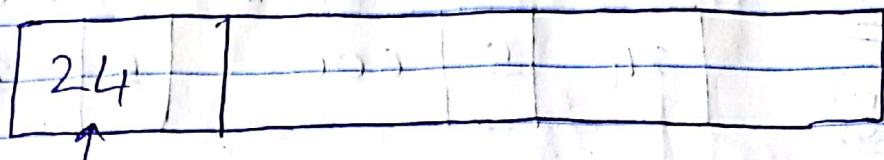


PROBLEM SET - 3: →

①. (a)



Header

$$\text{a) Total block size} = 1024 - 24 \\ = 1000 \text{ bytes}$$

$$\text{Record size with offset} = 50 + 4 \\ = 54$$

$$\left[\frac{1000}{54} \right] = 18 \quad \underline{\text{Ans}}$$

$$\text{b) Total block size} = 1024 - 24 \\ = 1000 \text{ bytes}$$

$$\text{Total offset size per record} = 4 \times 20 \\ = 80$$

$$\therefore = \left[\frac{1000 - 80}{20} \right] \\ = \underline{\underline{46}} \quad \text{Ans}$$

c) Now in this case as the record size is fixed so, there is no offset per record.

∴ Total block size (without header)

$$= 1024 - 24 \rightarrow 1000 \\ \therefore \left[\frac{1000}{50} \right] = \underline{\underline{20}} \quad \text{Ans}$$

d.)
(3)

Header.

	Record 1		Record 2a.	
	24	5	600	5 390

BLOCK-2

	Record 2b.				
	24	5	210	5	600 180

Remaining

(2)

(i)

SELECT π-rating, π-comment,

FROM Product p, Reviewer ππ, Reviewer πτ;

WHERE p-pname = 'ABC' AND
ππ-city = 'Chicago' AND
p.pid = π-pid AND
πτ-rid = π-rid

ORDER BY π-rating DESC.

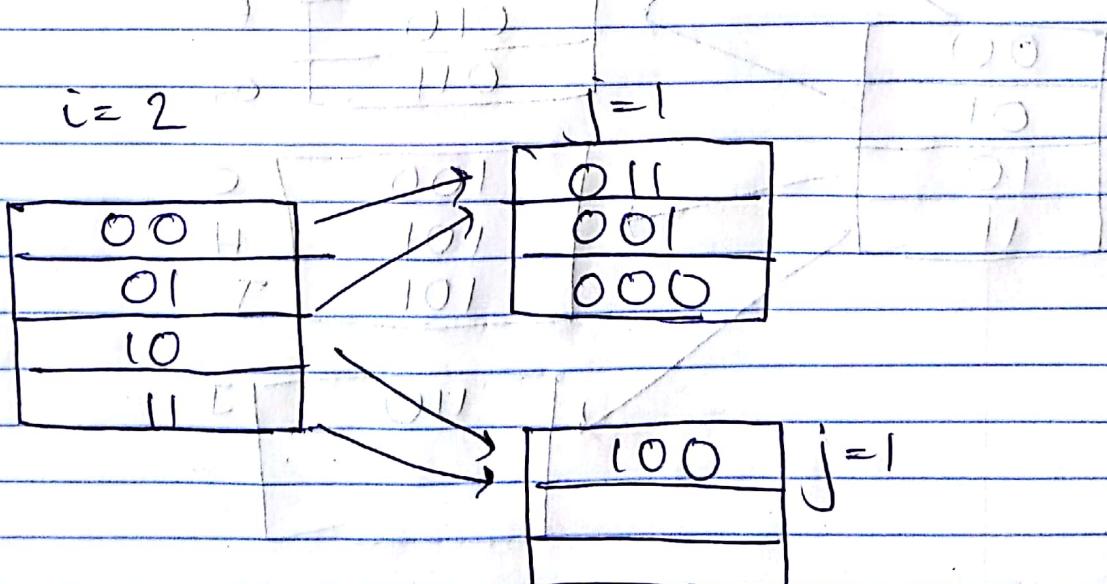
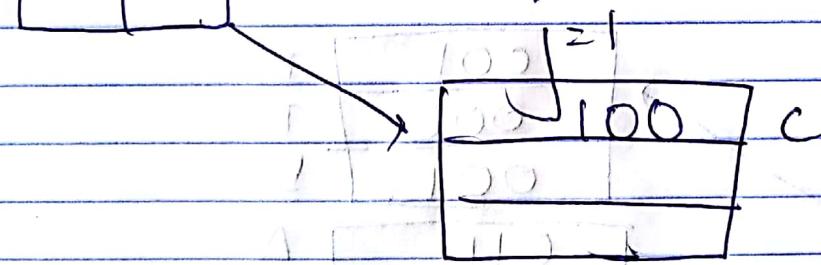
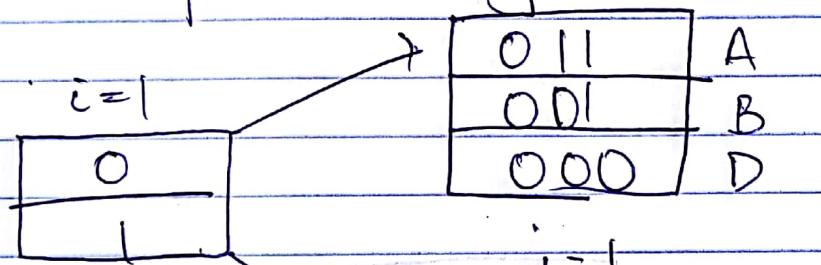
(ii) SELECT πτ-city, COUNT(πτ.rid)
FROM Reviewer πτ
GROUP BY πτ-city
ORDER BY πτ-city.

