

## DBMS Assignment-2

Ques-1 Consider the relation shown in the following table. List all the functional dependencies that this relation instances satisfy.

X	Y	Z
x <sub>1</sub>	y <sub>1</sub>	z <sub>1</sub>
x <sub>2</sub>	y <sub>1</sub>	z <sub>2</sub>
x <sub>1</sub>	y <sub>2</sub>	z <sub>2</sub>
x <sub>2</sub>	y <sub>1</sub>	z <sub>2</sub>

The functional dependencies are  $XY \rightarrow Z$ ,  $XZ \rightarrow Y$ ,  $YZ \rightarrow X$   
 Since in all these FDs if the value at left side is same then the value at right side is also same.

Ques-2 Given the following set S of functional dependencies:

- $M \rightarrow O$  (F1)
- $NP \rightarrow M$  (F2)
- $O \rightarrow N$  (F3)

Check and prove if the following dependencies can be deduced from S. If not, give counter-example with 5 tuples or less.

A)  $OP \rightarrow M$

F3)  $O \rightarrow N$

Applying Augmentation rule :

$OP \rightarrow NP$  — (F4)

F2)  $NP \rightarrow M$

Applying Transitive rule to F4 & F2, we get

$OP \rightarrow M$

Hence proved



B)  $NO \rightarrow M$

This FD cannot be derived from the given FDs  
 Counterexample:

M	N	O	P
$m_1$	$n_1$	$o_1$	$p_1$
$m_2$	$n_2$	$o_2$	$p_2$
$m_3$	$n_1$	$o_1$	$p_3$
$m_4$	$n_2$	$o_4$	$p_1$
$m_5$	$n_5$	$o_5$	$p_5$

C)  $MP \rightarrow N$

F1)  $M \rightarrow O$  , F3)  $O \rightarrow N$

Applying Transitive rule, we get  
 F5)  $M \rightarrow N$

Reflexivity ~~Transitive~~  $\Rightarrow$   ~~$MP \rightarrow N$~~   $NP \rightarrow N$  — (F6)  
 (since N is a subset of NP)

Applying Augmentation rule to F5

$MP \rightarrow NP$  (F7)

Applying Transitive rule to F6 & F7

$MP \rightarrow N$

Hence proved

d)  $MO \rightarrow P$

This FD cannot be derived from given FDs  
 Counterexample:

M	N	O	P
$m_1$	$n_1$	$o_1$	$p_1$
$m_2$	$n_2$	$o_2$	$p_2$
$m_3$	$n_3$	$o_3$	$p_3$
$m_2$	$n_2$	$o_2$	$p_4$
$m_5$	$n_5$	$o_5$	$p_5$



E)  $MN \rightarrow P$ 

This FD cannot be derived from the given FDs  
Counterexample:

M	N	O	P
m <sub>1</sub>	n <sub>1</sub>	o <sub>1</sub>	p <sub>1</sub>
m <sub>1</sub>	n <sub>2</sub>	o <sub>2</sub>	p <sub>2</sub>
m <sub>3</sub>	n <sub>3</sub>	o <sub>3</sub>	p <sub>1</sub>
m <sub>4</sub>	n <sub>2</sub>	o <sub>2</sub>	p <sub>4</sub>
m <sub>5</sub>	n <sub>5</sub>	o <sub>5</sub>	p <sub>5</sub>

Ques-3 Consider the relation schema  $R(A, B, C, D)$  with functional dependencies  $A \rightarrow D$ ,  $B \rightarrow CD$  and  $AC \rightarrow D$

A) find the attribute closure  $\{A\}^+$   
 $\{A\}^+ = \{A, D\}$

B) find the attribute closure ~~of~~  $\{A, B\}^+$   
 $\{A, B\}^+ = \{A, B, D, C\}$

C) Find the minimum cover (i.e. canonical cover) of the given functional dependencies

Step 1: Split

$A \rightarrow D$  (1)

$B \rightarrow C$  (2')

$B \rightarrow D$  (2'')

$AC \rightarrow D$  (3)

Step 2: Delete duplicate FDs

No duplicate FDs, set remains same

Step 3: In (3) 'C' is redundant extraneous

$A \rightarrow D$  (1)

