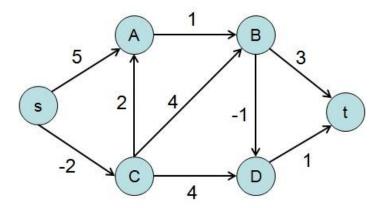
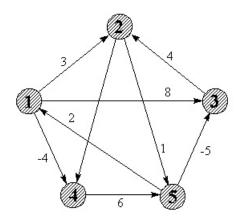
MC- 405 GRAPH THEORY

Assignment-II

1. Using Bellman Ford algorithm, find the shortest path between S and all other vertices.

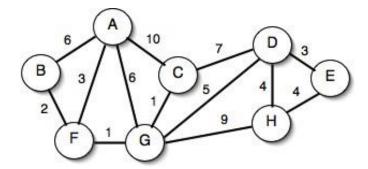


2. Using Floyd-Warshall algorithm, find the shortest path between all pair of vertices.



- 3. Prove that the following are equivalent for an n-vertex graph T.
 - (a) T is a tree.
 - (b) T is connected and has no cycles.
 - (c) For $u, v \in V(T)$, T has exactly one u v path.
 - (d) T is connected and has exactly n-1 edges.
 - (e) T is connected, but T e is disconnected for every edge e.
 - (f) T has no cycle, but T + xy does, for any two non-adjacent vertices $x, y \in V(T)$.
 - (g) T has n 1 edges and no cycles.
- 4. Show that there are n^{n-2} labelled trees with n vertices, $n \ge 2$.
- 5. Define a spanning tree of a graph. Find three spanning tree in the Peterson graph.

- 6. Show that a Hamiltonian path in a graph is a spanning tree.
- 7. Prove/Disprove that every spanning tree is a hamiltonian path.
- 8. Find the minimum spanning tree using Prim's and Kruskal's Algorithm.



9. Describe Traveling Salesman problem and Chinese Postman Problem. Give examples for both. Also, mention the main differences among the two.