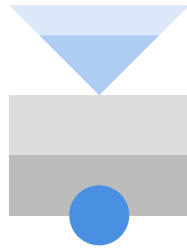


# Bangladesh University of Engineering & Technology

Department of Electrical and Electronics Engineering

## Lab Report



Experiment No. 3

Name of the Experiment:

### **Characterization of Light Emitting Diodes (LEDs)**

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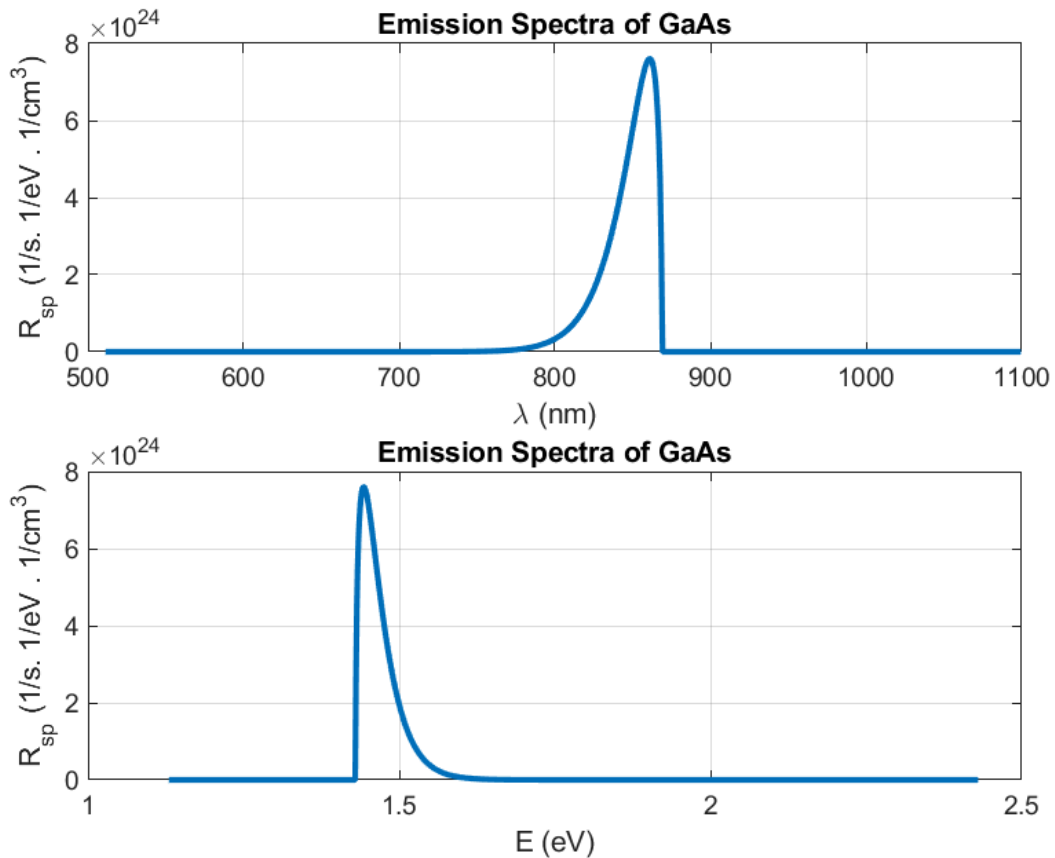
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## Part A:

### Task 1:

Graphical Output:



Calculated Parameters:

Total phonon flux for the LED:  $1.302182e+20$  1/s

Explanation:

GaAs LED Emission Spectra: The plots show the spontaneous emission rate ( $R_{sp}$ ) for GaAs plotted against both wavelength ( $\lambda$ ) and energy ( $E$ ). The key observations are:

