

# Berechnung der essentiellen Matrix

- 1) Intrinsische Matrizen, die von MATLAB ausgegeben wurden, transponieren

Linke: 
$$\begin{bmatrix} 2936,0146 & 0 & 911,4241 \\ 0 & 2939,5803 & 673,3906 \\ 0 & 0 & 1 \end{bmatrix}$$

Rechte : 
$$\begin{bmatrix} 4663,1058 & 0 & 960,8538 \\ 0 & 4664,9718 & 665,5394 \\ 0 & 0 & 1 \end{bmatrix}$$

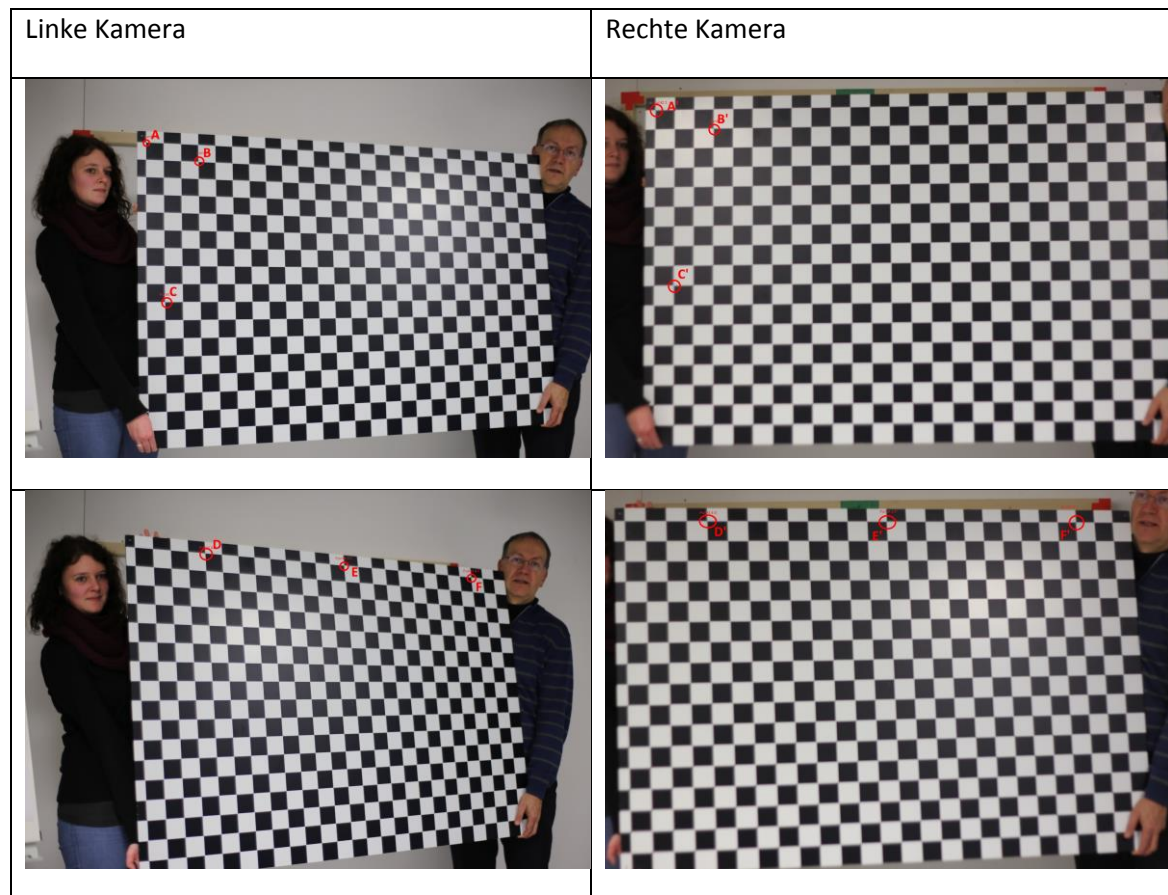
- 2) Dann in mm umrechnen. Wir erhalten K' (rechts) bzw. K (links)

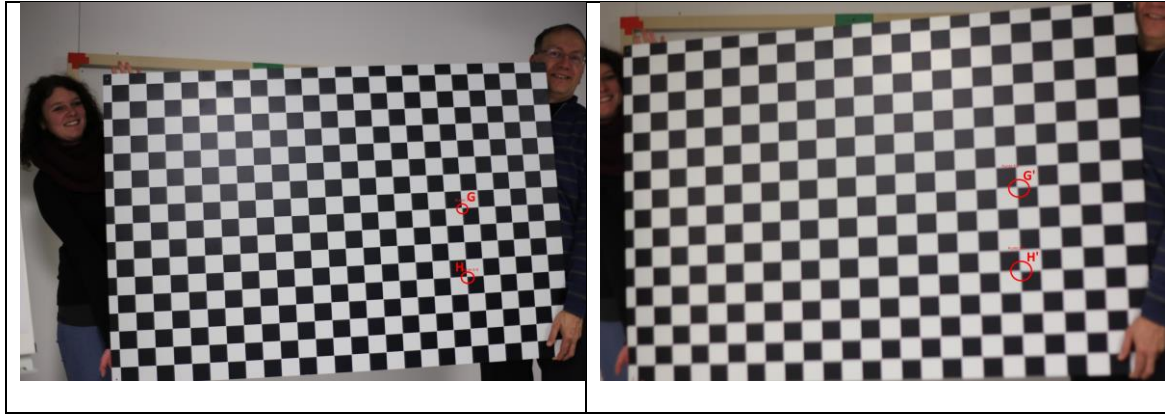
K = 
$$\begin{bmatrix} 19,084 & 0 & 5,924 \\ 0 & 19,107 & 4,377 \\ 0 & 0 & 1 \end{bmatrix}$$

