

# Lecture 22

PCFG (Probabilistic CFG)-PART I

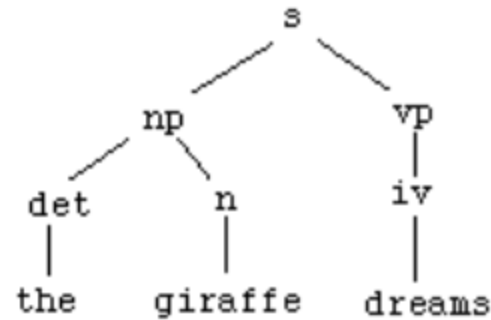
# CFG (Context Free Grammar)

- |                           |                                  |                                 |                               |
|---------------------------|----------------------------------|---------------------------------|-------------------------------|
| 1. $S \rightarrow VP\ NP$ | 4. $NP \rightarrow Det\ Adj\ NP$ | $N \rightarrow dog   man   cat$ | $Adj \rightarrow old   small$ |
| 2. $S \rightarrow NP\ VP$ | 5. $VP \rightarrow V\ NP$        | $Det \rightarrow the   a$       | $V \rightarrow ate   cried$   |
| 3. $VP \rightarrow V$     | 6. $NP \rightarrow Det\ N$       |                                 |                               |

# Writing the derivation/construct a tree after the parsing procedure is complete

(test sentence: the giraffe dreams)

s → np vp  
np → det n  
vp → tv np  
→ iv  
det → the  
→ a  
→ an  
n → giraffe  
→ apple  
iv → dreams  
tv → eats  
→ dreams



- Derivation:

S=>**np** vp=>**det** n vp=>the **n** vp=>  
the giraffe **vp**=>the giraffe **iv**=>the  
giraffe dreams

# How to convert CFG to PCFG

- **PCFG: Probabilistic CFG**

- Attach a **probability value** to each production such that the sum of probabilities of productions with the same LHS  $\sum_{\text{same LHS}} P(\text{productions})$  is equal to 1
- Utility: 1) Find the best tree for a sentence (for ambiguous grammar)  
2) Find the best output sentence (in case of multiple candidates)
- How to find the probability (tree) or probability (sentence)?
- Write the derivation for the test sentence/construct the tree
- Multiply the probabilities of all the productions used for making the tree

$$P(\text{sentence}) = \prod_{\text{tree}} P(\text{productions})$$

# PCFG (Probabilistic Context Free Grammar):

Human: Who cried?

Chatbot: the man cried/a dog cried

(tree&deriv  $\rightarrow$  P(sent)  $\rightarrow$  winner sentence as per maximum probability)

- $S \rightarrow VP NP$  (0.1)
- $S \rightarrow NP VP$  (0.9)
- $VP \rightarrow V$  (0.6)
- $NP \rightarrow Det Adj NP$  (0.3)
- $VP \rightarrow V NP$  (0.4)
- $NP \rightarrow Det N$  (0.7)

- $N \rightarrow dog$  (0.2)
- $N \rightarrow man$  (0.6)
- $N \rightarrow cat$  (0.2)
- $Det \rightarrow the$  (0.7)
- $Det \rightarrow a$  (0.3)
- $Adj \rightarrow old$  (0.5)
- $Adj \rightarrow small$  (0.5)
- $V \rightarrow ate$  (0.6)
- $V \rightarrow cried$  (0.4)