Homework 9

Animesh Sengupta

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```
setwd("/Users/animeshsengupta/Work Directory/DACSS/STAT625/Homeworks")
library(MASS)
library(alr4) # loads the installed package into the workspace so you can use it
## Loading required package: car
## Loading required package: carData
## Loading required package: effects
## lattice theme set by effectsTheme()
## See ?effectsTheme for details.
library(summarytools)
library(ggplot2)
library(plotly)
## Attaching package: 'plotly'
## The following object is masked from 'package:ggplot2':
##
##
       last_plot
## The following object is masked from 'package:MASS':
##
##
       select
## The following object is masked from 'package:stats':
##
##
       filter
## The following object is masked from 'package:graphics':
##
##
       layout
```

```
library(splines)
library(boot)
##
## Attaching package: 'boot'
## The following object is masked from 'package:car':
##
      logit
library(sandwich)
library(plotly)
Answer 10.3
colnames(mantel)
## [1] "Y" "X1" "X2" "X3"
mlm <- lm(Y ~ 1, data=mantel)</pre>
step(mlm,scope= ~ X1 + X2 + X3, direction="forward")
## Start: AIC=9.59
## Y ~ 1
##
        Df Sum of Sq
##
                        RSS
## + X3 1 20.6879 2.1121 -0.3087
## + X1 1 8.6112 14.1888 9.2151
## + X2 1 8.5064 14.2936 9.2519
## <none>
                      22.8000 9.5866
##
## Step: AIC=-0.31
## Y ~ X3
##
         Df Sum of Sq
                         RSS
                                 AIC
                      2.1121 -0.30875
## <none>
## + X2 1 0.066328 2.0458 1.53172
## + X1 1 0.064522 2.0476 1.53613
##
## Call:
## lm(formula = Y ~ X3, data = mantel)
##
## Coefficients:
## (Intercept)
                        ХЗ
```

0.7975

0.6947

```
mlm2 \leftarrow lm(Y \sim X1 + X2 + X3, data=mantel)
step(mlm2,scope=~1, direction="backward",)
## Start: AIC=-285.77
## Y \sim X1 + X2 + X3
## Warning: attempting model selection on an essentially perfect fit is nonsense
          Df Sum of Sq
                          RSS
                                   AIC
## - X3
                0.0000 0.0000 -287.749
                       0.0000 -285.768
## <none>
## - X1
           1
                2.0458 2.0458
                                 1.532
## - X2
           1
                2.0476 2.0476
                                 1.536
##
## Step: AIC=-287.75
## Y ~ X1 + X2
## Warning: attempting model selection on an essentially perfect fit is nonsense
##
          Df Sum of Sq
                          RSS
                                   AIC
## <none>
                        0.000 -287.749
## - X2
         1
                14.189 14.189
                                 9.215
## - X1
                14.294 14.294
           1
                                 9.252
##
## Call:
## lm(formula = Y ~ X1 + X2, data = mantel)
## Coefficients:
                                      X2
## (Intercept)
                         X1
##
         -1000
                                        1
#adding log(n) in step function to get BIC values
n=nrow(mantel)
mlm3<- lm(Y ~ 1, data=mantel)</pre>
step(mlm3,scope= ~ X1 + X2 + X3, direction="forward",k=log(n))
## Start: AIC=9.2
## Y ~ 1
##
          Df Sum of Sq
                           RSS
                                   AIC
               20.6879 2.1121 -1.0899
## + X3
           1
## + X1
           1
               8.6112 14.1888 8.4339
                8.5064 14.2936 8.4707
## + X2
## <none>
                       22.8000 9.1961
## Step: AIC=-1.09
## Y ~ X3
##
##
          Df Sum of Sq
                          RSS
## <none>
                       2.1121 -1.08987
## + X2
           1 0.066328 2.0458 0.36003
## + X1 1 0.064522 2.0476 0.36444
```

```
##
## Call:
## lm(formula = Y ~ X3, data = mantel)
##
## Coefficients:
   (Intercept)
                          ХЗ
##
##
        0.7975
                      0.6947
mlm4 \leftarrow lm(Y \sim X1 + X2 + X3, data=mantel)
step(mlm4,scope=~1, direction="backward",k=log(n))
## Start: AIC=-287.33
## Y \sim X1 + X2 + X3
## Warning: attempting model selection on an essentially perfect fit is nonsense
##
          Df Sum of Sq
                           RSS
                                     AIC
## - X3
                 0.0000 0.0000 -288.921
## <none>
                        0.0000 -287.331
## - X1
           1
                 2.0458 2.0458
                                   0.360
## - X2
           1
                 2.0476 2.0476
                                   0.364
##
## Step: AIC=-288.92
## Y ~ X1 + X2
## Warning: attempting model selection on an essentially perfect fit is nonsense
##
          Df Sum of Sq
                           RSS
                                     AIC
## <none>
                         0.000 -288.921
## - X2
                 14.189 14.189
           1
                                   8.434
## - X1
           1
                 14.294 14.294
                                   8.471
##
## lm(formula = Y ~ X1 + X2, data = mantel)
##
## Coefficients:
## (Intercept)
                          X1
                                        X2
         -1000
##
                           1
                                         1
```

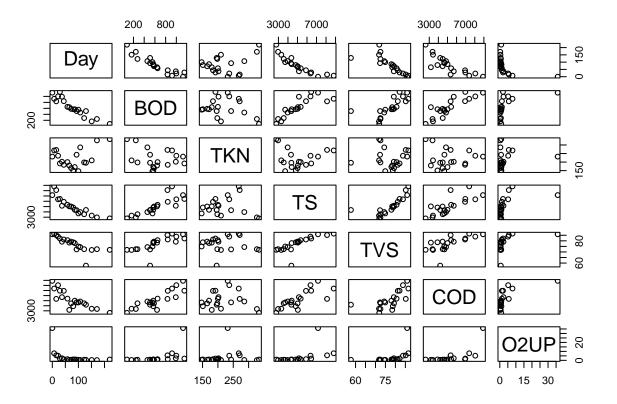
After performing backward and forward elimination using both AIC and BIC we can conlcude the following few things. As expected, the BIC is giving tougher penalties hence the BIC values in stepwise model comparison is smaller than AIC values. In backward selection, the AIC doesnt seem to change, and also RSS is 0, hence indicating perfect fit. This is also shown by the warning. from backward, removing x3, didn't change the model fit , so we can remove x3 and still get good level of fit. Hence x1 and x2 are active regressors.

```
\#\#Answer 10.5
```

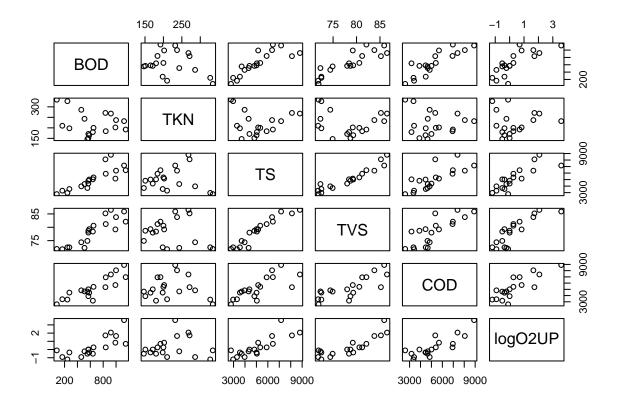
```
colnames(dwaste)
```

```
## [1] "Day" "BOD" "TKN" "TS" "TVS" "COD" "O2UP'
```

plot(dwaste)

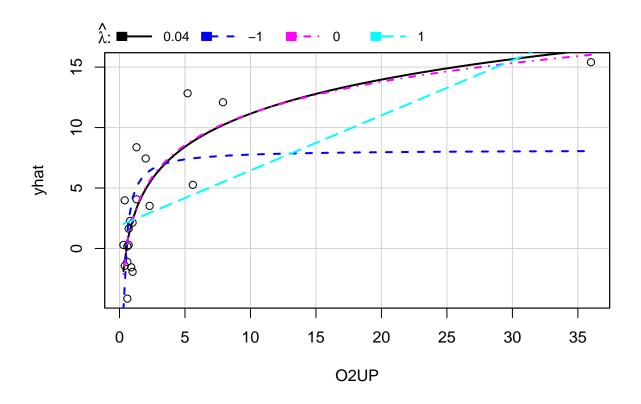


dwaste\$log02UP=log(dwaste\$02UP)
tvs_outlier=min(dwaste\$TVS)
dwaste1<-dwaste%>%filter(TVS!=tvs_outlier)%>%select(!Day&!02UP)
plot(dwaste1)



The very first part of any kind of regression analysis inludes a visual analysis using scatterplot matrix. This step was done for this particular dataset and few trends were identified from the scatterplot matrix of this dataset. The response variable O2UP wrt to other variable had non linear i.e curvy relationship with the other independent variables. This indicated that the response variable needed to undergo a transformation , most likely log transformation as suggested in the question itself. Also from analysing the TVS Scatterplot row and column, we can see a very distinct outlier. This outlier was also removed.

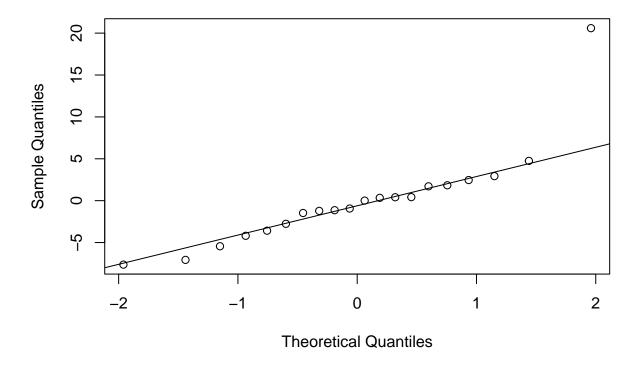
dlm1<-lm(02UP~BOD+TKN+TS+TVS+COD,data=dwaste)
invResPlot(dlm1)</pre>



```
## 1 1 ambda RSS
## 1 0.04467894 157.9096
## 2 -1.0000000 309.5380
## 3 0.00000000 158.4101
## 4 1.0000000 295.9262
```

qqnorm(dlm1\$residuals)
qqline(dlm1\$residuals)

Normal Q-Q Plot



To verify the need of transformation of the response variable , we checked the inverse residual plot of normal mean function without transformation. The Box cox method clearly shows a curved fitted line, hence we can go ahead with a transformed response model fit. Also the qq plot was plotted, which shows an almost linear relation bar one , where one residual is very far away from the line fit.

Next step is to analyse the inclusion of which independent variable will reduce the criterion. We chose the AIC criterion and ran the stepwise model selection process backward and forward

```
dlm2<-lm(log02UP~BOD+TKN+TS+TVS+COD,data=dwaste1)
step(dlm2,scope=~1, direction="backward",test="F")</pre>
```