$B \rightarrow C$  (2')



$$B \rightarrow D \text{ (2'')}$$

$$AC \rightarrow D \text{ (3)}$$

$$A \rightarrow D \text{ (3')}$$

Step 4: Removing (3') as it is redundant

$$A \rightarrow D \text{ (1)}$$

$$B \rightarrow C \text{ (2')}$$

$$B \rightarrow D \text{ (2'')}$$

This is the canonical cover of given set of FDs

D) List all the candidate key(s) of R

- nothing is extraneous
- all RHS are single attributes
- checking if initial & final set of FDs are equivalent or not

$$\text{Let } E = \{ A \rightarrow D, B \rightarrow CD, AC \rightarrow D \}$$

$$F = \{ A \rightarrow D, B \rightarrow C, B \rightarrow D \}$$

Checking if F covers E

In E

$$A \rightarrow D$$

Computing ~~FDs~~  $A^+$  using FDs in F

$$A^+ = \{ A, D \}$$

It contains D

$$B \rightarrow CD$$

Computing  $B^+$  using F

$$B^+ = \{ B, C, D \}$$

It contains C & D

$$AC \rightarrow D$$

Computing  $AC^+$

$$AC^+ = \{ A, C, D \}$$

It contains D

$\therefore$  F covers E

Checking if E covers F

In F

$$A \rightarrow D$$

Computing  $A^+$  using E

$$A^+ = \{ A, D \}$$

It contains D

$$B \rightarrow C$$

Computing  $B^+$  using E

$$B^+ = \{ B, C, D \}$$

It contains C

$$B \rightarrow D$$

Computing  $B^+$  using E

$$B^+ = \{ B, C, D \}$$

It contains D

$\therefore$  E covers F

$\therefore$  E & F are equivalent

$\therefore$  F is canonical cover of E

D) List all the candidate key(s) of R

$$F = \{A \rightarrow D, B \rightarrow C, B \rightarrow D\}$$

$$A^+ = \{A, D\} \quad B^+ = \{B, C, D\}$$

$$\{AB\}^+ = \{A, B, C, D\}$$

AB is a superkey because its closure contains all the attributes of relation R

But its proper subsets A & B do not have all the attributes in their closure.

So AB is a candidate key

Que=4 Consider the relation schema  $R(A, B, C, D, E, G)$  with functional dependencies  $F = \{AB \rightarrow C, AG \rightarrow E, B \rightarrow D, E \rightarrow G\}$

Notice F is the minimum cover of itself.

For each of the following decompositions of  $R(A, B, C, D, E, G)$  determine whether it is

- (a) dependency-preserving &
- (b) lossless

i)  $\{ABC, CDE, EG\}$

a) Dependency-preserving

$$\text{Let } R_1 = ABC, R_2 = CDE, R_3 = EG$$

$AB \rightarrow C$  is preserved in  $R_1$

$E \rightarrow G$  is preserved in  $R_3$

Closure of  $R_1$

$$A^+ = \{A\}$$

$$B^+ = \{B, D\} \text{ but } D \text{ is not in } R_1 \text{ so}$$

$$= \{B\}$$

$$C^+ = \{C\}$$

$$AB^+ = \{A, B, C, D\} \text{ but } D \text{ is not in } R_1 \text{ so}$$

$$= \{A, B, C\}$$

$$AB \rightarrow C \quad \text{--- (F}_1\text{)}$$



$$AC^+ = \{A, C\}$$

$$BC^+ = \{B, C, D\} \text{ but } D \text{ is not in } R_1 \text{ so}$$

$$= \{B, C\}$$

Closure in  $R_2$

$$C^+ = \{C\}$$

$$D^+ = \{D\}$$

$$E^+ = \{E, G\} \text{ but } G \text{ is not in } R_2 \text{ so}$$

$$= \{E\}$$

$$CD^+ = \{C, D\}$$

$$CE^+ = \{C, E, G\} \text{ but } G \text{ is not in } R_2 \text{ so}$$

$$= \{C, E\}$$

$$DE^+ = \{D, E, G\} \text{ but } G \text{ is not in } R_2 \text{ so}$$

$$= \{D, E\}$$

Closure in  $R_3$

$$E^+ = \{E, G\}$$

$$E \rightarrow G$$

$$G^+ = \{G\}$$

$AB \rightarrow C$  &  $E \rightarrow G$  are preserved but not  $AG \rightarrow E$ ,  $B \rightarrow D$

