```
FindNeighbours[IList_, JList_, Start_, nextI_, nextJ_, ConvexHull_] :=
  Module[{SortedPointsKeys = <||>, SortedPoints = {}, proportionJ,
    proportionI, jtemp, itemp, PotNextJDir, distanceNextPotPointJ, PotNextIDir,
    distanceNextPotPointI, NeighbourNumberJ, NeighbourNumberI, distanceJ,
    distanceI, NextJDir, NextIDir, StartPropJForFirstCompleteGridJ},
   Print["
   gib aus
Detect I and J rows of
       imaginäre Einheit I
       Points____
"];
   Clear[CheckPoints];
   lösche
   CheckPoints = {};
   StartPoint = Start;
   StartPointI = Start;
   StartPointJ = Start;
   NextPointI = nextI;
   NextPointJ = nextJ;
   Print["Start = ", Start];
   gib aus
   Print[" nextI = ", nextI];
   gib aus
   Print["nextJ = ", nextJ];
   gib aus
   IDirStart = {nextI[CoordI] - Start[CoordI], nextI[CoordJ] - Start[CoordJ]};
   JDirStart = {nextJ[CoordI] - Start[CoordI], nextJ[CoordJ] - Start[CoordJ]};
   Print["IDir = ", IDirStart];
   gib aus
   Print["JDir = ", JDirStart];
   StartProportionI = nextI[CoordJ] - Start[CoordJ];
   StartProportionJ = nextJ[CoordI] - Start[CoordI];
   StartDistanceI = Sqrt[Abs[IDirStart[[1]]^2 + IDirStart[[2]]^2]];
                     Qua ·· Absolutwert
   StartDistanceJ = Sqrt[Abs[JDirStart[[1]]^2 + JDirStart[[2]]^2]];
                     Qua· Absolutwert
   AssociateTo[StartPoint, {NeighbourJ → 1, NeighbourI → 1}];
   assoziiere mit
   AssociateTo[NextPointI, { NeighbourJ → 1, NeighbourI → 2}];
   assoziiere mit
   AssociateTo[NextPointJ, { NeighbourJ → 2, NeighbourI → 1}];
   AppendTo[SortedPoints, {StartPoint, NextPointI, NextPointJ}];
   hänge an bei
```

```
AppendTo[CheckPoints, Start];
hänge an bei
AppendTo[CheckPoints, nextJ];
hänge an bei
AppendTo[CheckPoints, nextI];
hänge an bei
NeighbourNumberJ = 2;
NeighbourNumberI = 2;
aI = 2;
aJ = 2;
NextJDir = JDirStart;
distanceJ = StartDistanceJ;
proportionJ = StartProportionJ;
StartPropJForFirstCompleteGridJ = StartProportionJ;
For[pp = 1, pp ≤ Length[JList] * 2, pp++,
For-Schleife
               Länge
 For [tt = 1, tt ≤ Length [JList], tt++,
For-Schleife
                  Länge
   If[JList[[tt]][CoordJ] # StartPointJ[CoordJ] &&
   lwenn
      JList[[tt]][CoordJ] ≥ NextPointJ[CoordJ] && JList[[tt]][CoordI] ≥
        NextPointJ[CoordI] || JList[[tt]][CoordI] ≤ NextPointJ[CoordI],
    PotNextJDir = {JList[[tt]][CoordJ] - NextPointJ[CoordJ],
       JList[[tt]][CoordI] - NextPointJ[CoordI]};
    distanceNextPotPointJ = Sqrt[Abs[PotNextJDir[[1]]^2 + PotNextJDir[[2]]^2]];
                             Qua· Absolutwert
   ];
   If[JList[[tt]][CoordJ] # NextPointJ[CoordJ] &&
     JList[[tt]][CoordJ] # StartPointJ[CoordJ] &&
      (JList[[tt]][CoordI]) ≤ NextPointJ[CoordI] + proportionJ + 0.3 &&
      (JList[[tt]][CoordI]) ≥ NextPointJ[CoordI] + proportionJ - 0.3 &&
     distanceNextPotPointJ ≤ (distanceJ + 0.5) &&
     JList[[tt]][CoordJ] ≥ NextPointJ[CoordJ] + (distanceJ/2),
    StartPointJ = NextPointJ;
    NextPointJ = JList[[tt]];
    Print["Test J = ", JList[[tt]]];
    gib aus
    NextJDir = {NextPointJ[CoordJ] - StartPointJ [CoordJ],
      NextPointJ[CoordI] - StartPointJ [CoordI] };