```
## Start:
          AIC=-14.28
## logO2UP ~ BOD + TKN + TS + TVS + COD
##
##
          Df Sum of Sq
                          RSS
                                  AIC F value Pr(>F)
                                       0.0657 0.80178
## - TS
               0.02406 4.7886 -16.186
## - BOD
           1
               0.03377 4.7983 -16.147
                                       0.0921 0.76628
## - TVS
               0.44702 5.2116 -14.578
                                       1.2197 0.28944
                       4.7646 -14.281
## <none>
  - TKN
           1
               0.53908 5.3036 -14.245
                                       1.4709 0.24679
## - COD
               1.26696 6.0315 -11.801
                                       3.4569 0.08577 .
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Signif. codes:
##
## Step: AIC=-16.19
## logO2UP ~ BOD + TKN + TVS + COD
##
```

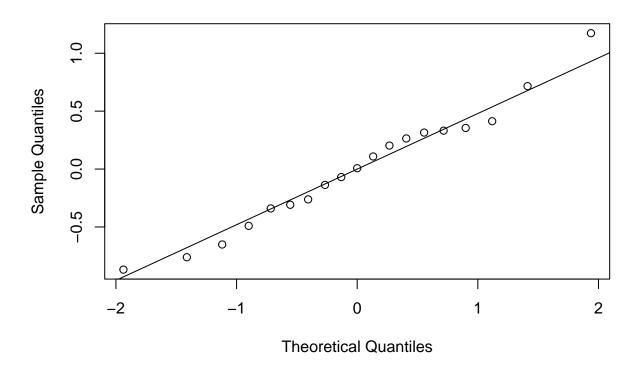
```
Df Sum of Sq
                       RSS AIC F value Pr(>F)
          1 0.02923 4.8178 -18.070 0.0855 0.77431
## - BOD
## <none>
                      4.7886 -16.186
## - TKN
              0.68905 5.4777 -15.632 2.0145 0.17768
          1
## - COD
          1
              1.25863 6.0472 -13.752 3.6797 0.07570 .
## - TVS
             1.95914 6.7478 -11.669 5.7277 0.03127 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=-18.07
## logO2UP ~ TKN + TVS + COD
##
                                AIC F value
##
         Df Sum of Sq
                       RSS
                                              Pr(>F)
## <none>
                      4.8178 -18.070
## - TKN
              0.93971 5.7576 -16.685 2.9257 0.107774
          1
## - COD
          1
            1.62925 6.4471 -14.535 5.0725 0.039717 *
## - TVS
          1 2.79152 7.6094 -11.386 8.6912 0.009972 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Call:
## lm(formula = logO2UP ~ TKN + TVS + COD, data = dwaste1)
## Coefficients:
## (Intercept)
                                   TVS
                                                COD
                       TKN
## -1.244e+01
                 4.176e-03
                              1.318e-01
                                          2.874e-04
dlm3<-lm(log02UP~1,data=dwaste1)</pre>
step(dlm3,scope=~BOD + TKN + TS + TVS + COD, direction="forward",test="F")
## Start: AIC=8.11
## log02UP ~ 1
##
         Df Sum of Sq
                         RSS
                                  AIC F value
                                                 Pr(>F)
##
             18.696 7.5035 -13.6522 42.3585 5.358e-06 ***
## + TVS
          1
## + TS
               18.184 8.0158 -12.3975 38.5652 9.507e-06 ***
          1
## + COD
             18.000 8.1999 -11.9661 37.3178 1.158e-05 ***
         1
             15.601 10.5989 -7.0902 25.0232 0.000109 ***
## + BOD
          1
## <none>
                      26.1999
                              8.1050
## + TKN
                0.151 26.0489
                               9.9952 0.0985 0.757414
         1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=-13.65
## logO2UP ~ TVS
##
##
         Df Sum of Sq
                        RSS
                                AIC F value Pr(>F)
## + COD
             1.74597 5.7576 -16.685 4.8520 0.04262 *
## + TKN
              1.05644 6.4471 -14.535 2.6218 0.12495
          1
                      7.5035 -13.652
## <none>
## + TS
          1 0.25009 7.2534 -12.296 0.5517 0.46840
## + BOD 1 0.09366 7.4099 -11.891 0.2022 0.65896
```

```
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Step: AIC=-16.68
## log02UP \sim TVS + COD
##
##
          Df Sum of Sq
                          RSS
                                   AIC F value Pr(>F)
                                        2.9257 0.1078
## + TKN
               0.93971 4.8178 -18.070
                       5.7576 -16.685
## <none>
## + BOD
           1
               0.27990 5.4777 -15.632
                                        0.7665 0.3951
## + TS
           1
               0.19455 5.5630 -15.338
                                        0.5246 0.4800
##
## Step: AIC=-18.07
## logO2UP ~ TVS + COD + TKN
##
##
          Df Sum of Sq
                          RSS
                                   AIC F value Pr(>F)
                       4.8178 -18.070
## <none>
## + BOD
           1 0.029232 4.7886 -16.186
                                       0.0855 0.7743
           1 0.019526 4.7983 -16.147 0.0570 0.8148
## + TS
##
## Call:
## lm(formula = log02UP \sim TVS + COD + TKN, data = dwaste1)
##
## Coefficients:
## (Intercept)
                        TVS
                                      COD
                                                   TKN
  -1.244e+01
                                2.874e-04
                                             4.176e-03
                  1.318e-01
```

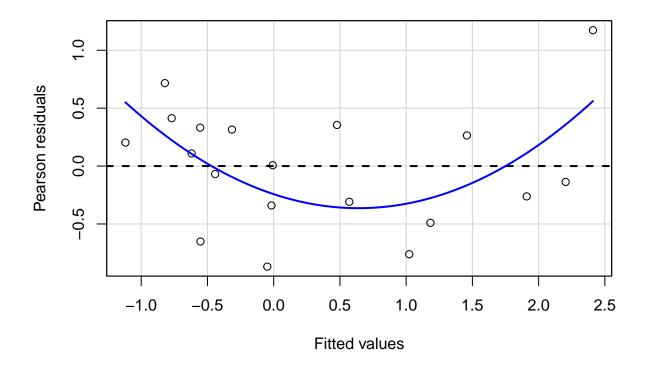
As seen by both the method , TVSL,COD and TXN are the active regressors which reduces the criterion with meaningful change in RSS. Iteratively removing the TS and BOD regressor from backward selection didnt have a significant reduction in the RSS. Hence models were chosen without these two regressors.

```
dlm4<-lm(log02UP ~ TVS + COD + TKN,data=dwaste1)
qqnorm(dlm4$residuals)
qqline(dlm4$residuals)</pre>
```

Normal Q-Q Plot



residualPlot(dlm4)



The mean function with the regressor selected from stepwise selection were chosen and the mean function was computed. The qqplot was plotted to check if the residual follows a straight line, and we can see that they do. The qqplot after the log transform significantly improves the residual plot. Also from the residual plot, we can see that the residuals are normally distributed.

Answer 3

3.a

Since it says that for the fitted model, previous wage is highly significant , we can reject the null hypothesis and we can determine that this regressor explains a lot of variation in response variable. Since gender isnt statistically significant , accepting the null hypothesis is true. I would not be too happy about the selection of model terms because the criterion is not defined. Since there are many other regressor variables, there are chances that some of them may have a positive impact in maximising the criterion in stepwise regression process.

3.b

Since AIC was chosen as a criterion and Gender was not chosen in this , it may be possible that the inclusion of the gender regressor didnt have a significant impact on the AIC criterion. This means that , adding or not adding the gender regressor didnt have much impact on the RSS of the mean function hence it was ignored.

3.c

Since the lasso regression methods adds penalty based on the coefficients of the regressors, hence scaling of regressor has a big effect during lasso regression and thus we see a change. when we scale the regressor, we are essentially changing its coefficient i.e scaling the coefficient. Thus if we divide the regressor by 10, to accommodate the change, the coefficient will increase and thus lasso will add more penalty. And this caused the lasso regression to reject scaled regressor here.

3.d

I would use one of the model selector process to select the regressors for my mean function. I will either choose AIC or BIC as my criterion or loss function. I would choose AIC over BIC because, BIC penalizes for overcomplicated models thus reducing the chances of overfitting. Using either of forward or backward stepwise regression , I would reduce the set of regressors.

Answer 4

4.1

```
N=100
M=60
dataset=matrix( rnorm(N*M,mean=0,sd=1), N, M)
```

4.2

```
out=data.frame(y=runif(100))
```

4.3

```
dataframe=as.data.frame(dataset)
names(dataframe)[-1] <- pasteO('x', 1:(ncol(dataframe)-1))
dataframe$y=out$y
head(dataframe,5)</pre>
```

```
##
             V1
                                   x2
                                             xЗ
                                                                   x5
                       x1
                                                         x4
## 1 -0.90982967
                           0.08744232 -0.4747939 -1.17351798 -0.2915251
                 2.0479712
## 2 1.60156684
                0.5891417 -0.31092167 0.9404758 -0.07024217 -1.1807199
## 3 -0.08429877 -0.2442605 -0.51505710 0.6911132 -0.57311171
    0.03624005 -0.9837655
                           ## 5 -1.93560587
                 1.5978877
                           0.42973468 -0.4919441 -0.84375276
                                                            1.0682855
##
             x6
                       x7
                                  x8
                                            x9
                                                        x10
## 1 -0.75242154 1.48815904 -0.4544319
                                     2.0291114 -0.509496074
## 2 -0.02470664 0.01738339 -0.7646093 0.5511657 -0.367982306 -0.2758185
## 3 0.68141382 1.61644685 -0.9787013 -1.8445017 -0.313757755 -1.5384185
## 4 -0.18208435 0.49002312 0.9928765 -0.1871311
                                               1.592111260 -2.1994586
## 5 0.36098662 0.26728637
                           2.4461087 -1.3767020
                                                0.006426222 -1.2983872
##
           x12
                      x13
                                 x14
                                           x15
                                                      x16
                                                                  x17
```

