

Assignment - 1

Student Information:

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Input:

n : number of points

next 2 x n lines for X and Y coordinates of each point

Output:

Area under a curve formed by joining successive points by a straight line

Approach:

Design:

- User enters number of points
- For each point user enters x coordinate and y coordinate
- User is notified each time :
 1. index of current point
 2. whether he is entering x coordinate or y coordinate
 3. area calculated so far so that user can deduce if something is wrong like negative area due to overflow without needing to enter large number of points
- Final area is printed
- For bad n values program is terminated with custom message
- Program termination message to avoid confusion

Workflow:

- Take number of points as input and store it in \$t0 register and **points** memory location
- if number of points is less than 1 then input is invalid and **badterminate** branch is executed
- if number of points is 1 then area is outputed as 0
- else all n integers are taken input and area calculated till that point is also shown for better experience
- finally **terminate** branch is executed, total area is shown and program is terminated

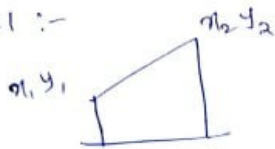
Area Calculation:

- Area of complete polynomial formed using n points can be broken into n-1 trapeziums with 2 sides parallel to y axis and 1 side parallel to x axis.
- Area is calculated in absolute values. Area below x-axis is negated to get positive area

- Any general case can be divided into 4 cases. Each area can be calculated individually and added to get area final

Area calculation:-

Case 1:-



$$y_1 > 0 \quad y_2 > 0$$

Area of trapezium =

$$\frac{h \times (a+b)}{2}$$

$$= \frac{(x_2 - x_1) \times (y_1 + y_2)}{2}$$

Case 2:-



$$y_1 < 0 \quad y_2 < 0$$

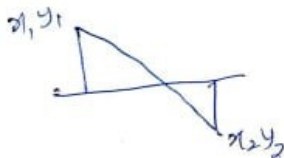
$$\text{Area} = \frac{(x_2 - x_1) \times (y_1 - y_2)}{2}$$

but $(y_1 + y_2) < 0$

hence area is negative

to make it positive $\text{Area} = \frac{(x_2 - x_1) \times (-y_1 - y_2)}{2}$

Case 3:-



$$y_1 > 0 \quad y_2 < 0$$

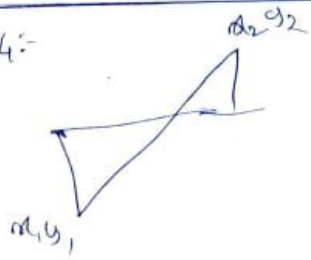
$$\text{Area} = \frac{(x_2 - x_1) \times y_1}{y_1 - y_2} + \frac{(x_2 - x_1) \times (-y_2)}{y_1 - y_2}$$



$$= \frac{1}{2} \times y_1 \times \frac{x_2 - x_1}{y_1 - y_2} + \frac{1}{2} \times \frac{x_2 - x_1}{y_1 - y_2} \times y_2^2$$

$$= \frac{(y_1^2 + y_2^2) \times (x_2 - x_1)}{y_1 - y_2 \times 2}$$

Case 4:-



reverse the y coordinates by ± 1 . Area remains same



And use formula for case 3. And replace $-y_1, -y_2$ with y_1, y_2 again for next iteration.

Registers used:

- t0 = No of points
- t1 = iterator for "for-loop"

- $t3 = X_{prev}$
 - $t4 = Y_{prev}$
 - $t5 = X_{curr}$
 - $t6 = Y_{curr}$
 - $f4$ = area so far
 - $t7, t8$ = temporary addition, subtractions
 - $f6, f8$ = temporary products which are large
-

Testing:

1. Bad number of inputs:

```
Enter number of points: -2
Bad number of points!
Number of Points must be greater than 0...
Program Terminated|
```

- ```
Enter number of points: 0
Bad number of points!
Number of Points must be greater than 0...
Program Terminated|
```
- 

### 2. With single point:

Area of single point is 0 irrespective of its x and y coordinates

```
Enter number of points: 1
Final calculated Area is : 0
Program Terminated
```