    distanceJ = Sqrt[Abs[NextJDir[[1]]^2 + NextJDir[[2]]^2]];
                 Qua ·· Absolutwert
    proportionJ = NextPointJ[CoordI] - StartPointJ[CoordI];
    aJ = aJ + 1;
    AppendTo[CheckPoints, JList[[tt]]];
    hänne an hei
```

```
Luaniae an nei
    AssociateTo[SortedPointsKeys,
    assoziiere mit
      { JList[[tt]], NeighbourJ → aJ, NeighbourI → 1}];
    AppendTo[SortedPoints, SortedPointsKeys];
    hänge an bei
    LastJPointsCellI = JList[[tt]][CellI];
    CheckLastPointJ = JList[[tt]];
    AssociateTo[CheckLastPointJ, {NeighbourJ → aJ, NeighbourI → 1}];
    assoziiere mit
   ];
  ];
];
(*];*)
AppendTo[SortedPoints, SaftyListJ[Start, CheckLastPointJ,
hänge an bei
  proportionJ, LastJPointsCellI, ConvexHull, distanceJ, NextJDir]];
AppendTo[SortedPoints, CompleteJGrid[nextI, ConvexHull, StartDistanceJ,
  StartPropJForFirstCompleteGridJ, Start, NeighbourNumberJ, aI]];
proportionI = StartProportionI;
distanceI = StartDistanceI;
NextIDir = IDirStart;
For pp = 1, pp \le Length[IList] * 2, pp++,
For-Schleife
                Länge
 For [tt = 1, tt ≤ Length [IList], tt++,
For-Schleife
                   Länge
   If[IList[[tt]][CoordI] # StartPointI[CoordI] &&
       IList[[tt]][CoordJ] > NextPointI[CoordJ] || IList[[tt]][CoordJ] 
        NextPointI[CoordJ] && IList[[tt]] [CoordI] ≥ NextPointI[CoordI],
    PotNextIDir = {IList[[tt]][CoordJ] - NextPointI[CoordJ],
       IList[[tt]][CoordI] - NextPointI[CoordI]};
    distanceNextPotPointI = Sqrt[Abs[PotNextIDir[[1]]^2 + PotNextIDir[[2]]^2]];
   ];
   If[IList[[tt]][CoordI] # NextPointI [CoordI] &&
     IList[[tt]][CoordI] # StartPointI[CoordI] &&
      (IList[[tt]][CoordJ]) ≤ NextPointI[CoordJ] + proportionI + 0.3 &&
      (IList[[tt]][CoordJ]) ≥ NextPointI[CoordJ] + proportionI - 0.3 &&
     distanceNextPotPointI ≤ distanceI + 0.5 &&
     IList[[tt]][CoordI] ≥ NextPointI[CoordI] + (distanceI / 3),
    Print["Test I = ", IList[[tt]]];
                 imaginäre Einheit I
    gib aus
    StartPointI = NextPointI;
    NextPointI = IList[[tt]];
```

```
NextIDir = {NextPointI[CoordJ] - StartPointI[CoordJ],
          NextPointI[CoordI] - StartPointI[CoordI]};
        distanceI = Sqrt[Abs[NextIDir[[1]]^2 + NextIDir[[2]]^2]];
                    Qua ·· Absolutwert
        proportionI = NextPointI[CoordJ] - StartPointI[CoordJ];
        (*propJForGrind =Abs[NextPointI[CoordJ]-StartPointI[CoordJ]];*)
                         Absolutwert
       propJForGrind = Abs[StartProportionJ];
                        Absolutwert
       aI = aI + 1;
        AppendTo[CheckPoints, IList[[tt]]];
       hänge an bei
        AssociateTo[SortedPointsKeys,
       assoziiere mit
         { IList[[tt]], NeighbourJ → 1, NeighbourI → aI}];
        AppendTo[SortedPoints, SortedPointsKeys];
       hänge an bei
        LastIPointsCellJ = IList[[tt]][CellJ];
       CheckLastPointI = IList[[tt]];
        AssociateTo[CheckLastPointI, {NeighbourJ → 1, NeighbourI → aI}];
       assoziiere mit
       NeighbourNumberJ = NeighbourNumberJ;
        AppendTo[SortedPoints, SaftyListI[Start, CheckLastPointI,
       hänge an bei