So the decomposition is not dependency preserving  
b) lossless

(ii)  $\{ABCD, AEG\}$

a) dependency preserving

$AB \rightarrow C$  is preserved in  $ABCD$

$AG \rightarrow E$  is preserved in  $AEG$

$B \rightarrow D$  is preserved in  $ABCD$

$E \rightarrow G$  is preserved in  $AEG$

$\therefore$  The decompositions are dependency preserving

b) lossless

1)  $ABCD \cup AEG = ABCDEG = R$

2)  $ABCD \cap AEG = A \neq \emptyset$

3)  $ABCD \cap AEG = A$

$A^+ = \{A\} \neq \{A, B, C, D\}$  or  $\neq \{A, E, G\}$

$\therefore$  The decompositions are not lossless

(iii)  $\{ABCE, BD, AEG\}$

a)  $AB \rightarrow C$  is preserved in  $ABCE$

$AG \rightarrow E$  is preserved in  $AEG$

$B \rightarrow D$  is preserved in  $BD$

$E \rightarrow G$  is preserved in  $AEG$

The decompositions are dependency preserving

b) 1)  $ABCE \cup BD \cup AEG = ABCDEG = R$

Considering ~~ABCE & BD~~ Chase Test:

	A	B	C	D	E	G
1	A	B	C	<del>d<sub>1</sub></del>	E	<del>g<sub>1</sub></del>
2	a <sub>2</sub>	B	C <sub>2</sub>	D	e <sub>2</sub>	g <sub>2</sub>
3	A	b <sub>3</sub>	C <sub>3</sub>	d <sub>3</sub>	E	G

1 & 3 have common AE in common

& ~~E~~  $E \rightarrow G$

So g<sub>1</sub> becomes G, B is common in 1 & 2 &  $B \rightarrow D$   
So d<sub>1</sub> becomes D

$\therefore$  This is a lossless decomposition



(iv)  $\{AB, ADE, BCG\}$

a) Closure in  $R_1 = AB$

$$A^+ = \{A\}$$

$$B^+ = \{B, D\} \text{ but } D \text{ is not in } R_1 \text{ so} \\ = \{B\}$$

Closure in  $R_2 = ADE$

$$A^+ = \{A\}$$

$$D^+ = \{D\}$$

$$E^+ = \{E, G\} \text{ but } G \text{ is not in } R_2 \text{ so} \\ = \{E\}$$

$$AD^+ = \{A, D\}$$

$$DE^+ = \{D, E, G\} \text{ but } G \text{ is not in } R_2 \text{ so} \\ = \{D, E\}$$

$$AG^+ = \{A, G, E\} \quad AE^+ = \{A, E, G\} \text{ but } G \text{ is not in } R_2 \\ = \{A, E\}$$

Closure in  $R_3 = BCG$

$$B^+ = \{B, D\} \text{ but } D \text{ is not in } R_3 \text{ so} \\ = \{B\}$$

$$C^+ = \{C\}$$

$$G^+ = \{G\}$$

$$BC^+ = \{B, C, D\} \text{ but } D \text{ is not in } R_3 \text{ so} \\ = \{B, C\}$$

$$CD^+ = \{C, D\} \text{ but } D \text{ is not in } R_3$$

$$BD^+ = \{B, D\}$$

$$CG^+ = \{C, G\}$$

$$BG^+ = \{B, G, D\} \text{ but } D \text{ is not in } R_3 \text{ so} \\ = \{B, G\}$$

None of the FDs are preserved  
so the decompositions are not dependency  
preserving



b)  $\{AB \cup ADE \cup BCG\} = ABCDEG = R$

Chase Test:

	A	B	C	D	E	G
1	A	B	c <sub>1</sub>	d <sub>1</sub> <sup>D</sup>	e <sub>1</sub>	g <sub>1</sub>
2	A	b <sub>2</sub>	c <sub>2</sub>	D	E	g <sub>2</sub>
3	a <sub>3</sub>	B	C	d <sub>3</sub> <sup>D</sup>	e <sub>3</sub>	G

This cannot generate a row which has all the attributes  
So this decomposition is not lossless

