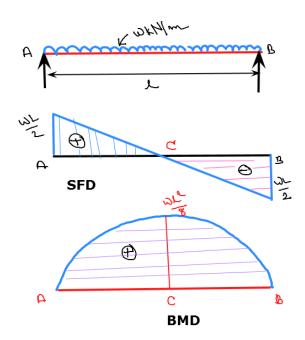
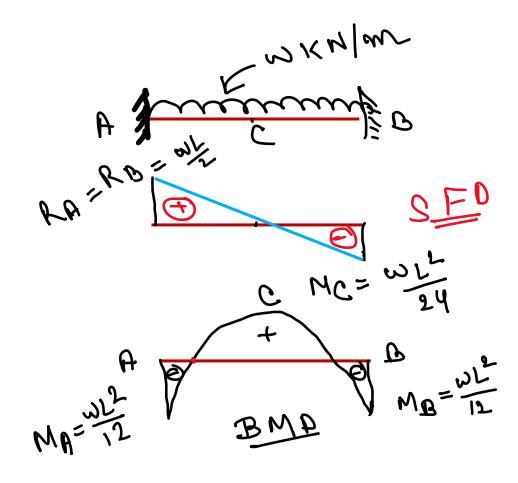
Design of Reinforced Concrete Structures

INTRODUCTION TO DESIGN OF SINGLY REINFORCED BEAM AS PER IS 456

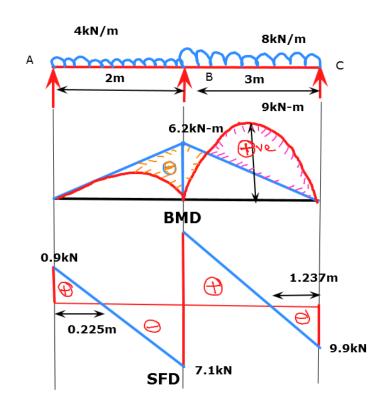
Simply Supported Beam

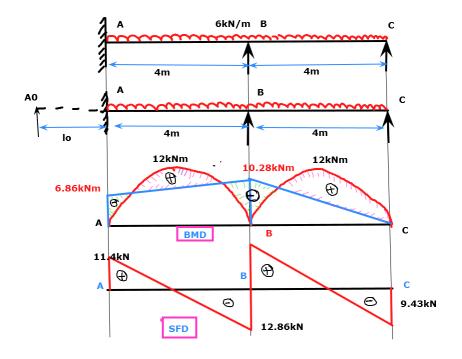




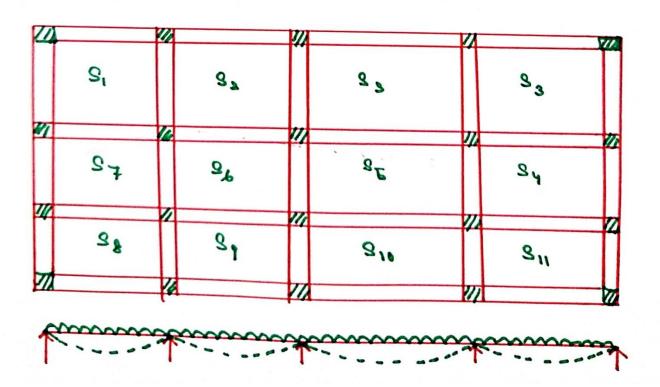
Fixed Beam

CONTINUOUS Beams





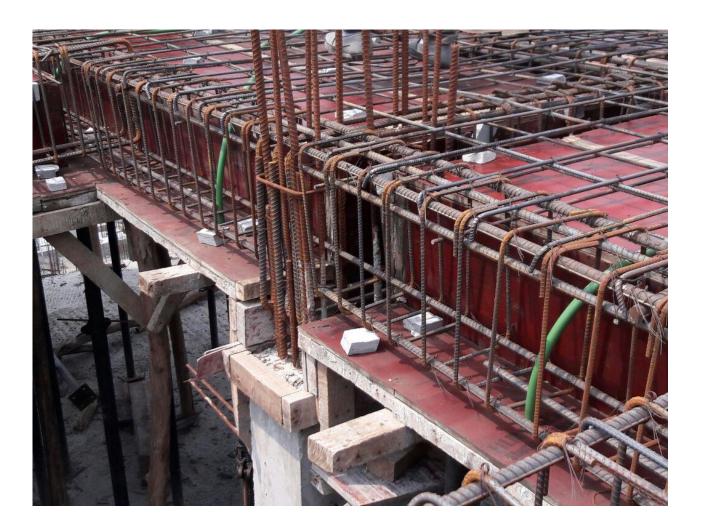
TWO WAY CONTINUOUS SLAB



Deflection pattern of the continuous beam











IS:456 2000 Recommendations For Design of Beams

Effective Span: Cl 22.2 IS:456-2000 Pg-34



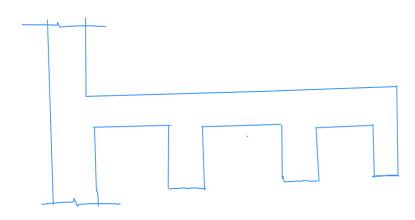
22.2 Effective Span

Unless otherwise specified, the effective span of a member shall be as follows:

a) Simply Supported Beam or Slab—The effective span of a member that is not built integrally with its supports shall be taken as clear span plus the effective depth of slab or beam or centre to centre of supports, whichever is less.

34

Effective Span: Cl 22.2 IS:456-2000 Pg-34



- b) Continuous Beam or Slab In the case of continuous beam or slab, if the width of the support is less than 1/12 of the clear span, the effective span shall be as in 22.2 (a). If the supports are wider than 1/12 of the clear span or 600 mm whichever is less, the effective span shall be taken as under:
 - For end span with one end fixed and the other continuous or for intermediate spans, the effective span shall be the clear span between supports;
 - For end span with one end free and the other continuous, the effective span shall be equal to the clear span plus half the effective depth of the beam or slab or the clear span plus half the width of the discontinuous support, whichever is less;
 - In the case of spans with roller or rocket bearings, the effective span shall always be the distance between the centres of bearings.
- c) Cantilever The effective length of a cantilever shall be taken as its length to the face of the support plus half the effective depth except where it forms the end of a continuous beam where the length to the centre of support shall be taken.
- d) Frames In the analysis of a continuous frame, centre to centre distance shall be used.

Reinforcement In Beam

Minimum & Maximum Reinforcement: Cl 26.5.2.1 IS:456-2000 Pg-48

given by the following:

$$\frac{A_s}{bd} = \frac{0.85}{f_y}$$

where

A = minimum area of tension reinforcement,

b = breadth of beam or the breadth of the web of T-beam,

d = effective depth, and

f_y = characteristic strength of reinforcement in N/mm².

b) Maximum reinforcement—The maximum area of tension reinforcement shall not exceed 0.04 bD.

Maximum Spacing of Reinforcement: Cl 26.3.3 IS:456-2000 Pg-46

26.3.3 Maximum Distance Between Bars in Tension

Unless the calculation of crack widths shows that a greater spacing is acceptable, the following rules shall be applied to flexural members in normal internal or external conditions of exposure.

a) Beams — The horizontal distance between parallel reinforcement bars, or groups, near the tension face of a beam shall not be greater than the value given in Table 15 depending on the amount of redistribution carried out in analysis and the characteristic strength of the reinforcement.

b) Slabs

- The horizontal distance between parallel main reinforcement bars shall not be more than three times the effective depth of solid slab or 300 mm whichever is smaller.
- 2) The horizontal distance between parallel reinforcement bars provided against shrinkage and temperature shall not be more than five times the effective depth of a solid slab or 450 mm whichever is smaller.

COVER: Nominal Cover for slab is taken from Table-16, IS:456-2000 Pg-47

IS 456: 2000

Table 16 Nominal Cover to Meet Durability Requirements

(Clause 26.4.2)

Exposure	Nominal Concrete Cover in mm not Less Than					
Mild	20					
Moderate	30					
Severe	45					
Very severe	50					
Extreme	75					

NOTES

- 1 For main reinforcement up to 12 mm diameter bar for mild exposure the nominal cover may be reduced by 5 mm.
- 2 Unless specified otherwise, actual concrete cover should not deviate from the required nominal cover by +10 mm
- 3 For exposure condition 'severe' and 'very severe', reduction of 5 mm may be made, where concrete grade is M35 and above.

Control of Deflection In Beams

Vertical Deflection Limit: Cl 23.2.1 IS:456-2000 Pg-37

23.2.1 The vertical deflection limits may generally be assumed to be satisfied provided that the span to depth ratios are not greater than the values obtained as below:

a) Basic values of span to effective depth ratios for spans up to 10 m:

Cantilever 7
Simply supported 20
Continuous 26

VI 2V IIIII TTIMVIIV TVI AU IVUU

- b) For spans above 10 m, the values in (a) may be multiplied by 10/span in metres, except for cantilever in which case deflection calculations should be made.
- c) Depending on the area and the stress of steel for tension reinforcement, the values in (a) or (b) shall be modified by multiplying with the modification factor obtained as per Fig. 4.
- d) Depending on the area of compression reinforcement, the value of span to depth ratio be further modified by multiplying with the modification factor obtained as per Fig. 5.