1. Peak Emission:

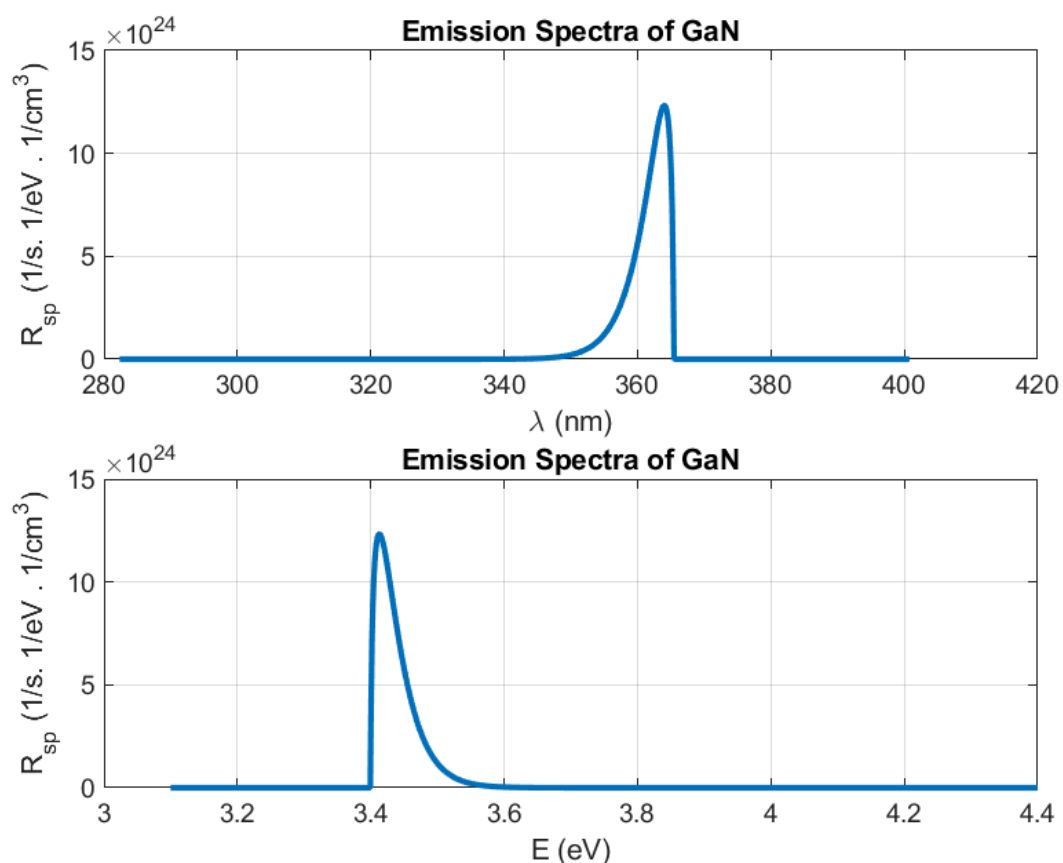
- Wavelength peak occurs at approximately 870 nm
- Energy peak is at around 1.43 eV, which closely matches GaAs's bandgap
- The peak emission rate is about  $7.5 \times 10^{24} \text{ cm}^{-3}\text{s}^{-1}\text{eV}^{-1}$

## 2. Theoretical Background:

- The emission spectra follow the relationship:  $R_{sp} \propto n \times p \times (h\nu - E_g)^{1/2} \times \exp(-h\nu/kT)$
- The sharp cutoff at lower wavelengths (higher energies) is due to the exponential term
- The gradual rise is due to the density of states and carrier distributions
- The n+-p junction design ( $5 \times 10^{17} \text{ cm}^{-3}$  n-type,  $10^{15} \text{ cm}^{-3}$  p-type) ensures efficient carrier injection

## Task 2:

Graphical Output:



## Calculated Parameters:

Total phonon flux for the LED:  $2.111738 \times 10^{20}$  1/s

## Explanation:

GaN LED Emission Spectra: The plots show similar data for GaN, but with notably different characteristics:

### 1. Peak Emission:

- Wavelength peak is around 365 nm (UV region)
- Energy peak occurs at approximately 3.4 eV, corresponding to GaN's wider bandgap
- Maximum emission rate reaches about  $12.5 \times 10^{24} \text{ cm}^{-3} \text{ s}^{-1} \text{ eV}^{-1}$