```
## 1 1.0339403 0.08798275 -1.2444007 0.2954165 -1.6336902 -1.601342835
## 3 1.3653386 0.62274626 -1.6643475 -1.1273456 0.8513610 -0.883233957
## 4 1.4112926 -1.85726887 -0.5030912 0.9241664 0.5556126 -0.633428055
## 5 0.3226505 -0.03119525 -0.2820275 -1.5103147 -2.4664147 0.001226719
           x18
                    x19
                              x20
                                        x21
                                                  x22
                                                            x23
##
                                                                      x24
## 1 2.6076485 0.4514618 0.7304581 0.2213890 -0.3110624 0.2077258 -0.9235910
## 2 1.4566633 0.7233056 -0.3127933 -0.4421995 0.9559966 0.9437798 0.1555026
## 3 -0.3536479 1.1910447 0.1828691 -0.9836475 -0.2594261 -2.2757614 0.1396729
## 4 -0.5646692 0.6058390 0.4536730 -0.1844041 -0.8770827 -0.1300044 -0.8657276
## 5 -0.7883407 0.1537723 1.0114952 -1.1781238 0.6852279 0.9570407 0.9598641
                     x26
                                          x28
                                 x27
                                                       x29
           x25
## 1 0.38086229 -0.8993359 0.473190461 0.2992237 -0.41825434 1.8936123
## 2 -0.02205499 -0.7378982 -0.009927375 -0.2207339 -0.31846566 0.4347553
## 3 0.53124846 0.6846547 0.404095150 0.6824973 -1.22796136 0.4679233
## 4 0.57378326 0.8850458 -1.572524409 1.0141847 1.04506204 -0.2144565
## 5 -2.20155890 -0.5062733 0.221106112 0.4176665 0.03378177 -0.3742102
##
          x31
                     x32
                               x33
                                          x34
                                                     x35
## 1 -0.8459192 1.48163137 0.3031052 1.4363142 -0.79017705 -1.3067816
## 2 -1.0008502 -0.74254349 -0.3180705 -0.1459698 0.76267107 1.8044414
## 3 -1.5687144 -0.08552344 1.3339016 -0.9718666 -0.46951281 -3.6706844
## 4 -0.5540977 -0.32292708 -0.1392774 -1.4278064 -0.09537114 -0.4009300
## 5 0.7665063 1.34905255 0.1790383 -1.3634539 0.08115861 -0.3030683
                                 x39
           x37
                      x38
                                           x40
                                                      x41
## 1 1.22145007 1.3334679 -0.96031193 -1.03658262 0.9689891 0.1830306
## 2 -0.22165288 2.2043696 0.88242949 -0.08685792 0.2770165 -0.3200227
## 3 0.02997449 0.8574277 0.95369303 -0.79844932 0.7532296 -1.5844198
## 4 1.00985706 1.9817584 -0.07922132 0.01084997 -0.7691610 1.3379714
## 5 0.29300327 -0.9335873 -0.35498267 1.73995046 -0.6034248 0.5103530
          x43
                    x44
                              x45
                                        x46
                                                   x47
                                                             x48
## 1 1.6133632 -0.7285868 -1.4482812 0.6685163 -0.08876227 0.3353242 0.38462455
## 2 0.3202847 1.0703749 0.6206867 -1.0232716 0.66250159 0.8667188 -0.02323949
## 3 1.1517151 -0.5349320 -2.2527506 0.1030834 0.71700874 -0.2714872 -0.56365808
## 4 1.0414331 1.6658742 -0.3021074 -0.4078348 0.53085025 1.0252489 -0.07109871
## 5 0.9525218 0.7344886 1.2694758 -0.9254663 -1.05541059 1.1102703 -0.59913868
          x50
                    x51
                             x52
                                         x53
                                                     x54
## 1 -1.2487904 1.4373881 0.8037242 -0.75802818 -0.12519870 2.36287870
## 2 0.7120740 -0.1992734 -0.5001011 0.07492439 -0.03322591 -1.38985418
## 4 -1.5764891 -0.3888780 -0.7140616 -1.93530129 0.69528781 1.70822444
## 5 -0.9330471 -0.5037535 -0.6602660 0.03915814 0.45749674 -1.49967497
           x56
                    x57
                               x58
                                         x59
## 1 -0.4249654 -1.9610324 0.5969617 1.6268132 0.3920372
## 2 -0.2707785 1.4397437 1.2417855 -1.5824184 0.1110635
## 3 -0.7765307 -0.2949970 1.1245339 -1.3670321 0.5744790
## 4 0.3036627 0.1034609 -1.9581678 -0.2846305 0.8664567
## 5 0.6267877 0.8756094 -0.1704365 -0.8606121 0.1407445
```

colnames(dataframe)

```
## [1] "V1" "x1" "x2" "x3" "x4" "x5" "x6" "x7" "x8" "x9" "x10" "x11" ## [13] "x12" "x13" "x14" "x15" "x16" "x17" "x18" "x19" "x20" "x21" "x22" "x23" ## [25] "x24" "x25" "x26" "x27" "x28" "x29" "x30" "x31" "x32" "x33" "x34" "x35" ## [37] "x36" "x37" "x38" "x39" "x40" "x41" "x42" "x42" "x43" "x44" "x45" "x46" "x47"
```

```
## [49] "x48" "x49" "x50" "x51" "x52" "x53" "x54" "x55" "x56" "x57" "x58" "x59" 
## [61] "y"
```

4.4

```
lm1<-lm(y~1,data=dataframe)</pre>
biggest <- formula(lm(y~.,dataframe))</pre>
sub=step(lm1,scope=biggest , direction="forward",test="F")
## Start: AIC=-244.25
## y \sim 1
##
                          RSS
                                   AIC F value
          Df Sum of Sq
               0.64647 7.8761 -250.13
## + x51
                                       8.0438 0.005548 **
               0.45969 8.0629 -247.79
                                        5.5872 0.020065
## + x57
               0.43303 8.0895 -247.46
                                       5.2460 0.024141 *
## + x44
               0.36651 8.1561 -246.64
## + x2
                                       4.4038 0.038430 *
               0.32869 8.1939 -246.18
## + x42
                                       3.9312 0.050198
           1
               0.26604 8.2565 -245.42
## + x4
           1
                                       3.1577 0.078670 .
               0.26521 8.2574 -245.41
## + x52
           1
                                       3.1476 0.079145
## + x27
               0.21627 8.3063 -244.82
                                       2.5517 0.113399
## <none>
                       8.5226 -244.25
## + x47
           1
               0.16093 8.3616 -244.15
                                        1.8861 0.172778
## + x21
               0.14089 8.3817 -243.91
                                        1.6473 0.202353
## + x45
           1
               0.12021 8.4024 -243.67
                                        1.4020 0.239252
## + x6
           1
               0.08820 8.4344 -243.28
                                        1.0248 0.313878
               0.08770 8.4349 -243.28
                                        1.0190 0.315252
## + x34
           1
## + x25
               0.07776 8.4448 -243.16
                                        0.9024 0.344464
               0.07162 8.4509 -243.09
                                        0.8306 0.364341
## + x7
           1
               0.06778 8.4548 -243.04
                                        0.7856 0.377589
## + x3
## + x10
               0.05996 8.4626 -242.95
                                        0.6943 0.406719
               0.05536 8.4672 -242.90
                                        0.6408 0.425362
## + V1
               0.05438 8.4682 -242.88
                                        0.6293 0.429518
## + x50
           1
## + x8
           1
               0.05318 8.4694 -242.87
                                        0.6154 0.434668
## + x5
               0.05243 8.4701 -242.86
                                        0.6066 0.437933
           1
## + x29
           1
               0.05038 8.4722 -242.84
                                        0.5827 0.447087
               0.04470 8.4779 -242.77
## + x18
           1
                                        0.5167 0.473969
## + x22
           1
               0.04145 8.4811 -242.73
                                        0.4789 0.490556
## + x17
               0.03793 8.4846 -242.69
                                        0.4381 0.509601
## + x1
               0.03710 8.4855 -242.68
                                        0.4284 0.514298
           1
               0.03260 8.4900 -242.63
## + x24
           1
                                        0.3763 0.541015
## + x11
               0.03223 8.4903 -242.62
                                        0.3720 0.543311
           1
## + x9
               0.03196 8.4906 -242.62
                                        0.3689 0.545002
               0.02984 8.4927 -242.60
                                        0.3443 0.558711
## + x13
           1
## + x37
               0.02690 8.4957 -242.56
                                        0.3103 0.578772
               0.02469 8.4979 -242.53
## + x55
                                        0.2848 0.594801
## + x35
               0.02407 8.4985 -242.53
                                        0.2776 0.599481
               0.02352 8.4990 -242.52
                                       0.2712 0.603693
## + x23
           1
## + x32
               0.02129 8.5013 -242.50
                                        0.2455 0.621389
           1
               0.02123 8.5013 -242.50
## + x53
           1
                                        0.2447 0.621919
               0.01993 8.5026 -242.48
## + x54
                                       0.2298 0.632775
               0.01956 8.5030 -242.47 0.2255 0.635974
## + x40
```

```
## + x16
              0.01922 8.5034 -242.47 0.2215 0.638939
## + x59
              0.01737 8.5052 -242.45 0.2002 0.655571
          1
              0.01692 8.5057 -242.44 0.1949 0.659812
## + x12
              0.01588 8.5067 -242.43 0.1830 0.669788
## + x56
          1
## + x33
              0.01292 8.5096 -242.40 0.1488 0.700478
## + x20
              0.01278 8.5098 -242.40 0.1472 0.702097
## + x48
              0.01222 8.5103 -242.39 0.1407 0.708368
          1
## + x43
              0.01168 8.5109 -242.38 0.1345 0.714562
          1
## + x38
          1
              0.01090 8.5117 -242.37 0.1255 0.723865
              0.01048 8.5121 -242.37 0.1207 0.729055
## + x31
          1
## + x14
              0.00872 8.5138 -242.35 0.1004 0.752031
          1
              0.00689 8.5157 -242.33 0.0793 0.778828
## + x19
          1
## + x39
              0.00660 8.5160 -242.32 0.0760 0.783437
          1
## + x58
              0.00577 8.5168 -242.31 0.0663 0.797281
## + x15
              0.00474 8.5178 -242.30 0.0545 0.815925
          1
## + x36
          1
              0.00147 8.5211 -242.26 0.0169 0.896732
## + x49
              0.00109 8.5215 -242.26 0.0125 0.911233
          1
## + x26
              0.00108 8.5215 -242.26 0.0124 0.911454
              0.00106 8.5215 -242.26 0.0122 0.912366
## + x41
          1
## + x30
          1
              0.00077 8.5218 -242.25
                                      0.0088 0.925251
## + x28
          1
              0.00066 8.5219 -242.25 0.0076 0.930594
## + x46
              0.00021 8.5224 -242.25 0.0024 0.961109
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=-250.13
## y \sim x51
##
##
                         RSS
                                 AIC F value Pr(>F)
          Df Sum of Sq
## + x44
              0.44711 7.4290 -253.98 5.8379 0.01756 *
          1
## + x57
           1
              0.38869 7.4874 -253.19
                                      5.0355 0.02711 *
## + x2
          1
              0.26812 7.6080 -251.60
                                     3.4185 0.06752 .
## + x45
              0.25924 7.6169 -251.48 3.3014 0.07231 .
## + x52
              0.24314 7.6330 -251.27 3.0898 0.08194 .
          1
## + x42
              0.21684 7.6593 -250.93 2.7462 0.10072
## + x27
              0.20733 7.6688 -250.80 2.6225 0.10861
          1
## + x21
              0.17124 7.7049 -250.33 2.1558 0.14527
## <none>
                       7.8761 -250.13
## + x4
              0.11151 7.7646 -249.56
                                     1.3930 0.24079
          1
## + x22
              0.09926 7.7768 -249.40
                                      1.2381 0.26859
           1
## + x47
          1
              0.09869 7.7774 -249.40
                                      1.2308 0.26999
## + x17
              0.08307 7.7930 -249.19
                                      1.0340 0.31175
          1
## + x32
          1
              0.08154 7.7946 -249.17
                                      1.0148 0.31627
## + x6
              0.07177 7.8043 -249.05 0.8920 0.34729
          1
## + x3
          1
              0.05926 7.8168 -248.89 0.7353 0.39328
## + x53
              0.04876 7.8273 -248.75
                                      0.6042 0.43887
          1
## + x1
          1
              0.04851 7.8276 -248.75
                                      0.6011 0.44005
## + x29
           1
              0.04616 7.8299 -248.72 0.5719 0.45134
## + x34
              0.04246 7.8336 -248.67
                                      0.5257 0.47016
           1
## + x12
          1
              0.03801 7.8381 -248.62 0.4704 0.49443
## + x5
              0.03773 7.8384 -248.61 0.4670 0.49602
          1
## + x8
              0.03634 7.8398 -248.60 0.4496 0.50411
## + x7
          1
              0.03630 7.8398 -248.60 0.4492 0.50431
## + x11
          1
              0.03430 7.8418 -248.57 0.4242 0.51637
```

