



INDIAN INSTITUTE OF
INFORMATION
TECHNOLOGY

Linked List - Data Structures

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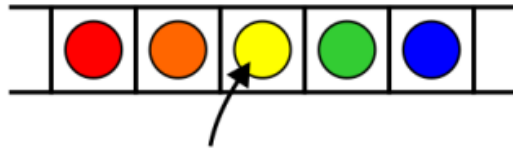
List

- Properties
 - Ordered list of items...precedes, succeeds; first, last
 - Index for each item...lookup or address item by index value
 - Finite Length for the list...can be empty, size can vary
 - Items of same type present in the list
- Operations
 - Create, destroy
 - Lookup by index, item value
 - Find size, if empty
 - Add, delete item

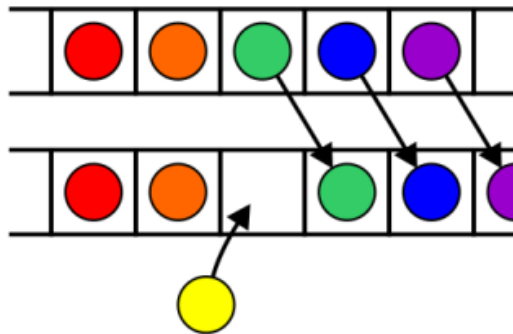
List Operations

- Operations at the k th entry of the list include:

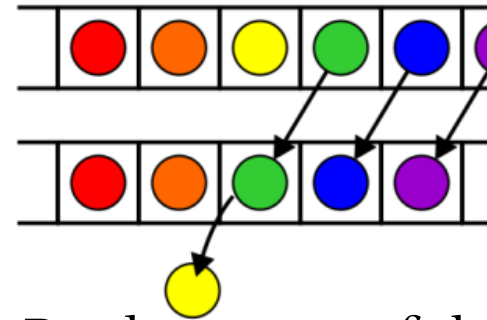
- Access to the object



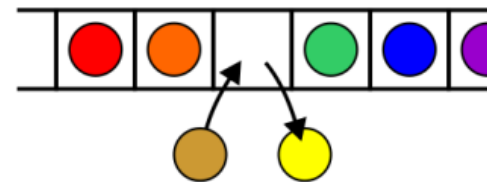
- Insertion of a new object



Erasing an object

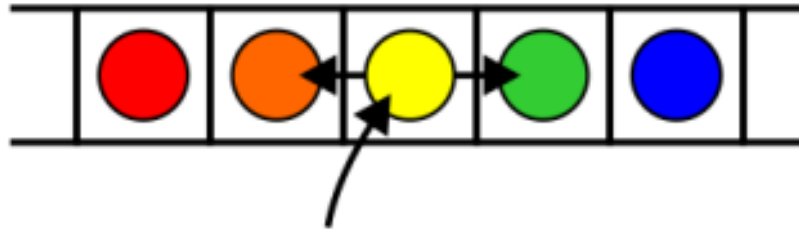


Replacement of the object



List Operations

- Given access to the k th object, gain access to either the previous or next object



- Given two abstract lists, we may want to
 - Concatenate the two lists
 - Determine if one is a sub-list of the other

Array List

Array List Operations

- List operations

- Create/Destroy
- Length
- Find
- Insert/Remove
- Next/Previous

$(A_1 \ A_2 \ \dots \ A_{n-1} \ A_n)$
length = n

- List properties

- A_i precedes A_{i+1} for $1 \leq i < n$
- A_i succeeds A_{i-1} for $1 < i \leq n$
- Size 0 list is defined to be the **empty list** $()$

Array List Operations

- First, **create** an array list.
- Then, we are able to perform: **insert** into, **access**, and **erase** from the values stored in the array list

Operations on an **arbitrary node** of the array list,

- Find the number of instances of an integer in the array list:

int count(int) const;

- Remove all instances of an integer from the array list:

int erase(int);

Array List Operations - Mapping Function

- Say n is the capacity of the array
- Simple mapping
 - E.g. using array for queues: add from front, remove from back.
 - $\text{get}(\text{index}) = \text{value of data at index}$
- Reverse mapping
 - E.g. using same array for reverse list.
 - $\text{get}(\text{index}) = \text{value of data at } (n - \text{index} - 1)$
- Hash-Mapping
 - $\text{get}(\text{index}) = \text{value of data at } (\text{position}(0) + \text{index}) \% n$
 - $\text{get}(0) = \text{value of data at head}$

Array List Operations

- `void create(initCapacity)` or `create(size)`
 - Create array with initial capacity (optional hint)
- `void set(index, item)`
 - Use mapping function to set value at position
- `void append(item)`
 - Insert after current “last” item...use size
- `void remove(index)` or `int erase(int)`
 - Remove item at index or Erase item at index and return its data (value as integer)

Array List Operations

- item get(index)
 - Use mapping function to set value at position
 - Student is class with methods getName, get RollNumber and “student” is its object
 - e.g., student.getName(15), student.getRollNumber(15)
- int indexOf(item)
 - Get “first” index of item with given value
 - String student.getRollNumber(15)
- To analyse or check the entire list:
 - Is the linked list empty?
boolean isEmpty() or bool empty();
 - How many objects are in the list? Counts the number of instances in the list,
int capacity() or int size()
 - The list is empty when the list_head pointer is set to nullptr

Array List Operations

Increasing capacity

- Start with initial capacity given by user, or default
- When capacity is reached
 - Create array with more capacity, e.g. double it
 - Copy values from old to new array
 - Delete old array space
- Can also be used to shrink space
 - Example: Sparse Matrices

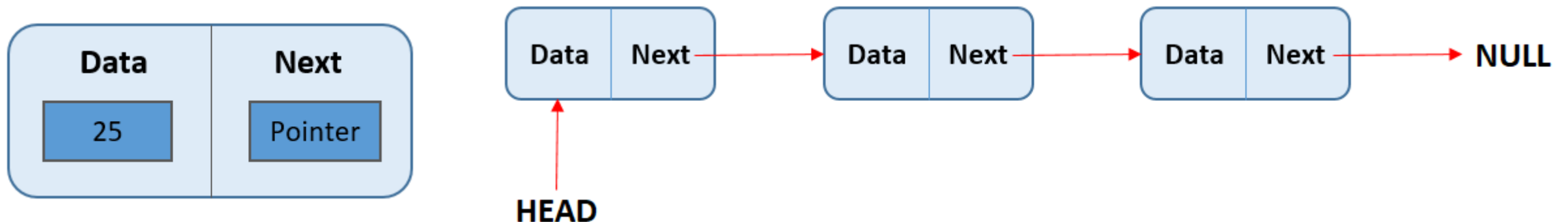
Array List Operations

- Pros and Cons of using Arrays.
- Complexity
 - Storage Complexity: Amount of storage required by the data structure, relative to items stored
 - Computational Complexity: Number of CPU cycles required to perform each data structure operation
 - `size()`, `set()`, `get()`, `indexOf()`

Linked List

Linked List - Definitions and Terminologies

- A linked list is a sequence of data structures, which are connected together via links.
- Linked list is a sequence of links which contains items.
- Each link contains a connection to another link.
- Important terms to understand the concept of linked list.
 - Data – Each link of a linked list can store a data called an element
 - Next – Each link of a linked list contains a link to the next link called Next
 - List – A list contains the connection link to the first link called Head
- It can be visualized as a chain of nodes, where every node points to the next node.




