

Linked List - Data Structures

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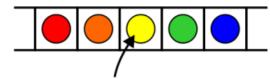
List

- Properties
 - Ordered list of items...precedes, succeeds; first, last
 - Index for each item...lookup or address item by index value
 - Finite Length for the list...can be empty, size can vary
 - Items of same type present in the list
- Operations
 - Create, destroy
 - Lookup by index, item value
 - Find size, if empty
 - Add, delete item

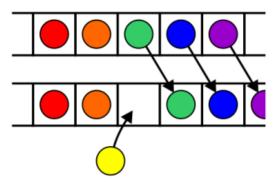
List Operations

• Operations at the kth entry of the list include:

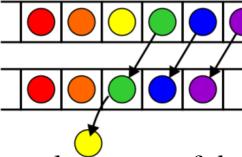
Access to the object



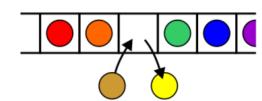
• Insertion of a new object



Erasing an object

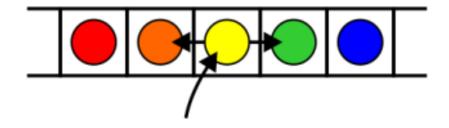


Replacement of the object



List Operations

• Given access to the kth object, gain access to either the previous or next object



- Given two abstract lists, we may want to
 - Concatenate the two lists
 - Determine if one is a sub-list of the other

Array List

- List operations
 - Create/Destroy
 - Length
 - Find
 - Insert/Remove
 - Next/Previous
- List properties
 - A_i precedes A_{i+1} for $1 \le i \le n$
 - A_i succeeds A_{i-1} for $1 \le i \le n$
 - Size 0 list is defined to be the **empty list ()**

```
( A_1 A_2 ... A_{n-1} A_n )
length = n
```

- First, create an array list.
- Then, we are able to perform: insert into, access, and erase from the values stored in the array list

Operations on an arbitrary node of the array list,

- Find the number of instances of an integer in the array list: int count(int) const;
- Remove all instances of an integer from the array list: int erase(int);

Array List Operations - Mapping Function

- Say n is the capacity of the array
- Simple mapping
 - E.g. using array for queues: add from front, remove from back.
 - get(index) = value of data at index
- Reverse mapping
 - E.g. using same array for reverse list.
 - get(index) = value of data at (n index 1)
- Hash-Mapping
 - get(index) = value of data at (position(0)+index) % n
 - get(0) = value of data at head

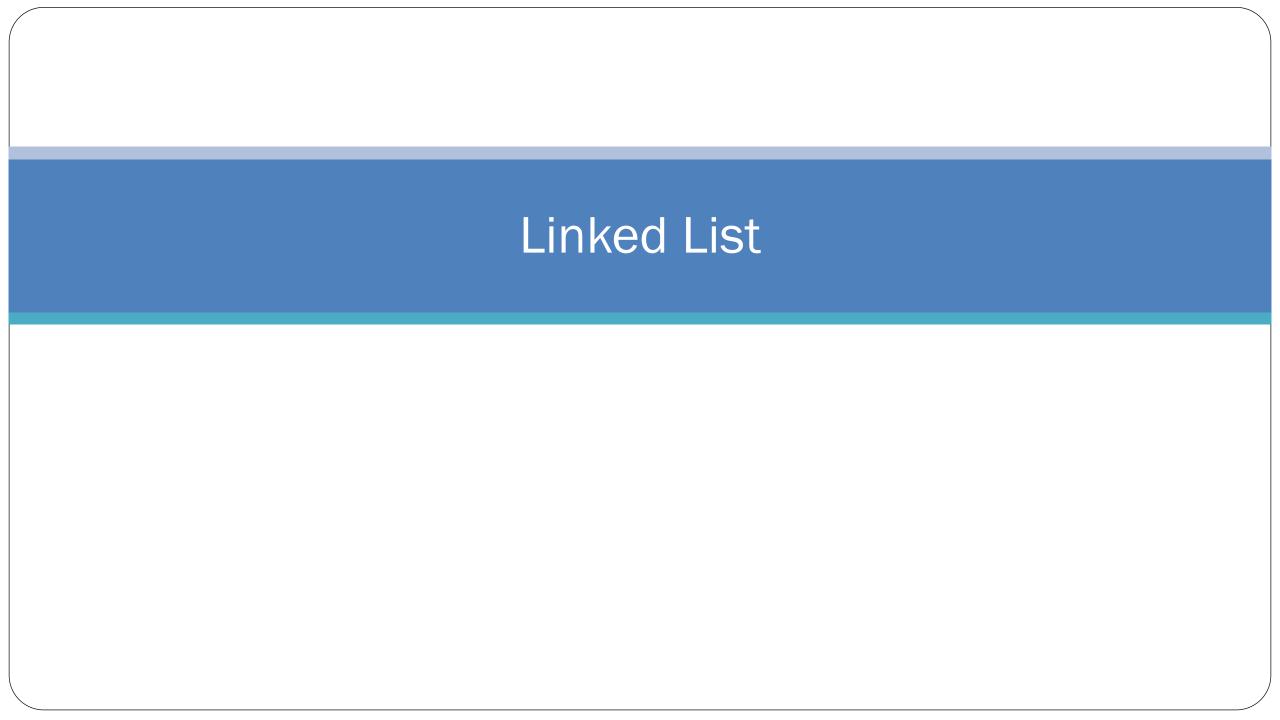
- void create(initCapacity) or create(size)
 - Create array with initial capacity (optional hint)
- void set(index, item)
 - Use mapping function to set value at position
- void append(item)
 - Insert after current "last" item...use size
- void remove(index) or int erase(int)
 - Remove item at index or Erase item at index and return its data (value as integer)