MOMENTS IN TWO WAY SIMPLY SUPPORTED RCC SLAB

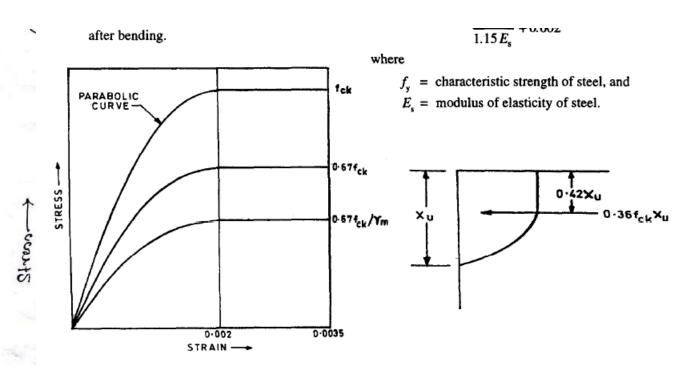
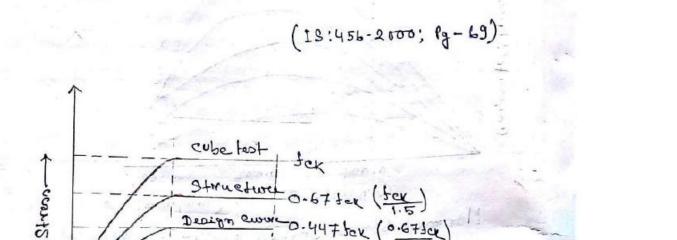


Fig. 21 Stress-Strain Curve for Concrete

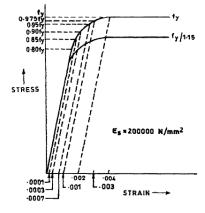
FIG. 22 STRESS BLOCK PARAMETERS

Id

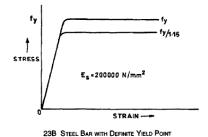


Idealized Stress Strain Curve for converte

0.0035



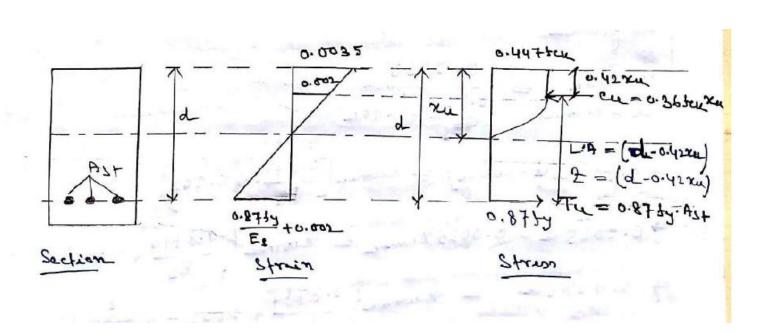
23A Cold Worked Deformed Bar



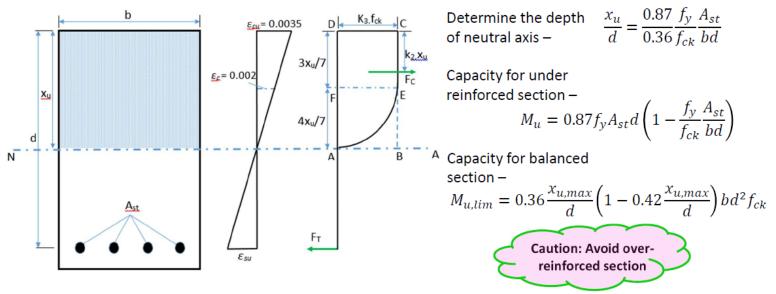
ZOD GTEEL DAR WITH DEFINITE TIELD FORM

 $Fig.\ 23\ Representative\ Stress-Strain\ Curves\ for\ Reinforcement$

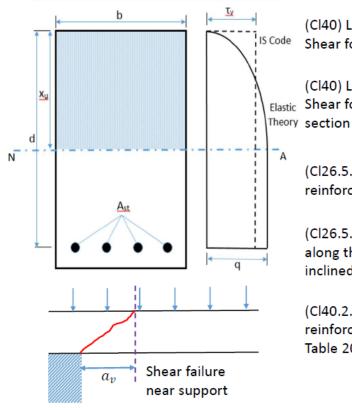
Stresses and forces in RCC Beam Section



Design Against Bending:



Important: (Cl26.2.3.4) Negative moment reinforcement – At least one-third of the reinforcement provided for negative moment at the support shall extent beyond the point of inflection for a distance not less than the effective depth of the member of 12ϕ or one-sixteenth of the clear span whichever is greater.



