

# 3D Shearing in Computer Graphics | Definition | Examples

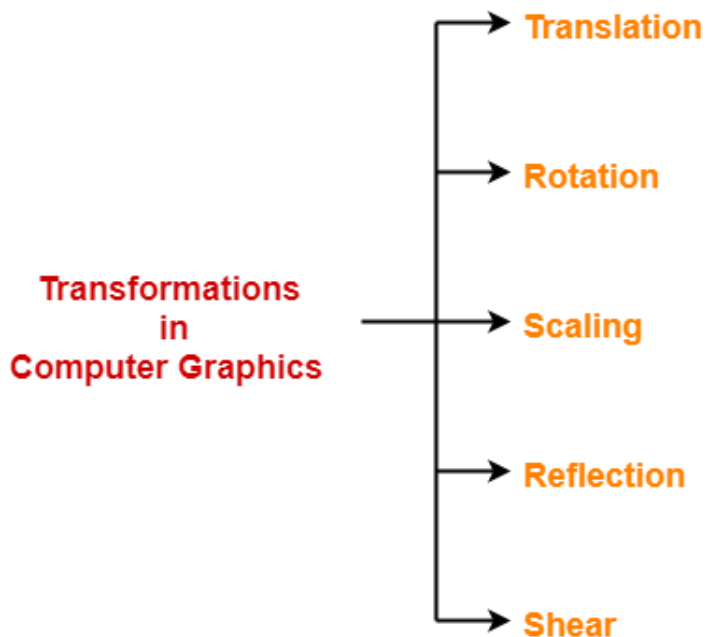
📁 Computer Graphics

## 3D Transformations in Computer Graphics-

We have discussed-

- Transformation is a process of modifying and re-positioning the existing graphics.
- 3D Transformations take place in a three dimensional plane.

In computer graphics, various transformation techniques are-



1. Translation
2. Rotation
3. Scaling
4. Reflection
5. Shear

In this article, we will discuss about 3D Shearing in Computer Graphics.

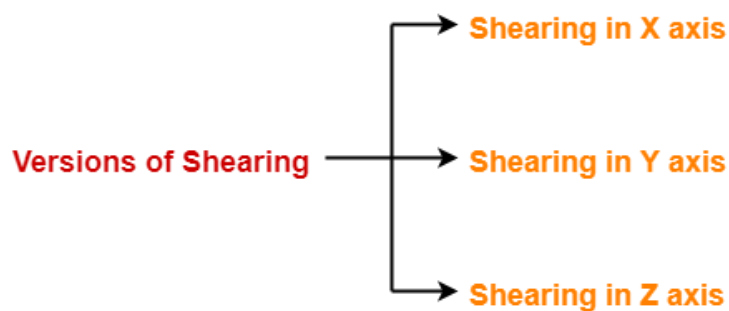
## 3D Shearing in Computer Graphics-

In Computer graphics,

3D Shearing is an ideal technique to change the shape of an existing object in a three dimensional plane.

In a three dimensional plane, the object size can be changed along X direction, Y direction as well as Z direction.

So, there are three versions of shearing-



1. Shearing in X direction
2. Shearing in Y direction
3. Shearing in Z direction

Consider a point object O has to be sheared in a 3D plane.

Let-

- Initial coordinates of the object  $O = (X_{old}, Y_{old}, Z_{old})$
- Shearing parameter towards X direction =  $Sh_x$

- Shearing parameter towards Y direction =  $Sh_y$
- Shearing parameter towards Z direction =  $Sh_z$
- New coordinates of the object O after shearing =  $(X_{new}, Y_{new}, Z_{new})$

### Shearing in X Axis-

Shearing in X axis is achieved by using the following shearing equations-

- $X_{new} = X_{old}$
- $Y_{new} = Y_{old} + Sh_y \times X_{old}$
- $Z_{new} = Z_{old} + Sh_z \times X_{old}$

In Matrix form, the above shearing equations may be represented as-

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ Sh_y & 1 & 0 & 0 \\ Sh_z & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

**3D Shearing Matrix**  
(In X axis)

### Shearing in Y Axis-

Shearing in Y axis is achieved by using the following shearing equations-

- $X_{new} = X_{old} + Sh_x \times Y_{old}$
- $Y_{new} = Y_{old}$
- $Z_{new} = Z_{old} + Sh_z \times Y_{old}$

In Matrix form, the above shearing equations may be represented as-

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & Sh_x & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & Sh_z & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

**3D Shearing Matrix**  
(In Y axis)

### Shearing in Z Axis-

Shearing in Z axis is achieved by using the following shearing equations-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Z_{\text{old}}$
- $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times Z_{\text{old}}$
- $Z_{\text{new}} = Z_{\text{old}}$

In Matrix form, the above shearing equations may be represented as-

$$\begin{bmatrix} X_{\text{new}} \\ Y_{\text{new}} \\ Z_{\text{new}} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & Sh_x & 0 \\ 0 & 1 & Sh_y & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X_{\text{old}} \\ Y_{\text{old}} \\ Z_{\text{old}} \\ 1 \end{bmatrix}$$

**3D Shearing Matrix**  
(In Z axis)

### PRACTICE PROBLEMS BASED ON 3D SHEARING IN COMPUTER GRAPHICS-

## **Problem-01:**

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

## **Solution-**

Given-

- Old corner coordinates of the triangle = A (0, 0, 0), B(1, 1, 2), C(1, 1, 3)
- Shearing parameter towards X direction ( $Sh_x$ ) = 2
- Shearing parameter towards Y direction ( $Sh_y$ ) = 2
- Shearing parameter towards Z direction ( $Sh_z$ ) = 3

## **Shearing in X Axis-**

### **For Coordinates A(0, 0, 0)**

Let the new coordinates of corner A after shearing = ( $X_{new}$ ,  $Y_{new}$ ,  $Z_{new}$ ).