```
## + x19
              0.02817 7.8479 -248.49 0.3481 0.55654
## + x25
              0.02502 7.8511 -248.45 0.3092 0.57948
          1
## + x43
              0.02398 7.8521 -248.44 0.2963 0.58747
              0.02259 7.8535 -248.42 0.2791 0.59852
## + x28
## + x48
              0.02096 7.8551 -248.40 0.2588 0.61208
              0.02082 7.8553 -248.40 0.2571 0.61329
## + x13
              0.01790 7.8582 -248.36 0.2210 0.63934
## + x46
## + x36
              0.01769 7.8584 -248.36 0.2184 0.64131
          1
              0.01612 7.8600 -248.34 0.1989 0.65657
## + x9
          1
              0.01518 7.8609 -248.33 0.1873 0.66612
## + x26
          1
## + V1
              0.01506 7.8610 -248.32 0.1858 0.66738
          1
## + x50
              0.01435 7.8618 -248.32 0.1771 0.67484
          1
## + x37
              0.01394 7.8622 -248.31 0.1720 0.67925
          1
## + x40
              0.01227 7.8638 -248.29 0.1513 0.69813
## + x24
              0.01090 7.8652 -248.27 0.1344 0.71469
          1
## + x20
          1
              0.01068 7.8654 -248.27 0.1317 0.71745
## + x35
              0.01043 7.8657 -248.27
                                      0.1286 0.72067
          1
## + x31
              0.01034 7.8658 -248.26 0.1275 0.72181
## + x59
              0.00912 7.8670 -248.25 0.1124 0.73816
## + x33
              0.00838 7.8677 -248.24 0.1033 0.74860
## + x58
              0.00814 7.8680 -248.24 0.1004 0.75204
## + x30
              0.00758 7.8685 -248.23 0.0935 0.76046
## + x18
              0.00727 7.8688 -248.23 0.0896 0.76535
          1
## + x23
              0.00411 7.8720 -248.19 0.0506 0.82252
          1
              0.00356 7.8725 -248.18 0.0438 0.83461
## + x10
          1
## + x56
          1
              0.00285 7.8733 -248.17 0.0351 0.85176
## + x16
              0.00105 7.8751 -248.15 0.0130 0.90961
          1
## + x15
          1
              0.00103 7.8751 -248.15 0.0127 0.91038
## + x14
              0.00094 7.8752 -248.15 0.0115 0.91471
## + x55
              0.00046 7.8756 -248.14 0.0056 0.94034
          1
## + x41
          1
              0.00040 7.8757 -248.14 0.0050 0.94403
## + x49
          1
              0.00037 7.8757 -248.14 0.0046 0.94612
## + x39
              0.00026 7.8758 -248.14 0.0032 0.95494
              0.00001 7.8761 -248.13 0.0001 0.99284
## + x54
          1
## + x38
              0.00000 7.8761 -248.13 0.0000 0.99832
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=-253.98
## y \sim x51 + x44
##
##
         Df Sum of Sq
                        RSS
                                AIC F value Pr(>F)
              0.34619 7.0828 -256.75 4.6923 0.03277 *
## + x57
          1
## + x45
              0.27993 7.1491 -255.82 3.7590 0.05546 .
              0.25348 7.1755 -255.45 3.3913 0.06863 .
## + x52
          1
## + x42
              0.24218 7.1868 -255.29 3.2350 0.07522 .
          1
## + x4
          1
              0.20687 7.2221 -254.80 2.7497 0.10053
              0.17622 7.2528 -254.38 2.3325 0.12999
## + x21
## + x2
              0.15391 7.2751 -254.07 2.0309 0.15737
          1
## + x22
              0.14959 7.2794 -254.01 1.9727 0.16338
           1
                      7.4290 -253.98
## <none>
## + x6
              0.13173 7.2973 -253.77 1.7330 0.19116
## + x27
          1
              0.12706 7.3019 -253.70 1.6704 0.19930
              0.10134 7.3277 -253.35 1.3277 0.25208
## + x17
```

```
## + x32
              0.07144 7.3576 -252.94 0.9321 0.33673
## + x47
              0.05836 7.3706 -252.77
                                      0.7601 0.38546
          1
## + x28
              0.05677 7.3722 -252.75 0.7393 0.39203
              0.05022 7.3788 -252.66 0.6534 0.42089
## + x11
           1
## + x1
              0.04951 7.3795 -252.65
                                      0.6441 0.42421
## + x7
              0.04309 7.3859 -252.56 0.5600 0.45608
## + x53
              0.03963 7.3894 -252.51 0.5149 0.47478
          1
## + x29
              0.03896 7.3900 -252.50 0.5062 0.47853
          1
               0.03881 7.3902 -252.50
## + x25
          1
                                      0.5041 0.47941
## + x12
          1
              0.03429 7.3947 -252.44
                                      0.4451 0.50627
## + x8
              0.03230 7.3967 -252.41
                                      0.4192 0.51890
          1
              0.02822 7.4008 -252.36
## + x5
           1
                                      0.3661 0.54656
## + x3
              0.02745 7.4016 -252.35
                                      0.3560 0.55214
          1
## + x41
              0.02377 7.4052 -252.30 0.3082 0.58010
## + x19
              0.01926 7.4097 -252.24 0.2495 0.61855
           1
## + x40
           1
              0.01893 7.4101 -252.23
                                       0.2453 0.62156
## + V1
              0.01868 7.4103 -252.23 0.2420 0.62391
           1
## + x30
               0.01676 7.4122 -252.20
                                      0.2171 0.64230
## + x10
              0.01653 7.4125 -252.20 0.2141 0.64460
           1
## + x9
              0.01535 7.4136 -252.19 0.1987 0.65674
              0.01295 7.4160 -252.15 0.1676 0.68315
## + x36
## + x50
              0.01217 7.4168 -252.14 0.1576 0.69229
## + x48
              0.01191 7.4171 -252.14 0.1541 0.69552
          1
               0.01081 7.4182 -252.12 0.1400 0.70915
## + x16
          1
              0.00948 7.4195 -252.11 0.1226 0.72698
## + x23
          1
## + x34
          1
              0.00887 7.4201 -252.10 0.1148 0.73552
## + x15
              0.00887 7.4201 -252.10 0.1147 0.73560
          1
              0.00848 7.4205 -252.09 0.1097 0.74116
## + x55
          1
## + x37
              0.00735 7.4216 -252.08 0.0951 0.75847
## + x43
              0.00634 7.4227 -252.06 0.0819 0.77531
          1
## + x56
          1
              0.00628 7.4227 -252.06 0.0813 0.77619
## + x18
          1
               0.00593 7.4231 -252.06 0.0767 0.78242
               0.00413 7.4249 -252.03 0.0534 0.81776
## + x59
## + x58
              0.00321 7.4258 -252.02 0.0414 0.83913
           1
## + x13
               0.00310 7.4259 -252.02 0.0401 0.84168
          1
## + x38
              0.00216 7.4268 -252.01 0.0280 0.86752
          1
## + x26
              0.00183 7.4272 -252.00 0.0236 0.87825
## + x35
              0.00157 7.4274 -252.00 0.0203 0.88694
          1
## + x14
              0.00121 7.4278 -251.99
                                      0.0156 0.90075
          1
## + x46
              0.00118 7.4278 -251.99 0.0152 0.90206
          1
              0.00117 7.4278 -251.99
## + x54
                                      0.0152 0.90227
## + x31
              0.00085 7.4281 -251.99 0.0110 0.91654
          1
              0.00063 7.4284 -251.99
## + x33
          1
                                       0.0082 0.92823
## + x49
              0.00038 7.4286 -251.98 0.0050 0.94405
          1
              0.00007 7.4289 -251.98 0.0009 0.97660
## + x20
          1
              0.00004 7.4290 -251.98 0.0005 0.98155
## + x39
          1
## + x24
          1
              0.00003 7.4290 -251.98 0.0004 0.98366
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Step: AIC=-256.75
## y \sim x51 + x44 + x57
##
##
         Df Sum of Sq
                          RSS
                                 AIC F value Pr(>F)
```