### 2. Key Features:

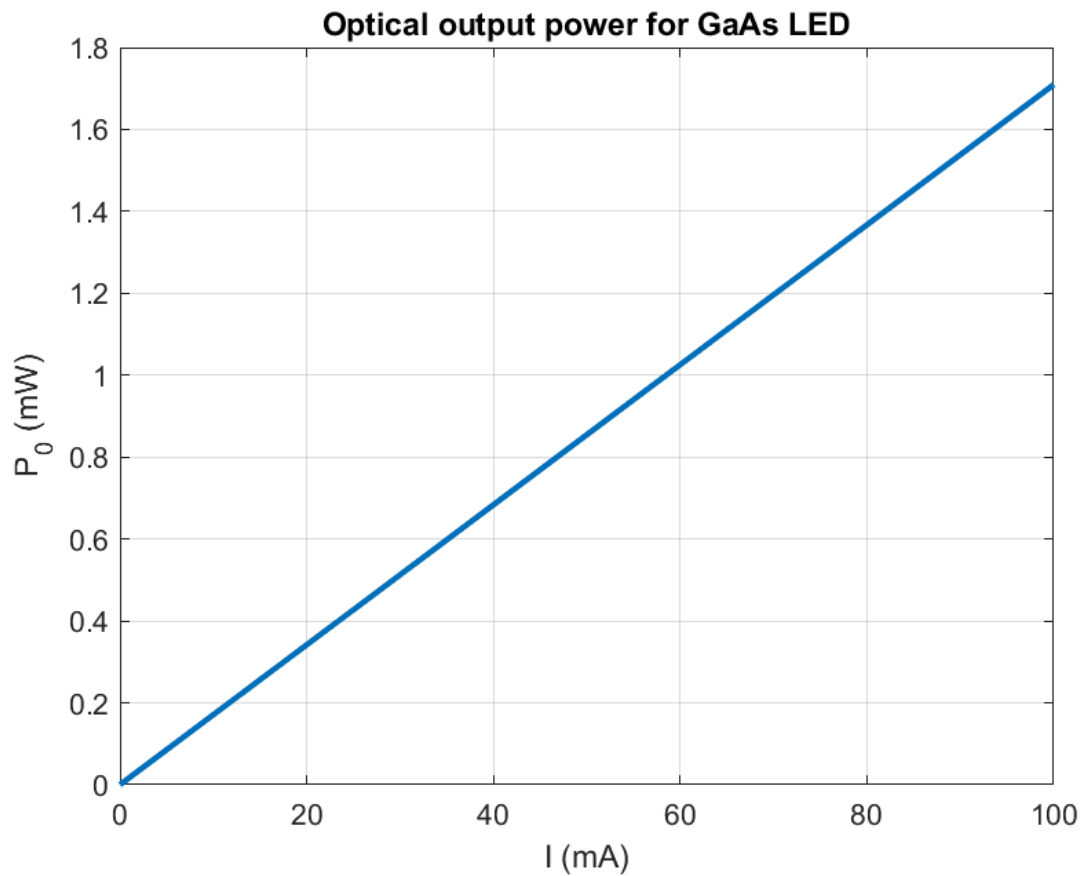
- The spectrum shows a narrower linewidth compared to GaAs
- Higher peak intensity indicates potentially more efficient recombination
- The higher energy/shorter wavelength emission is characteristic of GaN's wider bandgap
- Similar spectral shape governed by the same physical principles but shifted to higher energy

Both materials show asymmetric spectral shapes typical of semiconductor LEDs, with the position of the peaks determined by their respective bandgap energies. The differences in peak intensities and line widths reflect the active regions' different material properties and carrier concentrations.

## Part B

### Task 1:

Graphical Output:



Calculated Parameters:

Injection efficiency is 0.99894

Radiative recombination efficiency is 0.95457

Extraction efficiency is 0.01241

luminous efficiency is 0.05072

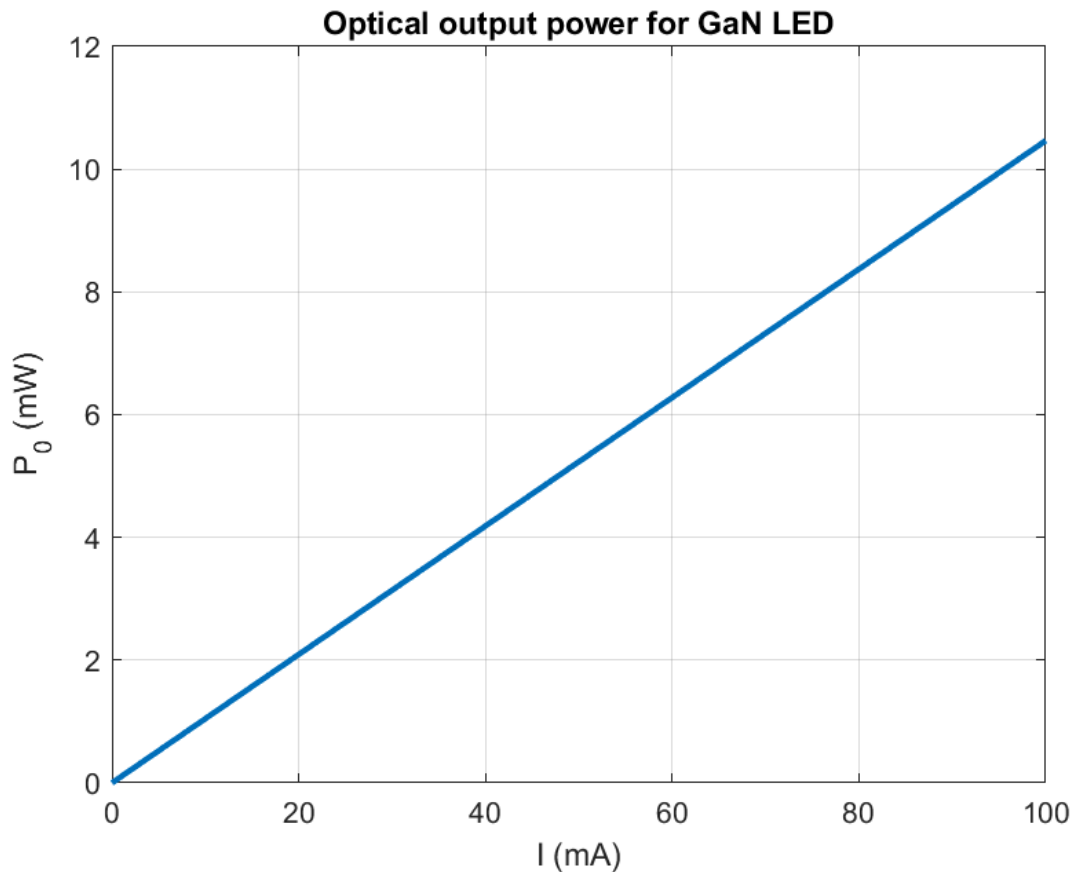
External conversion efficiency is 0.01183