(iii) `SELECT rvr.rname
FROM Reviewer rvr, Review rv
WHERE rvr.rid = rv.rid
GROUP BY rv.rid, rvr.rid, rvr.rname.
HAVING AVG(rv.rating) <= 2.`

(iv) `SELECT p.pname, p.description
FROM Product p, Review rv
WHERE p.pid = rv.rid
GROUP BY p.pid, p.pname, p.description
HAVING MIN(rv.rating) >= 4.`

3

<u>3</u>	A 00011	00011	00011	00011	00011	00011
	B 00001	00001	00001	00001	00001	00001
	C 00100	00100	00100	00100	00100	00100
	D 00000	00000	00000	00000	00000	00000
	E 00001	00001	00001	00001	00001	00001
	F 00010	00010	00010	00010	00010	00010
	G 00011	00011	00011	00011	00011	00011
	H 00101	00101	00101	00101	00101	00101
	I 00110	00110	00110	00110	00110	00110
	J 00101	00101	00101	00101	00101	00101
	K 00001	00001	00001	00001	00001	00001
	L 00110	00110	00110	00110	00110	00110



$i=2$

00
01
10
11

$j=2$

001
000
001

B

D

E

011
010
011

A

F

G

100
101
110

C

H

I

110
101
000

101
100
010

00
01
10
11

001
000
001

B

D

E

011
010
011

A

F

G

100
101
101

C

H

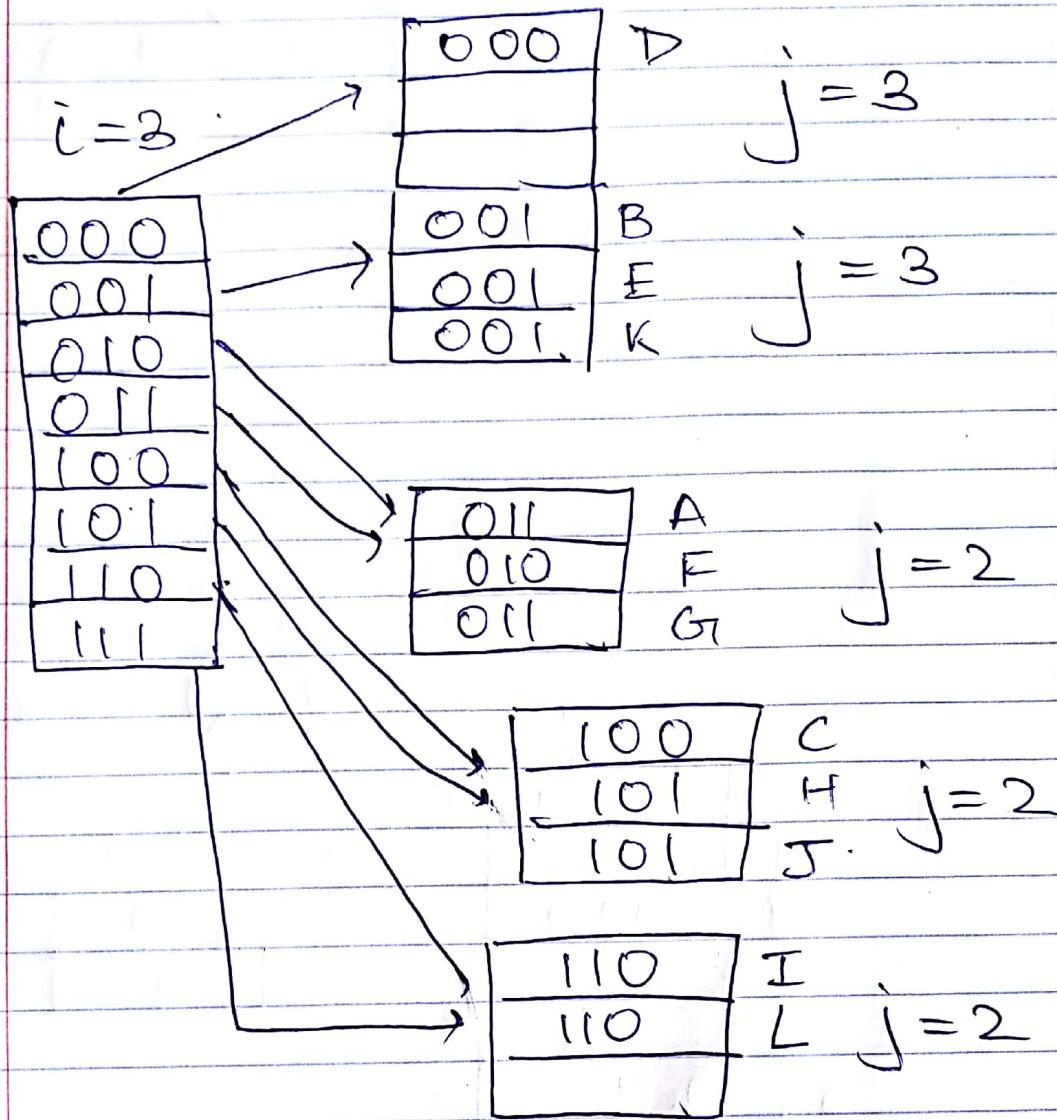
J

110
101
010

I

K

L



(4)

4.1 \rightarrow Minimum possible value of 'x'

$$\begin{array}{r} = 3 \\ \hline \end{array}$$

4.2 \rightarrow Max Value

$$\begin{array}{r} = 4 \times 2 \\ = 8 \\ \hline \end{array}$$

(5)

a) Total block size = $1024 - 32$
= 992 bytes.

1 record length = $12 + 5 + 6 + 7$
= 30 bytes

\therefore No. of records = $\left\lfloor \frac{992}{30} \right\rfloor$
= 33 records / block

b) (i) CHECK: \rightarrow

Record size = 23×32
= 736 bytes.

2 bytes per records = 32×2
= 64 bytes

