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**Course: MA311M (Scientific
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How to run the code:

Language: Python

Requirements: Libraries such as Numpy , Matplotlib and math are required.

Running: Can simply upload the .ipynb file attached on jupyter notebook or on google colab and run all at once.

Question 1: Firstly we will find the guess value of the root by using the bisection method and running three iterations of the same, considering $A_n = 0$ and $B_n = 1$ as the upper and lower bounds for the root and also checking $f(0)*f(1) < 0$ and perform the iterations by finding $C_n = A_n + (B_n - A_n)/2$.

- After 3 iterations on bisection method we get guess value of root = **0.625**.
- Considering the tolerance of $1e-5$ in the error using NMR , we get the saturation value after 2 iterations only:
 - 1) Iteration 1: $x_0 = 0.625 \rightarrow x_1 = 0.58798$, error = 0.000765
 - 2) Iteration 2: $x_1 = 0.58798 \rightarrow x_2 = 0.58853$, error = $1.68 * 1e-7$
- Final value of root = **0.58853**
- The last part boils down to show that the order of convergence is 2(quadratic in nature):
 - 1) First condition in our problem is satisfied as $f(m) * f(n) = -0.473592$ (< 0) with $m=0$ and $n=1$.
 - 2) $f(x) \neq 0$ for all x in $[m, n]$ as can be shown in Plot1 in python file. Also, from Plot 1 $f'(x)$ takes -ve values in $[0,1]$.
 - 3) $f''(x) > 0$ or < 0 in $[m, n]$. As can be seen in Plot2 in python file $f''(x) > 0$ in $[0,1]$ and this condition is satisfied.
 - 4) Here $m = 0$ and $n = 1$ therefore $m-n = 1$, and $\text{abs}(f(a))/ \text{abs}(f'(a)) = 0.50$ ($< (m-n)$), also $\text{abs}(f(b))/ \text{abs}(f'(b)) = 0.52147$ ($< (m-n)$)

Therefore all the 4 conditions satisfy for quadratic convergence.

Question 2: Solving the equations with $x = 1$ and $y = 2$ and tolerance = $1e-3$.

Following is printed on executing the code:

- 1) Iteration = 0 , $X_n = 1$, $Y_n = 2$, error = 0.134279
- 2) Iteration = 1 , $X_n = 1.079665$, $Y_n = 1.945385$, error = 0.008145
- 3) Iteration = 2 , $X_n = 1.086138$, $Y_n = 1.943713$, error = 7.72×10^{-5}

Finally **$X_n = 1.086138$, $Y_n = 1.943713$**

The execution stops here.