```
## + x42
               0.34330 6.7395 -259.72 4.8391 0.03025 *
           1
## + x52
               0.19609 6.8867 -257.56 2.7050 0.10334
           1
               0.18916 6.8936 -257.46 2.6068 0.10973
## + x21
               0.16338 6.9194 -257.08 2.2431 0.13753
## + x4
           1
## + x45
           1
               0.15563 6.9272 -256.97
                                       2.1344 0.14733
               0.15041 6.9324 -256.90 2.0612 0.15438
## + x6
           1
## + x17
               0.14199 6.9408 -256.77
                                       1.9434 0.16655
## <none>
                       7.0828 -256.75
## + x28
               0.09127 6.9915 -256.05
                                       1.2402 0.26824
           1
## + x22
           1
               0.09044 6.9924 -256.04
                                       1.2287 0.27046
## + x3
               0.08371 6.9991 -255.94
                                       1.1362 0.28917
           1
## + x2
               0.08076 7.0020 -255.90
                                       1.0957 0.29788
           1
## + x27
               0.07529 7.0075 -255.82
                                       1.0208 0.31491
           1
## + x12
               0.07415 7.0087 -255.80
                                      1.0051 0.31862
## + x29
               0.07213 7.0107 -255.77
                                       0.9775 0.32534
           1
## + x32
           1
               0.06562 7.0172 -255.68
                                       0.8884 0.34829
## + x11
               0.05152 7.0313 -255.48
                                       0.6961 0.40620
           1
## + x47
               0.04999 7.0328 -255.46
                                       0.6753 0.41327
                                       0.6647 0.41693
## + x53
               0.04922 7.0336 -255.45
           1
## + x10
           1
               0.04734 7.0355 -255.42
                                       0.6392 0.42601
               0.03853 7.0443 -255.30 0.5196 0.47277
## + V1
           1
## + x25
               0.03842 7.0444 -255.29
                                      0.5181 0.47343
## + x15
               0.03823 7.0446 -255.29
                                       0.5156 0.47450
           1
               0.03758 7.0452 -255.28
## + x7
           1
                                       0.5067 0.47832
               0.03197 7.0508 -255.20 0.4307 0.51324
## + x16
           1
## + x40
           1
               0.02875 7.0541 -255.16 0.3872 0.53526
## + x5
               0.02731 7.0555 -255.14
                                       0.3677 0.54569
           1
## + x26
           1
               0.02685 7.0560 -255.13 0.3615 0.54908
## + x23
               0.02660 7.0562 -255.13 0.3581 0.55098
           1
## + x19
               0.02524 7.0576 -255.11 0.3397 0.56138
           1
## + x1
           1
               0.01936 7.0634 -255.02 0.2603 0.61108
## + x8
           1
               0.01613 7.0667 -254.98 0.2169 0.64251
               0.01562 7.0672 -254.97
## + x50
                                       0.2100 0.64785
               0.01363 7.0692 -254.94 0.1831 0.66967
## + x46
           1
## + x43
               0.01062 7.0722 -254.90
                                       0.1427 0.70648
           1
## + x36
               0.01014 7.0727 -254.89 0.1362 0.71293
           1
## + x34
               0.01008 7.0727 -254.89 0.1353 0.71377
## + x41
               0.00999 7.0728 -254.89 0.1342 0.71495
           1
## + x49
               0.00964 7.0732 -254.89
                                       0.1295 0.71974
           1
## + x30
               0.00706 7.0757 -254.85
                                      0.0948 0.75878
           1
               0.00684 7.0760 -254.85
## + x38
           1
                                       0.0918 0.76256
## + x31
               0.00682 7.0760 -254.85
                                       0.0915 0.76289
           1
## + x18
           1
               0.00580 7.0770 -254.83
                                       0.0779 0.78075
## + x59
               0.00559 7.0772 -254.83 0.0751 0.78468
           1
               0.00460 7.0782 -254.81 0.0617 0.80429
## + x56
           1
               0.00404 7.0788 -254.81
## + x37
                                       0.0542 0.81633
           1
## + x55
           1
               0.00378 7.0790 -254.80
                                       0.0507 0.82227
               0.00340 7.0794 -254.80
## + x35
           1
                                       0.0456 0.83130
## + x9
               0.00276 7.0800 -254.79
                                       0.0370 0.84794
           1
## + x58
               0.00216 7.0806 -254.78
                                       0.0290 0.86506
           1
## + x20
               0.00120 7.0816 -254.77
                                       0.0161 0.89918
           1
## + x39
               0.00103 7.0818 -254.76 0.0139 0.90649
## + x14
               0.00093 7.0819 -254.76 0.0125 0.91126
           1
## + x48
           1
               0.00063 7.0822 -254.76 0.0084 0.92721
```

```
## + x54
              0.00036 7.0824 -254.75 0.0048 0.94485
          1
## + x33
              0.00007 7.0827 -254.75 0.0009 0.97625
          1
## + x24
              0.00003 7.0828 -254.75 0.0004 0.98380
              0.00002 7.0828 -254.75 0.0003 0.98730
## + x13
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Step: AIC=-259.72
## y \sim x51 + x44 + x57 + x42
##
         Df Sum of Sq
                         RSS
                                 AIC F value Pr(>F)
          1 0.203445 6.5361 -260.78 2.9259 0.09047
## + x52
## + x17
          1 0.160293 6.5792 -260.13 2.2902 0.13355
## + x28
          1 0.143211 6.5963 -259.87 2.0408 0.15644
## + x6
          1 0.142903 6.5966 -259.86 2.0363 0.15689
## + x4
          1 0.141415 6.5981 -259.84 2.0147 0.15909
                      6.7395 -259.72
## <none>
## + x53
          1 0.121130 6.6184 -259.53 1.7204 0.19284
          1 0.103470 6.6360 -259.27 1.4657 0.22907
## + x21
## + x22
          1 0.102868 6.6366 -259.26
                                     1.4570 0.23044
## + x45
          1 0.099113 6.6404 -259.20 1.4030 0.23920
## + x2
          1 0.086627 6.6529 -259.01 1.2240 0.27141
## + x12
          1 0.085051 6.6545 -258.99 1.2014 0.27584
          1 0.068331 6.6712 -258.74 0.9628 0.32900
## + x3
## + x16
          1 0.061909 6.6776 -258.64 0.8715 0.35294
## + x29
          1 0.061805 6.6777 -258.64 0.8700 0.35334
          1 0.058673 6.6808 -258.59 0.8255 0.36589
## + x11
## + x8
          1 0.050582 6.6889 -258.47 0.7108 0.40131
## + x27
          1 0.049652 6.6899 -258.46 0.6977 0.40569
## + x5
          1 0.044351 6.6952 -258.38 0.6227 0.43204
## + x15
          1 0.042019 6.6975 -258.34 0.5897 0.44444
## + x32
          1 0.035272 6.7042 -258.24 0.4945 0.48364
## + x23
          1 0.032868 6.7066 -258.21 0.4607 0.49898
          1 0.025534 6.7140 -258.10 0.3575 0.55134
## + x40
## + x25
          1 0.020738 6.7188 -258.03 0.2901 0.59141
## + x38
          1 0.020492 6.7190 -258.02 0.2867 0.59362
## + x10
          1 0.020207 6.7193 -258.02 0.2827 0.59620
## + x58
          1 0.019314 6.7202 -258.00 0.2702 0.60445
## + x31
          1 0.016328 6.7232 -257.96 0.2283 0.63390
## + x47
          1 0.015480 6.7240 -257.95 0.2164 0.64286
          1 0.015196 6.7243 -257.94 0.2124 0.64593
## + x1
          1 0.013745 6.7258 -257.92 0.1921 0.66218
## + x55
## + x46
          1 0.013133 6.7264 -257.91 0.1835 0.66933
## + x49
          1 0.012632 6.7269 -257.91 0.1765 0.67534
## + V1
          1 0.011600 6.7279 -257.89 0.1621 0.68816
## + x30
          1 0.010300 6.7292 -257.87 0.1439 0.70531
## + x19
          1 0.010189 6.7293 -257.87 0.1423 0.70683
          1 0.010135 6.7294 -257.87 0.1416 0.70757
## + x54
## + x41
          1 0.008099 6.7314 -257.84 0.1131 0.73740
## + x20
          1 0.006749 6.7328 -257.82 0.0942 0.75955
          1 0.006572 6.7329 -257.82 0.0917 0.76263
## + x18
## + x13
          1 0.005563 6.7339 -257.80 0.0776 0.78112
          1 0.005500 6.7340 -257.80 0.0768 0.78233
## + x7
## + x26
          1 0.004619 6.7349 -257.79 0.0645 0.80013
```

```
## + x37
          1 0.003770 6.7357 -257.77 0.0526 0.81908
## + x43
          1 0.003290 6.7362 -257.77 0.0459 0.83080
## + x50
          1 0.002887 6.7366 -257.76 0.0403 0.84137
## + x59
          1 0.002640 6.7369 -257.76 0.0368 0.84821
## + x35
          1 0.002637 6.7369 -257.76 0.0368 0.84829
## + x34
          1 0.002446 6.7371 -257.75 0.0341 0.85382
## + x39
          1 0.001489 6.7380 -257.74 0.0208 0.88569
## + x14
          1 0.001013 6.7385 -257.73 0.0141 0.90561
          1 0.000843 6.7387 -257.73 0.0118 0.91387
## + x24
## + x56
          1 0.000753 6.7388 -257.73 0.0105 0.91856
## + x33
          1 0.000526 6.7390 -257.73 0.0073 0.93193
          1 0.000370 6.7391 -257.72 0.0052 0.94289
## + x48
## + x36
          1 0.000322 6.7392 -257.72 0.0045 0.94674
## + x9
          1 0.000014 6.7395 -257.72 0.0002 0.98907
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=-260.78
## y \sim x51 + x44 + x57 + x42 + x52
##
##
         Df Sum of Sq
                         RSS
                                 AIC F value Pr(>F)
          1 0.157741 6.3783 -261.23 2.3000 0.1328
## + x6
          1 0.142304 6.3938 -260.99 2.0699 0.1536
## + x17
                      6.5361 -260.78
## <none>
## + x28
          1 0.122795 6.4133 -260.68 1.7807 0.1853
## + x2
          1 0.119891 6.4162 -260.63 1.7378 0.1907
## + x45
          1 0.096058 6.4400 -260.26 1.3872 0.2419
## + x21
          1 0.086115 6.4499 -260.11 1.2417 0.2680
## + x4
          1 0.081568 6.4545 -260.04 1.1753 0.2811
## + x16
         1 0.072441 6.4636 -259.90 1.0423 0.3099
## + x53
          1 0.070075 6.4660 -259.86
                                     1.0079 0.3180
## + x22
          1 0.068411 6.4677 -259.84 0.9837 0.3239
## + x12
          1 0.064586 6.4715 -259.78 0.9282 0.3378
## + x27
          1 0.054724 6.4813 -259.62 0.7852 0.3778
## + x11
          1 0.050773 6.4853 -259.56
                                     0.7281 0.3957
## + x40
          1 0.048000 6.4881 -259.52 0.6880 0.4090
## + x15
          1 0.047706 6.4884 -259.52 0.6838 0.4104
## + x29
          1 0.037277 6.4988 -259.36 0.5334 0.4670
## + x5
          1 0.033142 6.5029 -259.29 0.4740 0.4929
## + x30
          1 0.028953 6.5071 -259.23 0.4138 0.5216
          1 0.026608 6.5095 -259.19 0.3801 0.5390
## + x23
## + x3
          1 0.024065 6.5120 -259.15 0.3437 0.5591
## + x46
          1 0.022070 6.5140 -259.12 0.3151 0.5759
## + x8
          1 0.021848 6.5142 -259.12 0.3119 0.5779
## + x31
          1 0.018546 6.5175 -259.07 0.2646 0.6082
## + x38
          1 0.016895 6.5192 -259.04 0.2410 0.6246
## + x1
          1 0.016553 6.5195 -259.04 0.2361 0.6282
          1 0.016194 6.5199 -259.03 0.2310 0.6319
## + x47
## + x25
          1 0.015903 6.5202 -259.03 0.2268 0.6350
## + V1
            0.013125 6.5229 -258.99 0.1871 0.6663
          1
## + x18
          1 0.010883 6.5252 -258.95 0.1551 0.6946
## + x20
          1 0.009840 6.5262 -258.93 0.1402 0.7089
## + x10
          1 0.007313 6.5287 -258.89 0.1042 0.7476
## + x37
          1 0.006663 6.5294 -258.89 0.0949 0.7587
```