### Explanation:

The GaAs n<sup>+</sup>-p junction LED demonstrates a linear relationship between optical output power and forward current, reaching approximately 1.7 mW at 100 mA. This linearity indicates good carrier injection and recombination characteristics. The calculated injection efficiency of 0.99894 is exceptionally high, attributable to the asymmetric doping ( $n^+ = 5 \times 10^{17} \text{ cm}^{-3}$ ,  $p = 10^{15} \text{ cm}^{-3}$ ) which ensures dominant electron injection into the p-region. The radiative recombination efficiency of 0.95457 suggests that most carriers recombine radiatively rather than through non-radiative processes, indicating good material quality and minimal defect-assisted recombination. However, the extraction efficiency is relatively low at 0.01241, primarily due to GaAs's high refractive index ( $\approx 3.6$ ) leading to significant total internal reflection at the semiconductor-air interface. This results in a modest luminous efficiency of 0.05072 and an external conversion efficiency of 0.01183, which represents the overall photon extraction capability of the device.

## Task 2:

Graphical Output:



Injection efficiency is 0.99957

Radiative recombination efficiency is 0.97490

Extraction efficiency is 0.03112

luminous efficiency is 0.05101

External conversion efficiency is 0.03032

Explanation:

The GaN LED exhibits a steeper linear relationship between optical output power and forward current, achieving approximately 10.5 mW at 100 mA, significantly higher than the GaAs LED. This enhanced performance is reflected in its slightly higher injection efficiency of 0.99957 and radiative recombination