K' = 
$$\begin{bmatrix} 20,004 & 0 & 4,122 \\ 0 & 20,012 & 2,855 \\ 0 & 0 & 1 \end{bmatrix}$$

- 3) Dann:  $E = K'^T F K$

**1. Schritt:** Bestimmung der Punkte A – H





Die ermittelten Pixel Koordinaten aus den Bildern:

**Hinweis:** Der Nullpunkt (0,0) befindet sich oben links vom Bild

A = [409; 214; 1]	A_ = [170; 105; 1]
B = [586; 280; 1]	B_ = [367; 167; 1]
C = [474; 753; 1]	C_ = [232; 697; 1]
D = [609; 214; 1]	D_ = [345; 105; 1]
E = [1078; 255; 1]	E_ = [953; 106; 1]
F = [1508; 295; 1]	F_ = [1592; 109; 1]
G = [1493; 696; 1]	G_ = [1410; 626; 1]
H = [1510; 928; 1]	H_ = [1421; 909; 1]

Die ermittelten Pixel Koordinaten in mm umgerechnet

**Hinweis:** Die Pixelkoordinaten wurden mit dem jeweiligen Pixel Pitch der Kamera (linke: 6.5µm, rechts: 4.29µm) verrechnet:

A = [2.6585; 1.391; 1]	A_ = [0.7293; 0.4505; 1]
B = [3.809; 1.820; 1]	B_ = [1.5744; 0.7164; 1]
C = [3.081; 4.8945; 1]	C_ = [0.9953; 2.9901; 1]
D = [3.958; 1.391; 1]	D_ = [1.480; 0.4505; 1]
E = [7.007; 1.6575; 1]	E_ = [4.0884; 0.4547; 1]
F = [9.802; 1.9175; 1]	F_ = [6.8297; 0.4676; 1]
G = [9.7045; 4.526; 1]	G_ = [6.0489; 2.6855; 1]
H = [9.815; 6.032; 1]	H_ = [6.0961; 3.8996; 1]

## 2. Schritt: Bestimmung der Fundamentalmatrix

```
Funda = [
A_(1) * A(1), A_(1) * A(2), A_(1), A_(2) * A(1), A_(2) * A(2), A_(2), A(1), A(2), 1;
B_(1) * B(1), B_(1) * B(2), B_(1), B_(2) * B(1), B_(2) * B(2), B_(2), B(1), B(2), 1;
C_(1) * C(1), C_(1) * C(2), C_(1), C_(2) * C(1), C_(2) * C(2), C_(2), C(1), C(2), 1;
D_(1) * D(1), D_(1) * D(2), D_(1), D_(2) * D(1), D_(2) * D(2), D_(2), D(1), D(2), 1;
E_(1) * E(1), E_(1) * E(2), E_(1), E_(2) * E(1), E_(2) * E(2), E_(2), E(1), E(2), 1;
F_(1) * F(1), F_(1) * F(2), F_(1), F_(2) * F(1), F_(2) * F(2), F_(2), F(1), F(2), 1;
G_(1) * G(1), G_(1) * G(2), G_(1), G_(2) * G(1), G_(2) * G(2), G_(2), G(1), G(2), 1;
H_(1) * H(1), H_(1) * H(2), H_(1), H_(2) * H(1), H_(2) * H(2), H_(2), H(1), H(2), 1;
```

```
];
```

```
Funda = null(Funda);
```

```
Funda =
```

```

0.0009
-0.0602
0.2911
0.0469
-0.0018
0.5952
-0.1435
-0.4704
0.5598

```

```

Funda = [
0.0009, -0.0602, 0.2911;
0.0469, -0.0018, 0.5952;
-0.1435, -0.4704, 0.5598
];

```



### 3. Schritt: $E = K'^{(T)} F K$

```

K = [
19.084, 0, 5.924;
0, 19.107, 4.377;
0, 0, 1
]

```



```

K_ = [
20.004, 0, 4.122;
0, 20.012, 2.855;
0, 0, 1
]

```

```

// Essential Matrix
Essential = K_' * Funda * K

```

```
Essential =
```

```

0.3436 -23.0094 0.6589
17.9115 -0.6883 17.3135
-0.1124 -13.8274 0.2566

```

#### 4) Dann Singulärwertzerlegung von E $[U, S, V] = \text{svd}(\text{Essential})$

```
U =
```

```

0.8195 -0.2508 -0.5153
0.2991 0.9542 0.0112
0.4889 -0.1634 0.8569

```

```
S =
```

```

27.0569 0 0
0 24.7028 0
0 0 0.1040

```

```
V =
```

```

0.2064 0.6891 -0.6947
-0.9543 0.2985 0.0125
0.2160 0.6604 0.7192

```