- item get(index)
 - Use mapping function to set value at position
 - Student is class with methods getName, get RollNumber and "student" is its object
 - e.g., student.getName(15), student.getRollNumber(15)
- int indexOf(item)
 - Get "first" index of item with given value
 - String student.getRollNumber(15)
- To analyse or check the entire list:
 - Is the linked list empty?
 boolean isEmpty() or bool empty();
 - How many objects are in the list? Counts the number of instances in the list, int capacity() or int size()
 - The list is empty when the list_head pointer is set to nullptr

Increasing capacity

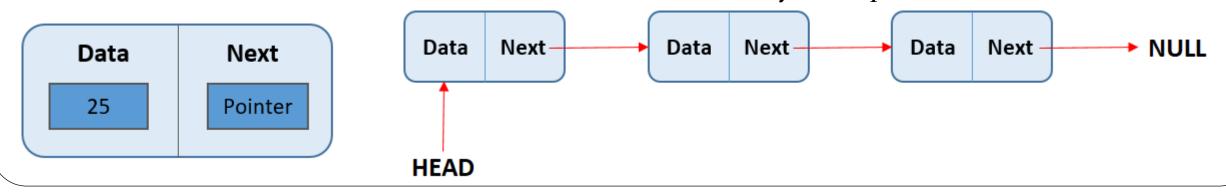
- Start with initial capacity given by user, or default
- When capacity is reached
 - Create array with more capacity, e.g. double it
 - Copy values from old to new array
 - Delete old array space
- Can also be used to shrink space
 - Example: Sparse Matrices

- Pros and Cons of using Arrays.
- Complexity
 - Storage Complexity: Amount of storage required by the data structure, relative to items stored
 - Computational Complexity: Number of CPU cycles required to perform each data structure operation
 - size(), set(), get(), indexOf()



Linked List - Definitions and Terminologies

- A linked list is a sequence of data structures, which are connected together via links.
- Linked list is a sequence of links which contains items.
- Each link contains a connection to another link.
- Important terms to understand the concept of linked list.
 - Data Each link of a linked list can store a data called an element
 - Next Each link of a linked list contains a link to the next link called Next
 - List A list contains the connection link to the first link called Head
- It can be visualized as a chain of nodes, where every node points to the next node.



Linked List - Definitions and Terminologies

- A linked list is a data structure where each object is stored in a node
- As well as storing data, the node must also contains a reference/pointer to the node containing the next item of data.
- We must dynamically create the nodes in a linked list
- Thus, because new returns a pointer, the logical manner in which to track a linked lists is through a pointer
- A Node class must store the data and a reference to the next node (also a pointer)

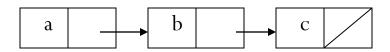
Linked List in C

One or more of its components is a pointer to itself.

```
typedef struct list {
    char data;
    list *link;
}
```

```
list item1, item2, item3;
item1.data='a';
item2.data='b';
item3.data='c';
item1.link=item2.link=item3.link=NULL;
```

Construct a list with three nodes item1.link=&item2; item2.link=&item3; malloc: obtain a node



Linked List in C

```
int data;
struct node *next;
Data Next
```

- Linked list contains a link element called Head
- Each link carries a data field(s) and a link field called next
- Each link is linked with its next link using its next link
- Last link carries a link as null to mark the end of the list

Linked List Representation

- Problem with array:
 - Pre-defined capacity, under usage, cost to move items when full
- Solution:
 - Grow backing data structure dynamically when we add or remove node
 - Only use as much memory as required
- Linked lists use pointers to contiguous chain items
 - Node structure contains item and pointer to next node in List
- Add or remove nodes when setting or getting items

Linked List Operations

- First, create a linked list.
- Then, we are able to perform: insert into, access, and erase from the values stored in the linked list
- Operations on the first node of the linked list
- Adding, retrieving, or removing the value at the front of the linked list

```
void push_front( int );
int front() const;
void pop_front();
```

To access the head of the linked list

```
Node *begin() const;
```

Node Class in C++

```
The node must store data and a pointer:
  class Node {
        public: Node( int = 0, Node * = nullptr );
        int value() const;
        Node *next() const;
        private:
                int node_value;
                Node *next_node;
        };
```

Node Constructor in C++

```
class Node {
  public: Node( int = 0, Node * = nullptr );
  int value() const;
  Node *next() const;
  private:
        int node_value;
        Node *next_node;
};
The constructor assigns the two member variables based on the arguments
     List::Node::Node( int e, Node *n ):
     node_value( e )
     next_node( n ) {// empty constructor}
The default values are given in the class definition:
```