Linked List - Definitions and Terminologies

- A linked list is a data structure where each object is stored in a node
- As well as storing data, the node must also contains a reference/pointer to the node containing the next item of data.
- We must dynamically create the nodes in a linked list
- Thus, because new returns a pointer, the logical manner in which to track a linked lists is through a pointer
- A Node class must store the data and a reference to the next node (also a pointer)

Linked List in C

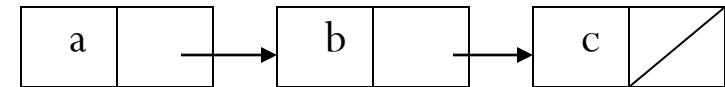
One or more of its components is a pointer to itself.

```
typedef struct list {  
    char data;  
    list *link;  
}
```



```
list item1, item2, item3;  
item1.data='a';  
item2.data='b';  
item3.data='c';  
item1.link=item2.link=item3.link=NULL;
```

Construct a list with three nodes
item1.link=&item2;
item2.link=&item3;
malloc: obtain a node



Linked List in C

```
struct node {  
    int data;  
    struct node *next;  
};
```



- Linked list contains a link element called Head
- Each link carries a data field(s) and a link field called next
- Each link is linked with its next link using its next link
- Last link carries a link as null to mark the end of the list

Linked List Representation

- Problem with array:
 - Pre-defined capacity, under usage, cost to move items when full
- Solution:
 - Grow backing data structure dynamically when we add or remove node
 - Only use as much memory as required
- Linked lists use pointers to contiguous chain items
 - Node structure contains item and pointer to next node in List
- Add or remove nodes when setting or getting items

Linked List Operations

- First, **create** a linked list.
- Then, we are able to perform: **insert** into, **access**, and **erase** from the values stored in the linked list
- Operations on the **first node** of the linked list
- Adding, retrieving, or removing the value at the **front** of the linked list

void push_front(int);

int front() const;

void pop_front();

- To access the head of the linked list

Node *begin() const;

Node Class in C++

The node must store **data** and a **pointer**:

```
class Node {  
    public: Node( int = 0, Node * = nullptr );  
  
    int value() const;  
    Node *next() const;  
  
    private:  
        int node_value;  
        Node *next_node;  
  
};
```

Node Constructor in C++

```
class Node {  
    public: Node( int = 0, Node * = nullptr );  
    int value() const;  
    Node *next() const;  
    private:  
        int node_value;  
        Node *next_node;  
};
```

The constructor assigns the two member variables based on the arguments

```
List::Node::Node( int e, Node *n ):  
    node_value( e )  
    next_node( n ) { // empty constructor }
```

The default values are given in the class definition:

Linked List Iterators in C++

General method of examining collections

```
List<Object> *list;
```

```
Object x;
```

```
...
```

```
ListIter<Object> *i = list->first();
```

```
while ( i->hasNext() ) {
```

```
    x = i->next();
```

```
}
```

Linked List Operations

- Iteration operations:
 - `ListItr<Object> first()`
 - `ListItr<Object> kth(int)`
 - `ListItr<Object> last()`
- Main operations:
 - `ListItr<Object> find(Object)`
 - `void insert(Object, listItr<Object>)`
 - `void remove(ListItr<Object>)`
 - `bool isEmpty()`

Linked List Operations in OOP (C++ or Java)

```
class LinkedList {
```

```
    Node* head;
```

```
    class Node* {
```

```
        int item
```

```
        Node* next
```

```
    }
```

```
    int size() {...}
```

```
    append() {...}
```

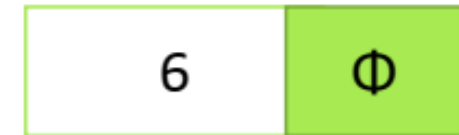
```
    get() {...}
```

```
    set() {...}
```

```
    remove {...}
```

```
}
```

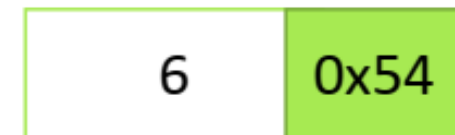
Node* head address
e.g. 0x37



item

Node next*
e.g. null

Node* head address



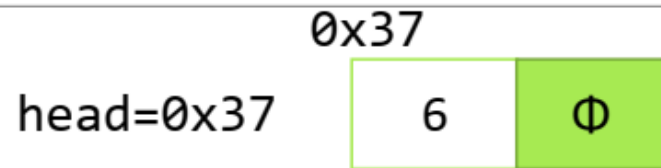
item

Node next*
e.g. 0x54

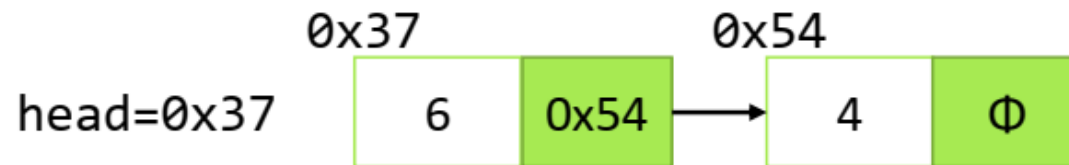
Linked List Operations

head=null

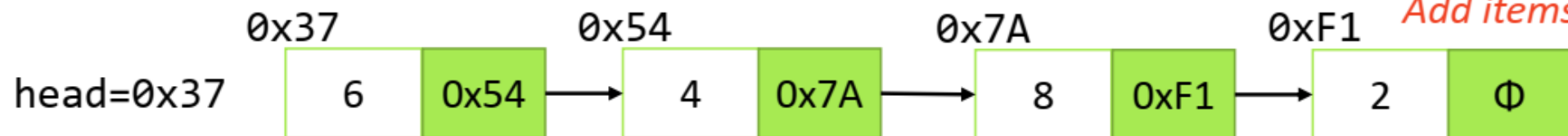
Initial empty list



Add item 6



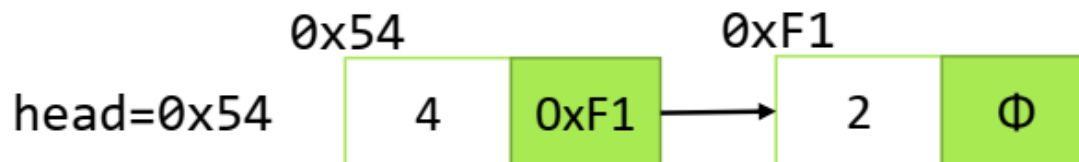
Add item 4



Add items 8, 2



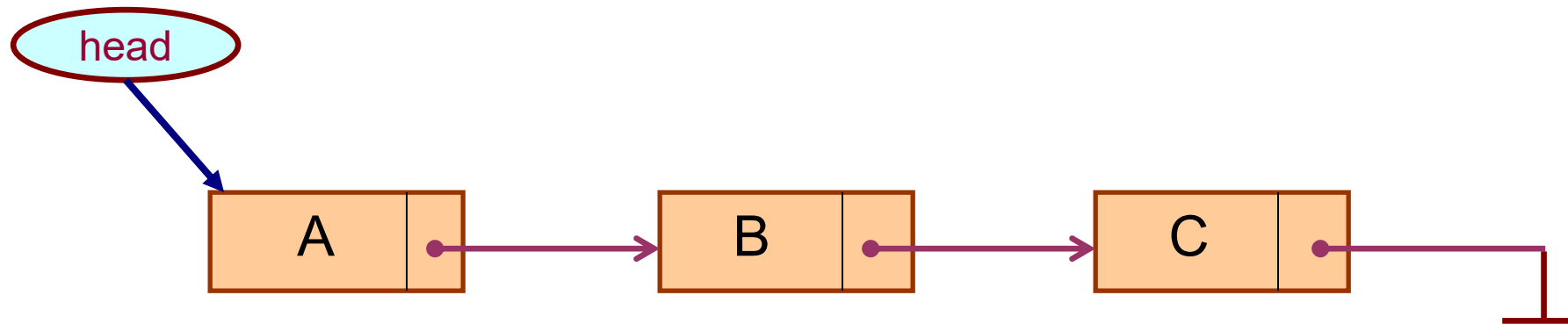
Remove 3



Remove 1

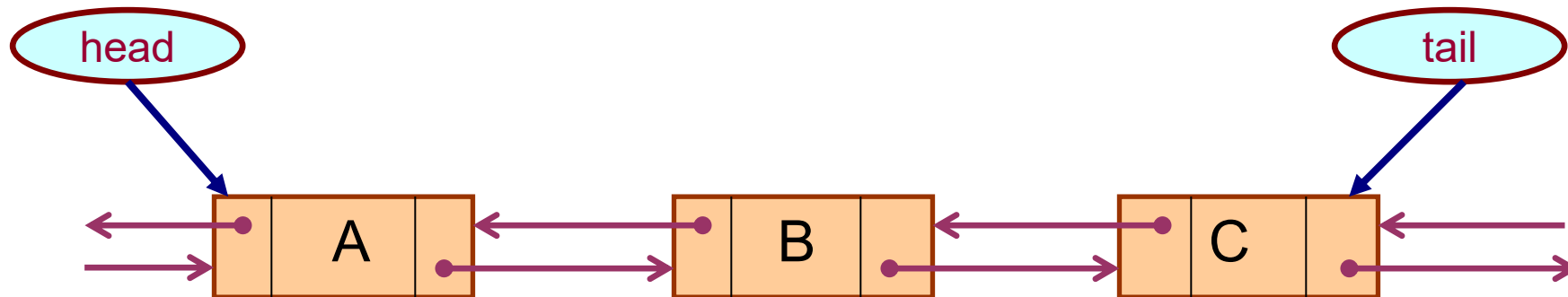
Types of Linked lists

- Depending on the way in which the links are used to maintain adjacency, several different types of linked lists are possible.
- Linear singly-linked list (or simply linear list)
 - One we have discussed so far.