(Cl40) Limit State of Collapse in Shear for uniform cross section

$$au_v = rac{V_u}{bd}$$
 Note: Design shear strength of concrete is given in Table 19

(Cl40) Limit State of Collapse in Shear for non-uniform cross
$$\tau_v = \frac{V_u + \frac{M_u}{d} tan(\beta)}{bd}$$
 Prefer to avoid in G+2 residential type

(Cl26.5.1.5) Minimum Shear $\frac{A_{sv}}{bs_v} \ge \frac{0.4}{0.87 f_v}$ reinforcement

$$\frac{A_{sv}}{bs_v} \ge \frac{0.4}{0.87f_y}$$

(Cl26.5.1.5) Maximum spacing of shear reinforcement - The maximum spacing along the axis of the member shall not exceed 0.75d for vertical stirrups and d for inclined stirrup at 45 degree

(Cl40.2.3) Nominal shear stress - Under no circumstances, even with shear reinforcement, shall the nominal shear stress in beams τ_v exceed τ_{cmax} given in Table 20

40 LIMIT STATE OF COLLAPSE: SHEAR

40.1 Nominal Shear Stress

The nominal shear stress in beams of uniform depth shall be obtained by the following equation:

$$\tau_{\mathbf{v}} = \frac{V_{\mathbf{u}}}{b_{\mathbf{d}}}$$

where

 V_{ij} = shear force due to design loads;

b = breadth of the member, which for flanged section shall be taken as the breadth of the web, b_w; and

d = effective depth.

40.3 Minimum Shear Reinforcement

When τ_v is less than τ_c given in Table 19, minimum shear reinforcement shall be provided in accordance with 26.5.1.6.

40.4 Design of Shear Reinforcement

When τ_v exceeds τ_c given in Table 19, shear reinforcement shall be provided in any of the following forms:

- a) Vertical stirrups,
- b) Bent-up bars along with stirrups, and

IS 456: 2000

Table 19 Design Shear Strength of Concrete, t, N/mm2 (Clauses 40.2.1, 40.2.2, 40.3, 40.4, 40.5.3, 41.3.2, 41.3.3 and 41.4.3)

100 4	Concrete Grade							
ы	M 15	M 20	M 25	M 30	M 35	M 40 and above		
(1)	(2)	(3)	(4)	(5)	(6)			
≤0.15	0.28	0.28	0.29	0.29	0.29	0.30		
	0.35	0.36	0.36	0.37	0.37	0.38		
0.25	0.46	0.48	0.49	0.50	0.50	0.51		
0.50	0.54	0.56	0.57	0.59	0.59	0.60		
0.75	0.60	0.62	0.64	0.66	0.67	0.68		
1.00	0.64	0.67	0.70	0.71	.0.73	0.74		
1.25	0.68	0.72	0.74	0.76	0.78	0.79		
1.50	0.71	0.75	0.78	0.80	0.82	0.84		
1.75	0.71	0.79	0.82	0.84	0.86	0.88		
2.00	0.71	0.81	0.85	0.88	0.90	0.92		
2.25	0.71	0.82	0.88	0.91	0.93	0.95		
2.50	0.71	0.82	0.90	0.94	0.96	0.98		
2.75 3.00	0.71	0.82	0.92	0.96	0.99	1.0)		

above NOTE — The term A is the area of longitudinal tension reinforcement which continues at least one effective depth beyond the section being considered except at support where the full area of tension reinforcement may be used provided the detailing conforms to 26.2.2 and 26.2.3

Table 20 Maximum Shear Stress, remax, N/mm² (Clauses 40.2.3, 40.2.3.1, 40.5.1 and 41.3.1)

Concrete	M 15	M 20	M 25	M 30	M 35	M 40 and
Grade						above
a Nimmi	25	2.8	3.1	3.5	3.7	4.0

Pt = 0.955 ≈1

Corresponding Te = 0.62 From Is-452, Table-19, Pg-73 Show force Coverised by Concrete Vue = Tex(bd) = 0.85 x (300 x 232) N = 64.21 X103 M

Show force covided by Steel (show reinforcumnt) Vus = (Vu-Vuc) = (124.2-dd.21) = 24.2d KM

