

Lab 1 tutorial Longitudinal Dynamics – Slip Control

SD2231 – Applied vehicle dynamics control

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1 Introduction

The following laboratory assignment is intended to give you knowledge and experience in the area of longitudinal control of rail and road vehicles. More specifically, the focus will be on controlling the wheel behaviour during operation, and thus increasing the stability of the wheel as well as acceleration and braking performance of the vehicle.

2 Theory

2.1 Slip control

Traction and braking forces of ground vehicles (here passenger cars and trains) are transferred from the wheel through the contact patch onto the ground, which can be a road or a rail. Each wheel can be categorised into a driven or non-driven wheel. The driven wheel is connected to the motor of the vehicle and experiences its demanded tractive torque. If a torque is applied for acceleration or coasting at a certain speed, it leads to the effect that the wheel spins with a higher speed than the longitudinal speed of the vehicle. Thus, the driven wheel does not roll, but actually rotates faster than the corresponding longitudinal velocity of the vehicle. A non-driven wheel is free-rolling and rotates with the same speed as the vehicle. Brakes are usually found on every wheel. During braking the wheel rotates at a slower speed that the longitudinal speed of the vehicle.

This difference in speed between the wheel speed and longitudinal vehicle speed is described as the slip of the wheel. Depending on the driving condition, tractive slip s_t and braking slip s_b can be distinguished:

$$s_t = \frac{r\omega - v_x}{r\omega}$$
 and $s_b = \frac{v_x - r\omega}{v_x}$ (1)

where r = wheel radius, $\omega =$ rotational speed of the wheel and $v_x =$ longitudinal speed of the vehicle. A qualitative slip curve of a rubber tyre including the maximum and dynamic friction coefficient (μ_{max} and μ_d) and the critical slip s_{crit} is shown in Figure 1. The maximum friction coefficient is reached at 10-20 % slip, depending on various tyre parameters (e.g. tyre pressure, rubber compound, thread, etc.), vehicle parameters (toe angle, camber angle, vehicle speed, etc.) and external factors (temperature, road surface, type of asphalt, etc.). Examples of slip curves are seen in Figure 2 for a road vehicle. The deviating characteristic of the brake slip for snow can be explained by snow piling up in front of the tyre like a wedge.

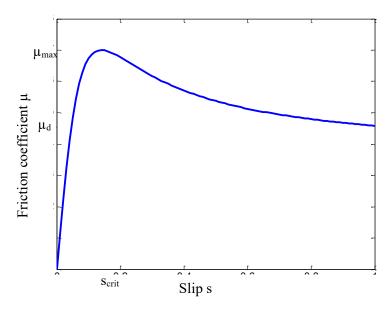


Figure 1. Qualitative slip curve of a typical rubber tyre of a passenger car.

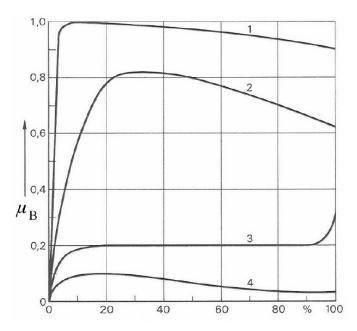


Figure 2. Typical brake slip curves of a rubber tyre for different road conditions: 1. Dry road, 2. Wet road, 3. Snowy road and 4. Icy road.

To find the used friction value μ for the front and the rear axle of a vehicle one can use Equation 2 and 3 respectively.

$$\mu_f = \frac{F_{xf}}{N_f} = \frac{F_{xf}}{(1 - \lambda)m \cdot g \cdot \cos \alpha + \kappa (F_{xf} + F_{xr})}$$
 (2)

$$\mu_r = \frac{F_{xr}}{N_r} = \frac{F_{xr}}{\lambda \cdot m \cdot g \cdot \cos \alpha - \kappa (F_{xf} + F_{xr})}$$
 (3)

Where F_{xf} and F_{xr} is the tractive or braking force on the front and rear axle respectively, λ is the ratio for CoG placement with regards to the wheel base L, α is the road inclination and $\kappa = h/L$ is the CoG height over wheel base ratio.