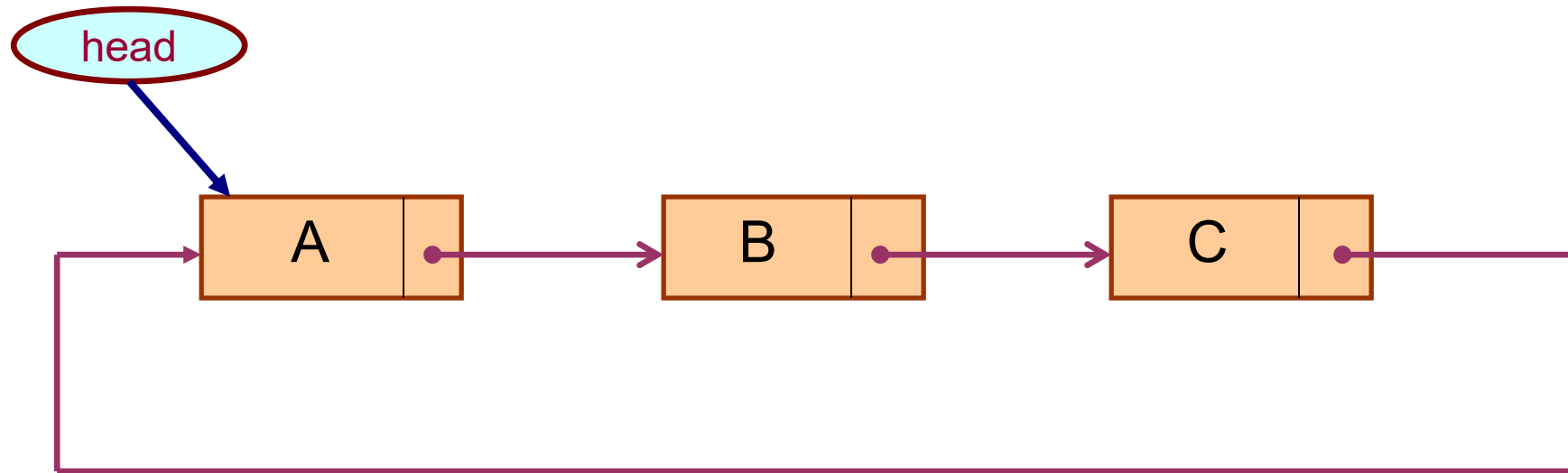
Types of Linked lists

- Doubly linked list
 - Pointers exist between adjacent nodes in both directions.
 - The list can be traversed either forward or backward.
 - Usually two pointers are maintained to keep track of the list, *head* and *tail*.



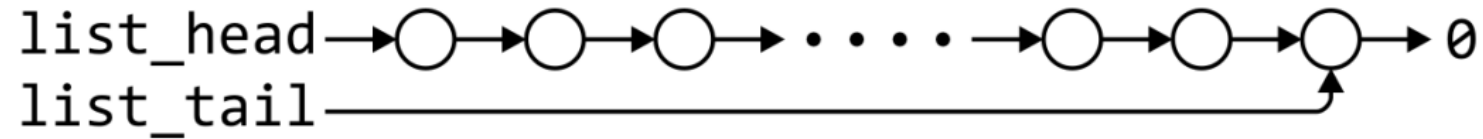
Types of Linked lists

- Circular linked list
 - The pointer from the last element in the list points back to the first element.

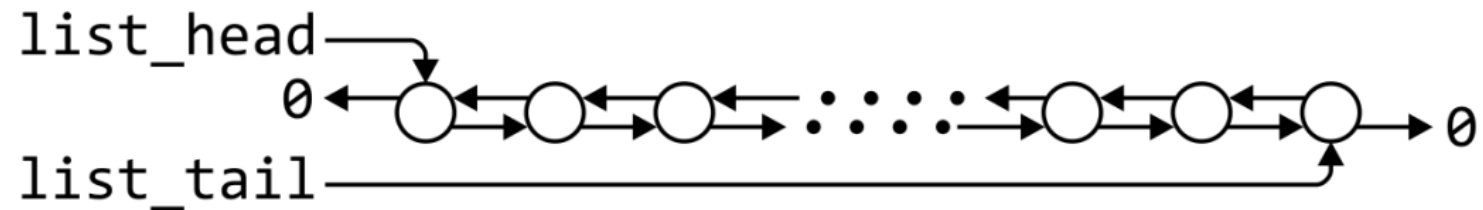


Types of Linked lists

- We will consider these for
 - Singly linked lists

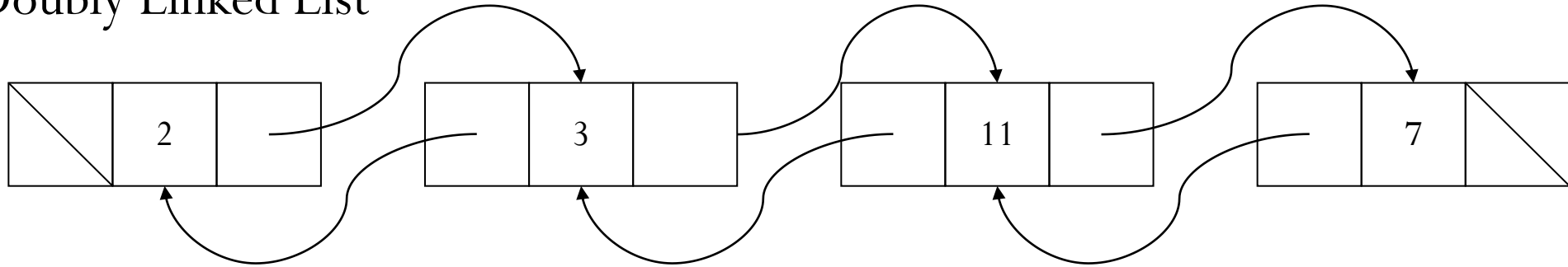


- Doubly linked lists

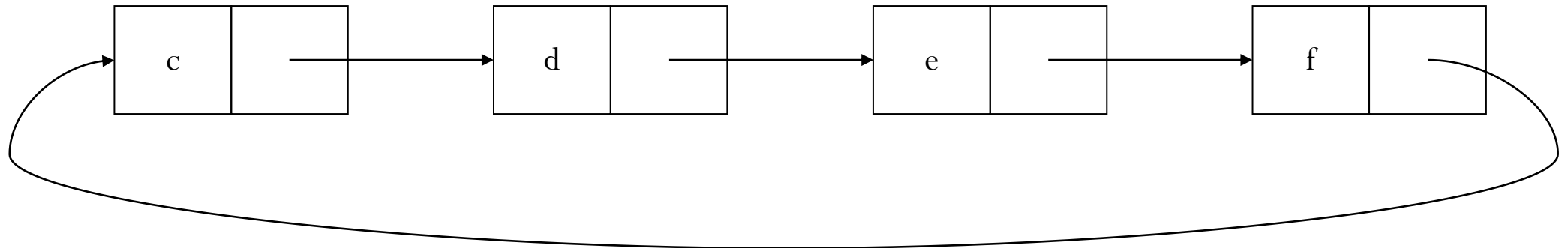


Types of Linked lists

- Doubly Linked List



- Circular List



Advantage of Linked List

- An Abstract List (or List ADT) is linearly ordered data where the programmer explicitly defines the ordering
- Most common operations and implementation uses either an Array or Linked list
- Arrays can be used to store linear data of similar types, with following limitations.
 - The size of the arrays is fixed
 - Inserting a new element in an array of elements is expensive
- Advantages over arrays
 - Dynamic size
 - Ease of insertion/deletion
- Drawbacks of linked list
 - Random access is not allowed. We cannot do binary search with linked lists.
 - Extra memory space for a pointer is required with each element of the list.