Let provide two loyed voctical stroughs of 8\$

Area of two leged vertical stirrups $Asv = 2 \times \frac{\pi}{4} \times 82$ = 100 mm 2

a) For vertical stirrups:

$$V_{ui} = \frac{0.87 f_{y} A_{sv} d}{s_{v}}$$

b) For inclined stirrups or a series of bars bent-up at different cross-sections:

$$V_{\rm us} = \frac{0.8.7 \, f_{\rm y} \, A_{\rm sv} d}{s_{\rm v}} \, \left(\sin \alpha + \cos \alpha \right)$$

c) For single bar or single group of parallel bars, all bent-up at the same cross-section:

73

26.5.1.5 Maximum spacing of shear reinforcement

The maximum spacing of shear reinforcement measured along the axis of the member shall not exceed 0.75 d for vertical stirrups and d for inclined stirrups at 45° , where d is the effective depth of the section

under consideration. In no case shall the spacing exceed 300 mm.

26.5.1.6 Minimum shear reinforcement

Minimum shear reinforcement in the form of stirrups shall be provided such that:

$$\frac{A_{\rm sv}}{bs_{\rm v}} \geq \frac{0.4}{0.87 f_{\rm y}}$$

where

A_{sy} = total cross-sectional area of stirrup legs effective in shear,

s_v = stirrup spacing along the length of the member,

b = breadth of the beam or breadth of the



Design of Singly reinforced Beam.

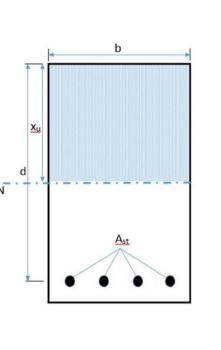
Design a Simply Supported rectangular beam of effective length of 6m. The beam is subjected to a total lead of 35 KN/m (including Self wt). Use M-20 grade Concrete and Fe-415 grade Steel. Using LSM.

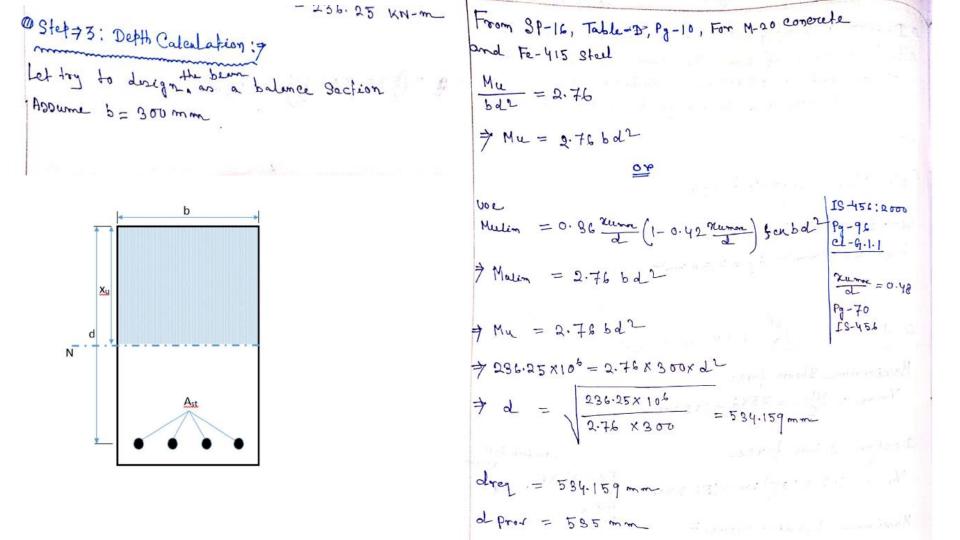
Stet # 1: Design Content: #

W= 35 KN/m, L = 6m

Scx = 20 N/mm2 by = 415 N/mm2 6m

OStet # 1: Design Content: > W= 35 KN/m, L=6m JCK = 20 N/mm> Jy = 415 N/mm O Step = 2: Load, and BM Calculation: Maximum Shear force $V_{max} = \frac{NL}{2} = \frac{35XB}{0} = 105 \text{ km}$ Design Show force Nr = (1.2 × 102) KM = 124. 2KM Maximum bending moment Mmax = "NC" = 35x62 = 157.5 KN-m Design bending moment Mu = (1.5 x 157.5) = 236.25 KN-m @ Clob - 7 . - .





