

Assignment-3

- ① We take one element of each list and put it in a min-heap. Along with each element we have to track which list we took it from.

While merging, we take the minimum element from the heap and insert another element off the list it came from (unless the list is empty). We continue until we empty the heap.

We have n steps and at each step we are doing an insertion into the heap, which is $\lg K$.

Problem 6.2

- (a) A d -ary heap can be implemented using a dimensional array as follows. The root is kept in $A[1]$, its d children are kept in order in $A[2]$ through $A[d+1]$ and so on. The procedures to map a node with index i to its parent and its j th child are given by:

D-ARY PARENT(i)
return $\lceil (i-2)/d + 1 \rceil$

D-ARY CHILD(i, j)
return $d(i-1) + j + 1$

- (b) Since each node has d children the height of the tree is $\Theta(\log_d n)$.
- (c) The Heap-Extract-Max algorithm given in the text

works fine for d -ary heaps; the problem is MAX-HEAPIFY. Here we need to compare the argument node to all its children. This takes $\Theta(d \log_d n)$ and dominates the overall time spent by HEAP-EXTRACT-MAX.

(d) The MAX-HEAP-INSERT given in the text works fine as well. The worst case running time is the height of the heap, that is $\Theta(\log_d n)$.

~~(e) The HEAP-INCREASE-KEY algorithm given in the text works fine.~~

(e) D-ARY-HEAP-INCREASE-KEY(A, i, k)
 $A[i] \leftarrow \max(A[i], k)$
 while $i > 1$ and $A[\text{PARENT}(i)] < A[i]$
 do exchange $A[i] \leftrightarrow A[\text{PARENT}(i)]$
 $i \leftarrow \text{PARENT}(i)$