Dynamic Memory Management

Memory Allocation

The constructor is called whenever an object is created, either:

Static allocation,

```
List ls;
```

defines ls to be a linked list and the compiler deals with memory allocation

Dynamic allocation

```
List *pls = new List();
```

requests sufficient memory from the OS to store an instance of the class

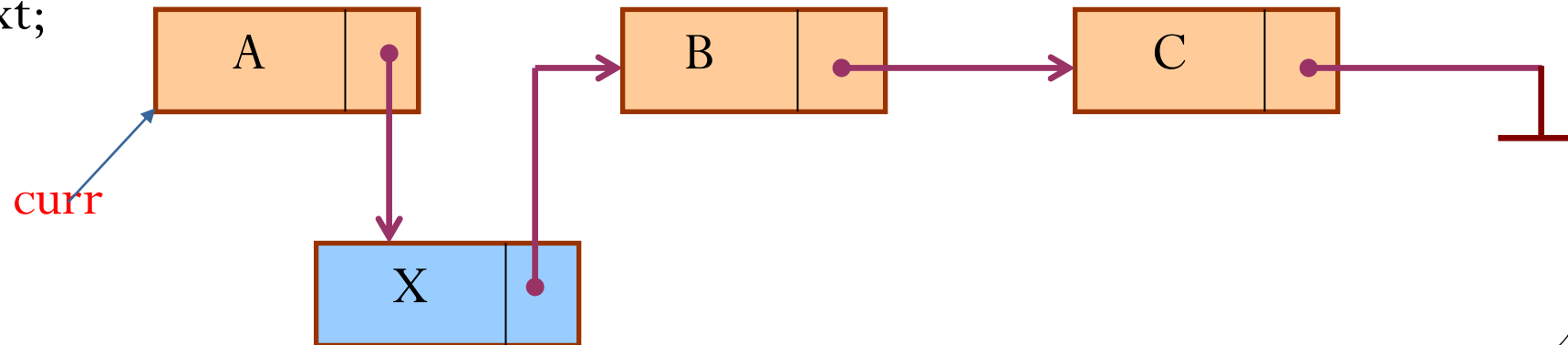
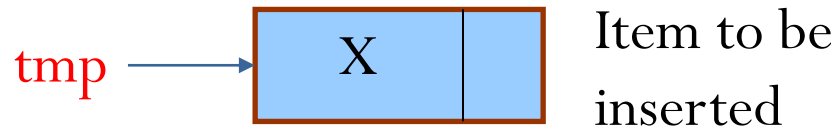
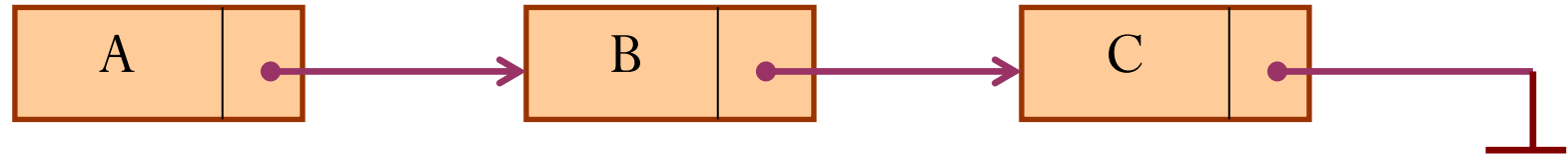
In both cases, the memory is allocated and then the constructor is called

Pseudo-code for insertion

```
typedef struct nd {  
    struct item data;  
    struct nd * next;  
} node;
```

```
void insert(node *curr)  
{  
    node * tmp;
```

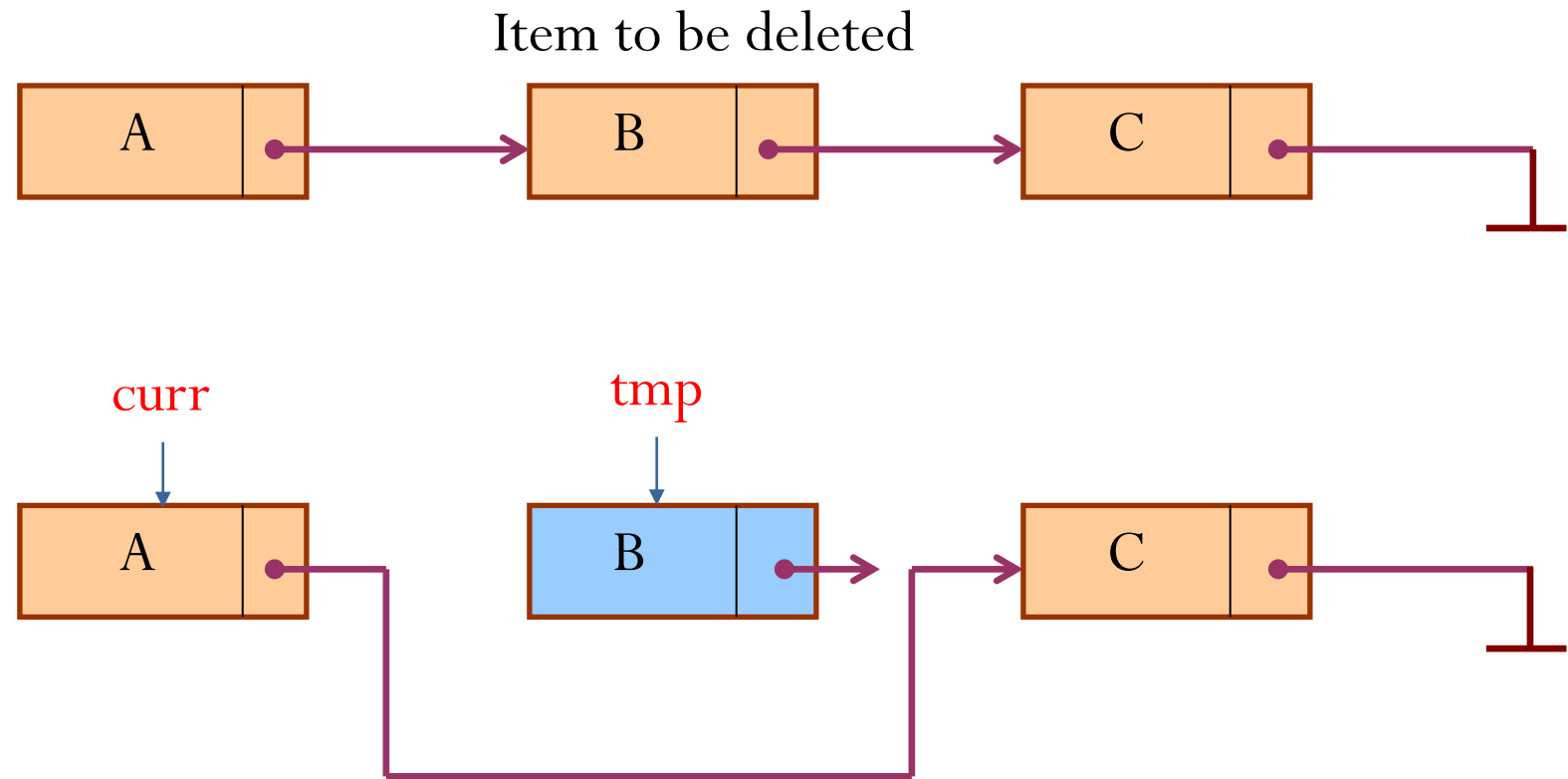
```
    tmp=(node *) malloc(sizeof(node));  
    tmp->next=curr->next;  
    curr->next=tmp;  
}
```



Pseudo-code for deletion

```
typedef struct nd {  
    struct item data;  
    struct nd * next;  
} node;
```

```
void delete(node *curr)  
{  
    node * tmp;  
    tmp=curr->next;  
    curr->next=tmp->next;  
    free(tmp);  
}
```



Pseudo-code

- For insertion:
 - A record is created holding the new item.
 - The **next** pointer of the new record is set to link it to the item which is to follow it in the list.
 - The **next** pointer of the item which is to precede it must be modified to point to the new item.
- For deletion:
 - The **next** pointer of the item immediately preceding the one to be deleted is altered, and made to point to the item following the deleted item.

