

Constraint Satisfaction Problems (CSPs)



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Queens puzzle

• Place eight queens on a chessboard so that no two attack each other

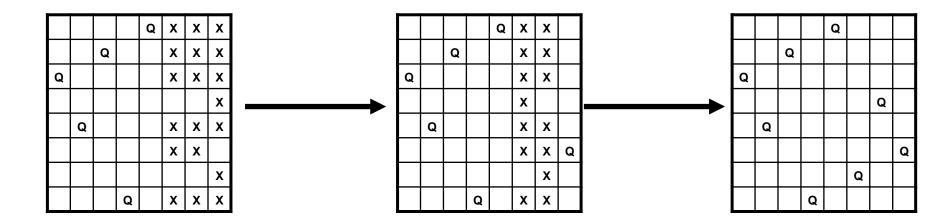
				Q			
		Q					
Q							
						Q	
	Q						
							Ø
					Q		
			Q				

Search formulation of the queens puzzle

• Successors: all valid ways of placing additional queen on the board; goal: eight queens placed Q Q Q Q Q

Keeping track of remaining possible values

- For every variable, keep track of which values are still possible
- General heuristic: branch on variable with fewest values remaining



only one possibility for last column; might as well fill in

now only one left for other two columns

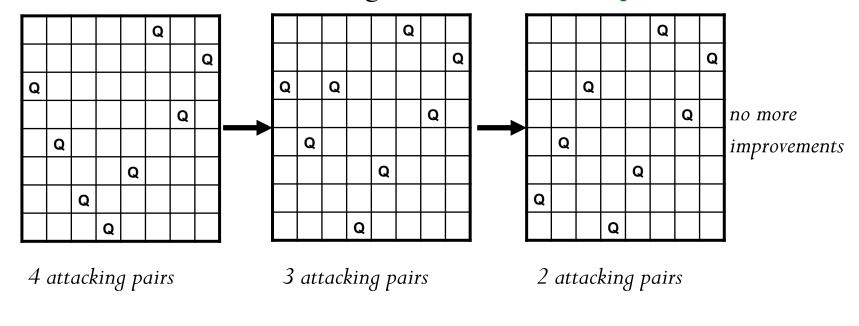
done!
(no real branching needed!)

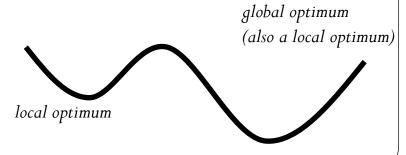
Constraint Satisfaction Problems (CSPs)

- Defined by:
 - A set of variables $x_1, x_2, ..., x_n$
 - A domain D_i for each variable x_i
 - Constraints $c_1, c_2, ..., c_m$
- A constraint is specified by
 - A subset (often, two) of the variables
 - All the allowable joint assignments to those variables
- Goal: find a complete, consistent assignment
- Queens problem: (other examples in next slides)
 - x_i in $\{1, ..., 8\}$ indicates in which row in the ith column to place a queen
 - For example, constraint on x_1 and x_2 : $\{(1,3), (1,4), (1,5), (1,6), (1,7), (1,8), (2,4), (2,5), \dots, (3,1), (3,5), \dots\}$

Local search: hill climbing

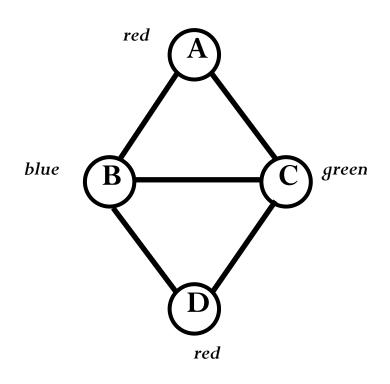
- Start with a complete state
- Move to successor with best (or at least better) objective value
 - Successor: move one queen within its column
- Local search can get stuck in a local optimum

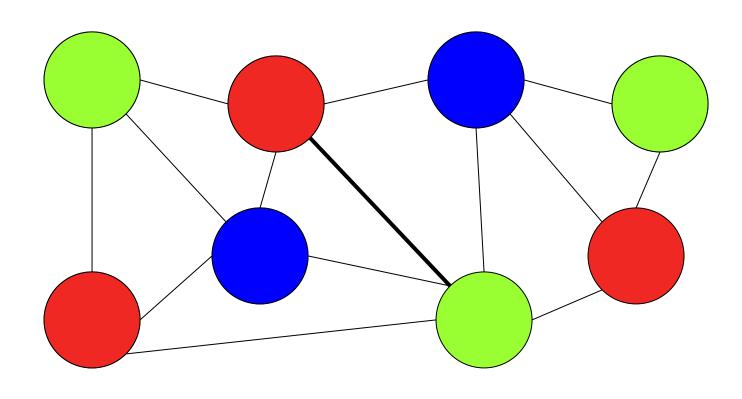




Graph coloring

• Fixed number of colors; no two adjacent nodes can share a color





Constrained optimization

- Process of optimizing an objective function with respect to some variables in the presence of constraints on those variables.
 - primarily equality constraints, inequality constraints, and integer constraints
 - set of candidate solutions that satisfy all constraints is called the feasible set
- A general constrained minimization problem may be written as follows:

$$egin{array}{ll} \min & f(\mathbf{x}) \ & \mathrm{subject\ to} & g_i(\mathbf{x}) = c_i & \mathrm{for}\ i = 1, \ldots, n & \mathrm{Equality\ constraints} \ & h_j(\mathbf{x}) \geqq d_j & \mathrm{for}\ j = 1, \ldots, m & \mathrm{Inequality\ constraints} \end{array}$$

where $g_i(x)$ and $h_j(x)$ are constraints that are required to be satisfied, and f(x) is the objective function that needs to be optimized subject to the constraints

References

• Vincent Conitzer, CPS 270: Artificial Intelligence http://www.cs.duke.edu/courses/fall08/cps270/

ขอบคุณ

תודה רבה Grazie Italian

Thai

Hebrew ಧನ್ಯವಾದಗಳು

Kannada

Sanskrit

धन्यवादः

Ευχαριστώ Greek

Thank You English

Gracias

Spanish

Спасибо

Russian

Obrigado

Portuguese

شكراً

https://sites.google.com/site/animeshchaturvedi07

Merci

French

Arabic

多謝

Traditional

Chinese

धन्यवाद

Hindi

Danke

German



Simplified

Chinese

நன்றி

Tamil

Tamil

ありがとうございました 감사합니다

Japanese

Korean