$$\therefore 736 + 64 \Rightarrow 800$$

$$\therefore 1024 - 32 - 800 = \underline{\underline{192}}$$

CHECK

(ii) $30 \times 20 \rightarrow 600$ bytes.

$10 \times 10 \rightarrow 100$ bytes.

$40 \times 2 \rightarrow 80$ bytes (Header).

$$= 1024 - 32 - 600 - 100 - 80$$

$$= 212 \text{ bytes.}$$

(iii) $5 \times 11 \rightarrow 55$ bytes. CHECK

$10 \times 13 \rightarrow 130$ bytes.

$20 \times 14 \rightarrow 340$ bytes.

$35 \times 2 \rightarrow 70$ bytes.

$$= 1024 - 32 - 55 - 130 - 340 - 70$$

$$= 394 \text{ bytes. } \underline{\text{CHECK}}$$

(iv) NO CHECK

$$(1024 - 32 - 4) - 992$$

-2 OUT OF SPACE

⑥

(i) Projection cannot be pushed below set union: →

$$\text{Let } R(A, B) = \{(1, 2)\}$$

$$S(A, B) = \{(1, 3)\}$$

Then $\text{pi}_A(R \cup S)$

$$= \text{pi}_A \{(1, 2), (1, 3)\}$$

$$= \{(1), (1)\}$$

But the union → $\{(1)\}$

Since the set union removes the duplicates from the union.

(ii) Projection cannot be pushed below set or bag difference: →

$$R(a, b, c) = \{(1, 2, 3), (1, 3, 2)\}$$

¶

$$S(a, b, c) = \{(1, 2, 3), (1, 4, 5)\}$$

This relation provides an example of schemas & instances.

(iii) Duplicate elimination cannot be pushed below projection: →

The relation schemas and instances
 $R(a, b, c) = \{(1, 2, 3), (1, 3, 2)\}$

$S(a, b, c) = \{(1, 2, 3), (1, 4, 5)\}$

gives an example which proves the assertion.

(iv) Duplicate elimination cannot be pushed below bag union or difference: →

$R(a) = \{(1), (1)\}$

$S(a) = \{(1), (1)\}$

gives relation schemas & instances which proves the assertion.