4 Stet = 3: Detth Calculation: 7 Let try to dusign the bean balance Saction Assume b = 300 mm Let provide 20 \$ dia books and &

and Fe-415 Steel

From SP-16, Table-D, Pg-10, For M-20 conocete

$$7 \text{ Modim} = 2.76 \text{ bd}^2$$
 $7 \text{ Mu} = 2.76 \text{ bd}^2$
 $7 \text{ 236.25} \times 10^6 = 2.76 \times 30$
 $7 \text{ d} = \frac{236.25 \times 10^6}{236.25 \times 10^6}$

xumax = 0.48

Dpm = (535+20+ 20) = 565mm

\$13-456:2000, Table-16,7

1 Step > 4: Area of Steel Calculation :> = 2.75 = 2.76

Now from SP-16, Page + 48 = 0.955 for corresponding value of the = 2.76 → bd = Astx100 = 0.955 \$ Ast = (0.955 × 300 × 535) = 1532.775 mm2

Area of 20 \$ bors = \$\frac{1}{4} x20^2 = 314.15mm No of born required = 1532.775 = 4.87 314.15 ~ 5 mon

Dpm = (535+20+ 20) = 565mm

fck = 20 N/mm²

M_u/bd^2		fy, N/mm²				M_0/bd^2 ,	f _y , N/mm ³				
N/mm ²	240	250	415	480	500	N/mm²	240	250	415	480	
0.30	0.146	0.140	0.085	0.073	0.070	2·22 2·24	1·253 1·267	1.203	0.725	0.627	0
0.35	0.171	0.164	0.099	0.086	0.082	2.24	1:267	1:216	0.733	0.633	Ŏ.
0.40	0.196	0.188	0.114	0.098	0.082 0.094	2.26	1.281	1·216 1·230	0·733 0·741	0.640	ŏ-
0.45	0.222	0.213	0.178	0.111	0.100	2.28	1·281 1·295	1.243	0.749	0.647	o.
0·45 0·50	0.247	0.237	0.143	0.123	0.119	2-30	1.309	1.256	0·749 0·757	0.654	Ŏ.
0·55 0·60	0·272 0·298	0.262	0·158 0·172	0-136	0·131 0·143	2·32 2·34	1·323 1·337	1·270 1·283 1·297	0·765 0·773	0.661	0.
0.60	0.298	0.286	0.172	0.149	0.143	2.34	1.337	1.283	0.773	0.668	0.
0.65	0.324	0.311	0.187	0.162	0.156	2-36	1.351	1.297	0.781	0.675	Ō.
0.70	0.350	0.336	0.203	0-175	0.168	2-38	1.365	1.311	0.790	0.683	0
0.75	0.376	0.361	0.218	0-188	0.181	2-38 2-40	1.380	1.324	0·781 0·790 0·798	0.690	0-
0-80	0 403 0 430	0.387	0·233 0·248	0-201 0-215 0-228	0·193 0·206	2·42 2·44	1·394 1·408	1·338 1·352	0.806 0.814	0.697	0
0.85	0.430	0.412	0.248	0.212	0.206	2.44	1.408	1.352	0.814	0.704	Ö-
0.90	0.456	0.438	0.264	0-228	0.219	2.46	1·423 1·438	1.366	0.823 0.831	0.711	0.
0-90 0-95 1-00	0.483	0.464	0.280	0.242	0-232 0-245	2.48	1.438	1-380	0-831	0.719	0
	0.511	0.490	0.295	0.255	0.245	2.50	1.452	1.394	0.840	0.726	0.
1·05 1·10	0.538	0.517	0.311	0·269 0·283 0·297	0.258	2.52	1.467	1.408	0.848	0.734	0
1·10	0·566 0·594	0·543 0·570	0·327 0·343	0.283	0·272 0·285	2·54 2·56	1:482	1.423	0.857	0.741	0.
1·15	0.594	0.570	0.343	0.297	0.285	2.56	1.497	1.437	0.866	0.748	0.
1·20 1·25	0.622	0.597	0.359	0.311	0.298	2.58	1.512	1.451	0.874	0.756	0-
1.25	0.650	0.624	0.376	0.325	0.312	2.60	1.527	1.466	0.883	0.764	0
1·30 1·35	0.678	0.651	0·392 0·409	0·339 0·354	0·326 0·339	2·62 2·64	1.542	1·481 1·495	0.892	0·771 0·779	0
1.35	0.707	0.679	0.409	0.354	0.339	2.04	1-558	1.495	0.901	0.779	0
1.40	0.736	0.707	0.426	0.368	0.353	2.66	1.573	1.510	0.910	0.786	0.
1·45 1·50	0·765 0·795	0·735 0·763	0·443 0·460	0·383 0·397	0·367 0·382	2·68 2·70	1·588 1·604	1·525 1·540	0.919 0.928	0.794	
	0.825	0.702	0.477	0:412	0-206	2:72	1-620	1-555	0.937		
1·55 1·60	0.855	0·792 0·821	0.494	0·412 0·427	0·396 0·410	2·72 2·74	1.620 1.636	1·555 1·570	0.946		
1.65	0.885	0.850	0.512	0.443	0.425	2.76	1.651	1.585	0.955		
1.70	0.916	0.879	0.530	0.458	0.440	2.78	1-667	1-601	0 755		
1·65 1·70 1·75	0.947	0·850 0·879 0·909	0.547	0·443 0·458 0·473	0·440 0·454	2·78 2·80	1-667 1-683	1.601 1.616			
1·80 1·85 1·90	0·978 1·009	0.939	0·565 0·584	0·489 0·505 0·521	0·469 0·484	2·82 2·84	1·700 1·716 1·732	1.632 1.647			
1.85	1.009	0.969	0.584	0.505	0.484	2.84	1.716	1.647			
i∙90	1-041	1.000	0.602	0.521	0.500	2.86	1.732	1.663			
1.95	1.073	1.030	0.621	0.537	0.515	2.88	1.749	1.679			
1·95 2·00	1·073 1·106	1.000 1.030 1.062	0·621 0·640	0·537 0·553	0·515 0·531	2·88 2·90	1.766	1.663 1.679 1.695			
2·02 2·04	1·119 1·132	1.074	0·647 0·655	0·559 0·566 0·573	0·537 0·543 0·550	2·92 2·94	1·782 1·799	1.711			
2.04	1.132	1.087	0.655	0.266	0.243	2.94	1.799	1·727 1·743			
2.06	1.145	1.099	0.662	0.573	0.220	2·96 2·98	1.816	1.743			
2·08 2·10	1·159 1·172	1.112	0.670	0.579	0·556 0·562	2.98	1.833	1.760			
2.10	1.172	1.125	0.678	0.286							
2·12 2·14	1.185	1.138	0.685	0·593 0·599	0·569 0·575	i					
2.14	1.199	1.121	0.693	0.399	0.375	I					
2.16	1.212	1.164	0.701	0.606	0.282						
2.18	1.226	1.177	0.709	0.613	0.588	I					
2.20	1.239	1.190	0.717	0-620	0.393	i					