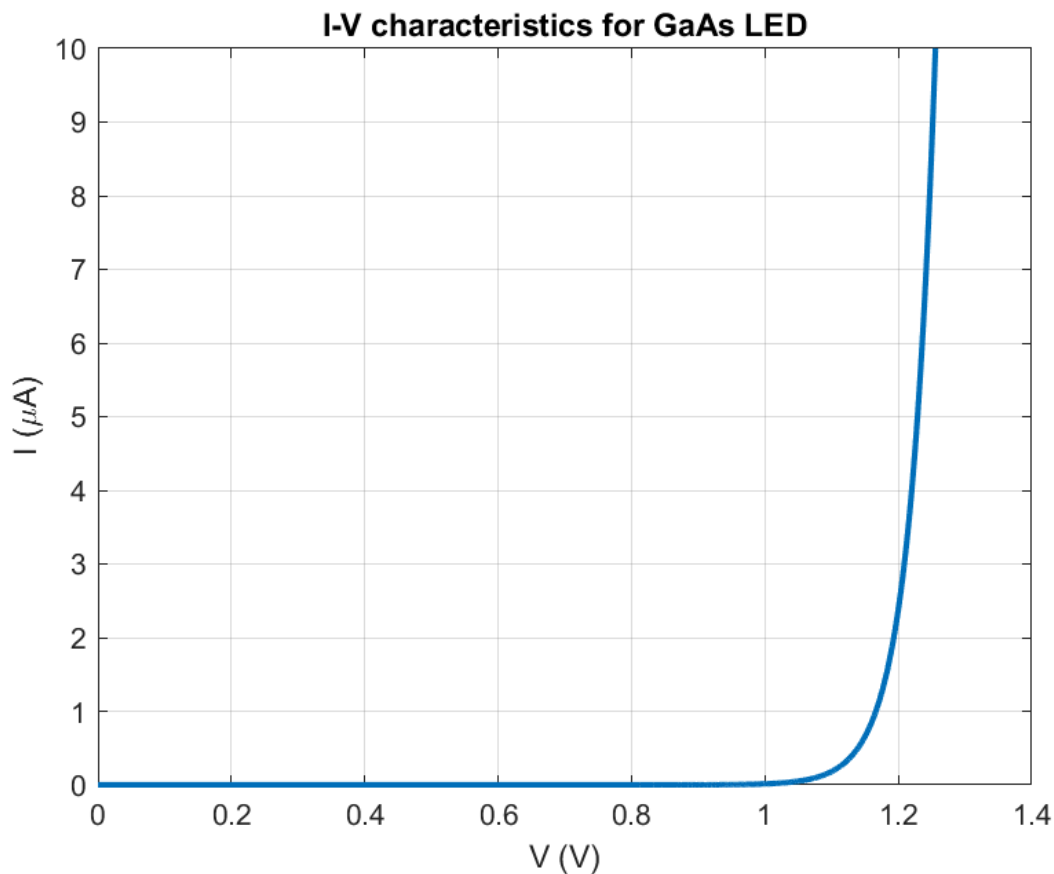


efficiency of 0.97490, indicating superior carrier transport and radiative processes. The extraction efficiency of 0.03112, while still low, is better than GaAs due to GaN's lower refractive index ( $\approx 2.5$ ) which allows for a larger escape cone at the semiconductor-air interface. The luminous efficiency of 0.05101 and external conversion efficiency of 0.03032 are consequently higher than GaAs. The improved performance of GaN can be attributed to its direct bandgap, strong carrier confinement, and better crystalline quality in modern growth processes. The plots for both LEDs show linear L-I characteristics without saturation within the given current range, indicating good heat dissipation and minimal efficiency droop effects that typically occur at higher current densities.

## Part C

### Task 1:

Graphical Output:



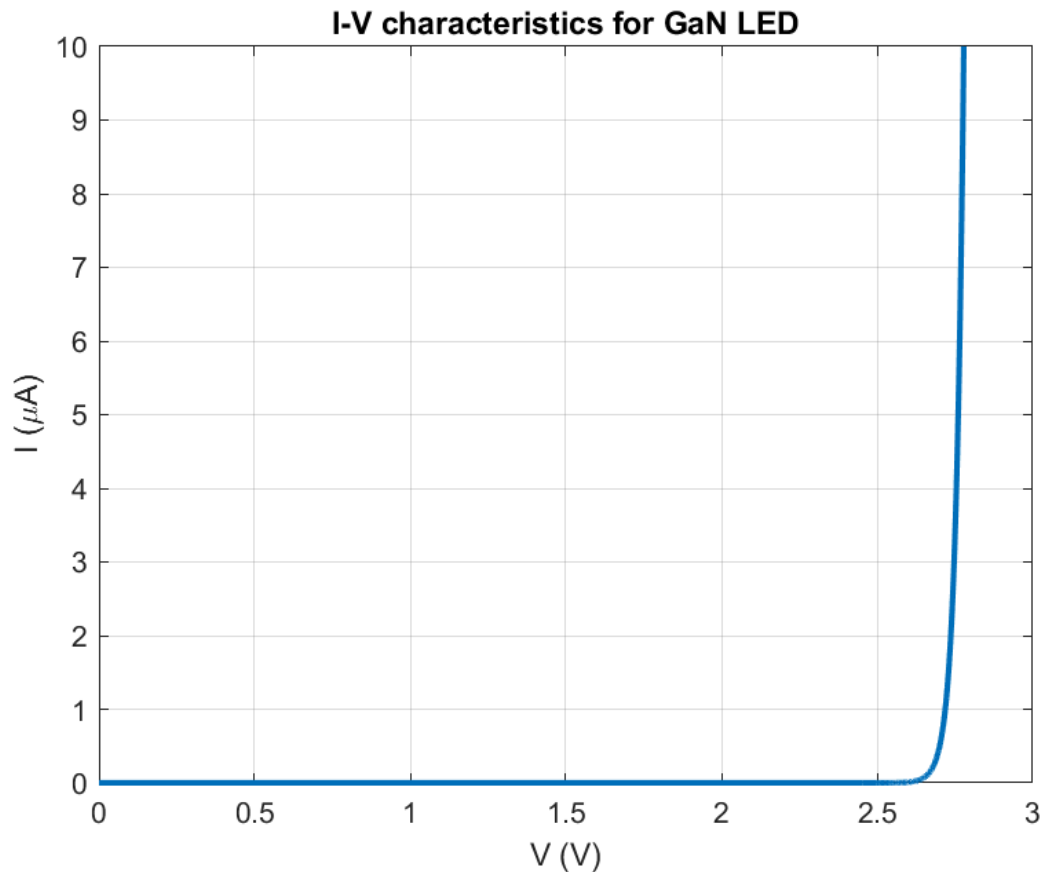
Explanation:

For the GaAs LED, the I-V characteristic shows the typical diode behavior with a turn-on voltage of approximately 1.1V, which corresponds well with GaAs's bandgap energy of about 1.42 eV. The plot demonstrates three distinct regions: a low-current region below turn-on where current is negligible, a sharp turn-on region around 1.1V, and an exponential current increase above turn-on voltage. The asymmetric doping ( $n^+ = 5 \times 10^{17} \text{ cm}^{-3}$ ,  $p = 10^{15} \text{ cm}^{-3}$ ) creates a one-sided abrupt junction, which influences the depletion region width and built-in potential. The ideality factor ( $n_f$ ) of 1.5 indicates that both diffusion and recombination currents contribute to the total current flow, typical for real LED

devices. The 1 mm<sup>2</sup> cross-sectional area affects the magnitude of the current, with the current reaching approximately 10 μA at 1.3V. The sharp rise in current after turn-on is described by the diode equation  $I = I_s(\exp(qV/nfkT) - 1)$ , where  $I_s$  is the saturation current.

## Task 2:

Graphical Output:



Explanation:

For the GaN LED, the I-V characteristic shows a significantly higher turn-on voltage of about 2.6V, consistent with GaN's wider bandgap of approximately 3.4 eV. The plot exhibits similar regions as the GaAs LED but shifted to higher voltages. The higher doping concentration in the n-region ( $N_D = 1 \times 10^{18} \text{ cm}^{-3}$ ) compared to the p-region ( $N_A = 10^{15} \text{ cm}^{-3}$ ) ensures efficient electron injection. The ideality factor of 1.0 suggests that the current is dominated by diffusion rather than recombination processes, indicating high-quality material and interfaces. The smaller cross-sectional area of  $0.5 \text{ mm}^2$  compared to the GaAs LED affects the current magnitude, though both reach similar maximum

currents of about 10  $\mu\text{A}$ . The steeper turn-on characteristic (more abrupt transition) in GaN compared to GaAs is partly due to the lower ideality factor and higher built-in potential. Both LEDs show negligible reverse leakage current in the shown voltage range, indicating good junction quality and minimal defect-assisted tunneling.

## Appendix: Part A

```
clc;
clearvars;
close all;

% Constants in SI unit
h = 6.626e-34;
h_cut = h/(2*pi);
c = 3e8;
k_B = 1.38e-23;
T = 300;
q = 1.6e-19;
mo = 9.1e-31;

%% Choose data
Task_no = 2; % Task 1: GaAs, Task 2: GaN

switch (Task_no)
    case 1
        material = 'GaAs';
        % Mobility in cm2/Vs
        u_n = 8500;
        u_p = 400;
        % Doping concentrations in (cm-3)
        Na = 1e15;
        Nd = 5e17;
        ni = 1.79e6; % intrinsic carrier concentration (cm-3)
        me = 0.067*mo; % effective mass
        mh = 0.5*mo;
        Eg = 1.43*q; % bandgap
    case 2
        material = 'GaN';
        % Mobility in cm2/Vs
        u_n = 1800;
        u_p = 30;
        % Doping concentrations in (cm-3)
        Na = 1e15;
        Nd = 1e18;
        ni = 1.9e-10; % intrinsic carrier concentration (cm-3)
        me = 0.27*mo; % effective mass
        mh = 0.8*mo;
```

```

Eg = 3.4*q;
%bandgap
end

deln = 1e17; % excess
minority      carrier
concentration

mr = (me*mh)/(me+mh); %
average effective mass

npo = ni^2/Na;
pno = ni^2/Nd;
Br = 1e-10;

%tau_n means lifetime of
minority electron in
p-region
tau_n =
1/(Br*(Na+npo+deln));
tau_p =
1/(Br*(pno+Nd+deln));

%% Emission Spectra

E =
linspace(Eg-0.3*q,Eg+q,10
00);
lambda = (h*c)./E;
delE = (E-Eg);

%Recombination happens in
p-GaAs region
tau_r = tau_p;

Ef_n =
k_B*T*log((Nd+deln)/ni);
% Ef_n-Ef_i
Ef_p =
k_B*T*log((Na+deln)/ni);
% Ef_i-Ef_p

% Efn_Efp = Ef_n + Ef_p;

R_sp =
(((2*mr)^1.5)/(2*pi^2*(h
_cut^3)*tau_r)) ...
*exp((Ef_n +
Ef_p-Eg)/(k_B*T)).*(delE.
^0.5).*exp(-delE./(k_B*T)
));

%SI to 1/s. 1/eV . 1/cm3
unit
R_sp_cgs = R_sp*q/100^3;

figure();
subplot(211);
plot(lambda/1e-9,real(R_s
p_cgs), 'LineWidth',2);
xlabel('\lambda (nm)');
ylabel('R_{sp} (1/s. 1/eV
. 1/cm^3)');
title(sprintf('Emission
Spectra of %s',
material));
grid on;

subplot(212);