### 3. With 2 points such that positive area = negative area:

3 points at  $(-10000, -10000)$ ,  $(0, 0)$ ,  $(10000, 10000)$ .  $Area1 = Area2$ . Hence,  $Area = Area1 + Area2 = \frac{1}{2} * 10000 * 10000 * 2 = 50000000 * 2 = 100000000$

```
Enter number of points: 3
Enter Data for point no. 1
X coordinate : -10000
Y coordinate : -10000
Area so far : 0
Enter Data for point no. 2
X coordinate : 0
Y coordinate : 0
Area so far : 500000000
Enter Data for point no. 3
X coordinate : 10000
Y coordinate : 10000
Area so far : 1000000000
Final calculated Area is : 1000000000
Program Terminated
```

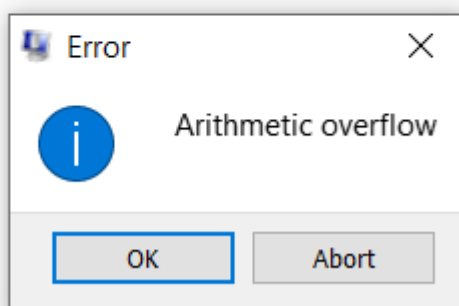
#### 4. With Large X and Y coordinate to check overflow:

Works till  $10^8$  x and y range. When  $y^2$  crosses 64-bit limit overflow occurs

```
Enter number of points: 2
Enter Data for point no. 1
X coordinate : -1000000000
Y coordinate : -1000000000
Area so far : 0
Enter Data for point no. 2
X coordinate : 1000000000
Y coordinate : 1000000000
Area so far : 1e+018
Final calculated Area is : 1e+018
Program Terminated
```

When  $y^2$  crosses 64-bit limit overflow occurs

```
Enter number of points: 2
Enter Data for point no. 1
X coordinate : -2000000000
Y coordinate : -2000000000
Area so far : 0
Enter Data for point no. 2
X coordinate : 2000000000
Y coordinate : 2000000000
```



#### 5. Points with same X coordinate:

for same x coordinate width of curve is 0 hence area should be 0 irrespective of height

```
Enter number of points: 2
Enter Data for point no. 1
X coordinate : 0
Y coordinate : 100
Area so far : 0
Enter Data for point no. 2
X coordinate : 0
Y coordinate : -100
Area so far : 0
Final calculated Area is : 0
Program Terminated
```

#### 6. Decimal area:

2 points at (0,0), (69,89). Area =  $(69-0) \cdot (89+0) / 2 = 69 \cdot 89 / 2 = 6141 / 2 = 3070.5$

```
Enter number of points: 2
Enter Data for point no. 1
X coordinate : 0
Y coordinate : 0
Area so far : 0
Enter Data for point no. 2
X coordinate : 69
Y coordinate : 89
Area so far : 3070.5
Final calculated Area is : 3070.5
Program Terminated
```

#### 7. Random numbers:

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```
Enter number of points: 10
Enter Data for point no. 1
X coordinate : 4
Y coordinate : -6
Area so far : 0
Enter Data for point no. 2
X coordinate : 5
Y coordinate : 10
Area so far : 4.25
Enter Data for point no. 3
X coordinate : 6
Y coordinate : 15
Area so far : 16.75
Enter Data for point no. 4
X coordinate : 7
Y coordinate : 13
Area so far : 30.75
Enter Data for point no. 5
X coordinate : 8
Y coordinate : -16
Area so far : 38.077586206896555
Enter Data for point no. 6
X coordinate : 10
Y coordinate : 23
Area so far : 58.205791335101679
Enter Data for point no. 7
X coordinate : 15
Y coordinate : 100
Area so far : 365.70579133510171
Enter Data for point no. 8
X coordinate : 16
Y coordinate : -3
Area so far : 414.29316997587841
Enter Data for point no. 9
X coordinate : 17
Y coordinate : 5
Area so far : 416.41816997587841
Enter Data for point no. 10
X coordinate : 20
Y coordinate : 20
Area so far : 453.91816997587841
Final calculated Area is : 453.91816997587841
Program Terminated
```