Pt = 0.955 ~1 3tep = 5: Design against Shear: Corresponding Te = 0.62 From IS-456, Table-19, Pg-73 Design Show force Vu = 157.5 KN Show force Coveried by Concrete Vuc = Tc x (bd) = 0.05 × (300 × 232) N = 99.21 X103 M Shewe force covided by Steel (shew reinforcumat SFD Vus = (Vu-Vuc) = (12 t.2-dd.21) = 24.2d KM Let provide two loged voctical stromps of 8\$ Area of two leged vertical Stivulas

 $A_{SV} = 2 \times \frac{1}{4} \times 82$

a	= 100 mm 2 from I3:456-2000, cl-40.4.a, pq-73 for vertical s = 0.87 by Asyd Sv = Specing of Stirrups
© Minimum Sheve reinforcement; From CL-26.5.1.6, IS-456:2000 ASV > 0.4 BSV > 0.8734 → SV ≤ 0.8734 → SV ≤ 300.87 mm Let provide two legal vertical Stierups of 80 born @ 300 e/c.	= 0.87×415×100×585 57.903 = 333.07 amm 6) Maximum Specing Critoria: From cl-26.5.1.5, 15-456:2000, Pg-47 Maximum Specing of Share reinforcement = min go.750l, 3007 = min gyo1.25, 3007 = 300 mm

OStep > 6: Checko:>

> Shear check: > [Pt = 1 From Table-19, IS-456:2000, Pg - 72 Corresponding Te

Nominal Shoor Strong

$$= \frac{300 \times 232}{99} = 0.381 \, \text{Mlmm}^{2}$$

From Table-20, IS-456:2000, Pg-73

Maximum Shear Stress for M-20 converts

Tenn = 2.8

Tomar > TV Hence design is late

70 = 0.62 NImm?

23.2.1 The vertical deflection limits may generally be assumed to be satisfied provided that the span to depth ratios are not greater than the values obtained as below:

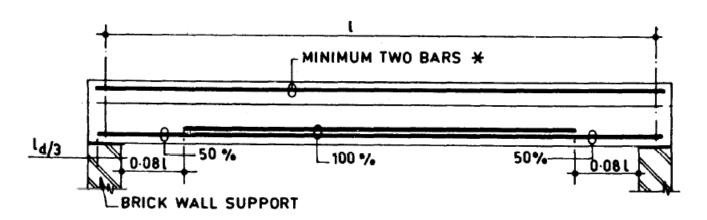
 a) Basic values of span to effective depth ratios for spans up to 10 m:

Cantilever Simply supported 20 26 Continuous

1) Deflection Check := Span = 6x103 = 11.21 Now from cl. 23.2.1, IS-456: 2000, Pg-37 3Pan = 20 for simply supported beam

1. 11.21 < 20 Hence the disign is Safe.

