

Q6. i) We define a PDA M as follows

$$M = (\{q_0, q_1, q_2\}, \{a, b, c\}, \{a, b, c, \epsilon\}, \delta, q_0, z_0, \{q_2\})$$

where δ is defined by

$$\delta(q_0, a, z_0) = \{(q_0, az_0)\}$$

$$\delta(q_0, b, z_0) = \{(q_0, bz_0)\}$$

$$\delta(q_0, b, a) = \{(q_1, \Lambda)\}$$

$$\delta(q_0, b, b) = \{(q_1, b)\}$$

$$\delta(q_1, a, z_0) = \{(q_1, az_0)\}$$

$$\delta(q_1, a, a) = \{(q_1, aa)\}$$

$$\delta(q_1, a, b) = \{(q_1, \Lambda)\}$$

$$\delta(q_1, b, a) = \{(q_1, a)\}$$

$$\delta(q_1, c, b) = \{(q_1, b)\}$$

$$\delta(q_1, b, a) = \{q_0, a\}$$

$$\delta(q_1, b, b) = \{q_0, bb\}$$

$$\delta(q_1, b, \Lambda) = \{q_0, n\}$$

$$\delta(q_0, c, a) = \{q_0, a\}$$

$$\delta(q_0, c, b) = \{q_0, b\}$$

$$\delta(q_0, c, z_0) = \{q_0, cz_0\}$$

$$\delta(q_0, \epsilon, z_0) = \{q_2, z_0\}$$

* ii) We define a PDA M as follows

$M = (\{q_0, q_1, q_2\}, \{a, b, c\}, \{a, b, c, z_0\}, \delta, q_0, z_0, \{q_2\})$
 where δ is defined by

$$\delta(q_0, a, z_0) = \{ (q_0, az_0) \}$$

$$\delta(q_0, a, a) = \{ (q_0, aa) \}$$

$$\delta(q_0, b, a) = \{ (q_0, baa) \}$$

$$\delta(q_0, b, z_0) = \{ (q_0, bz_0) \}$$

$$\delta(q_0, b, b) = \{ (q_0, bbb) \}$$

$$\delta(q_0, a, b) = \{ (q_0, abb) \}$$

$$\delta(q_0, \overset{c}{\cancel{a}}, z_0) = \{ (q_1, z_0) \}$$

$$\delta(q_0, c, a) = \{ (q_1, a) \}$$

$$\delta(q_0, c, b) = \{ (q_1, b) \}$$

$$\delta(q_1, b, b) = \{ (q_1, \Lambda) \}$$

$$\delta(q_1, a, a) = \{ (q_1, \Lambda) \}$$

$$\delta(q_1, \Lambda, z_0) = \{ (q_2, z_0) \}$$

$$\delta(q_1, \Lambda, z_0) = \{ (q_2, z_0) \}$$

iii) We define a PDA M as follows

$$M = (\{q_0, q_1, q_2, q_3, q_6\}, \{a, b, c\}, \{a, b, c, z_0, d, q_1, z_0, \{q_6\}\})$$

where δ is defined by

$$\delta(q_0, a, z_0) = \{(q_0, az_0)\}$$

$$\delta(q_0, a, a) = \{(q_0, aa)\}$$

$$\delta(q_0, b, a) = \{(q_1, \Lambda)\}$$

$$\delta(q_1, b, a) = \{(q_1, ba)\}$$

$$\delta(q_1, \Lambda, z_0) = \{(q_2, z_0)\}$$

$$\delta(q_2, b, z_0) = \{(q_2, bz_0)\}$$

$$\delta(q_2, b, b) = \{(q_2, bb)\}$$

$$\delta(q_2, c, b) = \{(q_3, \Lambda)\}$$

$$\delta(q_3, c, b) = \{(q_3, \Lambda)\}$$

$$\delta(q_3, \Lambda, z_0) = \{(q_6, z_0)\}$$