Dynamic Storage: Memory Management

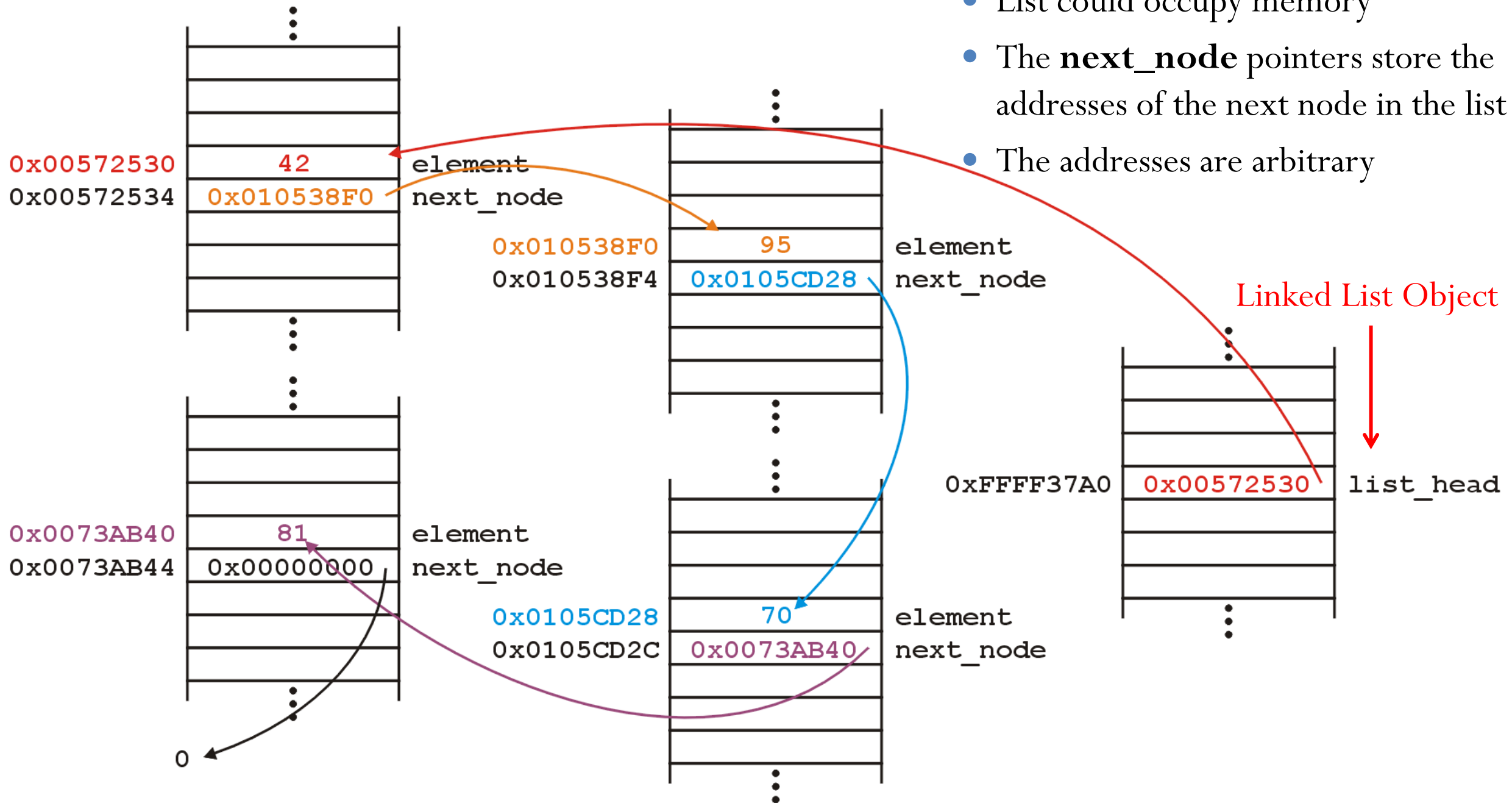
A linked list uses linked allocation, and therefore each node may appear anywhere in memory

Assuming a 32-bit machine

Memory required for each node equals the memory required by the member variables

- 4 bytes for the linked list (a pointer)
- 8 bytes for each node (an **int** and a pointer)

- List could occupy memory
- The **next_node** pointers store the addresses of the next node in the list
- The addresses are arbitrary



Dynamic Storage: Memory Management

- Clean representation as follows:



- We do not specify the addresses because they are arbitrary and:
 - The contents of the circle is the value
 - The `next_node` pointer is represented by an arrow

Applications of Linked List

Ordered List Examples

- MONDAY, TUESDAY, WEDNESDAY, THURSDAY, FRIDAY, SATURDAY, SUNDAY
- 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King, Ace
- 1941, 1942, 1943, 1944, 1945
- $a_1, a_2, a_3, \dots, a_{n-1}, a_n$
- **ordered (linear) list**: (item1, item2, item3, ..., item n)

Applications

- Everything!
 - Class list
 - compilers: list of functions in a program, statements in a function
 - graphics: list of triangles to be drawn to the screen
 - operating systems: list of programs running
 - music: compose crazy hard transcendental études
 - other data structures: queues, stacks!

Application: Polynomial ADT

A_i is the coefficient of the x^{n-i} term:

$$3x^2 + 2x + 5 \quad (3 \ 2 \ 5)$$

$$8x + 7 \quad (8 \ 7)$$

$$x^2 + 3 \quad (1 \ 0 \ 3)$$

Problem?

$$x^{2001} + 1$$

[illegible]

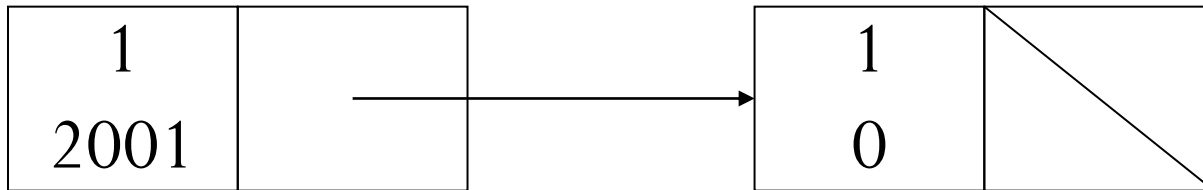
Sparse List Data Structure (?): $x^{2001} + 1$

(<1 2001> <1 0>)

Linked List

vs.

Array

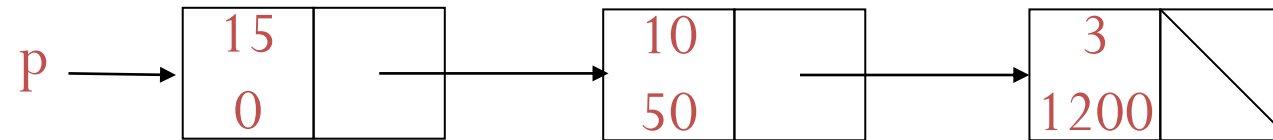


1	1
2001	0

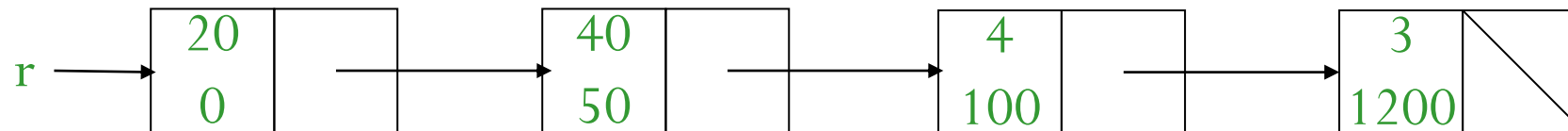
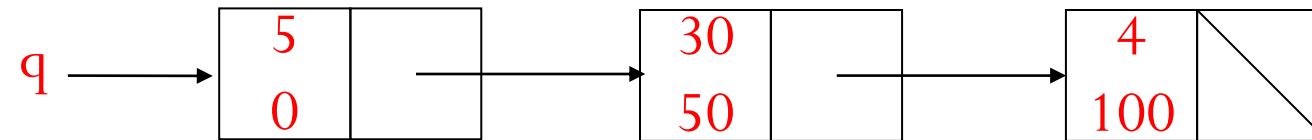
Addition of Two Polynomials