          proportionI, LastIPointsCellJ, ConvexHull, distanceI, NextIDir]];
       AppendTo[SortedPoints, CompleteJGrid[IList[[tt]],
       hänge an bei
          ConvexHull, distanceJ, propJForGrind, Start, NeighbourNumberJ, aI]];
      ];
   ];
   Print["Länge ConvexHull = ", Length[ConvexHull]];
   gib aus
                                 Länge
   Print["Länge SortedPoints = ", Length[Flatten[SortedPoints]]];
                                   Länge Lebne ein
   If[Length[Flatten[SortedPoints]] ≠ Length[ConvexHull] && splits ≤ 8,
   ... Länge ebne ein
                                       Länge
    splits = splits + 1;
    Clear[CheckPoints];
    lösche
    CheckPoints = {};
    Print["
    gib aus
Another
        round
```

```
"];
    FindMinMax[PointList],
    Print["
    gib aus
End and
beende Kontext
       Result_____
"];
    Print["SortedPoints = ", Flatten[SortedPoints]];
    gib aus
                             ebne ein
    DrawGraph[SortedPoints];
    splits = 2;
   ];
  ];
SaftyListJ[Start_, CheckLastPointJ_, proportionJ_,
   LastJPointsCellI_, ConvexHull_, distanceJ_, NextJDir_] :=
  Module[{SaftyList = {}, SaftyKeys = <||>, SaftyKeysList = {},
  Modul
    propJ, lastDirJ, lastdistanceJ, PotNextJDir, tempj,
    distanceNextPotPointJ, nextNeighbourNumber, StartAtThisJPoint},
   If[Length[SaftyKeysList] # 0,
   ... Länge
    Clear[SaftyKeysList];
    lösche
   ];
   StartAtThisJPoint = CheckLastPointJ;
   nextNeighbourNumber = CheckLastPointJ[NeighbourJ] + 1;
   propJ = proportionJ;
   lastDirJ = NextJDir;
   lastdistanceJ = distanceJ;
   For[ii = 1, ii ≤ Length[ConvexHull], ii++,
   For-Schleife
                   Länge
    If[ConvexHull[[ii]][CellI] == CheckLastPointJ[CellI] + 1 | |
    wenn
        ConvexHull[[ii]][CellI] == CheckLastPointJ[CellI] - 1 ||
        ConvexHull[[ii]][CellI] == CheckLastPointJ[CellI] &&
         ConvexHull[[ii]][CellJ] ≥ CheckLastPointJ[CellJ],
      AppendTo[SaftyList, ConvexHull[[ii]]];
      hänge an bei
     ];
   ];
   Print["SaftyList J = ", SaftyList];
```

```
Lyin aus
For [11 = 1, 11 \le Length[SaftyList], 11++,
                Länge
 If[SaftyList[[11]][CoordJ] # Start[CoordJ] &&
 wenn
    SaftyList[[11]][CoordJ] ≥ StartAtThisJPoint[CoordJ] &&
    SaftyList[[ll]][CoordI] ≥ StartAtThisJPoint[CoordI] ||
   SaftyList[[11]][CoordI] < StartAtThisJPoint[CoordI],</pre>
  PotNextJDir = {StartAtThisJPoint[CoordJ] - SaftyList[[11]][CoordJ],
    StartAtThisJPoint[CoordI] - SaftyList[[11]][CoordI]};
  distanceNextPotPointJ = Sqrt[Abs[PotNextJDir[[1]]^2 + PotNextJDir[[2]]^2]];
                           Qua ··· Absolutwert
 If[SaftyList[[11]][CoordJ] # Start[CoordJ] &&
 wenr
   SaftyList[[11]][CoordJ] # StartAtThisJPoint[CoordJ] &&
   SaftyList[[11]][CoordJ] ≥ StartAtThisJPoint[CoordJ] &&
   SaftyList[[11]][CoordI] ≤ StartAtThisJPoint[CoordI] + propJ + 0.3 &&
   SaftyList[[11]][CoordI] ≥ StartAtThisJPoint[CoordI] + propJ - 0.3 &&
   distanceNextPotPointJ ≤ lastdistanceJ + 0.5 &&
   SaftyList[[11]][CoordJ] ≥ StartAtThisJPoint[CoordJ] + lastdistanceJ/3
   (**(3/4)*) && MemberQ[CheckPoints, SaftyList[[11]]] == False,
                  enthalten?