Linked List Iterators in C++

General method of examining collections

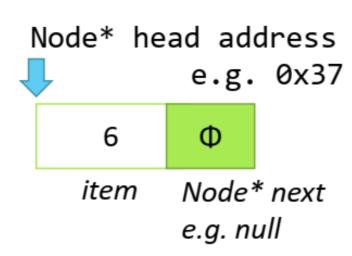
```
List<Object> *list;
Object x;
...
ListItr<Object> *i = list->first();
while (i->hasNext()) {
    x = i->next();
}
```

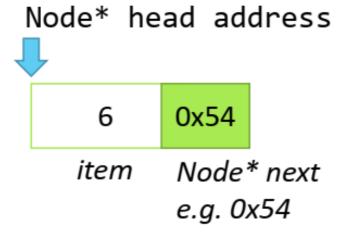
Linked List Operations

- Iteration operations:
 - ListItr<Object> first()
 - ListItr<Object> kth(int)
 - ListItr<Object> last()
- Main operations:
 - ListItr < Object > find(Object)
 - void insert(Object, listItr<Object>)
 - void remove(ListItr<Object>)
 - bool isEmpty()

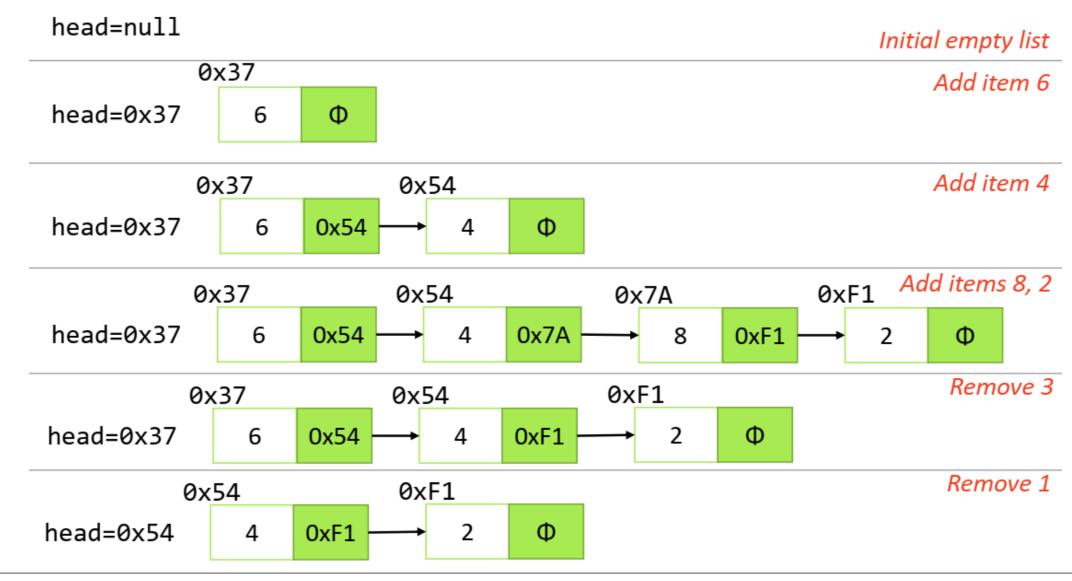
Linked List Operations in OOP (C++ or Java)

```
class LinkedList {
  Node* head;
  class Node* {
     int item
     Node* next
  int size() \{\ldots\}
  append() {...}
  get() {...}
  set() {...}
  remove {...}
```

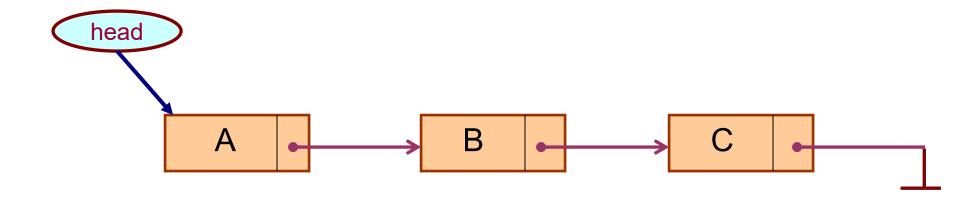




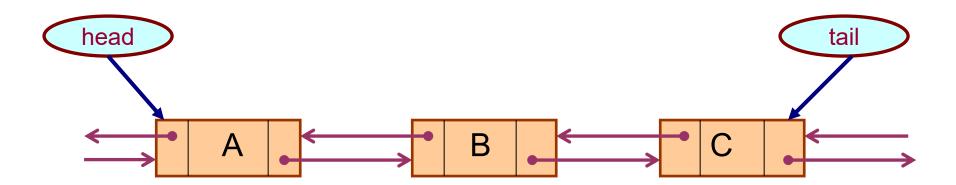
Linked List Operations



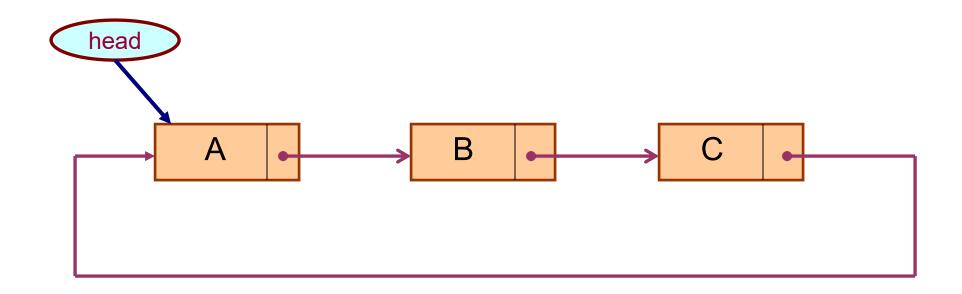
- Depending on the way in which the links are used to maintain adjacency, several different types of linked lists are possible.
- Linear singly-linked list (or simply linear list)
 - One we have discussed so far.