- Similar to merging two sorted lists

$$15 + 10x^{50} + 3x^{1200}$$



$$5 + 30x^{50} + 4x^{100}$$

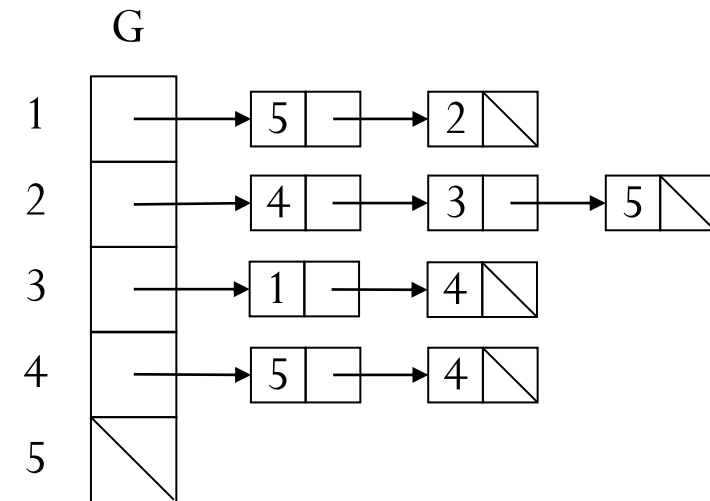
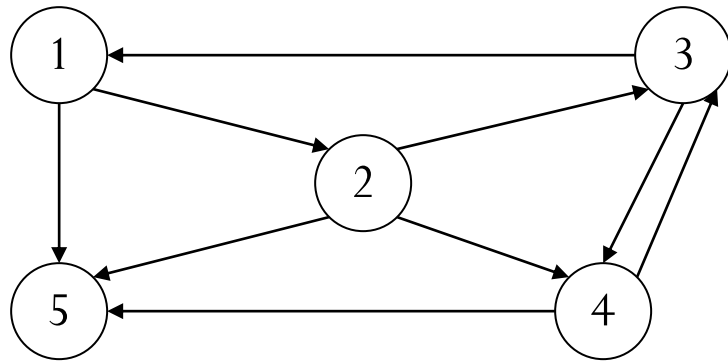


Multiple Linked Lists

- Many ADTS such as graphs, relations, sparse matrices, multivariate polynomials use multiple linked lists
- Several options
 - array of lists
 - lists of lists
 - multi lists
- General principle: use one ADT to implement a more complicated one.

Array of Linked Lists: Adjacency List for Graphs

- Array G of unordered linked lists
- Each list entry corresponds to an edge in the graph



Reachability by Marking

- Suppose we want to mark all the nodes in the graph which are reachable from a given node **k**.
 - Let **G[1..n]** be the adjacency list rep. of the graph
 - Let **M[1..n]** be the mark array, initially all **false**s.

```
mark(int i){  
    M[i] = true;  
    x = G[i]  
    while (x != NULL) {  
        if (M[x->node] == false)  
            mark(G[x->node])  
        x = x->next  
    }  
}
```

Thoughts on Reachability

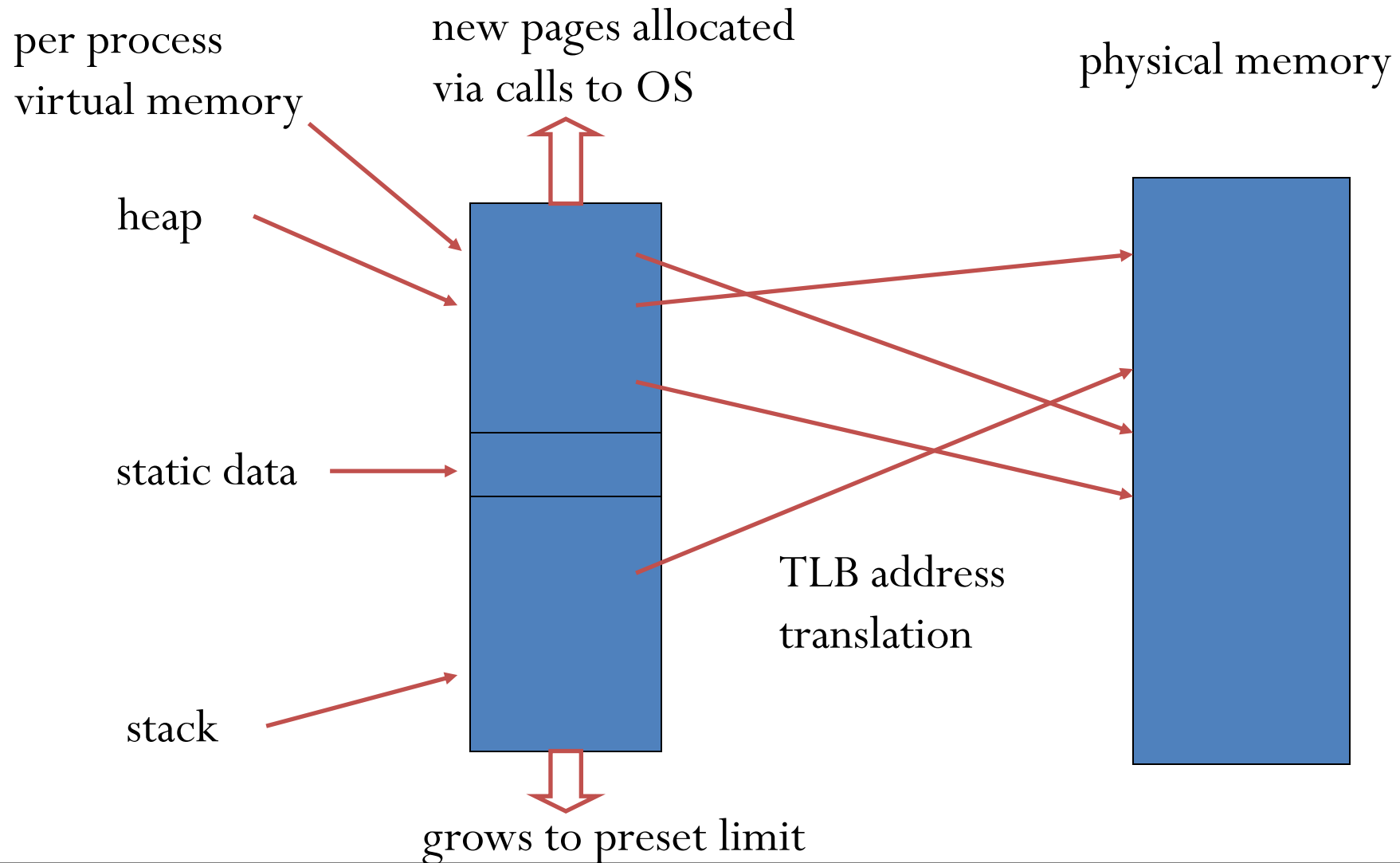
- The marking algorithm visits each node and each edge at most once.
- This marking algorithm uses Depth First Search. DFS uses a stack to track nodes. Where?
- Graph reachability is closely related to garbage collection
 - the nodes are blocks of memory
 - marking starts at all global and active local variables
 - the marked blocks are reachable from a variable
 - unmarked blocks are garbage

Garbage Collection

Garbage Collection

- Every modern programming language allows programmers to allocate new storage dynamically
 - New records, arrays, tuples, objects, closures, etc.
- Every modern language needs facilities for reclaiming and recycling the storage used by programs
- It's usually the most complex aspect of the run-time system for any modern language (Java, ML, Lisp, Scheme, Modula, ...)