Applying the shearing equations, we have-

- $X_{new} = X_{old} = 0$
- $Y_{new} = Y_{old} + Sh_y \times X_{old} = 0 + 2 \times 0 = 0$
- $Z_{new} = Z_{old} + Sh_z \times X_{old} = 0 + 3 \times 0 = 0$

Thus, New coordinates of corner A after shearing = (0, 0, 0).

**For Coordinates B(1, 1, 2)**

Let the new coordinates of corner B after shearing =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} = 1$
- $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times X_{\text{old}} = 1 + 2 \times 1 = 3$
- $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times X_{\text{old}} = 2 + 3 \times 1 = 5$

Thus, New coordinates of corner B after shearing = (1, 3, 5).

**For Coordinates C(1, 1, 3)**

Let the new coordinates of corner C after shearing =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} = 1$
- $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times X_{\text{old}} = 1 + 2 \times 1 = 3$
- $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times X_{\text{old}} = 3 + 3 \times 1 = 6$

Thus, New coordinates of corner C after shearing = (1, 3, 6).

Thus, New coordinates of the triangle after shearing in X axis = A (0, 0, 0), B(1, 3, 5), C(1, 3, 6).

**Shearing in Y Axis-****For Coordinates A(0, 0, 0)**

Let the new coordinates of corner A after shearing =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Y_{\text{old}} = 0 + 2 \times 0 = 0$
- $Y_{\text{new}} = Y_{\text{old}} = 0$
- $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times Y_{\text{old}} = 0 + 3 \times 0 = 0$

Thus, New coordinates of corner A after shearing = (0, 0, 0).

### **For Coordinates B(1, 1, 2)**

Let the new coordinates of corner B after shearing =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Y_{\text{old}} = 1 + 2 \times 1 = 3$
- $Y_{\text{new}} = Y_{\text{old}} = 1$
- $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times Y_{\text{old}} = 2 + 3 \times 1 = 5$

Thus, New coordinates of corner B after shearing = (3, 1, 5).

### **For Coordinates C(1, 1, 3)**

Let the new coordinates of corner C after shearing =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Y_{\text{old}} = 1 + 2 \times 1 = 3$
- $Y_{\text{new}} = Y_{\text{old}} = 1$
- $Z_{\text{new}} = Z_{\text{old}} + Sh_z \times Y_{\text{old}} = 3 + 3 \times 1 = 6$

Thus, New coordinates of corner C after shearing = (3, 1, 6).

Thus, New coordinates of the triangle after shearing in Y axis = A (0, 0, 0), B(3, 1, 5), C(3, 1, 6).

## **Shearing in Z Axis-**

### **For Coordinates A(0, 0, 0)**

Let the new coordinates of corner A after shearing = ( $X_{\text{new}}$ ,  $Y_{\text{new}}$ ,  $Z_{\text{new}}$ ).

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Z_{\text{old}} = 0 + 2 \times 0 = 0$
- $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times Z_{\text{old}} = 0 + 2 \times 0 = 0$
- $Z_{\text{new}} = Z_{\text{old}} = 0$

Thus, New coordinates of corner A after shearing = (0, 0, 0).

### **For Coordinates B(1, 1, 2)**

Let the new coordinates of corner B after shearing = ( $X_{\text{new}}$ ,  $Y_{\text{new}}$ ,  $Z_{\text{new}}$ ).

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Z_{\text{old}} = 1 + 2 \times 2 = 5$



- $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times Z_{\text{old}} = 1 + 2 \times 2 = 5$
- $Z_{\text{new}} = Z_{\text{old}} = 2$

Thus, New coordinates of corner B after shearing = (5, 5, 2).

### **For Coordinates C(1, 1, 3)**

Let the new coordinates of corner C after shearing =  $(X_{\text{new}}, Y_{\text{new}}, Z_{\text{new}})$ .

Applying the shearing equations, we have-

- $X_{\text{new}} = X_{\text{old}} + Sh_x \times Z_{\text{old}} = 1 + 2 \times 3 = 7$
- $Y_{\text{new}} = Y_{\text{old}} + Sh_y \times Z_{\text{old}} = 1 + 2 \times 3 = 7$
- $Z_{\text{new}} = Z_{\text{old}} = 3$

Thus, New coordinates of corner C after shearing = (7, 7, 3).

Thus, New coordinates of the triangle after shearing in Z axis = A (0, 0, 0), B(5, 5, 2), C(7, 7, 3).

To gain better understanding about 3D Shearing in Computer Graphics,

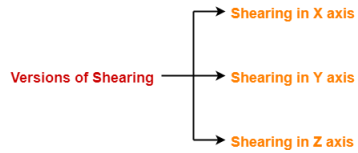
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## Summary



**Article Name** 3D Shearing in Computer Graphics  
| Definition | Examples

**Description** 3D Shearing in Computer Graphics  
is a process of modifying the  
shape of an object in 3D plane.  
Shearing Transformation in  
Computer Graphics Definition,  
Solved Examples and Problems.

**Author** Akshay Singhal

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