```
## + x35
          1 0.006400 6.5297 -258.88 0.0912 0.7634
## + x7
          1 0.006093 6.5300 -258.88 0.0868 0.7690
## + x14
          1 0.005977 6.5301 -258.88 0.0851 0.7711
          1 0.005023 6.5310 -258.86 0.0715 0.7897
## + x59
## + x49
          1 0.005001 6.5311 -258.86
                                     0.0712 0.7902
## + x36
          1 0.004680 6.5314 -258.86 0.0666 0.7969
          1 0.004421 6.5316 -258.85 0.0630 0.8024
## + x56
## + x54
          1 0.003995 6.5321 -258.85 0.0569 0.8120
          1 0.002535 6.5335 -258.82 0.0361 0.8498
## + x24
## + x58
          1 0.002381 6.5337 -258.82 0.0339 0.8543
## + x55
          1 0.002344 6.5337 -258.82 0.0334 0.8555
## + x39
          1 0.001891 6.5342 -258.81 0.0269 0.8700
## + x32
          1 0.001850 6.5342 -258.81 0.0263 0.8714
## + x41
          1 0.001626 6.5344 -258.81 0.0231 0.8794
## + x43
          1 0.001160 6.5349 -258.80 0.0165 0.8980
## + x33
          1 0.001108 6.5350 -258.80 0.0158 0.9003
## + x19
          1 0.001107 6.5350 -258.80 0.0158 0.9004
## + x13
          1 0.001017 6.5350 -258.80 0.0145 0.9045
## + x34
          1 0.000789 6.5353 -258.80 0.0112 0.9158
## + x26
          1 0.000781 6.5353 -258.80 0.0111 0.9162
## + x48
          1 0.000591 6.5355 -258.79 0.0084 0.9271
## + x50
          1 0.000030 6.5360 -258.78 0.0004 0.9835
## + x9
          1 0.000021 6.5360 -258.78 0.0003 0.9864
##
## Step: AIC=-261.23
## y \sim x51 + x44 + x57 + x42 + x52 + x6
##
         Df Sum of Sq
##
                         RSS
                                 AIC F value Pr(>F)
## + x17
          1 0.224989 6.1533 -262.82 3.3639 0.06987 .
## + x2
          1 0.152275 6.2260 -261.64 2.2501 0.13703
## + x45
          1 0.137269 6.2411 -261.40 2.0235 0.15826
## + x28
          1 0.133589 6.2447 -261.34 1.9681 0.16402
## <none>
                      6.3783 -261.23
## + x21
          1 0.107817 6.2705 -260.93 1.5819 0.21167
## + x16
          1 0.088416 6.2899 -260.62
                                     1.2932 0.25841
## + x4
          1 0.071962 6.3064 -260.36 1.0498 0.30824
## + x12
          1 0.065084 6.3132 -260.25 0.9484 0.33267
## + x22
          1 0.063828 6.3145 -260.23 0.9299 0.33740
## + x11
          1 0.058584 6.3197 -260.15
                                     0.8528 0.35817
## + x53
          1 0.057810 6.3205 -260.14 0.8415 0.36138
          1 0.052429 6.3259 -260.05 0.7625 0.38482
## + x15
## + x29
          1 0.051552 6.3268 -260.04 0.7496 0.38884
          1 0.046694 6.3316 -259.96 0.6785 0.41224
## + x23
## + x5
          1 0.040861 6.3375 -259.87 0.5932 0.44317
          1 0.039838 6.3385 -259.85 0.5782 0.44895
## + x27
## + x46
          1 0.031343 6.3470 -259.72 0.4543 0.50198
## + x3
          1 0.024816 6.3535 -259.62 0.3593 0.55035
## + x30
          1 0.024087 6.3542 -259.61 0.3487 0.55627
## + x43
          1 0.022119 6.3562 -259.57
                                     0.3201 0.57290
## + x25
          1 0.020801 6.3575 -259.55 0.3010 0.58458
## + x40
          1 0.019598 6.3587 -259.53 0.2836 0.59567
          1 0.017944 6.3604 -259.51 0.2596 0.61165
## + x59
## + x38
          1 0.017040 6.3613 -259.49 0.2464 0.62077
## + x20
          1 0.014154 6.3642 -259.45 0.2046 0.65209
```

```
## + x8
          1 0.013671 6.3646 -259.44 0.1976 0.65770
## + x37
          1 0.013606 6.3647 -259.44 0.1967 0.65846
## + x47
          1 0.011726 6.3666 -259.41 0.1694 0.68157
## + x54
          1 0.011452 6.3669 -259.41 0.1655 0.68510
## + x14
          1 0.010850 6.3675 -259.40 0.1568 0.69307
## + x36
          1 0.008690 6.3696 -259.36 0.1255 0.72394
          1 0.005262 6.3731 -259.31 0.0760 0.78347
## + x33
## + x1
          1 0.005123 6.3732 -259.31 0.0740 0.78628
          1 0.005008 6.3733 -259.31 0.0723 0.78863
## + x9
## + V1
          1 0.004875 6.3734 -259.30 0.0704 0.79138
## + x31
          1 0.004275 6.3740 -259.29 0.0617 0.80438
          1 0.003982 6.3743 -259.29 0.0575 0.81107
## + x10
## + x50
          1 0.003200 6.3751 -259.28 0.0462 0.83032
## + x41
          1 0.003179 6.3751 -259.28 0.0459 0.83088
## + x35
          1 0.002760 6.3756 -259.27 0.0398 0.84227
## + x49
          1 0.002392 6.3759 -259.26 0.0345 0.85302
## + x39
          1 0.002302 6.3760 -259.26 0.0332 0.85580
## + x34
          1 0.002217 6.3761 -259.26 0.0320 0.85845
          1 0.001487 6.3768 -259.25 0.0215 0.88388
## + x24
## + x56
          1 0.001368 6.3770 -259.25
                                     0.0197 0.88858
          1 0.000592 6.3777 -259.24 0.0085 0.92660
## + x19
## + x26
          1 0.000516 6.3778 -259.24 0.0074 0.93146
## + x32
          1 0.000303 6.3780 -259.23 0.0044 0.94744
## + x58
          1 0.000222 6.3781 -259.23 0.0032 0.95499
          1 0.000185 6.3781 -259.23 0.0027 0.95890
## + x13
## + x7
          1 0.000149 6.3782 -259.23 0.0022 0.96310
## + x48
          1 0.000048 6.3783 -259.23 0.0007 0.97902
          1 0.000028 6.3783 -259.23 0.0004 0.98393
## + x55
## + x18
          1 0.000016 6.3783 -259.23 0.0002 0.98780
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=-262.82
## y \sim x51 + x44 + x57 + x42 + x52 + x6 + x17
##
         Df Sum of Sq
                         RSS
##
                                AIC F value Pr(>F)
## + x28
          1 0.157774 5.9956 -263.42 2.3947 0.1252
## + x45
          1 0.145276 6.0081 -263.21 2.2004 0.1414
## + x21
          1 0.136843 6.0165 -263.07 2.0698 0.1537
                      6.1533 -262.82
## <none>
          1 0.113302 6.0400 -262.68 1.7070 0.1947
## + x4
## + x2
          1 0.107027 6.0463 -262.57 1.6108 0.2076
## + x27
          1 0.080887 6.0724 -262.14 1.2121 0.2738
## + x16
          1 0.074570 6.0788 -262.04 1.1163 0.2935
## + x15
          1 0.063292 6.0900 -261.85 0.9457 0.3334
## + x11
          1 0.048731 6.1046 -261.61 0.7264 0.3963
## + x53
          1 0.041452 6.1119 -261.49 0.6172 0.4341
## + x29
          1 0.038283 6.1150 -261.44 0.5697 0.4523
## + x22
          1 0.037603 6.1157 -261.43 0.5595 0.4564
## + x5
          1 0.031700 6.1216 -261.33 0.4712 0.4942
## + x30
          1 0.029654 6.1237 -261.30 0.4407 0.5085
## + x12
          1 0.029567 6.1238 -261.30 0.4394 0.5091
## + x23
          1 0.029053 6.1243 -261.29 0.4317 0.5128
## + x43
          1 0.025565 6.1278 -261.23 0.3796 0.5393
```

```
## + x3
          1 0.024356 6.1290 -261.21 0.3616 0.5491
## + x8
          1 0.024290 6.1290 -261.21 0.3606 0.5496
## + x59
          1 0.022763 6.1306 -261.19 0.3379 0.5625
          1 0.019796 6.1335 -261.14 0.2937 0.5892
## + x31
## + x55
          1 0.019734 6.1336 -261.14 0.2928 0.5898
## + x38
          1 0.019282 6.1340 -261.13 0.2861 0.5941
## + x46
          1 0.017213 6.1361 -261.10 0.2553 0.6146
## + x40
          1 0.015654 6.1377 -261.07 0.2321 0.6311
## + x20
          1 0.014444 6.1389 -261.05 0.2141 0.6447
## + x1
          1 0.012382 6.1409 -261.02 0.1835 0.6694
## + x26
          1 0.011503 6.1418 -261.00 0.1704 0.6807
## + x37
          1 0.009377 6.1440 -260.97 0.1389 0.7103
## + x49
          1 0.009051 6.1443 -260.96 0.1341 0.7151
## + x25
          1 0.007174 6.1462 -260.93 0.1062 0.7452
## + x10
          1 0.006777 6.1466 -260.93 0.1003 0.7522
## + x39
          1 0.005923 6.1474 -260.91 0.0877 0.7678
## + x35
          1 0.005765 6.1476 -260.91 0.0853 0.7709
## + x14
          1 0.005743 6.1476 -260.91 0.0850 0.7713
## + x33
          1 0.004331 6.1490 -260.89 0.0641 0.8007
## + x47
          1 0.004212 6.1491 -260.89 0.0623 0.8034
## + x41
          1 0.003463 6.1499 -260.87 0.0512 0.8214
## + x34
          1 0.002590 6.1507 -260.86 0.0383 0.8453
## + x13
          1 0.001812 6.1515 -260.85 0.0268 0.8703
## + x18
          1 0.001800 6.1515 -260.85 0.0266 0.8707
## + x32
          1 0.001686 6.1516 -260.85 0.0249 0.8748
## + x24
          1 0.001439 6.1519 -260.84 0.0213 0.8843
## + x56
          1 0.001385 6.1519 -260.84 0.0205 0.8865
          1 0.001043 6.1523 -260.83 0.0154 0.9014
## + V1
## + x48
          1 0.000807 6.1525 -260.83 0.0119 0.9132
## + x54
          1 0.000803 6.1525 -260.83 0.0119 0.9135
## + x9
          1 0.000798 6.1525 -260.83 0.0118 0.9137
## + x58
          1 0.000756 6.1526 -260.83 0.0112 0.9160
          1 0.000475 6.1529 -260.82 0.0070 0.9334
## + x7
## + x50
          1 0.000339 6.1530 -260.82 0.0050 0.9437
## + x36
          1 0.000042 6.1533 -260.82 0.0006 0.9802
## + x19
          1 0.000000 6.1533 -260.82 0.0000 0.9984
##
## Step: AIC=-263.42
## y \sim x51 + x44 + x57 + x42 + x52 + x6 + x17 + x28
##
         Df Sum of Sq
                        RSS
                                AIC F value Pr(>F)
## + x27
          1 0.154232 5.8413 -264.02 2.3763 0.1267
## + x45
          1 0.139319 5.8562 -263.77 2.1411 0.1469
## <none>
                      5.9956 -263.42
## + x21
          1 0.118572 5.8770 -263.41 1.8158 0.1812
## + x15
          1 0.102362 5.8932 -263.14 1.5633 0.2144
## + x2
          1 0.078381 5.9172 -262.73 1.1922 0.2778
## + x38
          1 0.067986 5.9276 -262.56 1.0322 0.3124
## + x4
          1 0.049912 5.9456 -262.25 0.7555 0.3870
## + x53
          1 0.040048 5.9555 -262.08 0.6052 0.4386
## + x35
          1 0.040003 5.9556 -262.08 0.6045 0.4389
## + x16
          1 0.039642 5.9559 -262.08 0.5990 0.4410
## + x22
          1 0.031958 5.9636 -261.95 0.4823 0.4892
          1 0.029965 5.9656 -261.92 0.4521 0.5031
## + x46
```