Rail vehicles have no rubber tyres, but a metal to metal contact patch. As explained before, slip is necessary for the force transfer of the wheel. The slip is created due to the massive weight of the rail vehicle. Both, the wheel and the rail expand and counteracts in different regions when the wheel is driven. Examples of slip curves are seen in Figure 3 for a rail vehicle.

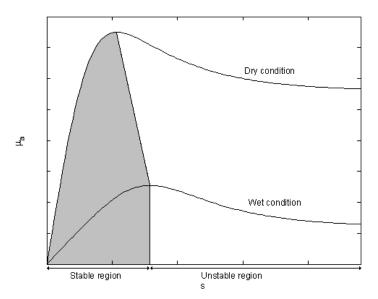


Figure 3. Brake slip curve of a rail vehicle for different rail conditions.

The aim of slip control is to keep the slip in a certain range during acceleration and braking in order to achieve the maximum traction and steer-ability of the vehicle. Special focus has to be given to braking manoeuvres.

If the braking torque on the wheel is too high, the wheel will lock and start sliding. Due to the dependency of longitudinal and lateral tyre forces (friction circle), a locked wheel will not be able to build up any lateral force. The longitudinal force utilises the dynamic friction coefficient at 100% brake slip, which is lower than the maximum friction coefficient, and therefore the stopping distance will also be longer. Thus, in order to prevent the wheel from locking, an anti-lock braking system (ABS) is used. It controls the relative slip of the wheels during braking to prevent wheel lock-up.

A typical case of a spinning wheel during acceleration is found on low friction ground, such as icy roads. The wheel starts spinning faster than the vehicle is moving forward, leading to a loss of the lateral tyre force and smaller longitudinal tyre force. A traction control system (TCS) is applied in order to utilize the available adhesion effectively and prevent high tractive slip values. Both systems help also to reduce the wear of a tyre or a wheel.

The following challenges for the slip control have to be considered:

- Detection of the slip on the wheel.
- Control of the slip within certain thresholds.

- Handling the issue of division by zero in the slip equations.
- Ensure that the tradition control and ABS is only activated when it should.

Anti-lock braking system

ABS was introduced in 1978 as the first active chassis system in passenger cars. The basic objective is to prevent the wheel from locking while braking by modulation of the brake pressure; i.e. braking just as much that the slip ranges in the area of the critical slip where a maximum force can be transferred, see Figure 4. Besides reaching a shorter stopping distance, the main advantage is the steerability during braking. Each wheel is controlled individually in order to utilise the available friction potentials at their optima.

A major practical challenge of the ABS is that wheel slip cannot be measured with inexpensive sensors on a passenger vehicle. Often the only measurements available are those for the rotational speeds at each wheel. Longitudinal speed has to be determined within algorithms in order to calculate the actual slip values for each wheel.

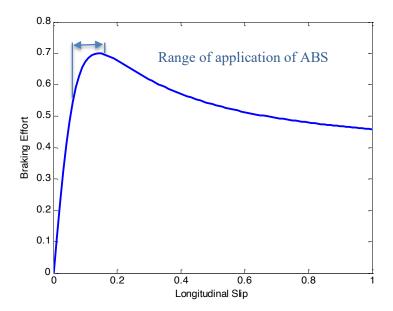


Figure 4. A typical slip curve of a braked wheel.

2.2 Control Theory

There are different control strategies which could be used for slip control. PID control, neural networks and fuzzy logic are some of the methods. Here the focus will be on the PID controller for controlling the slip.

2.2.1 PID Control

PID control is by far the most common way of using feedback in natural and man-made systems. It is a simple three term controller composed of a proportional, integral and derivative term where the transfer function of the most basic form of PID controller is;

$$C(s) = K_P + \frac{K_I}{s} + sK_D \tag{4}$$

Where K_P , K_I and K_D are proportional, integral and derivative gains respectively.

The controller could be implemented into system in different structure (output feedback, error feedback and so on). In Figure 5 the error feedback structure is demonstrated. Where "u" is control or input signal, "Y" is output or measured signal and "R" is reference or command signal.

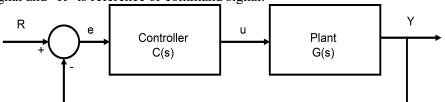


Figure 5. Sample of a closed loop control.