  Print["SaftyListPoint = ", SaftyList[[11]]];
  AppendTo[CheckPoints, SaftyList[[11]]];
  AssociateTo[SaftyKeys, { SaftyList[[11]],
    NeighbourJ → nextNeighbourNumber, NeighbourI → CheckLastPointJ[NeighbourI]}];
  AppendTo[SaftyKeysList, SaftyKeys];
  hänge an bei
  lastDirJ = {StartAtThisJPoint [CoordJ] - SaftyList[[11]] [CoordJ],
    StartAtThisJPoint[CoordI] - SaftyList[[11]][CoordI]};
  lastdistanceJ = Sqrt[Abs[lastDirJ[[1]]^2 + lastDirJ[[2]]^2]];
                   Qua ··· Absolutwert
  propJ = SaftyList[[11]][CoordI] - StartAtThisJPoint[CoordI];
  StartAtThisJPoint = SaftyList[[11]];
  Print["StartAtThisJPoint = ", StartAtThisJPoint];
  gib aus
  nextNeighbourNumber = nextNeighbourNumber + 1;
  For[ii = 1, ii ≤ Length[ConvexHull], ii++,
                  Länge
  For-Schleife
   If[ConvexHull[[ii]][CellI] == StartAtThisJPoint[CellI] + 1 | |
   wenn
       ConvexHull[[ii]][CellI] == StartAtThisJPoint[CellI] -1 ||
       ConvexHull[[ii]][CellI] == StartAtThisJPoint[CellI] &&
        ConvexHull[[ii]][CellJ] ≥ StartAtThisJPoint[CellJ],
     AppendTo[SaftyList, ConvexHull[[ii]]];
```

```
Friarihe ari nei
       ];
     ];
    ];
   ];
   Clear[SaftyList];
   lösche
   Return[SaftyKeysList];
   gib zurück
  ];
SaftyListI[Start_, CheckLastPointI_, proportionI_,
   CheckCellJForI_, ConvexHull_, distanceI_, NextIDir_] :=
  Module [SaftyList = {}, SaftyKeys = <| |>, SaftyKeysList = {}, propI,
  Modul
    lastDirI, lastdistanceI, PotNextIDir, tempi, distanceNextPotPointI,
    nextNeighbourNumber, StartAtThisIPoint},
   If[Length[SaftyKeysList] # 0,
   Länge
    Clear[SaftyKeysList];
    lösche
   ];
   StartAtThisIPoint = CheckLastPointI;
   nextNeighbourNumber = CheckLastPointI[NeighbourI] + 1;
   propI = proportionI;
   lastDirI = NextIDir;
   lastdistanceI = distanceI;
   For[kk = 1, kk ≤ Length[ConvexHull], kk++,
   For-Schleife
                   Länge
    If[ConvexHull[[kk]][CellJ] == CheckLastPointI[CellJ] + 1 | |
        ConvexHull[[kk]][CellJ] == CheckLastPointI[CellJ] - 1 &&
         ConvexHull[[kk]][CellI] ≥ CheckLastPointI[CellI],
      AppendTo[SaftyList, ConvexHull[[kk]]];
      hänge an bei
     ];
   ];
   Print["SaftyList I = ", SaftyList];
                     imaginäre Einheit I
   gib aus
   For [uu = 1, uu ≤ Length[SaftyList], uu++,
                   Länge
    (*Print["Start At This JPoint = ",StartAtThisJPoint];*)
    If[SaftyList[[uu]][CoordI] # Start[CoordI] &&
        SaftyList[[uu]][CoordI] ≥ StartAtThisIPoint[CoordI] &&
        SaftyList[[uu]][CoordJ] ≥ StartAtThisIPoint[CoordJ] ||
```

```
SaftyList[[uu]][CoordJ] ≤ StartAtThisIPoint[CoordJ],
 PotNextIDir = {StartAtThisIPoint[CoordI] - SaftyList[[uu]][CoordI],
   StartAtThisIPoint[CoordJ] - SaftyList[[uu]][CoordJ]};
 distanceNextPotPointI = Sqrt[Abs[PotNextIDir[[1]]^2 + PotNextIDir[[2]]^2]];
                          Qua ··· Absolutwert
If[SaftyList[[uu]][CoordI] # Start[CoordI] &&
  SaftyList[[uu]][CoordI] # StartAtThisIPoint[CoordI] &&
  SaftyList[[uu]][CoordI] ≥ StartAtThisIPoint[CoordI] &&
  SaftyList[[uu]][CoordJ] ≤ StartAtThisIPoint[CoordJ] + propI + 0.3 &&
  SaftyList[[uu]][CoordJ] ≥ StartAtThisIPoint[CoordJ] + propI - 0.3 &&
  distanceNextPotPointI ≤ lastdistanceI + 0.5 &&
  SaftyList[[uu]][CoordI] ≥ StartAtThisIPoint[CoordI] + lastdistanceI / 3
  (**(3/4)*) && MemberQ[CheckPoints, SaftyList[[uu]]] == False,
                 enthalten?
