

## CHAPTERS 21 AND 22 NOTES

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### CONTENTS

21. Electric Charge and Electric Field	1
21.1 Electric Charge	1
21.1.1 Electric Charge and the Structure of Matter	2
21.1.2 Electric Charge is Conserved	2
21.2 Conductors, Insulators, and Induced Charges	2
21.2.1 Charging by Induction	3
21.3 Coulomb's Law	3
21.4 Electric Field and Electric Forces	4
21.5 Electric-Field Calculations	4
21.6 Electric Field Lines	5
21.7 Electric Dipoles	5
21.7.1 Force and Torque on an Electric Dipole	5

### 21. ELECTRIC CHARGE AND ELECTRIC FIELD

Electromagnetic interactions involve particles that have electric charge, an attribute that is as fundamental as mass. Just as objects with mass are accelerated by gravitational forces, so electrically charged objects are accelerated by electric forces.

#### 21.1 Electric Charge.

**Definition 1. Electric Charge:** is the state of having more or less than a natural amount of electrons. *Positive* if less or *Negative* if more.

**Remark.** Two positive charges or two negative charges repel each other. A positive charge and a negative charge attract each other.

**Definition 2. Electrostatics:** the interactions between electric charges that are at rest (or nearly so).

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*Date:* June 16, 2021.

### 21.1.1 Electric Charge and the Structure of Matter.

**Definition 3. Parts of Atom:** Positive Protons, negative Electrons and Neutral Neutrons. Protons and Neutrons are held by *Strong Nuclear Force* to form the Nucleus and are themselves comprised of *Quarks*. The Majority of Atom is the *Electron Cloud*

**Definition 4. Ionization:** Normally positive charge and negative charge cancel out, but through an addition or loss of an electron the atom becomes ionized, becoming either a *positive* or *negative* ion

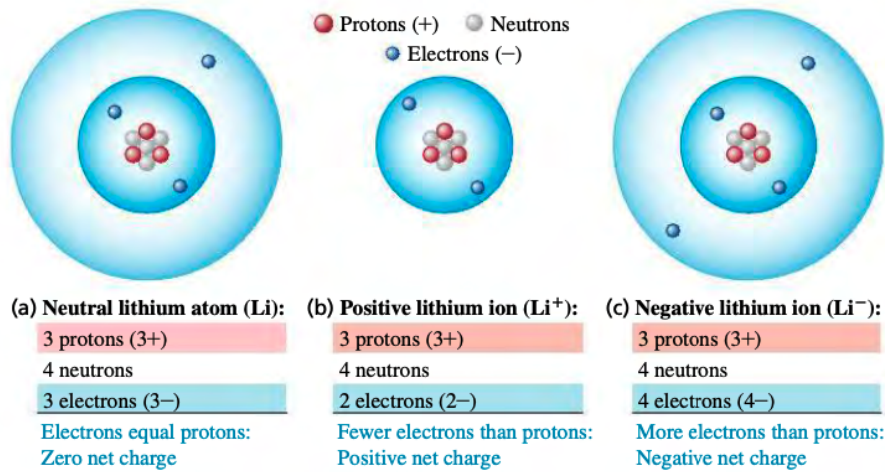


FIGURE 1. Atomic Structure and Ionization

### 21.1.2 Electric Charge is Conserved.

**Theorem 1. Principle of conservation of charge:** The algebraic sum of all the electric charges in any closed system is constant. In any charging process, charge is not created or destroyed; it is merely transferred from one body to another.

**Theorem 2. Quantized Nature of Charge:** The magnitude of charge of the electron or proton is a natural unit of charge.

## 21.2 Conductors, Insulators, and Induced Charges.

**Definition 5. Conductivity and Insulation:** *Conductors* are materials that transfer electrons well, such as copper and other metals. The opposite are *Insulators* which are poor and transferring charge, these are often nonmetals. Some materials called *semiconductors* are intermediate in their properties between good conductors and good insulators.

### 21.2.1 Charging by Induction.

**Definition 6. Induction:** a method used to charge an object without actually touching the object to any other charged object. This is done by rearranging electrons already present in object

**Definition 7. Polarization:** The slight shifting of charge within the molecules of the neutral insulator when placed near a charge object. This is what causes charge by Induction

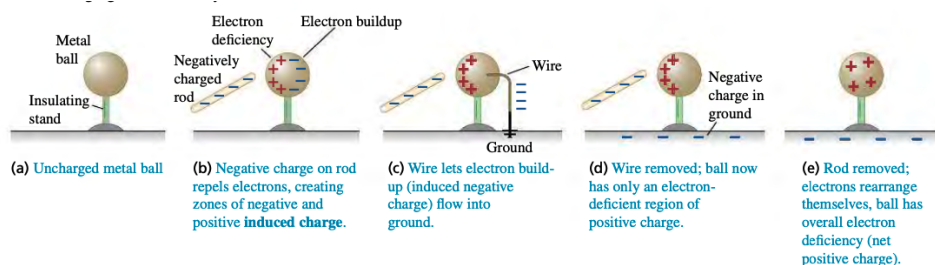


FIGURE 2. Charge by Induction

### 21.3 Coulomb's Law.

**Definition 8. : Point Charges:** Simple charged bodies whose mass is irrelevant.

**Theorem 3. Coulomb's Law:** The magnitude of the electric force between two point charges is directly proportional to the product of the charges and inversely proportional to the square of the distance between them. In mathematical terms shown as  $F = k \frac{|q_1 * q_2|}{r^2}$  where the coulomb constant  $k = 8.987551787 * 10^9 N \cdot m / C^2$  and can also be described in SI units as  $\frac{1}{4\pi\epsilon_0}$ .