Generally, in this context the role of the PID-controller is to regulate the wheel slip and thereby the use of the adhesive force. A control method can be formulated by examining the adhesion characteristics. This can be done by choosing a reference slip and use this as a control signal. From the characteristics of the slip curve it is easy to observe that different slip implies different optimums of the adhesive force. The reason is that the adhesion coefficient differs between dry, wet and icy road, see Figure 2.

A PID controller takes control action based on past, present and prediction of future control errors and tries to minimize the error. However, in the absence of a feed forward term, the output never reaches the reference and hence we are left with non-zero steady state error.

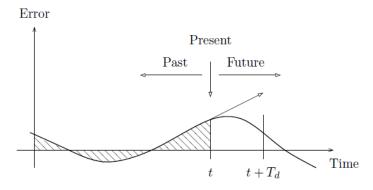


Figure 6. Formation of control signal, **u**, from the error, **e**.

The ideal version of the PID controller is given by the formula;

$$u(t) = k_p \cdot e(t) + k_i \cdot \int_0^t e(\tau) \cdot d\tau + k_d \frac{e(t)}{dt}$$
 (5)

Where u is the control signal and e is the control (tracking) error (e = R - Y), which is sent to the PID controller. The reference value (R) is also called the setpoint. The control signal is thus a sum of three terms: a proportional term that is proportional to the error, an integral term that is proportional to the integral of the error, and a derivative term that is proportional to the derivative of the error.

The proportional part acts on the present value of the error, the integral represents an average of past errors and the derivative can be interpreted as a prediction of future errors based on linear extrapolation, Figure 6.

The controller can also be parameterized as:

$$u(t) = k_p \cdot \left(e(t) + \frac{1}{T_i} \cdot \int_0^t e(\tau) \cdot d\tau + T_d \frac{de(t)}{dt} \right)$$
 (6)

where T_i is the integral time constant and T_d is the derivative time constant.

2.2.2 Designing and tuning the PID controller

We are most interested in four major characteristics of the closed-loop step response, Figure 7. They are;

- 1. Rise Time (t_r) : the time it takes for the plant output to rise beyond 90% of the desired level for the first time (0%-100% for underdamped second order systems, 5%-95% for critically damped and 10%-90% for over damped systems).
- 2. Overshoot: how much the peak level is higher than the steady state.
- 3. Settling Time (t_s) : the time it takes for the system to converge to its steady state
- 4. <u>Steady-state error</u>: the difference between the steady-state output and the desired output.

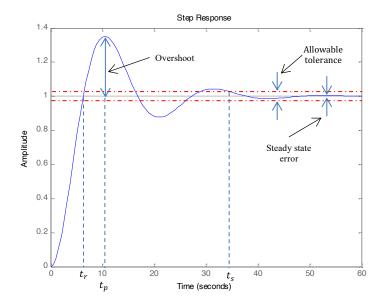


Figure 7. Characteristics of the closed-loop step response.

Generally, a proportional controller (K_P) will reduce the rise time but never eliminate the steady-state error. An integral control (K_I) will eliminate the steady-state error for a constant or step input, but it may make the transient response slower. A derivative control (K_D) increases the stability of the system, reducing the overshoot, and improving the transient response.

The effects of increasing each of the controller parameters K_P , K_I and K_D on system characteristics can be summarized in Table 1.

Response	Rise Time	Overshoot	Settling Time	S-S Error
K_P	Decrease	Increase	Small Change	Decrease
K_{I}	Decrease	Increase	Increase	Eliminate
V	Small Change	Decrease	Decrease	No Change

Table 1. Relation between controller parameters and system characteristics.

Note that these correlations might not be explicitly show the overall behaviour of the system after applying the individual parameter change, because K_P , K_I and K_D are dependent on each other. In fact, changing one of these variables can change the effect of the other two. For this reason, the table should only be used as a reference for determining the values for K_P , K_I and K_D . Typical step response of a system affected by different controller is depicted in Figure 8.