```

```

plot(E/q,real(R_sp_cgs),
'LineWidth',2);
xlabel('E (eV)');
ylabel('R_{sp} (1/s. 1/eV
. 1/cm^3)');
title(sprintf('Emission
Spectra of %s',
material));
grid on;

% Calculate total
spontaneous emission rate
R_total = trapz(E*q,
real(R_sp)); % Numerical
integration over energy

% Volume in m^3

V = 0.5e-9; % 0.5 mm^3 in
m^3

% Calculate photon flux
Phi = R_total / V; %
Total photon flux
fprintf('Total phonon
flux for the LED: %e 1/s
\n',Phi)

% Save the plot as a PNG
file
saveas(gcf,
'C:\SPB_Data\EEE460_Jan20
24_byakc\Exp3_BYAKC\repor
tprepare\partA_task2.png'
);

```

## Appendix: Part B

```

clc;
clearvars;
close all;

% Constants in SI unit
h = 6.626e-34;
h_cut = h/(2*pi);
c = 3e8;
k_B = 1.38e-23;

T = 300;
q = 1.6e-19;
mo = 9.1e-31;

%% Choose data
Task_no = 2; % Task 1:
GaAs, Task 2: GaN

switch (Task_no)

```



```

case 1                                     % Mobility in
material = cm2/Vs
'GaAs';                                u_n = 1800;
% Mobility in                               u_p = 30;
cm2/Vs
u_n = 8500;                                % Doping
u_p = 400;                                concentrations in (cm-3)
Na = 1e15;                                Nd = 1e18;
% Doping
concentrations in (cm-3)
Na = 1e15;                                ni = 1.9e-10; %
Nd = 5e17;                                intrinsic carrier
concentration (cm-3)
ni = 1.79e6; %
intrinsic carrier                        % effective mass
concentration (cm-3)                    me = 0.27*mo;
mh = 0.8*mo;
% effective mass
me = 0.067*mo;                                % Refractive
mh = 0.5*mo;                                index
nr1 = 2.55; %GaN
% Refractive
index
nr1 = 3.68; %GaAs
Eg = 1.43*q; %
bandgap                                %bandgap
lamda0 = 360e-9;
%Peak Wavelength from
Exp1
end
deln = 1e17; % excess
minority carrier
concentration
A = 1*(1/10)^2; %
Cross section Area in cm2

```

```

mr = (me*mh) / (me+mh); %
average effective mass

%% Injection efficiency
npo = ni^2/Na;
pno = ni^2/Nd;

% cm2/s
Dn = (k_B*T*u_n) / q;
Dp = (k_B*T*u_p) / q;
Br = 1e-10;

%tau_n means lifetime of
minority electron in
p-region
tau_n =
1 / (Br * (Na+npo+deln));
tau_p =
1 / (Br * (pno+Nd+deln));

Ln = (Dn*tau_n)^0.5;
Lp = (Dp*tau_p)^0.5;

Nin =
(Dn*npo/Ln) / ((Dn*npo/Ln) +
(Dp*pno/Lp)); %injection
effiiciency
fprintf('Injection
efficiency is %0.5f
\n',Nin)

%% radiative
recombination efficiency

sr = 1e-15;
NT = 1e13; % Trap density
(cm-3)
Vth =
((3*k_B*T) / mr) ^ (.5) * 1e2;
tau_nr = (sr*Vth*NT) ^ -1;

Nr =
1 / (1 + (tau_n/tau_nr)); %
radiative recombination
efficiency
fprintf('Radiative
recombination efficiency
is %0.5f \n',Nr)

%% Extraction efficiency

% Refractive index ->
nr1=material
nr2 = 1; %Air

Ne =
(1/4) * (nr2/nr1) ^ 2 * (1 - ((nr
1-nr2) / (nr1+nr2)) ^ 2);
fprintf('Extraction
efficiency is %0.5f
\n',Ne)

%% luminous efficiency

data =
importdata('sensitivity_G
aAs.txt');