```
## + x11
          1 0.027959 5.9676 -261.88 0.4217 0.5178
## + x43
          1 0.025755 5.9698 -261.85 0.3883 0.5348
## + x3
          1 0.020936 5.9746 -261.76 0.3154 0.5758
## + x12
          1 0.020908 5.9746 -261.76 0.3149 0.5761
## + x23
          1 0.020820 5.9747 -261.76 0.3136 0.5769
## + x8
          1 0.020067 5.9755 -261.75 0.3022 0.5838
          1 0.017609 5.9779 -261.71 0.2651 0.6079
## + x59
## + x5
          1 0.017361 5.9782 -261.70 0.2614 0.6104
          1 0.015163 5.9804 -261.67 0.2282 0.6340
## + x30
## + x29
          1 0.014802 5.9808 -261.66 0.2227 0.6381
## + x41
          1 0.012842 5.9827 -261.63 0.1932 0.6613
## + x40
          1 0.011656 5.9839 -261.61 0.1753 0.6764
## + x55
          1 0.010089 5.9855 -261.58 0.1517 0.6978
## + x39
          1 0.009967 5.9856 -261.58 0.1499 0.6996
## + x49
          1 0.008689 5.9869 -261.56 0.1306 0.7186
## + x19
          1 0.008546 5.9870 -261.56 0.1285 0.7209
## + x14
          1 0.005995 5.9896 -261.51 0.0901 0.7648
## + x31
          1 0.005740 5.9898 -261.51 0.0862 0.7697
## + x1
          1 0.005360 5.9902 -261.50 0.0805 0.7772
## + x36
          1 0.004407 5.9911 -261.49 0.0662 0.7975
          1 0.003969 5.9916 -261.48 0.0596 0.8077
## + x20
## + x24
          1 0.003921 5.9916 -261.48 0.0589 0.8088
## + x56
          1 0.003349 5.9922 -261.47 0.0503 0.8231
## + x25
          1 0.003172 5.9924 -261.47 0.0476 0.8277
## + x32
          1 0.002903 5.9927 -261.46 0.0436 0.8351
## + x47
          1 0.002825 5.9927 -261.46 0.0424 0.8373
## + x26
          1 0.002476 5.9931 -261.46 0.0372 0.8475
## + x13
          1 0.002310 5.9932 -261.45 0.0347 0.8527
## + x10
         1 0.002304 5.9933 -261.45 0.0346 0.8529
## + x18
         1 0.002232 5.9933 -261.45 0.0335 0.8552
          1 0.001292 5.9943 -261.44 0.0194 0.8895
## + x50
## + V1
          1 0.001066 5.9945 -261.43 0.0160 0.8996
          1 0.000653 5.9949 -261.43 0.0098 0.9213
## + x7
## + x37
          1 0.000584 5.9950 -261.43 0.0088 0.9256
## + x34
          1 0.000371 5.9952 -261.42 0.0056 0.9406
## + x54
          1 0.000203 5.9954 -261.42 0.0030 0.9561
## + x58
          1 0.000099 5.9955 -261.42 0.0015 0.9693
## + x33
          1 0.000052 5.9955 -261.42 0.0008 0.9779
## + x48
          1 0.000011 5.9955 -261.42 0.0002 0.9899
          1 0.000007 5.9955 -261.42 0.0001 0.9921
## + x9
##
## Step: AIC=-264.02
## y \sim x51 + x44 + x57 + x42 + x52 + x6 + x17 + x28 + x27
##
         Df Sum of Sq
                         RSS
                                 AIC F value Pr(>F)
          1 0.174446 5.6669 -265.05 2.7397 0.1014
## + x45
## + x21
          1 0.143253 5.6981 -264.50 2.2375 0.1382
## + x15
          1 0.129036 5.7123 -264.25 2.0104 0.1597
## <none>
                      5.8413 -264.02
## + x4
          1 0.074870 5.7665 -263.31 1.1556 0.2853
## + x38
          1 0.072377 5.7689 -263.27
                                     1.1166 0.2935
## + x2
          1 0.057055 5.7843 -263.00 0.8779 0.3513
## + x16
          1 0.054043 5.7873 -262.95 0.8311 0.3644
## + x43
          1 0.033278 5.8080 -262.59 0.5099 0.4770
```

```
## + x22
          1 0.033191 5.8081 -262.59 0.5086 0.4776
## + x35
          1 0.028527 5.8128 -262.51 0.4368 0.5104
## + x46
          1 0.027790 5.8135 -262.50 0.4254 0.5159
          1 0.027535 5.8138 -262.49 0.4215 0.5179
## + x3
## + x5
          1 0.026705 5.8146 -262.48 0.4088 0.5242
## + x53
          1 0.024791 5.8165 -262.45 0.3793 0.5395
## + x29
          1 0.024648 5.8167 -262.44 0.3771 0.5407
## + x10
          1 0.021358 5.8200 -262.39 0.3266 0.5691
          1 0.020445 5.8209 -262.37
## + x11
                                     0.3126 0.5775
## + x8
          1 0.020288 5.8210 -262.37 0.3102 0.5790
## + x30
          1 0.017494 5.8238 -262.32 0.2673 0.6064
## + x23
          1 0.016262 5.8251 -262.30 0.2485 0.6194
## + x41
          1 0.014820 5.8265 -262.27 0.2264 0.6354
## + x55
          1 0.014289 5.8270 -262.27 0.2182 0.6415
## + x59
          1 0.013794 5.8275 -262.26 0.2107 0.6474
## + x39
          1 0.011962 5.8294 -262.23 0.1826 0.6702
## + x58
          1 0.011172 5.8302 -262.21 0.1705 0.6806
## + x14
          1 0.010014 5.8313 -262.19 0.1528 0.6968
          1 0.009952 5.8314 -262.19 0.1519 0.6977
## + x24
## + x12
          1 0.008461 5.8329 -262.17 0.1291 0.7202
## + x25
          1 0.007703 5.8336 -262.15 0.1175 0.7325
## + x1
          1 0.007518 5.8338 -262.15 0.1147 0.7357
## + V1
          1 0.007271 5.8341 -262.15 0.1109 0.7399
## + x34
          1 0.005846 5.8355 -262.12 0.0892 0.7659
## + x19
          1 0.005479 5.8358 -262.12 0.0836 0.7732
## + x7
          1 0.005463 5.8359 -262.12 0.0833 0.7735
## + x49
          1 0.004550 5.8368 -262.10 0.0694 0.7929
          1 0.003312 5.8380 -262.08 0.0505 0.8227
## + x36
## + x33
          1 0.002373 5.8390 -262.06 0.0362 0.8496
## + x9
          1 0.002319 5.8390 -262.06 0.0354 0.8513
## + x20
          1 0.002159 5.8392 -262.06 0.0329 0.8565
## + x13
          1 0.001623 5.8397 -262.05 0.0247 0.8754
## + x40
          1 0.001512 5.8398 -262.05 0.0230 0.8797
## + x18
          1 0.000833 5.8405 -262.04 0.0127 0.9106
## + x37
          1 0.000788 5.8405 -262.04 0.0120 0.9130
## + x31
          1 0.000634 5.8407 -262.03 0.0097 0.9219
## + x32
         1 0.000540 5.8408 -262.03 0.0082 0.9279
## + x48
          1 0.000253 5.8411 -262.03 0.0039 0.9506
## + x26
          1 0.000111 5.8412 -262.02 0.0017 0.9673
          1 0.000038 5.8413 -262.02 0.0006 0.9809
## + x56
          1 0.000010 5.8413 -262.02 0.0002 0.9901
## + x50
## + x47
          1 0.000002 5.8413 -262.02 0.0000 0.9952
          1 0.000000 5.8413 -262.02 0.0000 0.9985
## + x54
##
## Step: AIC=-265.05
## y \sim x51 + x44 + x57 + x42 + x52 + x6 + x17 + x28 + x27 + x45
##
##
         Df Sum of Sq
                       RSS
                                 AIC F value Pr(>F)
## + x21
          1 0.159400 5.5075 -265.91 2.5469 0.1141
## <none>
                      5.6669 -265.05
          1 0.102346 5.5645 -264.88 1.6185 0.2066
## + x15
## + x4
          1 0.086271 5.5806 -264.59 1.3604 0.2466
## + x38
          1 0.058565 5.6083 -264.09 0.9189 0.3404
## + x14
          1 0.047750 5.6191 -263.90 0.7478 0.3895
```