Memory layout



Garbage Collection

- What is **garbage**?
 - A value is garbage if it **will not be used** in any subsequent computation by the program
- Is it easy to determine which objects are garbage?
 - No. It's undecidable. Eg:
if long-and-tricky-computation then **use v**
else **don't use v**

Garbage Collection

- Since determining which objects are garbage is tricky, people have come up with many different techniques
 - It's the programmers problem:
 - Explicit allocation/deallocation
 - Reference counting
 - Tracing garbage collection
 - Mark-sweep, copying collection
 - Generational Garbage Collection

Explicit Memory Management

- User library manages memory; programmer decides when and where to allocate and deallocate
 - `void* malloc(long n)`
 - `void free(void *addr)`
 - Library calls OS for more pages when necessary
 - Advantage: people are smart
 - Disadvantage: people are dumb and they really don't want to bother with such details if they can avoid it

Explicit Memory Management

- How does malloc/free work?
 - Blocks of unused memory stored on a **freelist**
 - **malloc**: search free list for usable memory block
 - **free**: put block onto the head of the freelist
- Drawbacks
 - **malloc is not free**: we might have to do a significant search to find a big enough block
 - As program runs, the heap **fragments** leaving many small, unusable pieces

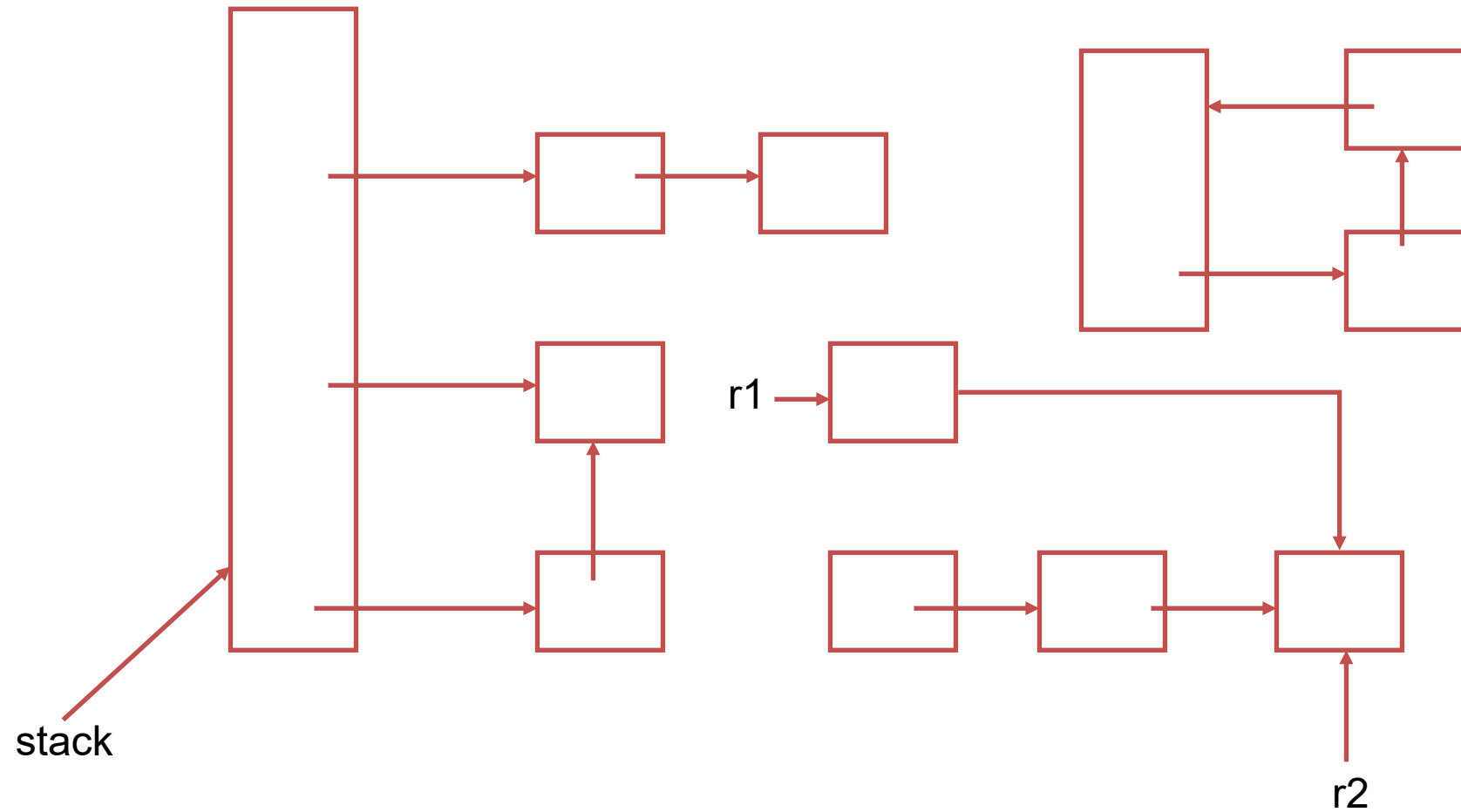
Automatic Memory Management (MM)

- Languages with Explicit MM are much harder to program than languages with Automatic MM
 - Always worrying about **dangling pointers**, **memory leaks**: a huge software engineering burden
 - Impossible to develop a **secure system**, impossible to use these languages in emerging applications involving **mobile code**
 - Soon, languages with unsafe, Explicit MM will all but **disappear**

Automatic Memory Management

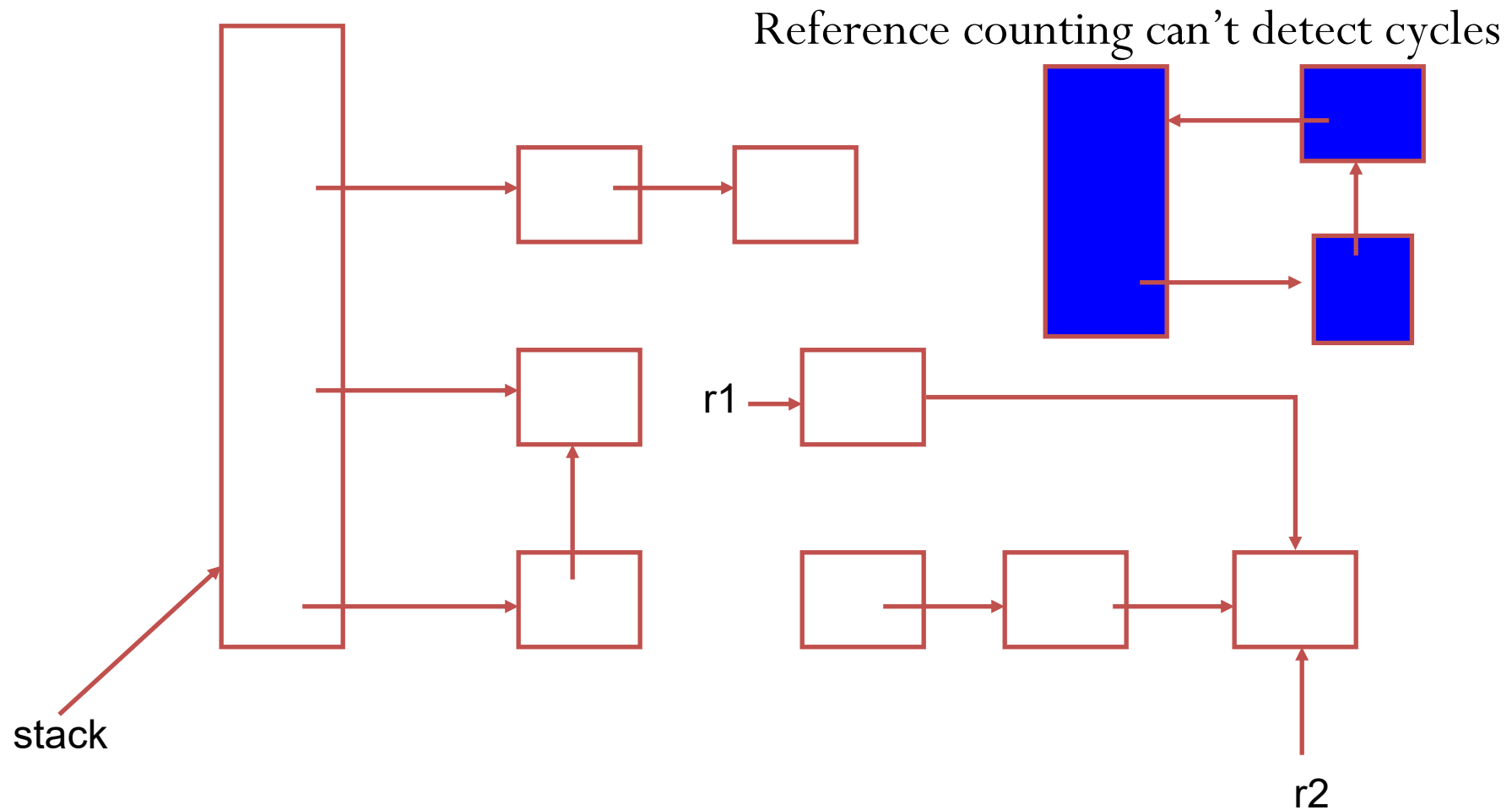
- Question: how do we decide which objects are garbage?
 - We conservatively approximate
 - Normal solution: an object is garbage when it becomes unreachable from the roots
 - The roots = registers, stack, global static data
 - If there is no path from the roots to an object, it cannot be used later in the computation so we can safely recycle its memory

Object Graph



- How should we test reachability?

