

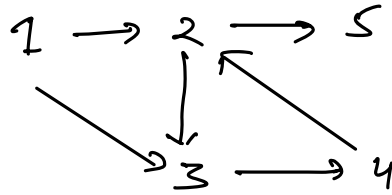
Welcome 😊

Agenda : BFS traversal
questions
Topological Sort

Breadth First Search (BFS) Traversal.

1 2 3 5 4

O/p \Rightarrow 1 2 3 5 4



code

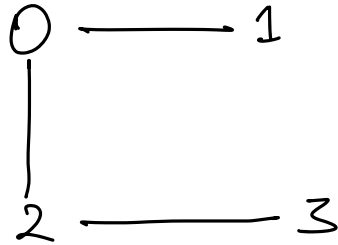
```
 $\forall i$  vst[i] = false  
for ( i  $\rightarrow$  1 to N )  
{  
    if ( ! vst[i] ) bfs(i)  
}  
  
void bfs ( node n )  
{  
    vst[n] = True  
    q.enqueue ( n )  
    while ( ! q.isEmpty() )  
    {  
        y = q.dequeue ()  
        print ( y )  
        for ( z : adj[y] )  
        {  
            if ( ! vst[z] )  
            {  
                q.enqueue ( z )  
            }  
        }  
    }  
}
```

T.C = $O(N+E)$

S.C = $O(N)$

vst[z] = True

Quiz



o/p

0 1 2 3

0 2 1 3

Q Rotten Oranges

Given a matrix of integers

0 → empty

1 → fresh orange

2 → rotten orange

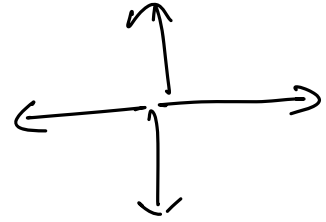
Every minute any fresh orange which is adjacent to rotten orange become rotten

In how many minutes, will all oranges become rotten? If not possible, then return -1

	0	1	2	3	4
0	1 _x	2	1 _x	0	1 _x
1	2 _x	0	0	0	2
2	0	2 _x	0	0	1 _x ²
3	0	1 _x	2	1 _x	1 _x ²

T=0

ans = 2



Multi-source BFS

(0,1) (1,4) (3,2) (0,0) (0,2) (0,4) (2,4) (3,1) (3,3) (1,0) (3,4)
~~(2,1)~~

code
 fresh 0 = 0
 min = 0

// 1. Traverse and insert rotten orange into a queue. Also keep count of fresh orange.

```
if (fresh 0 == 0) {
    return 0
}
```

```
while (!q.isEmpty()) {
    cell = q.dequeue()
```

```
    x = cell[0]
```

```
    y = cell[1]
```

```
    min = cell[2]
```

```
    for (i → 0 to 3)
```

```
    {
        newX = x + dx[i]
```

dx [-1 1 0 0]

dy [0 0 -1 1]

$new\ y = y + dy[i]$

if ($new\ x \geq 0$ && $new\ x < N$ &&
 $new\ y \geq 0$ && $new\ y < N$ &&
 $grid[new\ x][new\ y] == 1$)

{

$grid[new\ x][new\ y] == 2$

$fresh\ 0 --$

$q.enqueue(\{ new\ x, new\ y, min+1 \})$

}

}

}

return ($fresh\ 0 == 0$) ? $min : -1$

Q Elephant delivery. Find min. distance from warehouse.
 for each pincode.

	0	1	2	3	4
0	0	0	0	1	0
1	0	0	0	0	0
2	0	1	0	0	0
3	0	0	0	0	0

Same as previous question

Q Possibility of finishing course

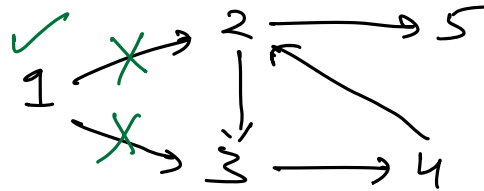
N=5

1 \rightarrow 2 & 3 (1 is pre-requisite for 2 & 3)

2 \rightarrow 3 & 5

3 \rightarrow 4

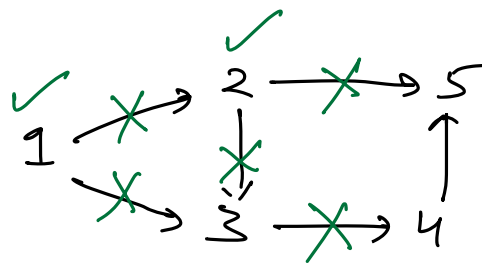
4 \rightarrow 2



NO

\Rightarrow If there is a cycle in graph, return false.
else true.

1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5



Topological Order \longrightarrow Directed Acyclic Graph

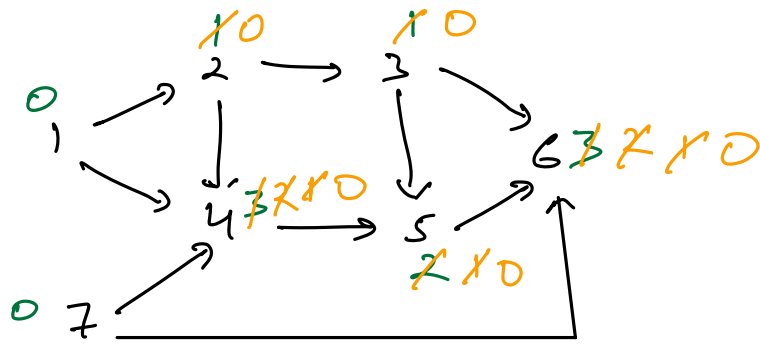
\Rightarrow linear ordering of nodes s.t if there is an edge from node $i \rightarrow j$, then i will be on the left of j

\Rightarrow Multiple topological orders can exist for graphs.



1 3 2
3 1 2

Code



~~1~~ ~~2~~ ~~3~~ ~~4~~ ~~5~~ ~~6~~ ~~7~~

O/p \Rightarrow 1 7 2 3 4 5 6

Code

Compute indegree

1. Insert all nodes in queue with indegree 0
2. \forall degree, visit all neighbour and update indegree (reduce by 1)
3. If updated indegree of any node becomes zero, insert it into queue and repeat step 2 & 3 till queue is empty.

$$T.C = O(N+E)$$

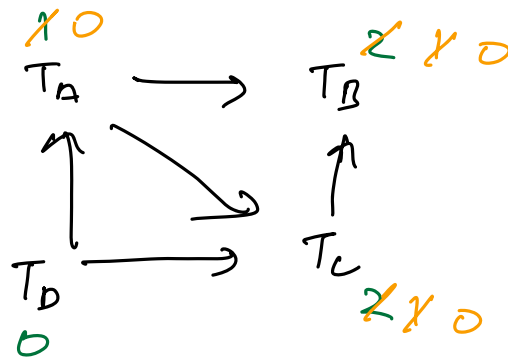
$$S.C = O(N)$$

Topological sort (Right to left)

Topological sort can end if
outdegree = 0 for that node.

→ length of adj. list.

⇒ print it in reverse order



$T_D \quad T_A \quad T_C \quad T_B$

⇒ BFS leads to the shortest path to destination.