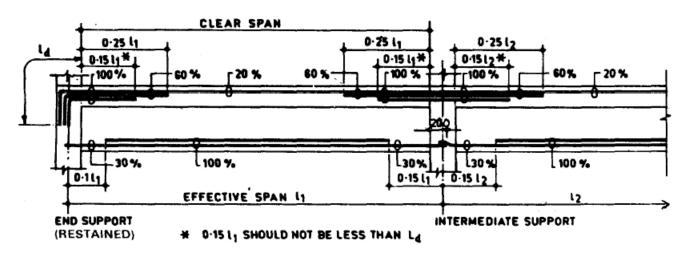
1 Summary of the design :> 300 mm Beam Size (bxD) \$ (300 x 565) mm classe cover 720 mm 5-200 Tensile Steel > 209-5mos Slivous + 8 p two leged voctical stiroups of @ 300 de



*In case partially restraint members, 35 percent of the reinforcement shall also be provided for negative moment at the support and fully anchored.

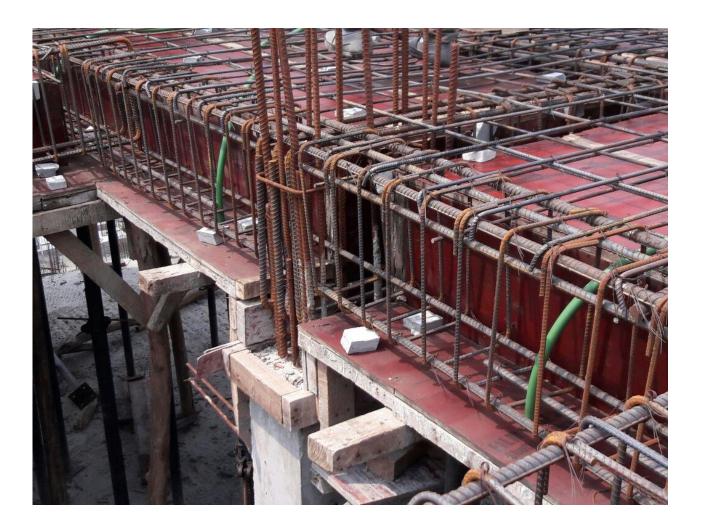
Fig. 8.16 Simplified Curtailment Rules for Simply Supported Beam

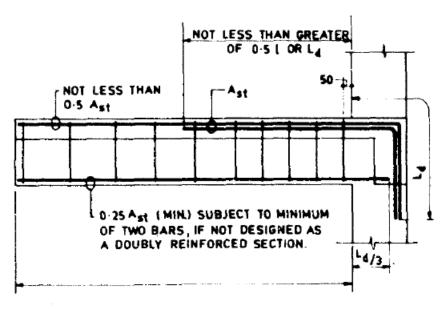
SP: 34(S&T)-1987



NOTE Applicable to continuous beams with approximately equal spans (not differing more than 15 percent) and subjected to predominantly U.D.L., and designed without compression steel.

Fig. 8.15 Simplified Curtailment Rules for Continuous Beams





8.17A CANTILEVER BEAM PROJECTING FROM A COLUMN

Fig. 8.17 Simplified Curtailment Rules for a Cantilever Beam (Continued)

SP: 34(S&T)-1987

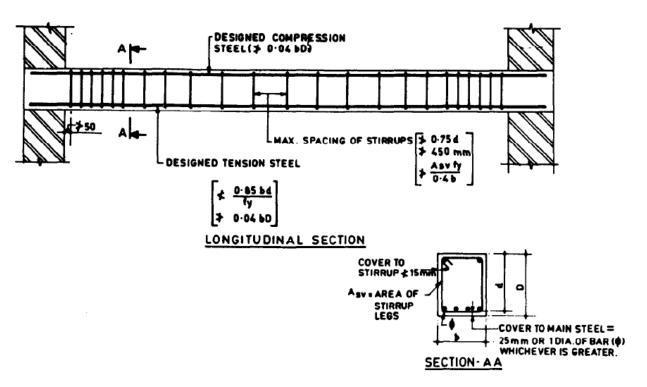


Fig. 8.11 Reinforcement Requirements for Beams