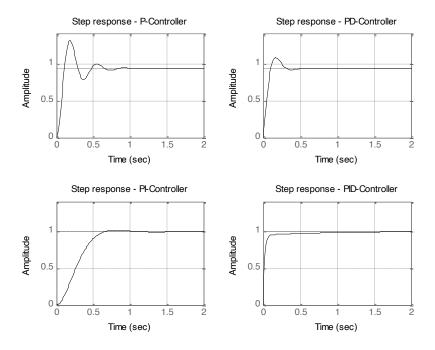


Figure 8. Step responses for different controllers.

Typical steps for designing a PID controller could be listed as following:

- 1. Obtain an open-loop response and determine what needs to be improved.
- 2. Determine what characteristics of the system need to be improved.
- 3. Use K_P to improve the rise time.
- 4. Use K_D to reduce the overshoot and settling time.
- 5. Use K_I to eliminate the steady-state error.
- 6. Adjust each of K_P , K_I and K_D until you obtain a desired overall response. You can always refer to the table shown earlier find out which controller controls what characteristics.

Finally, please keep in mind that you do not need to implement all three controllers (proportional, derivative, and integral) into a single system, if not necessary. For example, if a PI controller gives a good enough response, then you don't need to implement a derivative controller on the system. Keep the controller as simple as possible.

2.2.3 Estimating PID parameters

There are predefined and well-known methods for deciding the values of the PID controllers. However, the most popular methods were given by Ziegler and Nichols (1942), Astrom and Hagglund (1984), and more recently Zhuang and Atherton (1993) and Luyben and Eskinat (1994). Different tuning methods are

due to different control objectives such as reference following and disturbance rejection, and different plants like first-order and second-order models.

Ziegler-Nichols is useful when there is no mathematical relation available for the system. This method is based on experiments and proposed rules for determining initial values of K_P , K_I and K_D based on the transient step response of a plant. It applies to plants whose unit-step response resembles an S-shaped curve with no overshoot where the system doesn't have any complex poles. This S-shaped curve is called the reaction curve, Figure 9.

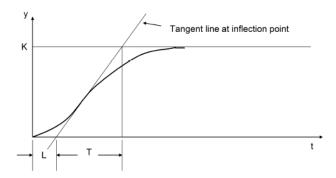


Figure 9. Reaction curve.

The S-shaped reaction curve can be characterized by two constants, delay time L and time constant T, which are determined by drawing a tangent line at the inflection point of the curve and finding the intersections of the tangent line with the time axis and the steady-state level line.

Using the parameters L and T, we can set the values of K_P , K_I and K_D according to the table below.

Controller	K_P	K_I	K_D
P	$\frac{T}{L}$	0	0
PI	$0.9 \frac{T}{L}$	$0.27 \; \frac{T}{L^2}$	0
PID	$1.2 \frac{T}{L}$	$0.6 \; \frac{T}{L^2}$	0.6 <i>T</i>

Table 2. Parameter identification using Ziegler-Nichols method

These parameters will typically give a response with an overshoot about 25% and good settling time. We may then start fine-tuning the controller using the basic rules that relate each parameter to the response characteristics.

2.3 Frequency analysis

The frequency response method of controller design has certain advantages, especially in real-life situations such as modelling transfer functions from physical data.

2.3.1 Nyquist stability criterion

This is a unique method for determining stability of a closed loop system. A closed loop system is stable if all of the closed loop poles are in the left half of the s-plane. That's a very basic fact about a system. Using this technique, it is possible to get information about closed loop pole location by plotting open loop frequency response data.

In order to understand the Nyquist stability criterion, having a perception of what a Nyquist plot is necessary. A Nyquist plot is a plot of the magnitude of the amplitude gain and phase shift of a system for sinusoidal inputs. Furthermore, it is a map of the $j\omega$ -axis in the s-plane using a transfer function, G(s), as the mapping function.

The Nyquist plot allows us to predict the stability and performance of a closed-loop system by observing its open-loop behaviour. The Nyquist criterion can be used for design purposes regardless of open-loop stability (remember that the Bode design methods assume that the system is stable in open-loop and when we try to determine the close loop stability of an unstable open loop plant with Bode, we might possibly come with wrong answers). Therefore, we use this criterion to determine closed-loop stability when the Bode plots display confusing information.

3 Assignment

3.1 Simulation setup

The simulation model in this assignment is based on Matlab/Simulink. You will use two different models to get to know the characteristics of the controller and implement a control strategy.