v)  $\{BDEG, ABC\}$

a)  $R_1 = BDEG$

Closure in  $R_1 = BDEG$

$B^+ = \{B, D\}$

$B \rightarrow D$

$D^+ = \{D\}$

$E^+ = \{E, G\}$

$E \rightarrow G$

$G^+ = \{G\}$

$BD^+ = \{B, D\}$

$DE^+ = \{D, E, G\}$

$DE \rightarrow G$

$EG^+ = \{E, G\}$

$BE^+ = \{B, E, D, G\}$

$BE \rightarrow DG$

$BG^+ = \{B, G, D\}$

$BG \rightarrow D$

Closure in  $R_2 = ABC$

$A^+ = \{A\}$

$B^+ = \{B, D\}$

$= \{B\}$

$C^+ = \{C\}$

~~$GD^+ = \{G, D\}$~~   $AC^+ = \{A, C\}$

but D is not in  $R_2$  so

$AB^+ = \{A, B, C\}$

$AB \rightarrow C$

$BC^+ = \{B, C, D\}$

$= \{B, C\}$

$DG^+ = \{D, G\}$

$BDE^+ = \{B, D, E, G\}$

$BDE \rightarrow G$

$DEG^+ = \{D, E, G\}$

$BEG^+ = \{B, E, G, D\}$

$BDG^+ = \{B, D, G\}$

$BEG \rightarrow D$

The FDs in  $R_1$

$B \rightarrow D, E \rightarrow G,$



The dependency  $AG \rightarrow E$  is not preserved

b) 1)  $BDEG \cup ABC = ABCDEG = R$

2)  $BDEG \cap ABC = B \neq \Phi$

3)  $BDEG \cap ABC = B$

$B^+ = \{B, D\} \neq \{B, D, E, G\} \neq \{A, B, C\}$

$\therefore$  The decomposition is not lossless

Que-5 Consider the relation schema  $R(A, B, C, D)$  with functional dependencies  $A \rightarrow B$ ,  $BC \rightarrow A$  and  $B \rightarrow D$ , which is the minimum cover itself.

A) Find all the candidate keys of  $R$

$A^+ = \{A, B, D\}$   $C^+ = \{C\}$

$B^+ = \{B, D\}$   $D^+ = \{D\}$

$AB^+ = \{A, B, D\}$   $\checkmark AC^+ = \{A, B, C, D\}$

$\checkmark BC^+ = \{B, C, A, D\}$   $CD^+ = \{C, D\}$

$BC$  is a superkey,  $AC$  is a superkey

$AD^+ = \{A, B, D\}$   $BD^+ = \{B, D\}$

$ABC^+ = \{A, B, C, D\}$   $BCD^+ = \{B, C, D, A\}$

$ACD^+ = \{A, C, D, B\}$   $ABD^+ = \{A, B, D\}$

$ABC$ ,  $BCD$ ,  $ACD$  are superkeys

but their subsets  $BC$  &  $AC$  are also superkeys

$\therefore AC$  &  $BC$  are candidate keys

B) Is relation  $R$  in BCNF? Is it in 3NF? Justify your answers.

Assuming no multivalued attributes,

$R$  is in 1NF

$A, B, C$  are prime attributes,  $D$  is nonprime attribute

$B \rightarrow D$ , i.e. a subset of candidate key  $BC$  which is  $B$  determines  $D$  so  $R$  has partial dependency



$R$  is not in 2NF

Consequently  $R$  is not in 3NF or BCNF

c) Decompose the relation  $R(A, B, C, D)$  into a collection of BCNF relations, so that the decomposition is lossless. Is the decomposition dependency preserving?

$AC$  &  $BC$  are

$AC, BC, ABC, BCD, ACD$  are superkeys in  $R$   
for  $A \rightarrow B$ ,  $A$  is not a superkey but  $A \rightarrow B$  is a FD of  $R$   
 $\therefore R$  is not in BCNF

Acc. to Algorithm:

$$S = \{R\}$$

Picking  $A \rightarrow B$

$$\Rightarrow S = \{AB, ACD\}$$

~~ABCD~~

$\therefore$  The decomposition is  $\{AB, ACD\}$

1)  $AB \cup ACD = ABCD = R$

2)  $AB \cap ACD = A \neq \emptyset$

3)  $AB \cap ACD = A$ ,  $A \rightarrow$

$$A^+ = \{A, B\} \text{ (and } D \text{ which is not in } AB)$$

$$\therefore A \rightarrow AB$$

$\therefore \{AB, ACD\}$  is lossy decomposition

$BC \rightarrow A$  is not preserved in this decomposition

So it is not dependency preserving

d) Decompose the relation  $R(A, B, C, D)$  into a collection of 3NF relations so that the decomposition is both lossless and dependency preserving

Let us consider the decomposition  $\{ABC, BCD\}$   
It preserves all the dependencies so it is dependency preserving



$$1) ABC \cup B \oplus D = AB \oplus D = R$$

$$2) ABC \cap B \oplus D = B \oplus \neq \phi$$

$$3) ABC \cap B \oplus D = B \oplus \rightarrow R_1 \text{ or } R_2. B \rightarrow R_2(BD)$$

$$BC \rightarrow \{A, B, C, D\}$$

$\therefore$  The decomposition is lossless

1) Both decomposed relations are in 1NF as there are no multivalued attributes

2) There is no partial dependency so they are in 2NF

3) There is no transitive dependency so they are in 3NF