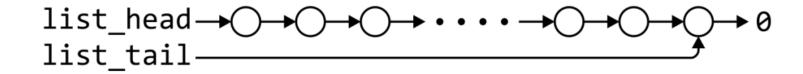
- Doubly linked list
 - Pointers exist between adjacent nodes in both directions.
 - The list can be traversed either forward or backward.
 - Usually two pointers are maintained to keep track of the list, *head* and *tail*.



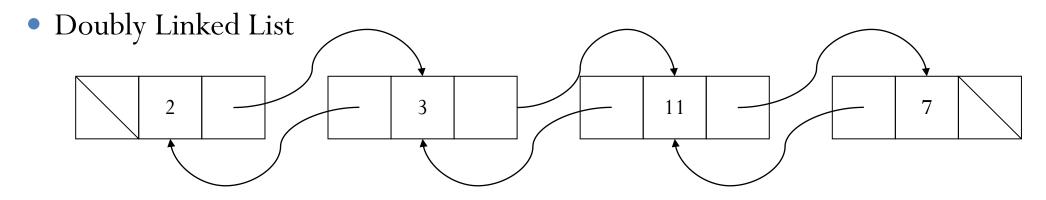
- Circular linked list
 - The pointer from the last element in the list points back to the first element.



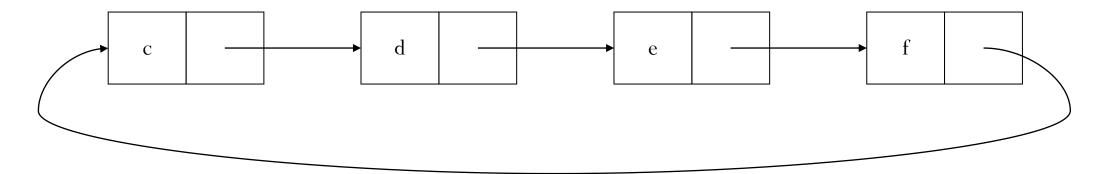
- We will consider these for
 - Singly linked lists



Doubly linked lists



• Circular List



Advantage of Linked List

- An Abstract List (or List ADT) is linearly ordered data where the programmer explicitly defines the ordering
- Most common operations and implementation uses either an Array or Linked list
- Arrays can be used to store linear data of similar types, with following limitations.
 - The size of the arrays is fixed
 - Inserting a new element in an array of elements is expensive
- Advantages over arrays
 - Dynamic size
 - Ease of insertion/deletion
- Drawbacks of linked list
 - Random access is not allowed. We cannot do binary search with linked lists.
 - Extra memory space for a pointer is required with each element of the list.

Dynamic Memory Management

Memory Allocation

The constructor is called whenever an object is created, either:

Static allocation,

List ls;

defines Is to be a linked list and the compiler deals with memory allocation

Dynamic allocation

List *pls = new List();

requests sufficient memory from the OS to store an instance of the class

In both cases, the memory is allocated and then the constructor is called

Pseudo-code for insertion

```
typedef struct nd {
 struct item data;
 struct nd * next;
 } node;
                                                    В
void insert(node *curr)
                                                 Item to be
                                       X
node * tmp;
                          tmp
                                                 inserted
tmp=(node *) malloc(sizeof(node));
tmp->next=curr->next;
                               A
curr->next=tmp;
                      curr
```

Pseudo-code for deletion

```
typedef struct nd {
                                               Item to be deleted
 struct item data;
                               A
                                                   В
 struct nd * next;
 } node;
                                                   tmp
void delete(node *curr)
                               curr
                               A
node * tmp;
                                                    В
tmp=curr->next;
curr->next=tmp->next;
free(tmp);
```

Pseudo-code

- For insertion:
 - A record is created holding the new item.
 - The next pointer of the new record is set to link it to the item which is to follow it in the list.
 - The next pointer of the item which is to precede it must be modified to point to the new item.
- For deletion:
 - The next pointer of the item immediately preceding the one to be deleted is altered, and made to point to the item following the deleted item.