First, a small PID-controller introduction file gives you the possibility to investigate the different influences of each part of the controller (proportional, integral, derivative). The system that shall be analysed is a single mass system with a spring and a damper mounted in parallel, see Figure 10. The wheels are frictionless and positive x-direction is given. Please find further explanations in the comments of the file "PID intro.m".

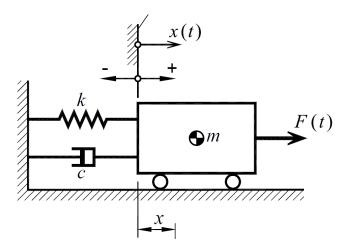


Figure 10. Single spring-mass-damper system.

The second model is the actual CarMaker/Simulink co-simulation model you will work on, see Figure 11.

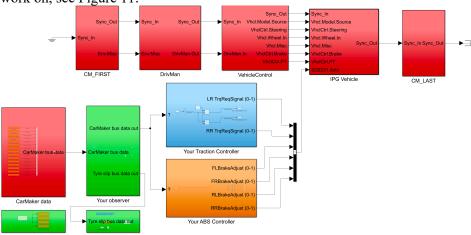


Figure 11. The base Simulink model you will start to work on that interfaces to the vehicle dynamics software CarMaker.

It consists of an m-file initialising all parameters "initial.m". Adjustments to the parameters are done in this file which is marked by the comments in the Matlab file. The vehicle model is built up in the CarMaker software and is a Tesla Model S with two electric motors on each of the rear wheels. The controller blocks that is Blue and Orange is where you will implement your traction and ABS controllers respectively. For the traction control you will implement one separate controller for the left and right rear wheel and for the ABS you will implement one separate controller for each of the four wheels. The green subsystem block you can also edit, the first one is the observer where you will be creating your longitudinal slip observer. The second one is the road friction subsystem which you need to make adjustments to in one of the assignments, and the third green subsystem is the used friction mapping subsystem that you can also make changes to in one of the assignments. So, for this Lab you should not change anything in the red subsystem blocks.

The driver model is the built-in driver model of CarMaker that provides values between 0 and 1 for the throttle signal and 0 to 1 for the brake pedal signal. The

delivered signal will always accelerate to a certain speed 80 km/h, hold this speed for the 1 second and decelerate the vehicle.

A sensor block is given with the available signals in accordance to a real vehicle. Please use these signals only.

The data of the CarMaker vehicle is also given in the "initial.m" matlab file for your convenience.

3.2 Tasks to do and questions to answer

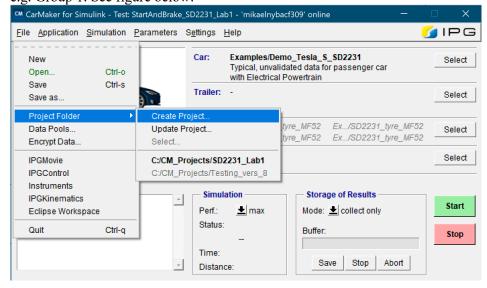
In this section you will find information about the tasks that you should do in this laboratory exercise and also the questions that you have to answer in the report. Please read through this section and the following section 3.3 before you start working with your assignment.

Important notes:

- * while writing the report, write the tasks in the order you have been asked in the handout and clearly mention the task and subtask number (Task 1.a, Task 2.c, etc) when you are giving explanations to a certain graph, question etc.
- ** The task which include plots or table, put them exactly after the related task and not at the end of the document.
- *** All numerical results should be arranged in tables in their respective section but not spread over the text.

Before you start

To get the computer ready you will have to open CarMaker 8 and then create a new project, name it with the computer name e.g. VEL1, and your group number e.g. Group 1. See figure below.



CM CarMaker for Simulink - New Project

New Project

Project Folder

C/CM_Projects/PROJECTNAME

Included Features

Sources / Build Environment

Sources: Extra Models

FMI Examples

CarMaker for Simulink Extras

Simulink Coder (RTW) Examples

Concerto Work Environment

Default

Make sure that all boxes are ticked when entering the name and clicking OK.