 Print["SaftyListPoint I = ", SaftyList[[uu]]];
                       imaginäre Einheit I
 gib aus
 AppendTo[CheckPoints, SaftyList[[uu]]];
hänge an bei
 AssociateTo[SaftyKeys,
 assoziiere mit
  { SaftyList[[uu]], NeighbourJ → 1, NeighbourI → nextNeighbourNumber}];
 AppendTo[SaftyKeysList, SaftyKeys];
hänge an bei
 lastDirI = {StartAtThisIPoint [CoordI] - SaftyList[[uu]] [CoordI],
   StartAtThisIPoint[CoordJ] - SaftyList[[uu]][CoordJ]};
 lastdistanceI = Sqrt[Abs[lastDirI[[1]]^2 + lastDirI[[2]]^2]];
                  Qua ··· Absolutwert
 propI = SaftyList[[uu]][CoordJ] - StartAtThisIPoint[CoordJ];
 StartAtThisIPoint = SaftyList[[uu]];
 nextNeighbourNumber = nextNeighbourNumber + 1;
 AppendTo[SaftyKeysList, CompleteJGrid[StartAtThisIPoint,
hänge an bei
   ConvexHull, lastdistanceI, propI, Start, 2, nextNeighbourNumber - 1]];
 For[ii = 1, ii ≤ Length[ConvexHull], ii++,
For-Schleife
  If[ConvexHull[[ii]][CellJ] == StartAtThisIPoint[CellJ] + 1 | |
     ConvexHull[[ii]][CellJ] == StartAtThisIPoint[CellJ] - 1 ||
     ConvexHull[[ii]][CellJ] == StartAtThisIPoint[CellJ] &&
      ConvexHull[[ii]][CellJ] ≥ StartAtThisIPoint[CellJ],
    AppendTo[SaftyList, ConvexHull[[ii]]];
    hänge an bei
   ];
 ];
];
```

```
Clear[SaftyList];
   Return[SaftyKeysList];
   gib zurück
  ];
CompleteJGrid[StartPointI_, ConvexHull_, StartDistanceJ_, proportionJ_,
   Start_, NeighbourNumberJ_, aI_] := Module[{PossiblePointsListJ = {},
    SortedPointsKeys = <||>, SaftyPossiblePointsListJ = {}, propJ, StartPointForJGrid ,
    distanceJ , NextNeighbourNumbrtJ, distanceNextPotGridPointJ , tempj,
    NextPointJDir, PotNextJDir, NextJDir, CheckPointJ, CheckCellForJ},
   propJ = proportionJ;
   StartPointForJGrid = StartPointI;
   distanceJ = StartDistanceJ;
   NextNeighbourNumbrtJ = NeighbourNumberJ;
   Print["proportionJ Complete Grid = ", proportionJ];
                                Gitter
   gib aus
   For[aa = 1, aa ≤ Length[ConvexHull], aa++,
    If[ConvexHull[[aa]][CellI] == StartPointForJGrid[CellI] +1||
       ConvexHull[[aa]][CellI] == StartPointForJGrid[CellI] - 1 | |
       ConvexHull[[aa]][CellI] == StartPointForJGrid[CellI] && ConvexHull[[aa]][
           CellJ] ≤ splits && MemberQ[CheckPoints, ConvexHull[[aa]]] == False,
                              enthalten?