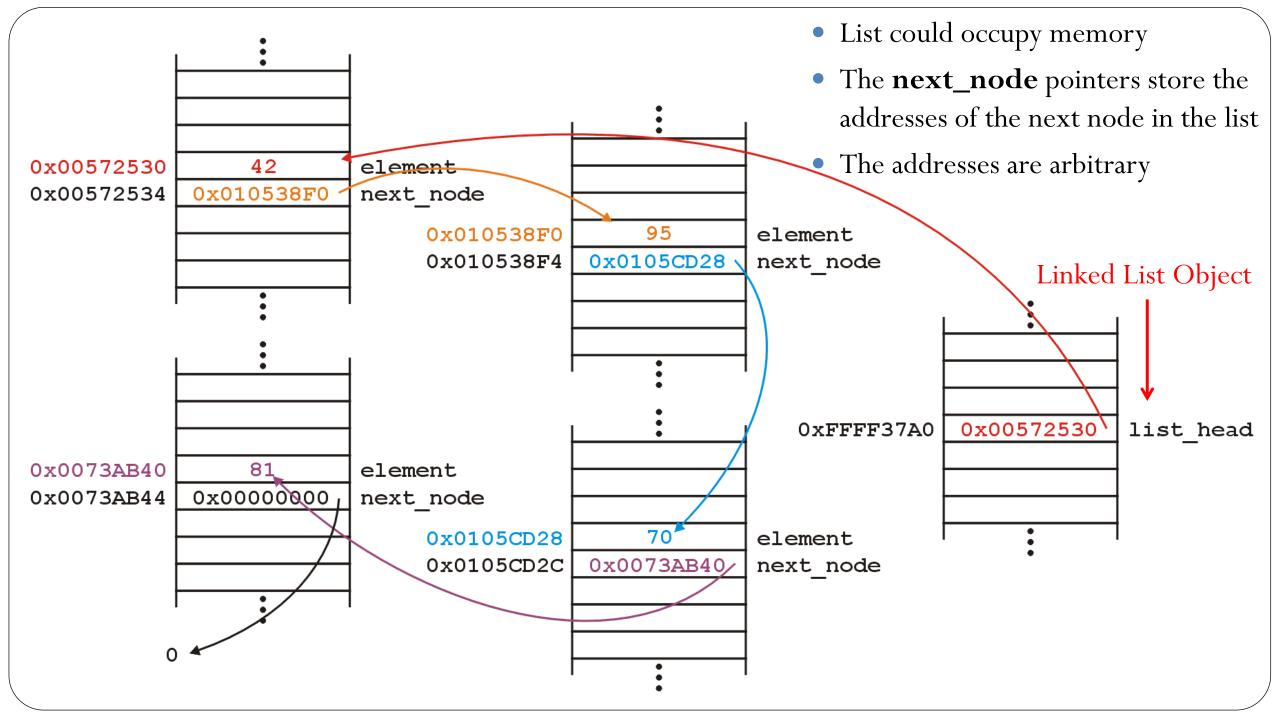
Dynamic Storage: Memory Management

A linked list uses linked allocation, and therefore each node may appear anywhere in memory

Assuming a 32-bit machine

Memory required for each node equals the memory required by the member variables

- 4 bytes for the linked list (a pointer)
- 8 bytes for each node (an **int** and a pointer)



Dynamic Storage: Memory Management

• Clean representation as follows:



- We do not specify the addresses because they are arbitrary and:
 - The contents of the circle is the value
 - The next_node pointer is represented by an arrow

Applications of Linked List

Ordered List Examples

- MONDAY, TUEDSAY, WEDNESDAY, THURSDAY, FRIDAY, SATURDAY, SUNDAY
- 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King, Ace
- 1941, 1942, 1943, 1944, 1945
- a1, a2, a3, ..., an-1, an
- ordered (linear) list: (item1, item2, item3, ..., item*n*)

Applications

- Everything!
 - Class list
 - compilers: list of functions in a program, statements in a function
 - graphics: list of triangles to be drawn to the screen
 - operating systems: list of programs running
 - music: compose crazy hard transcendental études
 - other data structures: queues, stacks!

Application: Polynomial ADT

 A_i is the coefficient of the x^{n-i} term:

$$3x^2 + 2x + 5$$

$$8x + 7$$

$$x^2 + 3$$

Problem?