**Theorem 4. Principle of Superposition of Forces:** To find sum of forces a vector sum must be calculated involving the composite internal forces.

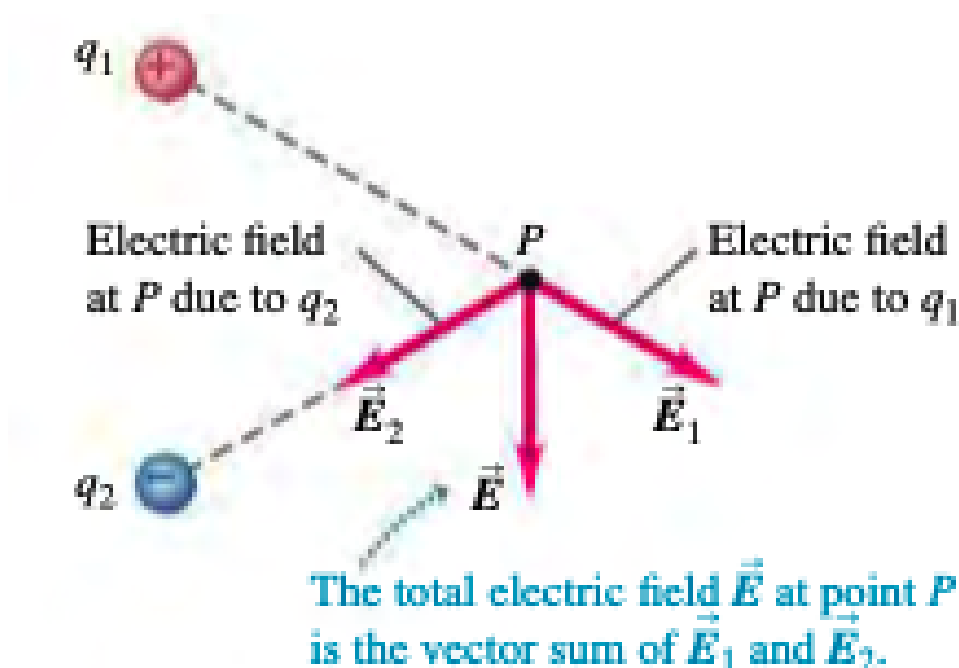


FIGURE 3. Superposition

#### 21.4 Electric Field and Electric Forces.

**Definition 9. Electric Field:** The intermediary through which charges interact. The equation to find the strength of an electric field is  $|E| = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$  where the sign relates to the direction of the field.

**Remark.** The electric force on a charged body is exerted by the electric field created by other charged bodies.

#### 21.5 Electric-Field Calculations.

**Theorem 5. Principle of Superposition of Electric Fields:** The total electric field at  $P$  is the vector sum of the fields at  $P$  due to each point charge in the charge distribution.

**Definition 10. Types of Charge Density:**

- (1) Linear Charge Density: Charge per unit length, measured in  $C/m$  and written as  $\lambda$
- (2) Surface Charge Density: Charge per unit area, measured in  $C/m^2$  and written as  $\sigma$
- (3) Volume Charge Density: Charge per unit volume, measured in  $C/m^3$  and written as  $\rho$ .

## 21.6 Electric Field Lines.

**Definition 11. Electric Field Line:** An imaginary line demonstrating direction of electric field — $\vec{E}$ — vector at point and the density of lines shows magnitude.

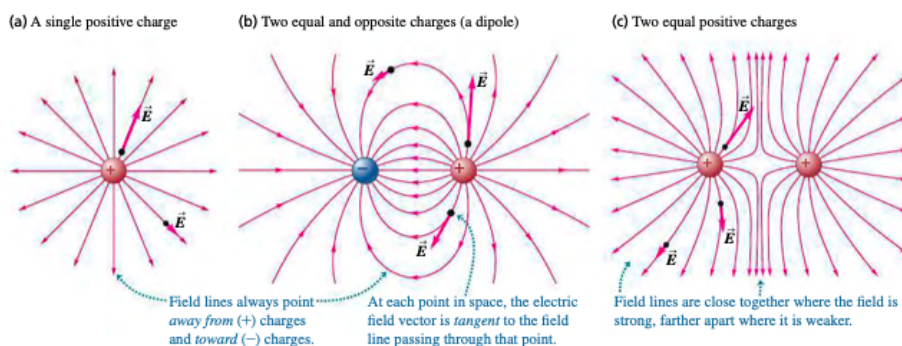


FIGURE 4. Field Lines

## 21.7 Electric Dipoles.

**Definition 12. Electric Dipole:** A pair of point charges with equal magnitude and opposite sign (a positive charge  $q$  and a negative charge  $-q$ ) separated by a distance  $d$ .

### 21.7.1 Force and Torque on an Electric Dipole.

**Definition 13. Electric Dipole Moment:** A measure of the system's overall polarity, can be calculated using  $p = qd$  where  $q$  is charge and  $d$  is separation. Direction of  $p$  is from negative to positive

**Definition 14. Torque on an Electric Dipole:** Because the point charges may not be parallel, a torque exists and can be found through the equation  $\tau = pE\sin\phi$  where  $p$  is the dipole moment and  $\phi$  is the angle between the dipole moment and  $E$

**Definition 15. Potential Energy of an Electric Dipole:** Because there is work being done there is a change in potential energy and we can find this through the equation  $U = -p \cdot E$  or as  $U = pE\cos\phi$