

Q2) We want to compose the risk of portfolio such that  $w_1 = 40\%$  and  $w_2 = 60\%$  with the risks of its components as measured by the variance. Direct computations give

$$\sigma_1^2 \cong 0.0184 \quad \sigma_2^2 \cong 0.0024 \quad \rho_{12} \cong -0.96309$$

By (5.8)

$$\sigma_v^2 \cong (0.4)^2 (0.0184) + (0.6)^2 (0.0024) + 2(0.4)(0.6)(-0.96309) \sqrt{0.0184} \sqrt{0.0024}$$

$$\cong 0.000736 = 7.36 \times 10^{-4}$$

Observe the variance  $\sigma_v^2$  is smaller than  $\sigma_1^2$  and  $\sigma_2^2$ .

Considering another portfolio  $w_1 = 80\%$  and weight 2 ( $w_2 = 20\%$ ), all other things being the same then

$$\begin{aligned} \sigma_v^2 &\cong (0.8)^2 (0.0184) + (0.2)^2 (0.0024) \\ &\quad + 2(0.8)(0.2)(-0.96309) \sqrt{0.0184} \sqrt{0.0024} \\ &\cong 0.009824 \end{aligned}$$

which is approximately  $\sigma_1^2$  and  $\sigma_2^2$

The variance  $\sigma_v^2$  of a portfolio cannot exceed the greater of the variances  $\sigma_1^2$  and  $\sigma_2^2$  of the components.

$$\sigma_v^2 \leq \max\{\sigma_1^2, \sigma_2^2\}$$

If short sales aren't allowed