$x^{2001} + 1$

Sparse List Data Structure (?): x²⁰⁰¹ + 1

$$(<1 \ 2001><1 \ 0>)$$

Linked List

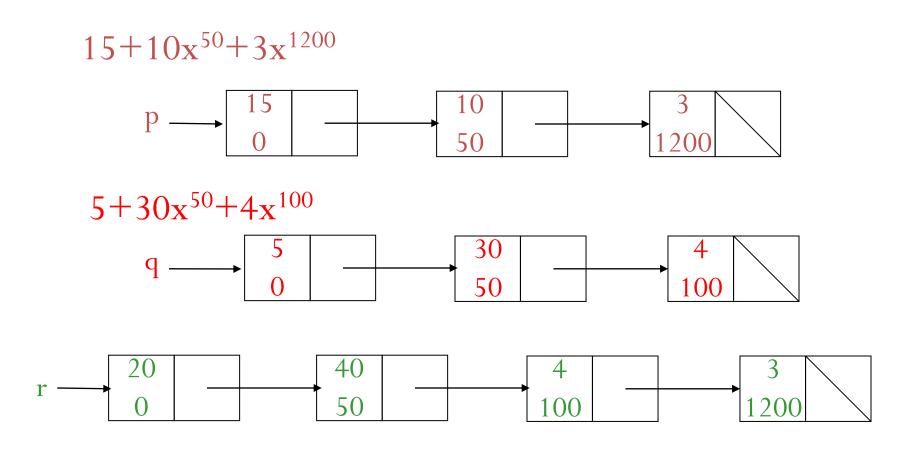
1 1 0

vs. Array

1	1
2001	0

Addition of Two Polynomials

Similar to merging two sorted lists

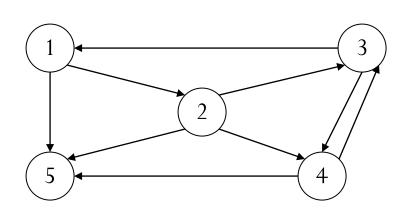


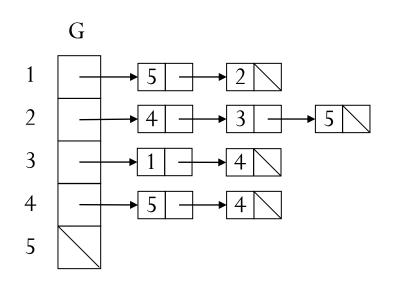
Multiple Linked Lists

- Many ADTS such as graphs, relations, sparse matrices, multivariate polynomials use multiple linked lists
- Several options
 - array of lists
 - lists of lists
 - multi lists
- General principle: use one ADT to implement a more complicated one.

Array of Linked Lists: Adjacency List for Graphs

- Array G of unordered linked lists
- Each list entry corresponds to an edge in the graph





Reachability by Marking

- Suppose we want to mark all the nodes in the graph which are reachable from a given node \mathbf{k} .
 - Let **G[1..n**] be the adjacency list rep. of the graph
 - Let **M[1..n]** be the mark array, initially all **false**s.

```
mark(int i){
    M[i] = true;
    x = G[i]
    while (x != NULL) {
        if (M[x->node] == false)
            mark(G[x->node])
        x = x->next
     }
}
```

Thoughts on Reachability

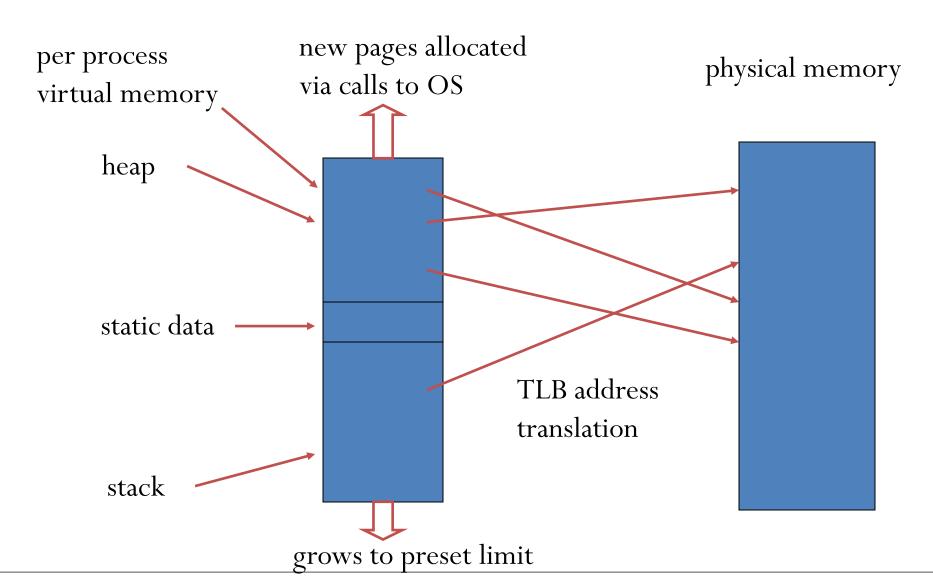
- The marking algorithm visits each node and each edge at most once.
- This marking algorithm uses Depth First Search. DFS uses a stack to track nodes. Where?
- Graph reachability is closely related to garbage collection
 - the nodes are blocks of memory
 - marking starts at all global and active local variables
 - the marked blocks are reachable from a variable
 - unmarked blocks are garbage

Garbage Collection

Garbage Collection

- Every modern programming language allows programmers to allocate new storage dynamically
 - New records, arrays, tuples, objects, closures, etc.
- Every modern language needs facilities for reclaiming and recycling the storage used by programs
- It's usually the most complex aspect of the run-time system for any modern language (Java, ML, Lisp, Scheme, Modula, ...)

Memory layout



Garbage Collection

- What is garbage?
 - A value is garbage if it will not be used in any subsequent computation by the program
- Is it easy to determine which objects are garbage?
 - No. It's undecidable. Eg:

```
if long-and-tricky-computation then use v else don't use v
```

Garbage Collection

- Since determining which objects are garbage is tricky, people have come up with many different techniques
 - It's the programmers problem:
 - Explicit allocation/deallocation
 - Reference counting
 - Tracing garbage collection
 - Mark-sweep, copying collection
 - Generational Garbage Collection

Explicit Memory Management

- User library manages memory; programmer decides when and where to allocate and deallocate
 - void* malloc(long n)
 - void free(void *addr)
 - Library calls OS for more pages when necessary
 - Advantage: people are smart
 - Disadvantage: people are dumb and they really don't want to bother with such details if they can avoid it

Explicit Memory Management

- How does malloc/free work?
 - Blocks of unused memory stored on a freelist
 - malloc: search free list for usable memory block
 - free: put block onto the head of the freelist
- Drawbacks
 - malloc is not free: we might have to do a significant search to find a big enough block
 - As program runs, the heap fragments leaving many small, unusable pieces