      AppendTo[PossiblePointsListJ, ConvexHull[[aa]]];
      hänge an bei
     ];
   ];
   Print["PossiblePointList = ", PossiblePointsListJ];
   gib aus
   For | pp = 1, pp ≤ Length[PossiblePointsListJ], pp++,
    If[PossiblePointsListJ[[pp]][CoordJ] # StartPointForJGrid[CoordJ] &&
    wenn
       PossiblePointsListJ[[pp]][CoordJ] ≥ StartPointForJGrid[CoordJ] &&
       PossiblePointsListJ[[pp]][CoordI] ≤ StartPointForJGrid[CoordI] ||
      PossiblePointsListJ[[pp]][CoordI] ≥ StartPointForJGrid[CoordI],
     PotNextJDir = {PossiblePointsListJ[[pp]][CoordJ] - StartPointForJGrid[CoordJ],
       PossiblePointsListJ[[pp]][CoordI] - StartPointForJGrid[CoordI]};
     distanceNextPotGridPointJ = Sqrt[Abs[PotNextJDir[[1]]^2 + PotNextJDir[[2]]^2]];
                                  Qua··· Absolutwert
    If [PossiblePointsList][[pp]][CoordJ] # StartPointForJGrid[CoordJ] &&
      PossiblePointsListJ[[pp]][CoordJ] # Start[CoordJ] &&
```

```
PossiblePointsListJ[[pp]][CoordJ] ≥ StartPointForJGrid[CoordJ] &&
      PossiblePointsListJ[[pp]][CoordI] ≤ StartPointForJGrid[CoordI] + propJ + 0.3 &&
      PossiblePointsListJ[[pp]][CoordI] ≥
        StartPointForJGrid[CoordI] + propJ - (*1.0*)3.0&&
      PossiblePointsListJ[[pp]][CoordJ] ≥ StartPointForJGrid[CoordJ] + distanceJ /3 &&
      distanceNextPotGridPointJ ≤ (distanceJ + 0.9) &&
      MemberQ[CheckPoints, PossiblePointsListJ[[pp]]] == False,
      enthalten?
     Print["[PossiblePointsListJ[[pp]]]; = ", PossiblePointsListJ[[pp]]];
     gib aus
     NextJDir = { PossiblePointsListJ[[pp]][CoordJ] - StartPointForJGrid[CoordJ],
        PossiblePointsListJ[[pp]][CoordI] - StartPointForJGrid[CoordI]};
     distanceJ = Sqrt[Abs[NextJDir[[1]]^2 + NextJDir[[2]]^2]];
                 Qua ··· Absolutwert
     propJ = PossiblePointsListJ[[pp]][CoordI] - StartPointForJGrid[CoordI];
     StartPointForJGrid = PossiblePointsListJ[[pp]];
     AppendTo[CheckPoints, PossiblePointsListJ[[pp]]];
     hänge an bei
     AssociateTo[SortedPointsKeys, {PossiblePointsListJ[[pp]],
     assoziiere mit
        NeighbourJ → NextNeighbourNumbrtJ, NeighbourI → aI}];
     AppendTo[SaftyPossiblePointsListJ, SortedPointsKeys];
     AssociateTo[StartPointForJGrid,
     assoziiere mit
      {NeighbourJ → NextNeighbourNumbrtJ, NeighbourI → aI}];
     NextNeighbourNumbrtJ = NextNeighbourNumbrtJ + 1;
    ];
   ];
   CheckPointJ = StartPointForJGrid;
   CheckCellForJ = StartPointForJGrid[CellJ];
   AppendTo[SaftyPossiblePointsList], SaftyListJ[Start, StartPointForJGrid,
   hänge an bei
     propJ, StartPointForJGrid[CellJ], ConvexHull, distanceJ, NextJDir]];
   Clear[PossiblePointsListJ];
   lösche
   Print["Checklist = ", CheckPoints];
   Print["NEXT"];
   gib aus
   Return[SaftyPossiblePointsListJ];
   gib zurück
  ];
CreateSyntheticPointsForFurtherChecks[] := Module[{},
                                           Modul
```