

## Quiz 2

Consider a two qubit state  $|\psi\rangle = \frac{1}{2} \begin{pmatrix} 1 \\ -1 \\ -1 \\ 1 \end{pmatrix}$ ;  $\rho_A = \text{Tr}_B(|\psi\rangle\langle\psi|)$ ;  $\rho_B = \text{Tr}_A(|\psi\rangle\langle\psi|)$

Then

- ☒ a.  $\text{Tr}(\rho_A \log_2 \rho_A) = \text{Tr}(\rho_B \log_2 \rho_B) = 0$
- ☐ b. None of the above
- ☐ c.  $\text{Tr}(\rho_A \log_2 \rho_A) = \text{Tr}(\rho_B \log_2 \rho_B) = 1$
- ☐ d.  $\text{Tr}(\rho_A \log_2 \rho_A) = 0 \neq \text{Tr}(\rho_B \log_2 \rho_B)$

Consider  $P = \frac{1}{2} \sum_{i=0}^{n-1} \sum_{k=0, k \neq i}^{n-1} |\phi\rangle\langle\phi|$ ; where  $|\phi\rangle = |ik\rangle - |ki\rangle$  and  $|ik\rangle = |i\rangle \otimes |k\rangle$   
then

- ☒ a.  $P^2 = \frac{P}{2}$
- ☐ b.  $P^* = -P$
- ☐ c.  $P = -P^+$
- ☐ d.  $P^2 = P$

Consider  $\rho_w = r|\psi\rangle\langle\psi| + \frac{1-r}{4}\mathbf{I}_4$ ;  $|\psi\rangle = \frac{1}{\sqrt{2}}(1, 0, 0, 1)^T$  and

$\mathbf{I}_4$ =Identity matrix of 4 dimension.  $0 \leq r \leq 1$ .

$\rho_w$  is entangled if

- ☐ a.  $r > 0$
- ☒ b.  $r > \frac{1}{3}$
- ☐ c. independent of  $r$
- ☐ d.  $r > \frac{1}{4}$

Consider the following operations:

$$\begin{vmatrix} \rho_{11} & \rho_{12} & \rho_{13} \\ \rho_{21} & \rho_{22} & \rho_{23} \\ \rho_{31} & \rho_{32} & \rho_{33} \end{vmatrix} \rightarrow \begin{vmatrix} \rho_{33} & \rho_{23} & \rho_{13} \\ \rho_{32} & \rho_{22} & \rho_{12} \\ \rho_{31} & \rho_{21} & \rho_{11} \end{vmatrix}$$

The operation is

- ☐ a. Not Hermitian
- ☐ b. Completely Positive
- ☐ c. Completely negative
- ☒ d. Positive not completely positive