Download the files in the zipped file on Canvas for Lab 1 and move the files into the respective folder in the project that you have just created (should be under C:/CM_Projects/[YOUR NAME]), just follow the names of the folders in the zipped file that should match the folder name in your project.

Task 1. Determine control parameters.

Task 1.a: Derive the equation of motion for the single mass system in Figure 10 and build the transfer function $T(s) = \frac{X(s)}{F(s)}$. Implement the transfer function T(s) in the m-file PID_intro . The m-file will plot the step response of the transfer function without an active controller. Sliders for each control parameter as well as for the mass, spring stiffness and damping coefficient will help you to adjust the step response. Show how you derived the transfer function in the report.

Task 1.b: Use the model to find the control parameters that correspond to Figure 8 for a P-, PD-, PI- and PID-controller. You can use Table 1 to estimate the effectiveness of each controller parameter rather than a pure trial and error method.

Note: please be aware that achieving a relatively similar behavior is enough!

Extra task 1.c: Analyse the stability of the open loop system and closed-loop systems using your method of choice for all the controllers mentioned above, a total of five analyses.

Task 2. Slip observer

Task 2.a: Implement the tractive and braking slip in the observer block and plot the slip over time. Use the formulation in Equation 1. Only use built in Simulink blocks and not embedded Matlab functions. Show the plot in the report.

Task 2.b: Reflect on the results you presented in Task 2.a, what issues can you see? Propose a solution and ensure that the traction and brake slip is

calculated and given when it is supposed to. Show the plot of the adjusted slip observer in the report along with your reflections.

Task 2.c: Save needed data in the Matlab Workspace and implement calculations of the used friction in the initial.m matlab file and plot the used friction (μ) over longitudinal slip (s). Show your equations in the report along with the plot. Present the reference slip that you selected and reflect on why you selected this value.

Task 3. Design PID controller

Task 3.a: Add activation logics for the controllers (TCS and ABS). Note that it shall work for all driver inputs (throttle and brake pedal) as soon as traction threshold is reached. Describe under which circumstances the TCS and the ABS will be active.

Task 3.b: Design your own P-, PD-, PI-, PID-controller and compare /discuss the results. You should not use the built in PID blocks, build your own P-, PD-, PI-, PID-controllers using standard blocks.

Task 3.c: Discuss each system and compare them based on system characteristics such as settling time, rise time, overshoot and steady state error. (for each of the controllers; P-, PD-, PI-, PID-controller)

Task 3.d: Is it necessary to use all type of gains for the Traction and ABS controller? Motivate your answer.

Task 4. PID controller optimisation

Task 4.a: Present the best controller that has the fastest response, least overshoot and smallest steady state error as well the shortest overall distance.

Extra task 4.b: Study the controller during changing friction during acceleration and braking event. Do you have to re-tune your model(s) to make your controller handle the disturbance better, if so, show the new tuned PID values and elaborate on the effect between them?

Task 5. More advanced PID

Extra task 5: Implement a more advanced PID of your choosing, you are free to use any block in Simulink. Discuss and reflect on your design and if you are able to improve the performance.

Competition!

The winner should reach the **shortest distance** while keeping **minimum steady-state error** between the reference and actual longitudinal slip.

4 Examination

For details on the grading process of this course please consult the SD2231 Grading Criteria.pdf document on Canvas.

4.1 Report writing

A good report includes exactly the information which is needed for the reader to understand the results and nothing more. Start working with the report from the start by writing down each of the steps you have done including the approach, gathered information and the rationale of each of the steps i.e. why you decided to go in a certain direction and why that is better than another way. This will help you in the course and it will be easier to finalize the report in time.

Note: arrange your report hierarchy exactly based on the tasks arrangement in this hand-out.

Include the following files when submitting your report:

- Your finalized report as *pdf* or *docx*
- A zip file including all your organized Matlab and Simulink files, teachers have to be able to run your files after downloading them from Canvas.

Do not forget to answer the questions in this hand-out!

You should use the template on Canvas for your final report, you can use LaTeX also but should be well formatted.

4.2 People that will support this laboratory assignment

- Mikael Nybacka, mnybacka@kth.se, 08 790 76 38
- Wenliang Zhang, wez@kth.se