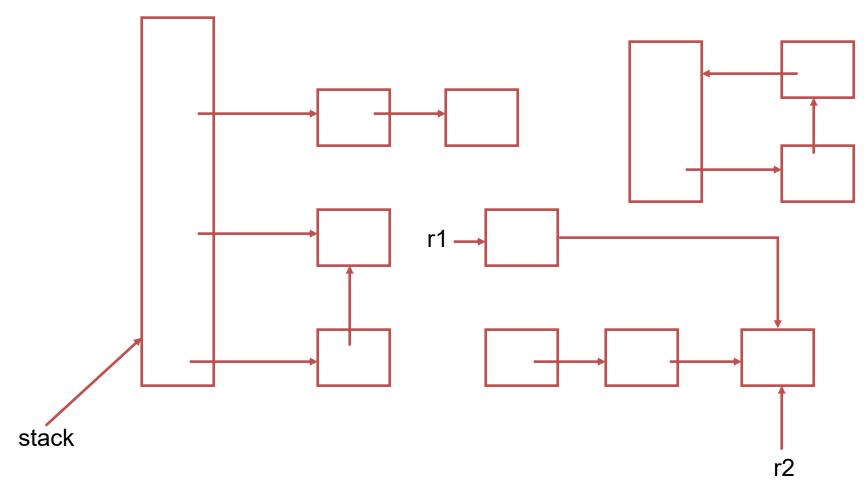
Automatic Memory Management (MM)

- Languages with Explicit MM are much harder to program than languages with Automatic MM
 - Always worrying about dangling pointers, memory leaks: a huge software engineering burden
 - Impossible to develop a secure system, impossible to use these languages in emerging applications involving mobile code
 - Soon, languages with unsafe, Explicit MM will all but disappear

Automatic Memory Management

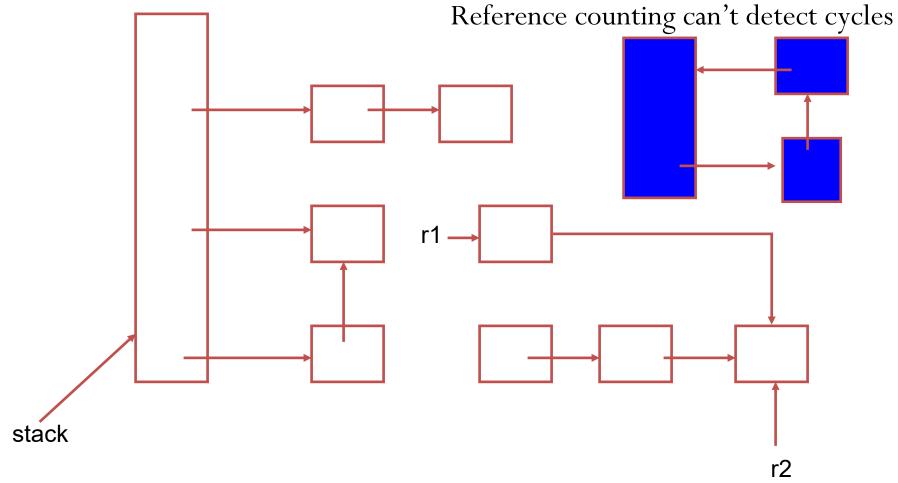
- Question: how do we decide which objects are garbage?
 - We conservatively approximate
 - Normal solution: an object is garbage when it becomes unreachable from the roots
 - The roots = registers, stack, global static data
 - If there is no path from the roots to an object, it cannot be used later in the computation so we can safely recycle its memory

Object Graph



• How should we test reachability?

Object Graph



- Keep track of the number of pointers to each object (the reference count).
- When the reference count goes to 0, the object is unreachable garbage

Copying Collection

- Basic idea: use 2 heaps
 - One used by program
 - The other unused until GC time
- Garbage Collection:
 - Start at the roots & traverse the reachable data
 - Copy reachable data from the active heap (from-space) to the other heap (to-space)
 - Dead objects are left behind in from space
 - Heaps switch roles

Student Linked List

Student Linked List

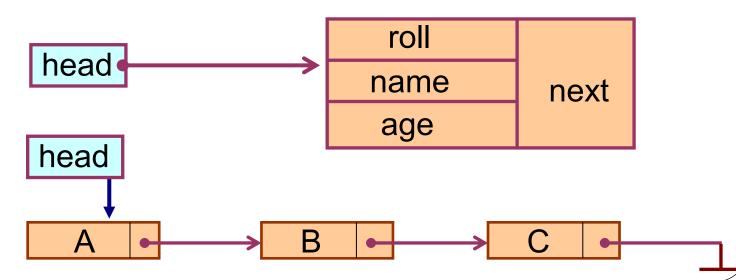
• Consider the structure of a node as follows:

```
int roll;
    char name[25];
    int age;
    struct stud *next;
};

/* A user-defined data type called "node" */
typedef struct stud node;
node *head;
```

Student Linked List

- To start with, we have to create a node (the first node), and make head point to it head = (node *) malloc(sizeof(node));
- If there are n number of nodes in the initial linked list:
 - Allocate **n** records, one by one.
 - Read in the fields of the records.
 - Modify the links of the records so that the chain is formed.