```
## + x53
          1 0.043927 5.6230 -263.83 0.6875 0.4093
## + x3
          1 0.039490 5.6274 -263.75 0.6175 0.4341
## + x5
          1 0.034801 5.6321 -263.67 0.5438 0.4628
## + x22
          1 0.034711 5.6322 -263.67 0.5423 0.4634
## + x35
          1 0.034548 5.6323 -263.67 0.5398 0.4645
## + x43
          1 0.034164 5.6327 -263.66 0.5337 0.4670
## + x46
          1 0.032801 5.6341 -263.63 0.5123 0.4760
## + x16
          1 0.032717 5.6342 -263.63 0.5110 0.4766
          1 0.031036 5.6358 -263.60 0.4846 0.4882
## + x30
## + x23
          1 0.030107 5.6368 -263.59 0.4700 0.4948
## + x58
          1 0.027044 5.6398 -263.53 0.4220 0.5176
## + x7
          1 0.021602 5.6453 -263.44 0.3367 0.5632
## + x11
          1 0.020470 5.6464 -263.42 0.3190 0.5736
## + x1
          1 0.020143 5.6467 -263.41 0.3139 0.5767
## + x29
          1 0.019479 5.6474 -263.40 0.3035 0.5831
## + x12
          1 0.019174 5.6477 -263.39 0.2988 0.5860
## + x41
          1 0.018897 5.6480 -263.39 0.2944 0.5888
## + x8
          1 0.017614 5.6493 -263.36 0.2744 0.6017
          1 0.015161 5.6517 -263.32 0.2361 0.6283
## + x10
## + x25
          1 0.015000 5.6519 -263.32 0.2336 0.6301
## + x2
          1 0.012167 5.6547 -263.27 0.1894 0.6645
## + x59
          1 0.011415 5.6555 -263.25 0.1776 0.6745
## + x36
          1 0.010016 5.6569 -263.23 0.1558 0.6940
## + x55
          1 0.009410 5.6575 -263.22 0.1464 0.7030
## + x18
          1 0.008344 5.6585 -263.20 0.1298 0.7195
## + x13
          1 0.008174 5.6587 -263.20 0.1271 0.7223
## + V1
          1 0.007575 5.6593 -263.19 0.1178 0.7323
## + x32
          1 0.007261 5.6596 -263.18 0.1129 0.7377
## + x24
         1 0.006629 5.6603 -263.17 0.1031 0.7489
## + x34
          1 0.006042 5.6608 -263.16 0.0939 0.7600
## + x9
          1 0.004837 5.6620 -263.14 0.0752 0.7846
## + x39
          1 0.004713 5.6622 -263.14 0.0733 0.7873
## + x49
          1 0.004640 5.6622 -263.13 0.0721 0.7889
## + x31
          1 0.003466 5.6634 -263.11 0.0538 0.8170
## + x40
          1 0.002544 5.6643 -263.10 0.0395 0.8429
## + x54
          1 0.001881 5.6650 -263.09 0.0292 0.8647
## + x47
         1 0.001538 5.6653 -263.08 0.0239 0.8775
## + x48
          1 0.000820 5.6661 -263.07 0.0127 0.9104
## + x50
          1 0.000688 5.6662 -263.06 0.0107 0.9179
## + x20
          1 0.000142 5.6667 -263.06 0.0022 0.9627
## + x56
          1 0.000082 5.6668 -263.06 0.0013 0.9716
## + x37
          1 0.000060 5.6668 -263.05 0.0009 0.9756
         1 0.000024 5.6669 -263.05 0.0004 0.9846
## + x19
## + x26
        1 0.000008 5.6669 -263.05 0.0001 0.9914
          1 0.000000 5.6669 -263.05 0.0000 0.9982
## + x33
##
## Step: AIC=-265.91
## y \sim x51 + x44 + x57 + x42 + x52 + x6 + x17 + x28 + x27 + x45 +
##
      x21
##
         Df Sum of Sq RSS AIC F value Pr(>F)
##
## <none>
                     5.5075 -265.91
## + x14 1 0.082483 5.4250 -265.42 1.3228 0.2532
```

```
## + x4
          1 0.077095 5.4304 -265.32 1.2351 0.2695
## + x5
          1 0.050396 5.4571 -264.83 0.8034 0.3725
## + x38
          1 0.050288 5.4572 -264.82 0.8017 0.3731
          1 0.047566 5.4599 -264.77 0.7579 0.3864
## + x35
## + x30
          1 0.042453 5.4650 -264.68 0.6758 0.4133
## + x53
          1 0.037876 5.4696 -264.60 0.6025 0.4397
## + x8
          1 0.035500 5.4720 -264.55 0.5644 0.4545
## + x7
          1 0.034577 5.4729 -264.54 0.5497 0.4605
## + x12
          1 0.032306 5.4752 -264.50 0.5133 0.4756
## + x58
          1 0.031747 5.4757 -264.48 0.5044 0.4795
## + x3
          1 0.028813 5.4787 -264.43 0.4575 0.5006
## + x22
          1 0.028456 5.4790 -264.42 0.4518 0.5032
## + x55
         1 0.025354 5.4821 -264.37 0.4024 0.5275
## + x41
         1 0.024359 5.4831 -264.35 0.3865 0.5358
## + x16
          1 0.020909 5.4866 -264.29 0.3316 0.5662
## + x24
          1 0.020754 5.4867 -264.28 0.3291 0.5677
## + x23
          1 0.020479 5.4870 -264.28 0.3247 0.5703
## + x39
          1 0.019033 5.4884 -264.25 0.3017 0.5842
## + x9
          1 0.017494 5.4900 -264.22 0.2772 0.5999
## + x10
          1 0.017466 5.4900 -264.22 0.2768 0.6002
## + x46
          1 0.017165 5.4903 -264.22 0.2720 0.6033
## + x32
          1 0.016930 5.4905 -264.21 0.2683 0.6058
## + x43
          1 0.015223 5.4923 -264.18 0.2411 0.6246
## + x1
          1 0.013649 5.4938 -264.15 0.2161 0.6432
## + x25
          1 0.013419 5.4941 -264.15 0.2125 0.6460
## + V1
          1 0.012890 5.4946 -264.14 0.2041 0.6526
## + x40
          1 0.012648 5.4948 -264.14 0.2003 0.6556
## + x36
          1 0.011900 5.4956 -264.12 0.1884 0.6653
## + x59
         1 0.009237 5.4982 -264.07 0.1462 0.7032
## + x29
         1 0.008021 5.4995 -264.05 0.1269 0.7225
## + x11
          1 0.007935 5.4995 -264.05 0.1255 0.7240
## + x31
          1 0.007545 5.4999 -264.04 0.1194 0.7306
          1 0.007298 5.5002 -264.04 0.1154 0.7349
## + x34
## + x54
          1 0.006880 5.5006 -264.03 0.1088 0.7423
## + x37
          1 0.005336 5.5021 -264.00 0.0844 0.7722
## + x20
          1 0.003763 5.5037 -263.98 0.0595 0.8079
## + x48
         1 0.003722 5.5038 -263.97 0.0588 0.8089
## + x18
          1 0.003597 5.5039 -263.97 0.0569 0.8121
## + x19
          1 0.003251 5.5042 -263.96 0.0514 0.8212
          1 0.001403 5.5061 -263.93 0.0222 0.8820
## + x47
## + x26
          1 0.001082 5.5064 -263.93 0.0171 0.8963
## + x56
          1 0.000949 5.5065 -263.92 0.0150 0.9028
         1 0.000345 5.5071 -263.91 0.0055 0.9413
## + x13
## + x49
         1 0.000172 5.5073 -263.91 0.0027 0.9586
## + x33
         1 0.000037 5.5074 -263.91 0.0006 0.9807
## + x50
          1 0.000001 5.5075 -263.91 0.0000 0.9967
          1 0.000000 5.5075 -263.91 0.0000 0.9984
## + x2
##
## Step: AIC=-266.15
## y \sim x51 + x44 + x57 + x42 + x52 + x6 + x17 + x28 + x27 + x45 +
##
      x21 + x15
##
                               AIC F value Pr(>F)
##
         Df Sum of Sq RSS
## <none>
                      5.3853 -266.15
```

```
## + x4
          1 0.075811 5.3095 -265.57 1.2279 0.2709
## + x14
          1 0.052920 5.3324 -265.14 0.8535 0.3582
## + x35
          1 0.046239 5.3391 -265.01 0.7448 0.3905
## + x30
          1 0.040639 5.3447 -264.91 0.6539 0.4209
## + x22
          1 0.039336 5.3460 -264.88
                                      0.6328 0.4285
## + x5
          1 0.037174 5.3482 -264.84 0.5978 0.4416
## + x24
          1 0.037079 5.3483 -264.84 0.5962 0.4421
## + x12
          1 0.036712 5.3486 -264.83 0.5903 0.4444
          1 0.033420 5.3519 -264.77
## + x38
                                     0.5370 0.4657
## + x8
          1 0.033015 5.3523 -264.76 0.5305 0.4684
## + x39
          1 0.032422 5.3529 -264.75 0.5209 0.4724
## + x7
          1 0.032330 5.3530 -264.75 0.5194 0.4730
## + x3
          1 0.026618 5.3587 -264.64 0.4272 0.5151
## + x41
          1 0.026202 5.3591 -264.64 0.4205 0.5184
## + x46
          1 0.024760 5.3606 -264.61 0.3972 0.5302
## + x9
          1 0.023939 5.3614 -264.60
                                      0.3840 0.5371
## + x53
          1 0.023857 5.3615 -264.59 0.3827 0.5378
## + x58
          1 0.022426 5.3629 -264.57
                                     0.3596 0.5503
## + x55
          1 0.021772 5.3636 -264.55 0.3491 0.5562
## + x29
          1 0.021363 5.3640 -264.55
                                     0.3425 0.5599
          1 0.020839 5.3645 -264.54 0.3341 0.5648
## + V1
## + x32
          1 0.019515 5.3658 -264.51 0.3128 0.5774
## + x23
          1 0.018381 5.3670 -264.49 0.2945 0.5887
## + x25
          1 0.013888 5.3715 -264.41 0.2223 0.6385
## + x16
          1 0.012066 5.3733 -264.37
                                     0.1931 0.6614
## + x36
          1 0.011581 5.3738 -264.36 0.1853 0.6679
## + x10
          1 0.010528 5.3748 -264.35 0.1685 0.6825
          1 0.008691 5.3766 -264.31 0.1390 0.7102
## + x43
## + x1
          1 0.008346 5.3770 -264.30 0.1335 0.7157
## + x40
         1 0.007711 5.3776 -264.29 0.1233 0.7263
## + x37
          1 0.007417 5.3779 -264.29 0.1186 0.7314
## + x18
          1 0.006821 5.3785 -264.28 0.1091 0.7420
          1 0.005205 5.3801 -264.25
## + x48
                                      0.0832 0.7737
## + x56
          1 0.004977 5.3804 -264.24 0.0796 0.7786
## + x54
          1 0.004522 5.3808 -264.23
                                      0.0723 0.7887
## + x33
          1 0.004025 5.3813 -264.22 0.0643 0.8004
## + x31
          1 0.003607 5.3817 -264.22 0.0576 0.8108
## + x13
          1 0.003505 5.3818 -264.21 0.0560 0.8135
## + x59
          1 0.002893 5.3824 -264.20
                                      0.0462 0.8303
          1 0.002704 5.3826 -264.20 0.0432 0.8358
## + x19
          1 0.002551 5.3828 -264.20
## + x11
                                     0.0408 0.8405
## + x47
          1 0.001678 5.3837 -264.18 0.0268 0.8703
          1 0.001629 5.3837 -264.18 0.0260 0.8722
## + x2
## + x34
          1 0.001234 5.3841 -264.17 0.0197 0.8887
## + x50
          1 0.000670 5.3847 -264.16 0.0107 0.9179
## + x26
          1 0.000424 5.3849 -264.16 0.0068 0.9346
## + x20
          1 0.000316 5.3850 -264.15 0.0050 0.9435
## + x49
          1 0.000301 5.3850 -264.15 0.0048 0.9449
```