```

```
## [1] 3.841865

max(abs(cca.res.scale$loadings$X - cca.res$loadings$X))

## [1] 8.113192

max(abs(cca.res.scale$loadings$Y - cca.res$loadings$Y))

## [1] 16.07948
```

3. Perform regularized CCA with all genes and lipids.

rcca.res <- rcc(X=nutrimouse\$gene, Y=nutrimouse\$lipid, ncomp=2, method="shrinkage")</pre>