```

```

lambda = data(5:end,1);
sensitivity = *exp((Efn_Efp-Eg)/(k_B*T)
data(5:end,2);).* (delE.^0.5).*exp(-delE
emission = data(5:end,3); ./ (k_B*T));

% figure;
%
plot(lambda,sensitivity)
% xlabel('\lambda (nm)');
% ylabel('Sensitivity');
% title('Photopic
sensitivity');
% grid on;

% Calculating Rsp
E =
(h*c)/(lambda.*1e-9);
delE = (E-Eg);
tau_r =
1/(Br*(Nd+pno+deln));

Ef_n =
k_B*T*log((Nd+deln)/ni);
% Ef_n-Ef_i
Ef_p =
k_B*T*log((Na+deln)/ni);
% Ef_i-Ef_p

Efn_Efp = Ef_n + Ef_p;

R_sp =
(((2*mr)^1.5)/(2*pi^2*(h
_cut^3)*tau_r)) ...

V =
sum(sensitivity.*R_sp);
P = sum(R_sp);
Nl = V/P;
fprintf('luminous
efficiency is %0.5f \n
\n',Nl)

%% Final efficiency
% Excluding NL (as Nl
very low)
N0 = Nin*Nr*Ne;
fprintf('External
conversion efficiency is
%0.5f \n',N0)

%% Output optical power
(L) as a function of
forward current (I)

I = linspace(0,100,100);
%mA
L = N0*I*(h*c/lamda0)/q;
% mW

figure
plot(I,L, 'LineWidth',2);
xlabel('I (mA)');
ylabel('P_0 (mW)');

```

```

title(sprintf('Optical
output power for %s
LED',material));
grid on;

```

```

% Save the plot as a PNG
file
saveas(gcf,
'C:\SPB_Data\EEE460_Jan20
24_byakc\Exp3_BYAKC\repor
tprepare\partB_task2.png'
);

```

## Appendix: Part C

```

clc;
clearvars;
close all;

%% Choose data/Task no

Task_no = 2; % Task 1:
GaAs, Task 2: GaN

switch (Task_no)
    case 1
        material =
'GaAs';
        % Mobility in
cm2/Vs
        u_n = 8500;
        u_p = 400;
        % Doping
concentrations in (cm-3)
        Na = 1e15;
        Nd = 5e17;

```

```

        ni = 1.79e6; %
intrinsic carrier
concentration (cm-3)

        A = 1*(1/10)^2;
% Cross section Area in
cm2
        nf = 1.5;

        lamda0 = 860e-9;
%Peak Wavelength from
Exp1

    case 2
        material = 'GaN';
        % Mobility in
cm2/Vs
        u_n = 1800;
        u_p = 30;

```

```

                                % Doping
concentrations in (cm-3)                                % cm2/s
    Na = 1e15;                                           Dn = (k_B*T*u_n)/q;
    Nd = 1e18;                                           Dp = (k_B*T*u_p)/q;
                                                         Br = 1e-10;

    ni = 1.9e-10; %
intrinsic carrier                                       %tau_n means lifetime of
concentration (cm-3) minority electron in
                                                         p-region

    A = 0.5*(1/10)^2; tau_n                                =
% Cross section Area in 1/(Br*(Na+npo+deln));
cm2 tau_p                                =
    nf = 1; 1/(Br*(pno+Nd+deln));

    lamda0 = 360e-9; Ln = (Dn*tau_n)^0.5;
%Peak Wavelength from Lp = (Dp*tau_p)^0.5;
Exp1
end V = linspace(0,3,10000);
% Peak Wavelength(nm) = % Voltage (X-axis)

1243/Bandgap(eV)

% Current Density (A/cm2)
% Constants in SI unit Js                                =
h = 6.626e-34; q*((Dn*npo/Ln)+(Dp*pno/Lp
k_B = 1.38e-23; )) ;
T = 300;
q = 1.6e-19; Is = A*Js;
I                                =
deln = 1e17; % excess Is*exp(((q*V)./(nf*k_B*T)
minority carrier )-1);
concentration

%% Plotting

%% Calculation
npo = ni^2/Na;
pno = ni^2/Nd;
plot(V,I/1e-6,
"LineWidth",2);

```

```

xlabel('V (V) ');
ylabel('I (\muA) ');
title(sprintf('I-V
characteristics for %s
LED',material));

ylim([0 10]);
% title('I-V
characteristics of
GaAs');

grid on;

% Save the plot as a PNG
file
saveas(gcf,
'C:\SPB_Data\EEE460_Jan20
24_byakc\Exp3_BYAKC\repor
tprepare\partC_task2.png'
);

```