7 (i) $\pi_{\text{sid}}((\pi_{\text{pid}} \sigma_{\text{color} = \text{"red"}} \text{Parts}) \bowtie \text{Catalog} \bowtie \text{Suppliers})$

(ii) $\pi_{\text{sid}}((\pi_{\text{pid}} \sigma_{\text{color} = \text{"red"} \vee \text{color} = \text{"green"}} \text{Parts}) \bowtie \text{Catalog})$

(iii) $\pi_{\text{sid}}((\pi_{\text{pid}} \sigma_{\text{color} = \text{"red"}} \text{Parts}) \bowtie \text{Catalog}) \cup \pi_{\text{sid}}(\sigma_{\text{address} = \text{"10 West 31st Street}}} \text{Suppliers})$

(iv) $\pi_{\text{sid}}((\pi_{\text{pid}} \sigma_{\text{color} = \text{"red"}} \text{Parts} \cap (\pi_{\text{pid}} \sigma_{\text{color} = \text{"green"}} \text{Parts})) \bowtie \text{Catalog})$

(v) $\pi_{R1.sid, R2.sid} \left(C_{R1.fid=R2.fid \wedge R1.sid \neq R2.sid \wedge R1.cost > R2.cost} \right)$

(pri Catalog x pre Catalog)

(vi) $\nabla_{R1 \cdot pid} (\sigma_{R1.pid = R2.pid} \wedge R1.sid \neq R2.sid$
 $(P_{R1} \text{ Catalog} \times P_{R2} \text{ Catalog})$.

(vii) $t1 \leftarrow ((\pi_{\text{yd}} \sigma_{\text{name} = "Yosemite Sham"} \text{ Supplier})$
 $\bowtie \text{Catalog})$

$$t_4 \leftarrow \pi_{t_2.sid, t_2.bid, t_2.cast} \sigma_{t_2.coef < t_3.cast} (p_{t_2}(t_1) \times p_{t_3}(t_1))$$

$\pi_{pid}(pts(sid, pid, cost) t)$

- $P+6 \text{ (sid, fid, cost) } t4$)

Q (i) $T(\text{library}) = 100$

$$T(a) = \frac{100}{2} (T(\text{library})) \\ V(\text{library, public})$$

(ii) ~~IT~~(book) = 100,000

$$V(\text{book}, \text{title}) = 50,000$$

$\nabla(\text{book}, \text{author}) = 30,000$

$$= \frac{T(\text{book})}{V(\text{book}, \text{title}) \cdot V(\text{book}, \text{author})}$$

$$= \left(\frac{100,000}{50,000 \cdot 30,000} \right)$$

$$= \left(\frac{1}{15,000} \right) = \frac{1}{15,000}$$

(iii) $T(a_r) \rightarrow$

$$= \frac{4 - 2 + 1}{\max(\text{book}, \text{edition}) - \min(\text{book}, \text{edition}) + 1} = \frac{1}{50,000} \cdot T(\text{book})$$

$$= \frac{3 \cdot 100,000}{15 \cdot 50,000}$$

$$= \frac{2}{5} \Rightarrow 0.4$$

$$(iv) V(\text{book}, \text{title}) = 50,000$$

$$T(\text{book}) = 10,000$$

$$\max(\text{library}, \text{budget}) = 70$$

$$\min(\text{library}, \text{budget}) = 10$$

$$T(\text{library}) = 100$$

$$\begin{aligned}
 T(q_1) &= \left(1 - \left[\left(1 - \frac{1}{V(\text{book}, \text{title})} \right) \right] \cdot T(\text{book}) \right) \\
 &\quad \left(\left(1 - \frac{1}{V(\text{book}, \text{title})} \right) \right) \cdot T(\text{book}) \\
 &= \left(1 - \left(1 - \frac{1}{50000} \right) \right) \cdot \left(1 - \frac{1}{50000} \right) \cdot 10000
 \end{aligned}$$

≈ 4

Selection result size $q_2 \rightarrow$

$$\begin{aligned}
 T(q_2) &= \frac{\max(\text{library}, \text{budget}) - 40 + 1}{\max(\text{library}, \text{budget}) - \min(\text{library}, \text{budget}) + 1} \cdot T(\text{library}) \\
 &= \frac{70 - 40 + 1}{70 - 10 + 1} \cdot 100
 \end{aligned}$$

≈ 51

$$\therefore T(q) \rightarrow 51 \cdot 100 = 5100 \text{ (Total)}$$

$$\frac{T(q_1) \cdot T(\text{catalog}) \cdot T(q_2)}{\max(\text{Value}_1) \cdot \max(\text{Value}_2)}$$

$$5100 = 5100 \cdot T$$

$$= \frac{4 \cdot 100 \cdot 51}{\max(2, 90000) \cdot \max(100, 51)}$$

$$\approx \frac{20,400}{90,000,000}$$

$$\begin{array}{r} 2 \\ \overline{)900} \end{array}$$