Object Graph



- Keep track of the number of pointers to each object (the reference count).
- When the reference count goes to 0, the object is unreachable garbage

Copying Collection

- Basic idea: use 2 heaps
 - One used by program
 - The other unused until GC time
- Garbage Collection:
 - Start at the roots & traverse the reachable data
 - Copy reachable data from the active heap (from-space) to the other heap (to-space)
 - Dead objects are left behind in from space
 - Heaps switch roles

Student Linked List

Student Linked List

- Consider the structure of a node as follows:

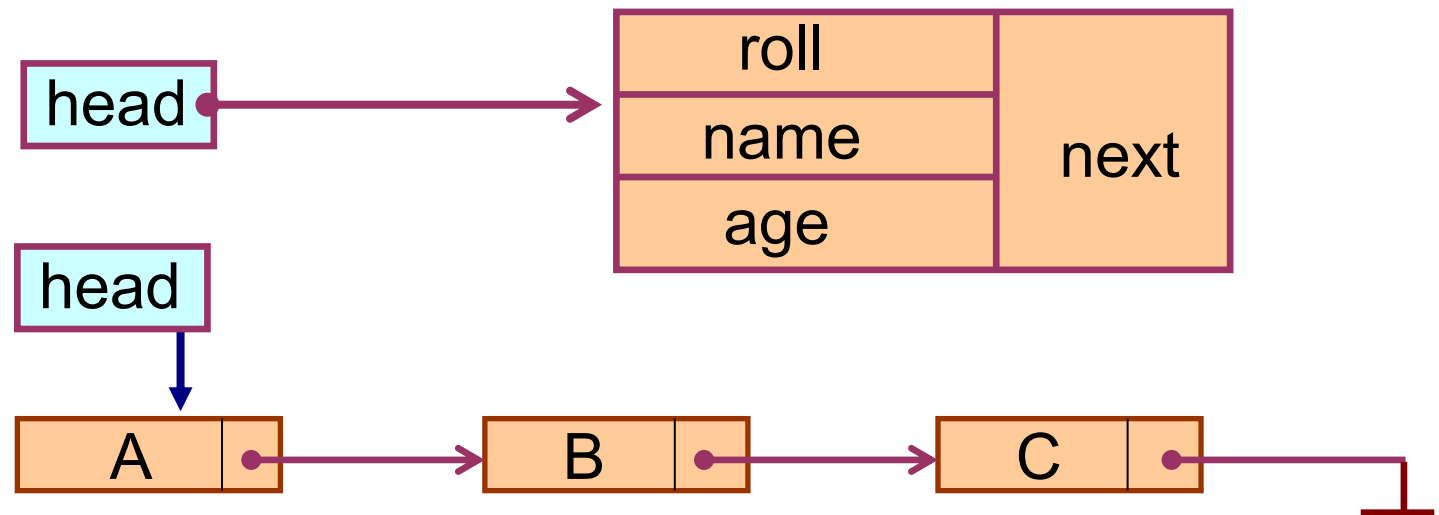
```
struct stud {  
    int    roll;  
    char   name[25];  
    int    age;  
    struct stud *next;  
};
```

```
/* A user-defined data type called "node" */
```

```
typedef struct stud node;  
node *head;
```


Student Linked List

- To start with, we have to create a node (the first node), and make **head** point to it
`head = (node *) malloc(sizeof(node)) ;`
- If there are **n** number of nodes in the initial linked list:
 - Allocate **n** records, one by one.
 - Read in the fields of the records.
 - Modify the links of the records so that the chain is formed.



Create the Student Linked List

To be called from `main()`
function as:

```
node *create_list()
{
    int k, n;
    node *p, *head;

    printf ("\n How many elements to enter?");
    scanf ("%d", &n);

    for (k=0; k<n; k++)
    {
        if (k == 0) {
            head = (node *) malloc(sizeof(node));
            p = head;
        }
        else {
            p->next = (node *) malloc(sizeof(node));
            p = p->next;
        }
        scanf ("%d %s %d", &p->roll, p->name, &p->age);
    }

    p->next = NULL;
    return (head);
}
```

`node *head;`

`.....`

`head = create_list();`

Traverse the Student Linked List

```
void display (node *head)
{
    int  count = 1;
    node *p;

    p = head;
    while (p != NULL)
    { printf ("\nNode %d: %d %s %d", count, p->roll, p->name, p->age);
      count++;
      p = p->next;
    }
    printf ("\n");
}
```

- To be called from `main()` function

```
node *head;
```

```
.....
```

```
display (head);
```

- After construction, *head* points to the first node of the list,
 - Follow the pointers.
 - Display the contents of the nodes as they are traversed.
 - Stop when the *next* pointer points to **NULL**.

Inserting a Node in a List

Inserting a Node in the Student Linked List

- The problem is to insert a node *before a specified node*.
 - Specified means some value is given for the node (called *key*).
 - In this example, we consider it to be *roll*.
- Convention followed:
 - If the value of roll is given as *negative*, the node will be inserted at the *end* of the list.

```
void insert (node **head)
```

```
{  
    int k = 0, rno;  
    node *p, *q, *new;
```

```
    new = (node *) malloc(sizeof(node));
```

```
    printf ("\nData to be inserted: ");
```

```
    scanf ("%d %s %d", &new->roll, new->name, &new->age);
```

```
    printf ("\nInsert before roll (-ve for end):");
```

```
    scanf ("%d", &rno);
```

```
    p = *head;
```

- To be called from main () function

```
node *head;
```

```
.....
```

```
insert (&head);
```

Insert a Node in the Student Linked List

- When a node is added at the beginning,
 - Only one next pointer needs to be modified.
 - *head* is made to point to the new node.
 - New node points to the previously first element.
- When a node is added at the end,
 - Two next pointers need to be modified.
 - Last node now points to the new node.
 - New node points to **NULL**.
- When a node is added in the middle,
 - Two next pointers need to be modified.
 - Previous node now points to the new node.
 - New node points to the next node.
- The pointers *q* and *p* always point to consecutive nodes.

```
if (p->roll == rno)    /* At the beginning */
{
    new->next = p;
    *head = new;
}
else
{
    while ((p != NULL) && (p->roll != rno))
    {
        q = p;
        p = p->next;
    }

    if (p == NULL)    /* At the end */
    {
        q->next = new;
        new->next = NULL;
    }
    else if (p->roll == rno)
        /* In the middle */
        {
            q->next = new;
            new->next = p;
        }
}
}
```

```

void delete (node **head)
{
    int rno;
    node *p, *q;

    printf ("\nDelete for roll :");
    scanf ("%d", &rno);

    p = *head;

```

- Required to delete a specified node.
 - Roll Number is given.
- Here also three conditions arise:
 - Deleting the first node.
 - Deleting the last node.
 - Deleting an intermediate node.

Delete a Node in the Student Linked List

```

if (p->roll == rno) /* Delete the first element */
{
    *head = p->next;
    free (p);
}

else
{
    while ((p != NULL) && (p->roll != rno))
    {
        q = p;
        p = p->next;
    }

    if (p == NULL) /* Element not found */
        printf ("\nNo match deletion failed");

    else if (p->roll == rno)
        /* Delete any other element */
        {
            q->next = p->next;
            free (p);
        }
    }
}

```

Exercises

- Write a function to:
 - Concatenate two given list into one big list.
- Insert an element in a linked list in sorted order. The function will be called for every element to be inserted.

```
node *concatenate (node *head1, node *head2);
```

```
void insert_sorted (node **head, node *element);
```

- Always insert elements at one end, and delete elements from the other end (**first-in first-out QUEUE**).

```
void insert_q (node **head, node *element)
```

```
node *delete_q (node **head)  /* Return the deleted node */
```


References

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