Create the Student Linked List

To be called from main () function as:

```
node *create list()
                                                     node *head;
    int k, n;
   node *p, *head;
                                                     head = create list();
   printf ("\n How many elements to enter?");
    scanf ("%d", &n);
    for (k=0; k< n; k++)
    \{ if (k == 0) \}
         head = (node *) malloc(sizeof(node));
         p = head;
      else {
             p->next = (node *) malloc(sizeof(node));
             p = p->next;
       scanf ("%d %s %d", &p->roll, p->name, &p->age);
   p->next = NULL;
    return (head);
```

Traverse the Student Linked List

```
void display (node *head)
                                           • To be called from main () function
                                            node *head;
  int count = 1;
  node *p;
                                             display (head);
  p = head;
  while (p != NULL)
  { printf ("\nNode %d: %d %s %d", count, p->roll, p->name, p->age);
    count++;
    p = p->next;
                    • After construction, head points to the first node of the list,
  printf ("\n");
                      • Follow the pointers.
```

• Display the contents of the nodes as they are traversed.

• Stop when the *next* pointer points to NULL.

Inserting a Node in a List

Inserting a Node in the Student Linked List

- The problem is to insert a node *before a specified node*.
 - Specified means some value is given for the node (called *key*).
 - In this example, we consider it to be roll.
- Convention followed:
 - If the value of roll is given as *negative*, the node will be inserted at the *end* of the list.

```
void insert (node **head)

int k = 0, rno;
    node *p, *q, *new;

new = (node *) malloc(sizeof(node));

printf ("\nData to be inserted: ");
    scanf ("%d %s %d", &new->roll, new->name, &new->age);
printf ("\nInsert before roll (-ve for end):");
    scanf ("%d", &rno);

p = *head;
*To be called from main() function

node *head;
```

Insert a Node in the Student Linked List

- When a node is added at the beginning,
 - Only one next pointer needs to be modified.
 - *head* is made to point to the new node.
 - New node points to the previously first element.
- When a node is added at the end,
 - Two next pointers need to be modified.
 - Last node now points to the new node.
 - New node points to NULL.
- When a node is added in the middle,
 - Two next pointers need to be modified.
 - Previous node now points to the new node.
 - New node points to the next node.
- The pointers q and p always point to consecutive nodes.

```
if (p->roll == rno) /* At the beginning *,
       new->next = p;
        *head = new;
else
  while ((p != NULL) \&\& (p->roll != rno))
            q = p;
            p = p->next;
            (p == NULL) /* At the end */
            q->next = new;
            new->next = NULL;
            (p->roll == rno)
   else if
                      /* In the middle */
                    q->next = new;
                    new->next = p;
```

```
void delete (node **head)
{    int rno;
    node *p, *q;

    printf ("\nDelete for roll :");
        scanf ("%d", &rno);

    p = *head;
```

- Required to delete a specified node.
 - Roll Number is given.
- Here also three conditions arise:
 - Deleting the first node.
 - Deleting the last node.
 - Deleting an intermediate node.

Delete a Node in the Student Linked List

```
if (p->roll == rno) /* Delete the first element */
       *head = p->next;
       free (p);
else
      while ((p != NULL) \&\& (p->roll != rno))
       q = p;
           p = p->next;
       if (p == NULL) /* Element not found */
         printf ("\nNo match deletion failed");
       else if (p->roll == rno)
               /* Delete any other element */
                q->next = p->next;
                free (p);
```

Exercises

- Write a function to:
 - Concatenate two given list into one big list.

```
node *concatenate (node *head1, node *head2);
```

• Insert an element in a linked list in sorted order. The function will be called for every element to be inserted.

```
void insert_sorted (node **head, node *element);
```

• Always insert elements at one end, and delete elements from the other end (first-in first-out QUEUE).

```
void insert_q (node **head, node *element)
node *delete_q (node **head) /* Return the deleted node */
```

Linked Bag in Java

LinkedBag.java: Initialize

```
public class LinkedBag<Item> implements Iterable<Item> {
   private Node first; // beginning of bag
   private int n;  // number of elements in bag
   // helper linked list class
   private class Node {
       private Item item;
       private Node next;
 * Initializes an empty bag.
public LinkedBag() {
    first = null;
    n = 0;
```

LinkedBag.java: Main

```
public static void main(String[] args) {
    LinkedBag<String> bag = new LinkedBag<String>();
    while (!StdIn.isEmpty()) {
        String item = StdIn.readString();
        bag.add(item);
    StdOut.println("size of bag = " + bag.size());
    for (String s : bag) {
        StdOut.println(s);
```

LinkedBag.java: Add item at First node

```
/**
  * Adds the item to this bag.
  * @param item the item to add to this bag
  */
public void add(Item item) {
    Node oldfirst = first;
    first = new Node();
    first.item = item;
    first.next = oldfirst;
    n++;
}
```

LinkedBag.java: Other functions

```
* Is this bag empty?
 * @return true if this bag is empty; false otherwise
public boolean isEmpty() {
    return first == null;
 * Returns the number of items in this bag.
 * @return the number of items in this bag
public int size() {
    return n;
```

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